Design Optimization of a Double Excitation Synchronous Machine in Railway Traction
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Les véhicules électriques en général et le transport ferroviaire électrique sont largement reconnus comme des modes de transports à haute efficacité énergétique, particulièrement dans un contexte où la réduction de l’utilisation d’énergies fossiles (dont les réserves s’épuisent) et de la pollution est devenue une priorité. Les solutions apportées à ces problématiques sont donc de plus en plus attractives aux yeux des chercheurs qui ont donc redoublé d’efforts pour imaginer et concevoir de nouvelles solutions plus efficaces.

La conception optimale d’un système de traction ferroviaire représente donc un enjeu majeur dont la spécificité réside dans trois aspects principaux :

- D’abord, ce système fait appel à de nombreuses disciplines (électriques, mécaniques, magnétiques, etc.) étroitement couplées entre elles. Les études récentes se sont surtout focalisées sur l’optimisation séparée des composants. L’inconvénient majeur de cette approche est que la combinaison des meilleurs composants ne permet pas d’aboutir à un meilleur système.

- Ensuite, le système de traction ferroviaire fait appel à des sous-systèmes fortement non linéaires. Ces systèmes rendent particulièrement délicat le travail d’analyse des concepteurs et a pour inconvénient d’augmenter le temps de calcul.

- Enfin, contrairement à de nombreuses autres applications où les machines sont conçues pour fonctionner sur quelques points de quelques points de fonctionnement, les applications de traction sont caractérisées par un cycle de fonctionnement pouvant contenir plusieurs centaines de points de fonctionnement (combinaison couple-vitesse) distincts.

La conception optimale est nécessaires obtenir des structures capables de fonctionner à rendement élevé sur divers points de fonctionnement. Dans des études récentes, aucune recherche n’a été n’a pris en compte les trois aspects mentionnés plus haut.

Par exemple, les auteurs de [1] ont présenté une approche pour la conception optimale du moteur
de traction dans le système de propulsion ferroviaire dans laquelle l’aspect multidisciplinaire et le cycle de conduite sont pris en compte, mais les modèles magnétiques utilisés sont linéaires. Dans [2], il est présenté la conception et l’optimisation d’une machine à aimants permanents à commutation de flux pour des applications de véhicules électriques. Dans cette référence, le modèle thermique a été négligé et le modèle de pertes simplifié. Dans [3], une méthode de conception efficace appliquée aux véhicules électriques a été utilisée pour envisager avec rigueur un couplage entre des modèles électromagnétiques et thermiques non linéaires. Pour cela, une surface de réponse est programmée à partir de calcul de couple à l’aide d’un modèle éléments finis mais, une fois de plus, le modèle de perte de fer a été fortement simplifié.

A la recherche d’une meilleure solution en termes d’efficacité énergétique, ce travail est dédié à la traction ferroviaire. Nous examinons plus particulièrement une classe spéciale de machine synchrone appelée machine synchrone à double excitation (MSDE). Le terme Double Excitation indique que le flux inducteur de la machine est créé par deux sources : des bobinages et des aimants permanents. Ce type de machine combine avantages des machines synchroes à aimants permanents (puissance massique élevée et à haute efficacité) et des machines synchroes bobinées (souplesse de commande). Cette propriété est très intéressante dans le contexte des applications avec un cycle de fonctionnement telles que le transport ou la production d’électricité. En effet, en jouant sur le dosage aimants permanents – excitation bobinée, on peut déplacer les zones de meilleur rendement sur les points du cycle les plus sollicités et ainsi améliorer l’efficacité énergétique sur un cycle de fonctionnement.

De ce point de vue la thèse tente de répondre à la question suivante : en termes d’économie d’énergie et de coût, une MSDE st-elle capable de faire mieux que les machines conventionnelles sur un cycle de fonctionnement donné ? Nous analyserons également les circonstances qui favorisent la MSDE par rapport aux machines conventionnelles. Les principales contributions de ce travail de thèse sont ainsi déclinées :

- Considérer une optimisation de la conception d’une MSDE multi-physique, avec l’utilisation d’un modèle magnétique non linéaire générique sur un cahier des charges contenant un cycle de plusieurs points de fonctionnement.

- Répondre à la question : une MSDE peut-elle dominer les machines conventionnelles sur des objectifs de minimisation conjointe de pertes et de coûts ?

- Répondre à la question : généralement, dans quels cas, une MSDE est plus efficace qu’une machine conventionnelle.

A cette fin, la thèse se déroule comme suit :

**Le chapitre 1** traite brièvement de l’histoire de la traction ferroviaire. Certains moteurs de traction sont présentés puis comparés dans ce chapitre. En outre, les travaux de recherches récents qui ont été faits sur la traction ferroviaire sont aussi examinés.
Il est mis en évidence que l’électrification du ferroviaire pourrait permettre de baisser les coûts, améliorer la puissance massique et surtout réduire la pollution sonore ainsi que les rejets polluants. Divers moteurs de traction sont disponibles : bien que les machines asynchrones soient les plus populaires dans le cadre de la traction ferroviaire, les moteurs synchrones à aimants permanents apparaissent comme des candidats très prometteurs. En particulier le coût des aimants, qui est un frein à l’expansion des machines synchrones dans le ferroviaire, est réduit si des aimants en ferrite sont utilisés à la place des aimants terres rares. Un autre inconvénient des machines synchrones à aimants permanents réside dans sa difficulté à assurer un fonctionnement adéquat dans la région de fonctionnement à haute vitesse à cause de sa capacité de défluxage limitée. Nous avons donc proposé d’utiliser une machine synchrone à double excitation afin de remédier à ce problème.

**Le chapitre 2** est consacré à la présentation et à la description des machines synchrones à double excitation. Le principe fonctionnement et différentes topologies documentées dans la littérature ainsi que celles mises au point dans le laboratoire SATIE sont présentés. Les avantages en termes de contrôle de flux et de rendement sont soulignés. Enfin, un prototype de machine synchrone à double excitation développé au laboratoire est choisi puis étudié finement à l’aide d’une analyse éléments finis 3-D.

Les machines synchrones à double excitation ont un flux d’excitation produit par des aimants permanents et des bobines d’excitation. Ce mixage de sources d’excitation permet d’imaginer une grande variété de structures, qui peuvent être classifiées suivant différents axes. On en propose deux dans cette thèse : en fonction de l’agencement des sources (structures séries ou parallèles) ou en fonction de l’emplacement des sources (rotor, stator, ou mixte). L’agencement peut conduire à des machines dont la structure est en trois dimensions, avec donc des trajets de flux tridimensionnels. Il est aussi rappelé, que même si nous nous focalisons sur des machines tournantes à flux radial, le principe de la double excitation s’étend également à des machines à flux axial. Divers machines utilisant ce principe ont été développées dans le monde entier. Au laboratoire SATIE, certains types ont été fabriqués et testés. Parmi ces prototypes, nous avons retenu celui qui a le meilleur contrôle du flux d’excitation.

Une analyse détaillée de ce prototype est effectuée. Dans ce prototype, certains trajets de flux sont en trois dimensions conduisant à l’utilisation de la méthode des éléments finis 3-D afin de mener l’analyse la plus précise possible. Ces trajets de flux complexes compliquent l’analyse, mais offrent l’opportunité d’envisager plusieurs options afin améliorer les performances de la machine. En raison des temps de calcul nécessaires pour une évaluation à l’aide d’un outil de calcul éléments finis 3-D, une méthode alternative plus rapide a été requise en vue d’émettre en œuvre un processus d’optimisation avec un grand nombre d’évaluations des modèles. Ce modèle rapide est au centre des chapitres suivants.

**Le chapitre 3** se concentre sur la modélisation de la machine en utilisant la méthode généralisée des schémas réducteurs dans le but de remplacer le modèle fin de calcul éléments finis 3-D.
L’objectif étant de diminuer le temps de calcul tout en conservant une bonne précision. Cette méthode de modélisation prend en effet compte la saturation magnétique. La validité de cette méthode est vérifiée par des comparaisons avec la méthode de calcul éléments finis. Une partie de ce chapitre est réservée à la discussion du calcul des pertes fer.

La Méthode généralisée des schémas réductants a prouvé être une méthode rapide d’analyse des machines électriques basée sur son analogie avec un réseau électrique. En termes de temps de calcul, elle est beaucoup plus rapide que la méthode des calculs éléments finis (particulièrement en 3-D, comme c’est le cas ici). Par conséquent, la méthode généralisée des schémas réductants est tout à fait adapté à la conception, particulièrement dans les phases préliminaires du dimensionnement. Pour le modèle étudié, une méthode nodale généralisée est mise en œuvre. L’idée principale de généralisation est que le nombre de noeuds et les éléments du réseau sont facilement paramétrables. L’élément de reluctance de base du réseau est un bloc de 4 réductances qui suppose que le flux obtenu est bidimensionnel (x et y dans un système de coordonnées cartesiennes).

La signification de “nodale” est que la formulation du système d’équations est basée sur la loi des nœuds de Kirchhoffs (par opposition au réseau “ maillé ” basé sur l’utilisation de la loi des mailles). Le choix d’une base nodale système rend le réseau plus facile à étendre. Cette propriété est très efficace compte tenu de la structure 3-D du prototype puisque la modélisation de l’ensemble de la machine nécessite une connexion des éléments bidimensionnels pour former une modèle tridimensionnel. La saturation magnétique est considérée en résolvant itérativement le système d’équations non linéaires obtenues.

Du point de vue de l’objectif principal de la thèse, à savoir l’optimisation sur cycle de fonctionne, deux aspects les plus importants de le modèle électromagnétique sont le couple et les pertes moyennes sur cycles. En raison des trajets de flux tridimensionnels et des matériaux utilisés (massifs et feuillets), les pertes fer sont particulièrement difficiles à estimer.


Le chapitre 4 présente le modèle thermique de la machine. Ce modèle est également basé sur un schéma électrique équivalent à constante localisées. Par rapport aux machines classiques, la machine synchrone à double excitation comporte des enroulements d’excitation additionnels, c’est à dire des sources de chaleur supplémentaire de ces pertes Joule dissipées dans les bobinages d’excitation. En particulier, la difficulté rencontrée ici provient du fait que la résistance thermique entre les bobinages et le stator est élevée, rendant ainsi très problématique l’évacuation de ces pertes Joule supplémentaires. Le modèle thermique est généralement développé en régime transitoire. Le régime permanent est alors facilement déduit. Les pertes mécaniques, notamment les pertes par frottement et celles dans les roulements sont prises en compte afin affiner
l’analyse thermique.

Les aspects thermiques de la machine sont analysés grâce à un modèle similaire au modèle magnétique présenté au chapitre 3. Contrairement au modèle électromagnétique, le modèle thermique nécessite des paramètres (les coefficients thermiques) qui ne peuvent être déterminées que de manière empirique compte tenu de l’état actuel de nos connaissances. Ces coefficients thermiques varient en fonction de différents paramètres mécaniques et sont difficilement applicables sans vérification expérimentale préliminaire. De plus, la structure de machine synchrone à double excitation étudiée est plus complexe en raison des enroulements d’excitation additionnels. Par conséquent, des essais expérimentaux sont nécessaires pour déterminer de nouveau plusieurs coefficients thermiques.

En raison du fait que tous les enroulements sont placés au stator, c’est-à-dire que toutes les principales sources de chaleur sont situées au stator (les pertes rotoriques sont en effet négligeables), le nombre de coefficients thermiques à déterminer est minimisé. Il convient de noter qu’il est trop difficile de vérifier tous les coefficients thermiques à moins démonter le prototype afin d’effectuer des essais séparés. Par conséquent, le processus de vérification expérimental permet de vérifier la bonne concordance entre les résultats théoriques et expérimentaux.


L’optimisation est traitée en utilisant une approche à deux niveaux et un algorithme basé sur les essais particulaires. Dans cette stratégie, l’objectif de l’optimisation interne est de trouver les contrôles optimaux pour chaque machine et celui de l’optimisation externe est de rechercher les machines à la géométrie optimale. Visant à réduire le calcul temps, un examen attentif est pris sur l’optimisation interne en utilisant une combinaison appropriée de particules et de générations nécessaires.

Afin de comparer la machine synchrone à double excitation avec une machine conventionnelle, une machine synchrone à aimants permanents est dérivée du modèle de la machine synchrone à double excitation en supprimant les parties spécifiques à la double excitation. Les analyses préliminaires des résultats tendent à montrer que pour les dimensions du prototype, la machine synchrone à aimants permanents semble plus performante que la machine synchrone à double excitation au point de fonctionnement nominal. La machine synchrone à double excitation a

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besoin d’un volume plus important principalement à cause des trajets de flux de fuite créés dans cette machine. Cependant, dans les circonstances où la vitesse maximale est beaucoup plus élevée que la vitesse dite de base, la capacité de défluxage de la machine synchrone à double excitation permet d’obtenir des machines plus performantes que les machines à aimants permanents. Ainsi, la capacité de contrôle du flux d’excitation des machines synchrones à double excitation peut s’avérer cruciale dans certains cas et donc dans les applications correspondantes.

Dans l’optimisation, en utilisant la stratégie des points représentatifs, deux cas sont considérés : 3 points représentatifs et 6 points représentatifs (sur 679 points). Il est intéressant de noter que pour générer une optimisation d’un type de machine (machine synchrone à aimants permanents ou machine synchrone à double excitation), un ordinateur de 12 cœurs cadencés à 3,5 Ghz prend environ 6 jours pour finir une optimisation sur 3 points. Cela limite drastiquement le nombre de points maximum à choisir et explique pourquoi nous nous sommes limités à considérer les 2 cas présentés ci-dessus.

Les résultats montrent que pour le cycle initialement envisagé, les machines à aimants permanents optimales sont meilleures que les machines synchrones à double excitation optimales pour les deux objectifs envisagés. La raison principale de la supériorité des machines synchrones à aimants permanents pour le cycle envisagé réside dans le rapport entre la vitesse maximale et la vitesse de base (d’environ 1,7) qui n’est pas suffisamment élevée pour exploiter la capacité de défluxage de la machine synchrone à double excitation. En outre, l’influence du nombre de points (cas avec 6 points) sont est réduite. Afin de vérifier que le ratio entre la vitesse maximale et la vitesse de base est bien la raison principale de la supériorité des machines synchrones à aimants permanents, des optimisations supplémentaires ont été effectuées avec un ratio plus élevé (4 et 5). Le résultat révèle que l’augmentation de ce ratio permet à la machine synchrone à double excitation de présenter de meilleures performances que la machine synchrone à aimants permanents.

Afin de pousser cette étude, plus de cas devrait être étudié dans les travaux futurs : d’abord, l’influence de différentes stratégies dans le choix des points représentatif sur des conceptions optimales. Deuxièmement, l’intégration de stratégies de contrôle ainsi que l’analyse transitoire thermique pour tenir compte des opérations en temps réel sur le cycle de conduite. Troisièmement, l’analyse d’autres structures de machines synchrones à double excitation mérite d’être menée afin d’étendre le périmètre de comparaison.
Electric vehicles in general and electrified railways in particular are widely recognized as energy efficient and environmentally friendly solutions especially in the context of the exhausted fossil fuels and environmental pollution. Energy saving solutions are therefore becoming priority targets and attracting more and more research attention.

A big challenge for optimal designs of a railway traction system lies in three main aspects: firstly, it contains many disciplines (electrical, mechanical, magnetic, etc.) and theirs interactions. Recent studies merely optimized individual components. The major drawback of this approach is that the combination of best components does not surely form a best system. Secondly, nonlinear characteristics make it complicated for designers to consider and increase computation time as well. Lastly, unlike many other applications where machines are designed to operate at few operating points, traction applications are characterized by a driving cycle where hundred working points (torque-speed combinations) are presented. Optimal designs are required to work with high efficiency at various points. In recent studies, no research has taken into account all three mentioned aspects. For instances, authors of [1] presented an approach for optimal design of traction motor in a railway propulsion system with considerations of multidisciplinary design and driving cycle but a linear model was used. [2] presented a design optimization of a flux switching permanent magnet machine for electric vehicle applications but thermal aspect was neglected also loss model was much simplified. In [3], an efficient design technique for electric vehicle was used to actually consider a coupling between nonlinear electromagnetic and thermal models. Torque output response surface is computed based on a couple of finite element calculations but the iron loss model was simplified.

In search of a better energy efficient solution, this work is dedicated to the railway traction with an application of a special class of synchronous machine called **Double Excitation Synchronous Machine (DESM)**. Double excitation term indicates that the field flux of the machine is created by two sources: field windings and permanent magnets. This type of machine combines advantages of permanent magnet synchronous machines (high power density and high efficiency) and
wound field synchronous machines (flexible flux control). This property is very interesting in the context of applications with an operating cycle such as transportation or power generation since this machine minimizes losses and hence improves efficiency on an operating cycle.

The main highlight of the thesis is trying to answer the question: In term of energy saving approach, is a DESM able to perform better than conventional machines within a given train driving cycle also in which circumstances DESMs are better. Contributions of the thesis work are briefed as follows:

- Consider a design optimization of a DESM with muti-disciplines, magnetic non-linearity and with multiple working points on the driving cycle
- Answer the question: does a DESM machine gain advantages over conventional machines with objectives of minimizing losses and cost?
- Answer the question: in which circumstance, a DESM performs better than conventional machines?

To this end, the thesis is proceeded as follows:

**Chapter 1** covers briefly the railway traction history. Some common traction motors to date and their comparisons are made in this chapter. Also, researches have been done on traction applications are briefed.

**Chapter 2** is dedicated to the basics of DESMs. The fundamental working principle and different topologies documented in the literature and ones has been developed in SATIE laboratory are introduced as well. Advantages in term of flux control and efficiency of DESM machines are emphasized. Finally, a prototype of DESM is decided as the analysis model in the thesis. 3D FEM analysis for this chosen prototype is conducted in detail.

**Chapter 3** concentrates on the machine modeling using generalized Equivalent Magnetic Circuit Network (EMCN) method with the aim to replace the high fidelity model (by FEM) with a cheap-to-evaluate one in term of computation time while still maintaining a good accuracy. This alternative modeling method takes into account saturation effect. The validity of the EMCN method is verified by comparisons with FEM. A part of this chapter is reserved for the discussion of iron loss calculation.

**Chapter 4** presents the thermal model of the machine by using lumped parameter thermal network. In comparison with classical machines, a DESM has additional excitation windings i.e. extra heat sources from these winding’s copper losses. In particular, the machine faces heat evacuation difficulty from its two global excitation windings due to high thermal resistance between the windings and the stator outer core. The thermal model is generally developed in transient regimes and the steady state mode could be easily deduced. Mechanical losses including windage and bearing friction losses are briefed for a more comprehensive losses consideration.
Chapter 5 targets optimizations of the machine considering a driving cycle using multi-physics model. The objectives are to minimize both material cost and total losses on the driving cycle. Results presented by pareto fronts are derived by using bi-level optimization approach in which lower level is to find the optimal control for each machine and upper level is to search the optimal geometries. Taking into account a thousand of points on the driving cycle makes optimization task become impossible even though fast models were used. Instead, a set of representative points is derived by using an energy center of gravity technique. Comparisons with a classical permanent magnet synchronous machine are conducted. These comparisons are done with the given driving cycle and also with extended speed range to evaluation performance of DESM in different regimes. Finally, a general conclusion is given.

Chapter 3 and 4 deal with conventional modeling techniques yet more complex due to three dimensional magnetic flux and thermal difficulty with additional excitation windings. Chapter 5 could be considered as an application of all done in its previous chapters to answer the question of the thesis. The biggest challenge in the optimization is dealing with computation time as a result of nonlinearity and multiple operating points considerations. Several techniques and assumptions must be made to keep the optimization process feasible.
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Chapter 1

A Brief of Railway Traction

This chapter covers a brief historical perspective of the railway traction dating back from hundred years ago to the current modern railway’s technologies.

The earliest record tramway for mine began in Germany about 1550 [4] due to an advantage of less rolling resistance of wheels on rails compared to those on roads; therefore, heavier loads to be pulled for the same power. This principle applies to all kinds of railway traction. The first engine to replace horse power in locomotive was steam engine in the early 1800’s. From its beginning, steam traction expanded rapidly with larger, faster and more powerful for the next century. However, the problem with steam engines regardless the fuel used (wood, coal) is the smoke coupled with high maintenance cost, frequent fueling and large quantities of water.

An alternative way of replacing steam locomotive was to use diesel. Diesel engines use compression rather than a spark to ignite the fuel were first invented by Rudolf Diesel. However, owing to technical difficulties, this type of traction was not considered until 1920s. Despite problems related to environment, pollution, maintenance, etc., but having higher thermal efficiency (about 40% compared to less than 10% of steam engines [5]), diesel engines have been widely used to phase out steam engines in railway traction and other transport sectors i.e. passenger cars, buses, trucks, trailers, locomotives, boats and ships [6, 7].
1.1 Diesel electric traction

Due to the fact that diesel engines face a major problem of lacking a reliable mechanical transmission, its early adoption by railways was prevented. In a new traction system using diesel engines, power is usually transmitted to the wheels through a form of electric transmission [8]. In this traction system, diesel engine drives an electric generator conveying electric power to traction motors. A typical system using diesel electric is illustrated in Fig. 1.2 [9]. Depending on the type of traction motor (to be discussed later in this chapter) used, there will be an option to equip or not an inverter in this diagram. Also, a battery storage system could be provided to enhance the operation reliability in case of failure happened to the diesel engine or generator.

This traction configuration has an obvious advantage of dependence elimination on power supply (e.g. using electrification system) i.e. removal of failure and maintenance activities of power system. In addition to this independence, no big capital investment required for building up a complex power supply system. This facilitates its usage all over the world especially in developing countries. But the train power is subjected to the power handling capability of the on-board engine which is limited due to factors such as engine volume constraint, mechanical system, etc.

1.2 Railway electrification

On the contrary to the traction system using diesel engine, electrification systems could overcome most of drawbacks that diesel electric counterparts have. Also, the power source of the electric locomotive is not installed on the train and so the overall system could be smaller, lighter and faster and consequently cheaper, capable to assure the supply of several trains at the same time. One configuration using electrification is depicted in Fig. 1.3 [10].

Locomotives equipped with regenerative brakes making use of energy sending back into the supply system and/or on-board resistors, which convert the excess energy to heat. Electrification usage ranges from low speed systems such as tramways in the cities to very high speed applications such as TGVs (France) or Shinkansen (Japan). Electrification distribution map with various kinds and levels of voltage in Europe is shown in Fig. 1.4 [11]. The DC voltage system is simple but requiring thick cables and short distances between feeder stations because of high current required and also significant resistive losses. On the contrary, with alternat-
1.2. Railway electrification

Main advantages of electrification include:

- Lower running cost of locomotives
- Lower maintenance cost of locomotives
- Higher power-to-weight ratio, resulting in:
  - Fewer locomotives
  - Faster acceleration
  - Higher speed limit
- Less noise pollution and no air pollution from the train itself
The main disadvantages are the capital cost of the electrification system, most significantly for long distance lines. Also, if the overhead wiring breaks down in some ways, all trains could be brought to standstill. Therefore, a more reliable system must be constructed. Also, upgrading brings significant cost especially where tunnels and bridges and other obstruction have to be altered for the clearance purpose.

With electrification systems, locomotives could take energy by two options either via overhead lines (Fig. 1.3) or a third rail. A third rail is a method of providing electric power to a railway train through one more rail running in parallel to the main rails. Using a third rail is cheap to install, more compact and easy for maintenance. The third rail system has its own corridors usually set underground so to avoid visual pollution like the overhead wires. It is also fully or almost fully segregated from the outside environment to ensure a safety condition. In most cases, third rail system supply direct current electricity [11].

1.3 Railway traction motors

According to the scope of the thesis, a traction motor is considered to be the most important component in the whole railway system. Various choices could be opted among DC motors, induction motors (the most popular one in the industry) and synchronous motors as displayed in Fig. 1.5.

![Popular electric motors used in railway traction. a) DC motor. b) Induction motor. c) Synchronous motor](image)

Briefly, at the early stage of development, DC motors, together with low-voltage DC traction lines, were the main traction power supply methods, due to the simpleness in term of both construction and controlling i.e. torque characteristic. However, dc motor drives have a bulky construction, low efficiency, low reliability and higher need of maintenance mainly due to the presence of the mechanical commutator [12].

Subsequently, with the development of power electronics, AC motors with their advantages have come into use. Among them, induction motors are the most popular choice in industrial applications having the most mature technology among all other AC competitors. A series of
advantages of cage induction motors for traction compared to DC motor was documented in [13], such as robust construction, much lower input for maintenance is required, low cost/power ratio, steep torque-speed characteristic. However, low power factor is still the disadvantage needed to be improved. Also, as mentioned in [12], the presence of a breakdown torque limits its extended constant-power operation. Moreover, efficiency at a high speed range may suffer in addition to the fact that induction motor efficiencies are inherently lower than that of permanent magnet motors, due to the absence of rotor winding and rotor copper loss.

Synchronous motor can overcome this disadvantage with high power factor and high efficiency. Although synchronous motors are costly with rather complex structures because it requires additional excitation sources (permanent magnets - PM or excitation winding) but with higher efficiency, the operating cost would be lower compared to induction motors. Although, this type of motor with PM excitation inherently has a short constant-power region due to their rather limited field weakening capability [12].

A general comparison between DC, induction and PM motors is summarized in Table. 1.1 based on six factors with a score out of 5 for each factor [14].

<table>
<thead>
<tr>
<th>Feature</th>
<th>DC</th>
<th>Induction</th>
<th>PM synchronous</th>
</tr>
</thead>
<tbody>
<tr>
<td>Power density</td>
<td>2.5</td>
<td>3.5</td>
<td>5</td>
</tr>
<tr>
<td>Efficiency</td>
<td>2.5</td>
<td>3.5</td>
<td>5</td>
</tr>
<tr>
<td>Controllability</td>
<td>5</td>
<td>5</td>
<td>4</td>
</tr>
<tr>
<td>Reliability</td>
<td>3</td>
<td>5</td>
<td>4</td>
</tr>
<tr>
<td>Technology maturity</td>
<td>5</td>
<td>5</td>
<td>4</td>
</tr>
<tr>
<td>Cost</td>
<td>3</td>
<td>5</td>
<td>4</td>
</tr>
</tbody>
</table>

1.3.1 Traction motor requirements

Motors utilized in the railway traction own some practical differences compared to other industrial machines due to the distinguishing requirements to be respected from locomotive’s operation [15].

- The traction motors are built in and carried along by their loads so that they must be physically robust
- Space limitations for installation
- Economic operation
- Harsh environment: vibration, shock, temperature and humidity
- Limitation on weight for axle/wheel loading
• More importantly, motors have to satisfy a requirement of variable loading which is characterized by the traction duty cycle.

The duty cycle consists of various operating modes even at a condition being greater than rated torque or power which is subject to the motor thermal constraints. A velocity-time curve of a station-to-station duty cycle with corresponding tractive effort and power requirements is shown in Fig. 1.6 [15].

![Traction vehicle trajectory, tractive effort and power for station-to-station motion](image)

Fig. 1.6: Traction vehicle trajectory, tractive effort and power for station-to-station motion

This duty cycle makes requirements, for example, nominal torque of the traction motor should be sufficient to achieve the specified acceleration on the maximum slope. DC separately excited, synchronous and induction motors are all suitable for traction. Table 1.2 compares different motors regarding to the traction duty cycle.

<table>
<thead>
<tr>
<th>Regime</th>
<th>DC separately excited</th>
<th>AC induction</th>
<th>AC synchronous</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant torque</td>
<td>Constant armature current (increase voltage with speed)</td>
<td>Constant flux (increase voltage with frequency)</td>
<td>Constant armature current (increase voltage with speed)</td>
</tr>
<tr>
<td>Constant power</td>
<td>Reduced field excitation with constant armature current</td>
<td>Constant voltage and current with increasing slip frequency</td>
<td>Reduce field excitation</td>
</tr>
<tr>
<td>Reduced power</td>
<td>Weak field operation with reduced armature current</td>
<td>Constant slip frequency and voltage</td>
<td>Same as constant power</td>
</tr>
</tbody>
</table>

Table 1.2: Comparison of machines by traction duty cycle
1.3.2 Traction motors comparison

Performance guide regarding traction duty cycle only is; however, not sufficient for motor evaluation. Some other factors below make differences between DC, AC induction and AC synchronous traction motors:

- Current supply: Power to a DC motor is supplied through a commutator with a sliding contact, this reduces volume available for energy conversion, limits speed and hence power density, additional losses and increases maintenance cost

- Efficiency: The induction motor is limited by low power factor and high slip at low speeds leading to low efficiency

- Thermal aspect: Both DC and wound field AC synchronous motors, temperature rise happens in both insulated windings in stator and rotor; hence, more cooling required. Meanwhile, AC induction motor is capable to reach higher temperature due to the uninsulated rotor whose temperature limited by the bearing

- Mounting: The mounting space for DC and wound field AC synchronous motors are further limited by commutators or slip rings.

However, if permanent magnets are used for the field excitation, thermal problem due to rotor windings and mounting constraint related to commutator/slip ring could be removed.

The comprehensive comparison between different types of traction motor is a tricky task when considering other factors such as manufacturing cost and power electronic drive. Table. 1.3 [15] presents a comparison between DC, synchronous and induction traction motors in term of power and speed range.

<table>
<thead>
<tr>
<th></th>
<th>DC</th>
<th>Synchronous Induction</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum power [MW]</td>
<td>2.2</td>
<td>6.55</td>
</tr>
<tr>
<td>Speed range at 2.2 MW [rpm]</td>
<td>940 - 1435</td>
<td>670 - 2000</td>
</tr>
</tbody>
</table>

This general comparison reveals advantages of synchronous traction motor over DC and induction counterparts. With field flux created by PMs instead of field windings, synchronous motors even further make an efficiency improvement and a more compact volume. Although, a conventional PM synchronous motor would have a difficulty controlling air-gap flux but this would be tackled by additional field winding as will be discussed later in this thesis.
Conclusion

This chapter has focused on a brief history of railway traction. Various types of traction motor are discussed with their advantages and disadvantages. Although induction motor has a long development history and hence currently is the most popular choice but permanent magnet synchronous motors through years appear as a very promising candidate especially PM cost is being reduced if ferrite PMs are used instead of rare earth ones. In the next chapter, a special type of permanent magnet machine will be focused which is expectedly to be an energy efficient solution for the railway traction.
Chapter 2

Double Excitation Synchronous Machines (DESMs)

In chapter 1, various traditional traction motors have been briefly presented including DC, induction and synchronous motors. In this chapter, one type of machine which is expected to be a good candidate for traction applications. This machine, namely Double Excitation Synchronous Machines (DESMs), belongs to the synchronous type with a special configuration. This chapter aims at reviewing the stage-of-art of DESMs. The basic working principle of the machine as well as different classifications will be presented. Potential advantages of DESMs in railway traction will be discussed and finally a prototype will be adopted for further analysis in this thesis.

2.1 Basic working principle of a DESM

A classical type of wound field synchronous machine (WFSM) has been replaced by permanent magnet synchronous machines (PMSMs) in applications requiring high power density and high efficiency. Especially in a context that permanent magnet (PM) price has become reasonable. However, the problem related to PMSMs is the fact that flux created by PMs are almost fixed. Therefore it becomes disadvantageous to applications where air-gap flux control is desirable. Meanwhile, this flux control is easy to tackled with WFSMs. An idea to give a PMSM a good capability of air-gap flux control or in other word, to combine both advantages of WFSMs and PMSMs has given a birth to DESMs. Therefor, a DESM basically proposes additional excitation windings in a permanent magnet synchronous motor (PMSM) [16–19]. As a result, two flux sources are presented in one machine: one from PMs and the other from field windings. Although many variants would be realized but the fundamental working principles are based on flux sources combination: series and parallel principles.

2.1.1 Series DESM principle

In a series configuration as shown in Fig. 2.1, flux created by field winding passes through PM; hence, the series type. By changing field current, the flux in the air-gap is varied accordingly.
The most important advantage of the series excitation circuit variant is the simplicity and the global reduction of the flux density. In this specific example, air-gap flux is being weakened owing to opposite trajectories of two flux sources. Considering a field winding of \( N \) turns carrying a DC current \( i \) and hence a magnetomotive force \( Ni \) is presented, the air-gap flux is the linear sum of flux created by field winding and PM \( (\phi_{PM}) \) (if saturation is neglected) as (2.1):

\[
\phi = \frac{Ni}{R_a + R_{PM} + R_c} + \phi_{PM}
\]  

(2.1)

where \( R_a \) and \( R_{PM} \) are reluctance of air-gap and PM respectively. \( R_c \) is all other reluctance on the flux paths created by field winding.

Obviously, flux by field winding is much limited by reluctance of PM which is usually big and much bigger than \( R_a \) and \( R_c \), so controlling air-gap flux by series principle is not quite effective. Also a risk of demagnetization is likely to occur since flux from field winding must pass through PM. A case study for this series type is demonstrated in Fig. 2.2. With a PM of 15 mm thickness (in the magnetization direction), and residual flux density \( B_r = 0.4 \) T. A field winding of 1500 AT. As seen, the air-gap flux is almost canceled out in this case.

![Series combination of flux sources](image)

Fig. 2.1: Series combination of flux sources

![Induction distribution for a series type.](image)

(a) By field winding.  
(b) By PM.  
(c) Flux combination

Fig. 2.2: Induction distribution for a series type.  
(a) By field winding.  
(b) By PM.  
(c) Flux combination

Thesis K. HOANG
2.1. Basic working principle of a DESM

2.1.2 Parallel DESM principle

With the parallel principle, PM does not suffer flux from field windings; therefore demagnetization phenomenon is avoided. This principle is demonstrated in Fig. 2.3 with flux in the air-gap “A” being reinforced due to the same trajectories of two flux sources. For this parallel type, there is no PM reluctance $R_{PM}$ in (2.1) therefore field winding become more effective in controlling air-gap flux. Induction distributions for this case are demonstrated in Fig. 2.4. With a PM of 15 mm thickness (in the magnetization direction), and residual flux density $B_r = 0.4$ T. A field winding of 500 AT (only one third of one in the series case).

![Fig. 2.3: Parallel combination of flux sources](image)

(a) (b) (c)

![Fig. 2.4: Induction distribution for a parallel type. a) Due to field winding. b) Due to PM. c) Due to flux combination](image)

The key advantage of this parallel principle is that it overcomes disadvantages of the series type i.e. demagnetization and low efficiency of air-gap flux control. Moreover, this potentially has more configurations could be realized compared to the series one. This is explained by more possible flux trajectories from field winding compared to series case (flux must pass through PM). Certainly, this flexible would result in more complex structures compared to series counterparts.

Another principle which is worth mentioning is juxtaposed circuits displayed in Fig. 2.5, [20]. This type of structure could be considered as parallel comprising two rotors placed together.
Chapter 2. Double Excitation Synchronous Machines (DESMs)

The stator consists of two longitudinal regions magnetically separated from each other by a stator gap having one or more cooling air passages.

In the rotor combination, one rotor is wound type and the other is PM type. In fact, the flux control is not implemented by reducing air-gap flux in the PM rotor part, overall flux is reduced by creating a flux on the wound rotor opposite to that of PM rotor. The flux control is therefore global. One important point discussed in [21] is the axial length of wound rotor is longer than that of PM one due to the fact that flux created by PMs is normally bigger compared to winding with the same axial length. Therefore, in order to reduce global air-gap flux, two available options are: use less current with more axial length or more current with shorter length. The first option results in a lower copper loss compared to the second one.

2.2 Literature review of DESM topologies

The double excitation principle allows a wide variety of structure to be realized. The classification of this machine type could be based on:

- 2-D and 3-D types: This is based on the flux paths are limited to only a 2-D plane (the plane perpendicular to the machine’s axis) or extended in the axial direction.

- Series and parallel types (as discussed in 2.1)

- Radial and axial types: Based on air-gap flux is flowing in the radial or axial directions.

- Locations of field winding and PMs: Both sources could be located either in the stator or rotor, or one is placed on the rotor and the other is on the rotor. Placing both field windings and PMs on the stator which is a fixed part would present some advantages from manufacturing and operating points of view, for example avoiding sliding contact, it is also far easier to evacuate losses from fixed parts in comparison with moving ones. Although having both flux sources in the stator together with the armature windings would take
2.2. Literature review of DESM topologies

up a lot of space and active stator core is reduced consequently. As a result, saturation is likely to occur.

- Global and non-global excitation windings: with the global type, windings are normally in toroidal shapes wrapping around the periphery of the machine. The air-gap flux is adjusted globally, normally one or two windings are enough. With non-global type, many excitation windings are usually concentrated around teeth, each winding acts locally on air-gap flux in its region.

These classifications are not independent i.e. a 2-D type could be series or parallel, etc. More details with some specific structures will be addressed in the following.

2.2.1 General review

In [22], authors presented a structure with consequent-pole for a 3 kW generator. As shown in Fig. 2.6. This topology belongs to the 3-D parallel type due to the presence of flux in axial direction. This 3-D flux distribution introduces extra losses and increases material and manufacturing requirements [22]. The field winding is set on the stator while PMs are on the rotor.

![Fig. 2.6: Consequent pole PM machine](image)

In this topology, field flux flows from one iron pole to the next pole through the stator and rotor yoke. Magnetizing and demagnetizing effects are shown in Fig. 2.7. The advantage of this topology is a simple DC current control with no brushes or slip rings required.

Radomski [23] introduced a claw-pole DESM for an alternating current generator. The rotor is shown in Fig. 2.8a) and its circuit principle is shown in Fig. 2.8b). In this topology, the field coil is placed on the rotor connected to slip rings. PMs are also put on rotor and each PM is interposed between and in contact with side surfaces of adjacent poles. When the field coil is not excited, PMs are short-circuited by the rotor and flux developed by PMs does not link the armature windings. When the field coil is energized with an uni-directional current, the magneto-motive force of the field coil opposes the one of PM and thereby causes PM flux to cross the air-gap and link the armature windings.
Chapter 2. Double Excitation Synchronous Machines (DESMs)

Fig. 2.7: Operations of the consequent pole PM machine. a) Magnetizing effect of field flux. b) Demagnetizing effect of field flux

One special variant of DESM topology with variable number of pole pairs was presented in [24] with the topology principle is displayed in Fig. 2.9. When the excitation windings are not energized, the number of machine’s pole pairs is due to permanent magnets which is 3 and the flux linked to stator windings is minimum. However, when being supplied with currents, these excitation windings will create additional pole pairs to be double i.e. 6 pole pairs.

This machine configuration belongs to the parallel type since flux generated by field windings does not pass through PMs. Also the flux control is global due to the fact that the main flux paths from two sources (PMs and field windings) does not affect each other locally. With this type of DESM, field windings must be placed on the rotor causing a problem with sliding contacts. Another topology with similar working principles are presented in [25].

An application of DESM with axial-gap prototype was discussed in [26] is also presented in Fig. 2.10. This axial flux machine comprises two stators and one rotor which has permanent magnets and pole portions. Without the frame, PM flux closes its path through air-gap, teeth,
2.2. Literature review of DESM topologies

Fig. 2.9: DESM with variable number of pole pairs

Yokes and rotor poles. A field coil is not placed neither on stator nor rotor but mounted to the housing and located very close to the rotor. The frame acts as a magnetic path to conduct field coil flux. When the field coil has no current supplied, the PM flux closes its path through the frame. To prevent flux going through the frame, the control current in the field coil produces a countering magneto-motive forces compared to ones from PMs. In the weakening mode, field coil generate flux aiming to reduce flux going through rotor pole.

Fig. 2.10: Double excitation principle with axial flux machine

Working based on the idea similar to one using dual rotors presented in Fig. 2.5, authors of [27] proposed a parallel DESM with combination of a variable reluctance machine and a PMSM. The two sections or the machine is seen in Fig. 2.11.

In this prototype, the field windings are naturally wound on the stator of the electrical excitation section. In order to combine two different sections; theoretically, the number of teeth and slots is equal for both sections. Moreover, the numbers of rotor poles in two sections are the same [27]. The core length ratio between two sections should be taken into a careful consideration at least at a point that the stack length of the section with field winding should be large for a efficient field regulation. In contrast, the stack length of PM section is desirable as large as possible to improve the power density.
Chapter 2. Double Excitation Synchronous Machines (DESMs)

Fig. 2.11: Dual rotor combination in a parallel DESM. a) Electrical excitation section. b) PM section

Fig. 2.12: DESM with surface PM type

Another structure also could be explored as in [28] with surface PM type i.e. less efficiency of field windings because of a large equivalent air-gap. The topology principle is demonstrated in Fig. 2.12.

2.2.2 DESMs developed in SATIE laboratory

The rest of this part will be dedicated to some topologies have been developed in SATIE laboratory. Double excitation principle was applied to a flux switching machine introduced in [29] as illustrated in Fig. 2.13.

Both excitation sources are located in the stator and the salient rotor is simply made of stacked soft iron sheets. The operation principle is briefly explained as in Fig. 2.14. This prototype is proposed to be employed to make a high speed motor, or motor for difficult thermal environment [29].

Another topology developed in SATIE which is composed of two magnetically isolated parts was presented in [21]. The split view of the structure is seen in Fig. 2.15.

The stator consists of two identical parts linked together, the rotor consists of two parts: one comprises ferrite magnets (with flux concentration principle) and two teeth and the other being
2.2. Literature review of DESM topologies

Fig. 2.13: DESM with flux switching permanent magnet machine

Fig. 2.14: Working principle of hybrid flux switching permanent magnet machine. a) Enhanced field. b) Weakened field

Fig. 2.15: Imbricated DESM principle

According to [21], this topology not only avoids the risk of demagnetization due to the excitation winding but also the risk of demagnetization due to the armature reaction since the flux of armature reaction does not go through the magnet zone. Based on the implicated principle, a
machine was sized firstly to serve as a car generator as seen in the Fig. 2.18. Authors of [21] suggested the best method of flux weakening is a combination of armature current control and hybrid excitation.

In a research to study the suitability of DESM for vehicle traction applications, authors of [16] worked on a bipolar configuration as in Fig. 2.19 to confirm the advantage of energy efficiency of the double excitation principle. Flux trajectories of the machine are somewhat complex and some are truly 3-D with the homopolar flux paths by PMs displayed in Fig. 2.20.

In this prototype, the blue parts are made of laminated iron sheet and the yellow ones are solid to conduct 3-D flux. Due to the 3-D flux path characteristic, considerations for materials and iron losses should be considered. Another similar variants of this topology were also presented in [30,31] with modifications.
2.3 Efficiency advantage of DESMs

The main advantage of the DESM appears especially in those applications where the electric drives operate under partial loads most of the time. For such applications, the electric motor should not only have the highest efficiency at a given partial load, but should also be able to operate at full load conditions. Unlike classical machines (induction, dc, synchronous), where these requirement are quite difficult to achieve, DESMs, thanks to their hybrid excitation field topology, are able to satisfy these specifications. Frankly, a comprehensive comparative study for comparisons between DESMs and other types of traction motor is a quite challenging task since it requires various factors to consider such as cost, weight, available technology, system being used, etc. Among these factors, a good efficiency should be a priority for every electrical motor used in a traction system. At this early stage, a focus on highlighting advantage of DESMs regarding the efficiency will be presented.

Generally, an efficiency map constitutes a convenient way to assess motor design. Efficiency maps are sketched by isolines of efficiency, it gives an idea about the torque/speed combinations at which a specific motor drive is efficient. An efficiency map of a PMSM is shown in Fig. 2.21 [32] as an example. In most industrial applications, motors usually operate at one or a few predefined
operating points. Therefore, motors could be optimized to have the best performances at these specific points, and the efficiency of the system is well defined [33]. However, it is not the case in propulsion applications such as railway traction where traction motors are expected to perform well in a wide range of torque-speed combination.

![Efficiency map of a PMSM motor with superimposed sampled operation points of a typical drive cycle](image)

Fig. 2.21: Efficiency map of a PMSM motor with superimposed sampled operation points of a typical drive cycle

Remarked in [34], by a proper control of field current in a DESM and hence the air-gap flux, the torque-speed characteristic can be easily shaped to meet the special requirements. Also, the efficiency map of the motor drive can be optimized throughout the whole operating range. Thus, the efficiency at those operating regions can be improved. As mentioned in [35], using auxiliary field winding to control the speed, the flux density and iron losses are reduced in all motor active parts and as a result an efficiency improvement at wide speed range is achieved. Authors of [35] also pointed out that efficiency of a DESM in a wide speed operation can be improved by control strategy combination: As the motor reaches the rated operating point, a higher speed is obtained through the negative $d$-axis armature current procedure, then at a certain value of $d$-axis current, the speed increase is continued by field current injection resulting in a global improved efficiency.

Research done in [16] emphasized advantageous feature of a DESM for vehicle propulsion with higher efficiency compared to a PM and a WFSM motors. Traction motors should have maximum efficiency at the most frequently used operating points. Firstly, a separate comparison between PM and WFSM in term of efficiency map is discussed. Fig. 2.22 [16] draws an efficiency map comparison between a PM motor and a WFSM one excluding mechanical losses and static converter efficiency. As it can be seen, under the base speed, both machines reveals the same maximum efficiency. At high speed; however, PM machine has a lower efficiency that that of WFSM due to a high $d$-axis current required for flux weakening [33]. WFSM also possesses a better speed range due to the easy of reducing flux compared to the PM case.

In comparison with a PM machine, some DESM topologies are expected to have extended operating area as for a WFSM with the maximum efficiency as same as one of a PM machine. With a combination between PM and WFSM is characterized by a coefficient, namely hybridization.
2.3. Efficiency advantage of DESMs

Fig. 2.22: Efficiency maps. a) PM motor. b) Wound field synchronous motor

ratio $\alpha$ defined as (2.2) [16]

$$\alpha = \frac{\Phi_a}{\Phi_{\text{max}}}$$  \hspace{1cm} (2.2)

where $\Phi_a$ is PM flux linkage and $\Phi_{\text{max}}$ is maximum value of the total excitation flux. $\alpha = 0$ corresponds to the WFSM case and $\alpha = 1$ corresponds to the case where field windings are only for flux weakening but not flux enhancing mode. By adjusting this value, it is possible to shift a high efficiency area into the desired (torque, speed) area. This would significantly increase vehicle range due to energy consumption saving [36]. The studied machine in this research is shown in Fig. 2.19, hybridization ratio is adjusted as $\alpha \approx 0.72$ (both flux weakening and enhancing are available) and $\alpha = 1$ (weakening only). Experiments of efficiency map for these two cases are demonstrated in Fig. 2.23 [16].

As it can be observed in Fig. 2.23, when hybridization ratio changes from 0.72 to 1, the highest
efficiency zones are shifted to a higher values of normalized torque.

After all things considered, obviously DESM type could be suggested as a very good candidate for traction applications with flexible operation in flux weakening as well as flux enhancing mode. Also, its energy efficiency is very promising. However, to comprehensively evaluate its performance, more details should be taken into account i.e. its performance in the whole system. In the last section of this chapter, a prototype of DESM will be chosen as the analysis model in the thesis.
2.4 DESM prototype for analysis

In SATIE laboratory, a group of DESM topologies with similar configurations has been developed one of them were already shown in Fig. 2.19. Authors of [30] also presented a work related to this topology group. In detail, three prototypes with power rating of 3 kW will be presented. Two of them are modular; therefore an easy assembly could be made to have different configurations: homopolar and bipolar. Shortly, three prototypes possess identical stators, the difference lies on the rotor parts.

2.4.1 Configurations of different prototypes

This part will briefly summarize work of [30]. Schematic of the first prototype is sketched in Fig. 2.24, corresponding 3-D topology and experimental photo are seen in Fig. 2.25 and Fig. 2.26 respectively. This first topology belongs to the parallel type with two global field windings placed on the stator and PMs are located on the rotor. In order to increase air-gap flux density, flux concentration principle is applied by using side PMs together with azimuth ones as shown in Fig. 2.24. Therefore, PMs with low residual flux density hence low cost could be used. In this case, ferrite PMs are equipped ($B_r = 0.4$ T).

![Fig. 2.24: Schematic of the first prototype](image)

The rotor consists of two parts which are magnetically insulated: solid and laminated ones. Due to the existence of some truly 3-D flux paths in the machine (will be explained later in this part), solid material for external stator yoke and end-shield parts are adopted to conduct flux created by field windings (This is also the reason for the solid core part in the rotor). Specifications of the first prototype are detailed in Table. 2.1. These specifications are applied mostly to the second and third prototypes except a slight modification are made. Schematics of the second and third prototypes are correspondingly shown in Fig. 2.27 and Fig. 2.28.

Compared to the rotor of the first prototype, side PMs are removed in these two rotors. In
addition, these two rotors are modulated resulting in easy changes in their assemblies to have homopolar of bipolar configurations [30]. One should be noted that if rotating one solid rotor core (for example the lower green part) of rotor in Fig. 2.27b) by one rotor pole, it will turn into the bipolar configuration as seen in Fig. 2.28b). A more detailed difference between these two rotors lies on the laminated rotor cores as displayed in Fig. 2.29. An inner ring is introduced in the laminated rotor part of the third prototype (Fig. 2.29b)) made it simpler compared to that of the second prototype from the construction point of view. However, this in turn increases flux leakage from PMs leading to lower performance.
Table 2.1: Specifications of the first prototype

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of phases</td>
<td>3</td>
</tr>
<tr>
<td>Number of turns per phase</td>
<td>33</td>
</tr>
<tr>
<td>Number of turns per field winding</td>
<td>150</td>
</tr>
<tr>
<td>Number of pole pairs</td>
<td>6</td>
</tr>
<tr>
<td>Motor length</td>
<td>115 mm</td>
</tr>
<tr>
<td>Outer stator diameter</td>
<td>184 mm</td>
</tr>
<tr>
<td>Air-gap diameter</td>
<td>114.5 mm</td>
</tr>
<tr>
<td>Number of slots</td>
<td>36</td>
</tr>
<tr>
<td>Air-gap length</td>
<td>0.5 mm</td>
</tr>
<tr>
<td>PM residual flux density</td>
<td>0.4 T (ferrite PM)</td>
</tr>
<tr>
<td>Based speed</td>
<td>2000 rpm</td>
</tr>
<tr>
<td>Rated power</td>
<td>3 kW</td>
</tr>
</tbody>
</table>

Fig. 2.27: Second prototype with homopolar configuration. a) Schematic. b) Rotor

2.4.2 Comparisons between prototypes

Owing to similar topologies between prototypes and hence similar operation principles. The first prototype will be taken as the representative for the working principle explanation.

2.4.2.1 Homopolar and bipolar flux paths

The double excitation principle creates somewhat complex flux paths in some circumstances especially in cases with operation principle due to flux paths appears in different planes i.e. three dimensional. In these configurations, two kinds of flux path are presented by both PMs and field windings: homopolar and bipolar paths [30,37]. Simply, homopolar flux paths create
only one type of pole (north or south) under the active part. Meanwhile, bipolar flux paths create north and south poles under the active part. Field windings only generate homopolar flux paths and PMs could have both types. The bipolar flux paths are illustrated in Fig. 2.30. The homopolar flux paths that are more complex are illustrated in Fig. 2.31.

![Bipolar flux paths created by PMs](image)

**Fig. 2.30:** Bipolar flux paths created by PMs
counter-effective flux as in Fig. 2.31c). The effective flux plays the key role for air-gap flux regulation. Meanwhile, counter-effective flux tends to extenuate the the function of effective flux since it generates opposite flux trajectories. For example in the flux enhancing mode, while the main flux from field windings are acting on the unconcentrated flux area to increase air-gap flux, the counter-effective flux are passing through PM in demagnetized direction and they certainly tend to cancel out homopolar flux created by PM i.e. producing a counter-effect. It happens quite similarly in the flux weakening mode except that PMs are not demagnetized as counter-effective flux reverse their directions. Even though the counter-effective flux is generally small compared to main flux because it has to pass through PMs but when the magnetic path of main flux becomes saturated (at highly positive values of field current), any further increase of field current will turn field winding flux into counter-effective, in that situation global flux will reduce.

Due to the presence of these homopolar flux paths, the armature winding arrangement (concentrated or distributed - the case being studied) will affect the its flux linkage distribution in which a DC component may or may not exist. To explain this, aligned and unaligned rotor positions will be examined. Fig. 2.32 shows the case with concentrated windings and homopolar flux paths by side PM (other homopolar flux path type are similar). In direction perpendicular to the paper plane, the armature winding is stacked above. The flux by homopolar path due to the lower side PMs linked armature winding will be in clockwise direction. For the upper side PMs, this will be in counter-clockwise direction. Because of the concentrated arrangement,
these two flux will add up together. At the unaligned position, the flux linkage (usually zero for a classical machine) is shifted by a DC component due to the fact that the armature winding still overlaps a part of side PMs as seen in Fig. 2.32a). At the aligned position, flux linkage will be maximum due to side PMs are entirely overlapped by armature windings as seen in Fig. 2.33. To summarize, an illustrative flux linkage distribution is seen in Fig. 2.34.

Fig. 2.32: 2-D Illustrative homopolar flux paths by side PMs with concentrated winding

![Illustrative homopolar flux paths by side PMs with concentrated winding](image)

Fig. 2.33: A homopolar flux type created by side PMs with concentrated winding. a) 1st alignment. b) Unalignment. c) 2nd alignment

![A homopolar flux type created by side PMs with concentrated winding](image)

Fig. 2.34: Illustrative phase flux linkage with concentrated winding

![Illustrative phase flux linkage with concentrated winding](image)

The case with a distributed armature winding will be seen in Fig. 2.35. Linked homopolar flux paths by side PMs are seen in Fig. 2.36.

It can be seen that at the 1st aligned position, the flux linked by lower side PMs is maximum whereas one by upper side PMs is zero. At 2nd aligned position in Fig. 2.36a), flux linkage is
2.4. DESM prototype for analysis

Fig. 2.35: 2-D Illustrative homopolar flux paths by side PMs with distributed winding

reversed with the zero flux linked by lower side PMs and maximum flux linked by upper side PMs. At the unaligned position in Fig. 2.36c), flux linked by upper and lower side PMs will cancel out each other due to the overlapped areas by armature winding for upper and lower PMs are the same and flux direction is reversed as shown in Fig. 2.36b). So that for the distributed arrangement, no DC component is presented in the flux linkage waveform.

Fig. 2.36: A homopolar flux type created by side PMs with distributed winding. a) 1st alignment. b) Unalignment. c) 2nd alignment

2.4.2.2 A comparison regarding flux control range characteristic

A distinguishing feature of a DESM is air-gap flux control capability. Therefore, a comparison with regard to this characteristic will be examined and on the basis of that analysis, a prototype will be chosen for the further study in this thesis. Also some more factors would be discussed. As mentioned earlier, the second and third prototypes would be modified leading to two configurations: bipolar and homopolar. The experimental result in Fig. 2.37 will show maximum flux per turn with respect to field current in both operation modes: flux weakening and flux enhancing.

As clearly seen, second prototype owns higher flux compared to the third one, this is due to the inner ring introduced in the third prototype making azimuth PM short-circuited and flux linkage is therefore reduced. Though this ring facilitates the fabrication of the rotor core.
In comparison with the bipolar configuration, the homopolar one has a better performance with field current varies in a small range around zero but it is more highly saturated when field current reaches high. Although two configurations have a same field weakening capability. This is explained by the fact that with homopolar configuration, field current does not act evenly on rotor magnetic poles i.e. one pole would be saturated while the other would not. For bipolar configuration, saturation occurs at the same time for both magnetic poles. For that reason, bipolar will have a wide range of flux variation [30].

A detail comparison for different curves in Fig. 2.37 are shown in Table. 2.2 with slopes are calculated for the linear range around zero field current area.

### Table 2.2: Flux control curve characteristic of different machines

<table>
<thead>
<tr>
<th>Machine prototype</th>
<th>Max. flux [mWb]</th>
<th>Min. flux [mWb]</th>
<th>Flux range [mWb]</th>
<th>Slope [mWb/A]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1st</td>
<td>4.3</td>
<td>1.0</td>
<td>3.3</td>
<td>0.36</td>
</tr>
<tr>
<td>2nd (homopolar)</td>
<td>4.3</td>
<td>1.1</td>
<td>3.2</td>
<td>0.23</td>
</tr>
<tr>
<td>2nd (bipolar)</td>
<td>5.1</td>
<td>1.1</td>
<td>4.0</td>
<td>0.22</td>
</tr>
<tr>
<td>3rd (homopolar)</td>
<td>3.5</td>
<td>1.4</td>
<td>2.1</td>
<td>0.19</td>
</tr>
<tr>
<td>3rd (bipolar)</td>
<td>4.7</td>
<td>0.7</td>
<td>4.0</td>
<td>0.23</td>
</tr>
</tbody>
</table>

Regarding the flux control effectiveness, the first prototype exhibits the most efficient solution since the slope of flux variation is biggest i.e. to achieve same flux (either increase of decrease), the first prototype requires a smaller amount of field current leading to a smaller copper loss. This highest slope is due to the use of solid core in the first prototype for the reluctance path of flux created by field windings, while other prototypes utilize laminated cores.
2.4. DESM prototype for analysis

Regarding the flux control range (difference between maximum and minimum flux), bipolar configurations show the best feature among all prototypes and the 2\textsuperscript{nd} prototype is even better than the 3\textsuperscript{rd} one with higher flux level. Even though the 2\textsuperscript{nd} bipolar prototype has the maximum flux of 0.8 mWb higher compared to one with the 1\textsuperscript{st} prototype but it requires too much field current (9 A more) causing much copper loss and temperature increased as well.

Due to this dominance in flux control over the others, the first prototype will be chosen for a further investigation. In the next part, more analysis result done by 3-D FEM will be conducted.

2.4.3 3-D FEM analysis of the first prototype

This part performs a more detailed analysis of the first prototype. Due to a 3-D flux path characteristic, a 3-D FEM is necessarily required. In this study, 3-D FEM ANSYS Maxwell will be employed. Thanks to the symmetry property, only one pole pair (corresponds to 60 mechanical degree) will be analyzed. Periodic boundary condition is used to ensure the magnetic vector potential are exactly the same on the boundary surfaces. To begin, Fig. 2.38 shows the B-H magnetization curve for the FeSi core material at 50 Hz.

![B-H characteristic of a 0.35 mm FeSi lamination](image)

Fig. 2.38: B-H characteristic of a 0.35 mm FeSi lamination

3-D mesh for a part of the motor is presented in Fig. 2.39 with about 60,000 elements. Unlike some other solutions, for example in [38] the 3-D mesh is derived from an extrusion of a 2-D mesh, the mesh created in Maxwell program is truly 3-D.

![3-D mesh of a part of the studied prototype](image)

Fig. 2.39: 3-D mesh of a part of the studied prototype
Owing to one pole pair corresponding to 60 mechanical degree, 60 points with a step of one mechanical degree will be analyzed. An interesting point is that for quantities related to winding such as current, back electromotive force (EMF), analysis data for one sixth of one pole pair is enough because of winding symmetry i.e. data could be deducted from the first one sixth. Thus saving computation time if only winding quantities are calculated. This is explained as follows:

Without loss of generality, one could assume:

\[
\begin{align*}
x_a &= X \sin(\omega t - 2\pi/3) \\
x_b &= X \sin(\omega t + 2\pi/3) \\
x_c &= X \sin(\omega t)
\end{align*}
\] (2.3)

where \(x\) represents phase quantities (current, voltage, etc.), \(X\) is the amplitude, \(t\) is the time variable. If quantity \(x\) is equally divided into 6 periods: \(\{x_1, x_2, ..., x_6\}\). Then quantities for \(x_i\) \((i = 2 \div 6)\) could be deducted from \(\{x_{a(1)}, x_{b(1)}, x_{c(1)}\}\) such as (2.4):

\[
\begin{align*}
x_{a(2)} &= -x_{b(1)} & x_{a(3)} &= x_{c(1)} \\
x_{a(4)} &= -x_{a(1)} & x_{a(5)} &= -x_{a(2)} & x_{a(6)} &= -x_{a(3)}
\end{align*}
\] (2.4)

Flux density distribution is displayed in Fig. 2.40 at no-load condition and field windings are not excited \((I_{dc} = 0)\). The effect of homopolar flux paths could be observed in this map that the flux densities in the stator teeth (let’s say teeth-1 group) facing the concentrated flux area are higher than others (teeth-2 group). However, when exiting field windings with a current of 3 A (enhancing). Field winding will increase flux densities in teeth-2 group and at the same time reduce ones in teeth-1 group due to counter-effective flux as discussed in 2.4.2.1.

### 2.4.3.1 PM demagnetization examination

Even though this DESM prototype belongs to parallel type since the main effective flux (flux to intentionally adjust air-gap flux) from field winding does not pass though PMs leading to a general statement that a parallel configuration could avoid a risk of demagnetization. However,
2.4. DESM prototype for analysis

Fig. 2.41: Flux density distribution at aligned position, no-load, $I_{dc} = 3$ A

in this case demagnetization still occurs due to the counter-effect flux paths created by field windings (discussed in 2.4.2.1), passing through PMs in demagnetizing direction in the flux enhancing mode. This could be considered as an “unintentional demagnetization”. This is more risky when the magnetic paths of the main flux are saturated, all further increased flux will become counter-effective and make demagnetization worse.

This could be partly observed in Fig. 2.40 and Fig. 2.41 when field current increases from zero to 3 A in the flux enhancing mode. The teeth facing the unconcentrated area approach saturation and at the same time, flux densities in teeth-1 group are reduced. In order to more elaborately examine the demagnetization effect, the flux densities in both side and azimuth PMs will be computed at their centers according to a wide range of field current as seen in Fig. 2.42. As seen, because side and azimuth PMs have same thickness (6 mm) so flux density for two kinds of PM are almost the same. Fig. 2.42 also reveals that counter-effect flux from field windings becomes stronger when increasing field current i.e. the slope increases. This is due to more and more counter-effect flux from field windings passing through PMs as explained above.

Fig. 2.42: PM demagnetization due to field winding at aligned position, no-load

At a field current of 8 A, flux densities of PMs reduce to 0.222 T which is generally higher than the knee point of commonly used ferrite PMs [39]; therefore, no big danger appears. Also for
the prototype being studied, field current is not expected to be higher than values around 7 A due to the thermal limit. However in cases when PM thickness is reduced, demagnetization risk will increase and hence a careful consideration should be made accordingly.

2.4.3.2 Flux control range examination

This part discusses air-gap flux regulation of the studied prototype in both flux weakening and enhancing modes. An example is shown in Fig. 2.43 for flux linkage and back EMF of a phase. Here back EMF is calculated by taking derivative of flux linkage with respect to time. For a good motor design, back EMF waveform must be well estimated [40]. Harmonic content of a back EMF waveform at no-load, \(i_{dc} = 0\) A is demonstrated in Fig. 2.44. As reported, 5\(^{th}\) accounts for a big portion of harmonic content, this would result in a big torque pulsation, iron loss. However, discussion about this influence is currently not an objective.

\[
\begin{align*}
\text{Flux linkage [Wb]} & \\
0 & 0.2 & 0.4 & 0.6 & 0.8 & 1 \\
-0.15 & -0.1 & -0.05 & 0 & 0.05 & 0.1 & 0.15 \\
\end{align*}
\]

\[
\begin{align*}
\text{Back E.M.F [V]} & \\
0 & 0.2 & 0.4 & 0.6 & 0.8 & 1 \\
-15 & -10 & -5 & 0 & 5 & 10 & 15 \\
\end{align*}
\]

Fig. 2.43: Air-gap flux control at no-load due to field current variation. a) Phase flux linkage. b) Phase back EMF at a speed of 170 rpm

Obviously, due to a certain change in field current, the linked flux will alter accordingly and hence its back EMF. With a change of 3 A corresponding to 900 AT (two field windings and 150 turns per each), the maximum flux changes by 36 mWb. In order to further explore flux control capability, a wide range of field current will be utilized. For this purpose, the maximum flux
2.4. DESM prototype for analysis

Fig. 2.44: Back EMF harmonic content at no-load, \( i_{dc} = 0 \) A

per turn will be computed as illustrated in Fig. 2.45. As it will be seen, three regions appear. The first region corresponds to a very negative field current, this causes end-shield saturated as in Fig. 2.46a) as all homopolar flux paths going in the same direction through end-shield and add up together leading to no change in both main and counter-effect flux from field windings and global flux would stay unchanged.

Fig. 2.45: Maximum flux at no-load according to field current variation

The second region corresponds to the linear range as in Fig. 2.40 or Fig. 2.41 where the trend follows the change in the main flux from field winding. The last region corresponds to highly positive field current, this causes saturation of magnetic paths for main flux from field winding as in Fig. 2.46b) hence no increase for that. Any increase in field current will increase counter-effect flux and hence, global flux decreases. This counter-effective flux seems to be a drawback. However, this is not a big problem since the points beyond the maximum are not of interest.

2.4.3.3 Torque calculation

Maxwell Stress Tensor (MST) and virtual work principle are two most common methods used to compute electromagnetic torque. MST method calculates torque acting on a rigid body.
Fig. 2.46: Induction distribution at aligned position, no-load (B-H magnetization curve saturates at 1.8 T). a) Field current $I_{dc} = -8$ A. b) Field current $I_{dc} = 8$ A

expressed as (2.5) \[41,42\]

$$T_e = \oint_S r \times \sigma dS = \oint_S r \left\{ \frac{1}{\mu_0} (B.n)B - \frac{1}{2\mu_0} B^2 n \right\} dS$$

(2.5)

with $r$ is the radius of the surface $S$, $\sigma$ is the stress tensor, $B$ is the magnetic flux density, $n$ is the unit normal vector of the integration surface and $\mu_0$ is permeability of the air. A closed integration surface that surrounds the rotor in free space must be chosen. For a two dimensional electromagnetic field models (for a majority of motors), the surface integral is reduced to a line integral along the air-gap, (2.5) then becomes (2.6)

$$T_e = \frac{L}{\mu_0} \int_0^{2\pi} r^2 B_r B_\theta d\theta$$

(2.6)

with $L$ is the active length of the motor, $B_r$ and $B_\theta$ are the radial and tangential components of flux density $B$.

From (2.6), it may be noted that only the flux densities on the integration contour are employed which allows for simple and quick calculations. As remarked in [41], MST method owns several advantages such as the field computation is required once, the choice of the surface $S$ is arbitrary, provided that no medium other than empty space is crossed (a good practice is that the surface $S$ should pass through nodes in the region where the mesh does not change). However, MST method is prone to the mesh discretisation [43–45]. In order to achieve a good accuracy, an appropriate mesh is importantly required. For the studied DESM prototype, handling a very fine 3-D mesh in the air-gap is quite a challenge as the number of elements is limited due to time and computer resources.

The virtual work method is based on the stored magnetic co-energy change or the virtual work with a small displacement. By this method, electromagnetic torque is calculated as the derivative of the magnetic co-energy $W_{co}$ with respect to angular position $\theta$ at a constant current expressed as (2.7):

$$T_e = \frac{\partial W_{co}}{\partial \theta} \bigg|_{i=\text{const}}$$

(2.7)
2.4. DESM prototype for analysis

Basically, this method requires calculations at two successive rotor angular positions and hence computation time is doubled. Moreover, it may be necessary a trial-end-error procedure to select a suitable value of the position increment, $\Delta \theta$. If $\Delta \theta$ is too small the co-energy variation will be insufficient to overcome round off error. If $\Delta \theta$ is too large, the calculated torque will no longer be accurate for the specified position [46]. But it gains an advantage due to the global information used which could avoid errors due to localised inaccuracy associated with the discretisation as with MST method.

Using the virtual work principle, the flux-MMF diagram is a generalized version of the flux-linkage versus current $(\psi - i)$ diagram used commonly for analyzing switched reluctance motors [47–50]. It plots the variation of instantaneous effective flux linking a particular phase against the instantaneous MMF of that phase. This plot is a closed trajectory over one electrical cycle indicating the average torque produced over one electrical cycle for any one phase as (2.8) [49]. The total area consists of a number of incremental areas bound by the magnetization curves at successive rotor positions and each of these areas indicates the instantaneous torque at a particular rotor position for any one phase [49].

\[
T_e = mp \frac{\Delta W_{co}}{2\pi}
\]  

(2.8)

where $m$ is the number of phases, $p$ is the number of pole pairs and $\Delta W_{co}$ is the co-energy converted per phase over an electrical cycle. In this illustrative example, four flux-MMF diagram are plotted corresponding to currents of $i = 0, i_1, i_2$ and $i_3$. The average torque at $i_3$ is reflected by the area enclosed by the biggest ellipse (yellow). Two magnetization curves are presented, $A_1A_2A_3A_4$ for position $\theta_k$ and $B_1B_2B_3B_4$ for position $\theta_{k+1}$. With an assumption that due to a very small angular difference, $A_4$ and $B_4$ are vertically the same. Therefore, the instantaneous torque at $(\theta_k, i_3)$ is reflected by the area bound by these two magnetization curves (the blue area) i.e. $S_{A_1A_2A_3A_4B_1B_2B_3B_4}$.

Important features of the flux-MMF diagram are summarized as follows [49]:

- Ability to represent many performance characteristics of a machine graphically including torque capability and torque smoothness
- Area enclosed indicates torque capability
- Shape indicates nature of excitation (ideally ellipsoidal for sinewave and rectangular for squarewave)
- Deviation from ideal shape and uneven spacing of magnetization curves indicates torque ripple and saturation

For the DESM prototype being studied, flux-MMF diagrams at different armature currents are sketched in Fig. 2.48. The torque angle is set to zero.
Chapter 2. Double Excitation Synchronous Machines (DESMs)

From this flux-MMF diagram, big torque ripple is predicted due to the uneven spacing of magnetization curves.

Average torques at different armature currents are displayed in Fig. 2.49 at zero field current and Fig. 2.50 is average torque according to variations of both armature and field currents. Thanks to the contribution of field windings, a certain torque value could be achieved by various combinations of armature and field currents; therefore, providing a solution with the best combination yielding the minimum copper loss.

Fig. 2.51 displays instantaneous torques at various armature currents with respect to rotor position. For the instantaneous torque calculation, firstly instantaneous torque is calculated for one phase by computing the incremental areas in the flux-MMF diagram bound by the magne-
2.4. DESM prototype for analysis

Fig. 2.49: Generated torque at various armature currents, non-excited ($I_{dc} = 0$)

Fig. 2.50: Average torque at various armature and field currents. a) Torque map. b) Torque contour
tization curves (the black lines inside the closed trajectories in Fig. 2.48). Then interpolations are made for two other phases by shifting angles of $\pm 2\pi/3$. The instantaneous torque is the sum of individual ones. From these torque waveform, torque ripples are calculated ranging between 30% and 40% which confirm the torque ripple prediction from flux-MMF diagram. This big torque ripple would be undesirable for low speed applications. For railway traction, this problem would be mitigated due to very high train inertia. Torque ripple could be reduced by using some geometry modification techniques such as slot opening adjustment, skewing, tooth tip shaping, etc. Moreover, it could be handled with current controlling approaches either armature or excitation currents. Despite that fact, torque ripple minimization is not the target of this research.

![Fig. 2.51: Instantaneous torque at different armature currents, ($I_{dc} = 0$)](image)

**Fig. 2.51: Instantaneous torque at different armature currents, ($I_{dc} = 0$)**

**Conclusion**

This chapter has reviewed a basis on DESMs with a number of topologies were developed. Advantages of DESMs were highlighted in terms of both flux control flexibility and energy efficiency. A prototype realized in SATIE was chosen for further study in this thesis according to its dominance in air-gap flux regulation over others. Owing to a 3-D flux path characteristic, a 3-D FEM package is required for highly accurate performance predictions. This results in a long computation time. In this specific machine simulated by 3-D Maxwell FEM package, computation time at one point takes about 58 seconds (with about 60000 tetrahedron elements). However in the early design stage, there is usually a need of a numerous model’s evaluations; therefore, this process will be incredibly time consuming if 3-D FEM analyses are used. In order to handle this task, next chapter will present a fast model for the 3-D FEM replacement.
Chapter 3

Modeling with Equivalent Magnetic Circuit Network (EMCN)

In the previous section, a DESM prototype was analyzed by 3-D FEM. Using this high fidelity model could yield accurate results; however the inherited problem with FEM (especially in 3-D cases) is time consuming [51]. In the motor design phase, an enormous number of evaluations are iteratively taken, for example an optimization process. Therefore, a model with acceptable accuracy but fast to evaluate is obviously prioritized to mitigate the burden on computation time. In contrast to FEM, equivalent magnetic circuit network (EMCN) provides a noticeable compromise between computation time and accuracy. This chapter is dedicated to the EMCN exploration and its application with the studied DESM prototype. The result accuracy and computation time advantage will be elaborated by comparisons with 3-D FEM ones.

3.1 Equivalent Magnetic Circuit Network

EMCN method has long been proven as an effective alternative tool for motor analysis with much shorter computation time while maintaining results close to ones performed by FEM [52–56]. The EMCN model has been used for electrical machine analyses such as switched reluctance motors [55], asynchronous motors [52] and permanent magnet motors [56]. Using EMCN is also advantageous over the FEM when there is a need to couple with other analyses such as thermal or acoustic ones [57]. In EMCN, two important circuit laws guiding equation system formulation namely Kirchhoff’s current law and Kirchhoff’s voltage law leading to nodal based and mesh based equations, respectively [58]. In this thesis, the Kirchhoff’s current law which is the most common method due to the ease of establishing and extending equation system compared to the latter one.

3.1.1 Nodal based EMCN formulation

To begin, some basic components of an EMCN model will be shortly recalled. Conventionally, two methods could be used with EMCN are tooth contour [59] and flux tube [60]. In this work, flux tube method which is the most popular implementation of EMCN will be employed.
Chapter 3. Modeling with Equivalent Magnetic Circuit Network (EMCN)

The flux is considered to be constant inside the tube and two ends of the tube are assumed equipotential planes as displayed in Fig. 3.1.

\[ R = \int_0^L \frac{dl}{\mu_0 \mu_r S(l)} \]  
(3.1a)

\[ P = \frac{1}{R} \]  
(3.1b)

where \( L \) is the length of the tube, \( S \) is the cross section of the tube at position \( l \), \( \mu_r \) is the relative permeability of the tube material and \( \mu_0 \) is the permeability of the air. With a tube of length \( L \), constant cross section \( S \) over the tube, (3.1a) becomes (3.2):

\[ R = \frac{L}{\mu_0 \mu_r S} \]  
(3.2)

Another important component in EMCN is the source which is either magneto-motive force source (MMF) or flux source. In fact these two sources are interchangeable i.e. a MMF with an internal reluctance \( R \) in series could be replaced by an equivalent flux source \( \phi \) connected in parallel with that reluctance as illustrated in Fig. 3.2 with \( \phi = \frac{F}{R} \).

In electrical machines, a MMF sources is usually the representation of a permanent magnet or coils carrying a current. A permanent magnet can be modeled by a reluctance connected in series with an equivalent MMF (shown in Fig. 3.2a)) as (3.3):

\[ F_{\text{pm}} = \frac{B_r h_m}{\mu_0} \]  
(3.3)

where \( B_r \) and \( h_m \) are PM thickness and residual magnetic flux density respectively.

A coil consisting of \( N \) turns carrying a current \( i \) is equivalent to an MMF expressed by (3.4):

\[ F_{\text{coil}} = N i \]  
(3.4)
With these basic components, formulation for the nodal based network could be explained by a circuit having \( n \) nodes (\( u_i \)) \((i = 1 \div n)\) demonstrated in Fig. 3.3. \( F_{ij} \) is a MMF source placed between node \( i \) and node \( j \), \( R_{ij} \) is reluctance between node \( i \) and node \( j \), hence its permeance \( P_{ij} = \frac{1}{R_{ij}} \)

![Fig. 3.3: A simple nodal based circuit](image)

Applying Kirchhoff’s current law to the magnetic circuit i.e. flux conservation law (3.5) at node \( k \):

\[
\sum_k \phi_k = 0 \quad (3.5)
\]

One could be obtained (3.6):

\[
\sum_{i=1, i \neq k}^n \frac{(u_i - u_k - F_{ik})}{R_{ik}} = 0 \quad (3.6a)
\]

\[
\sum_{i=1, i \neq k}^n (u_i - u_k - F_{ik}) P_{ik} = 0 \quad (3.6b)
\]

\[
u_k \sum_{i=1, i \neq k}^n P_{ik} - \sum_{i=1}^n u_i P_{ik} = \sum_{i=1}^n F_{ik} P_{ik} \quad (3.6c)
\]

Similarly applying for all other nodes, (3.6c) is generalized as (3.7):

\[
\begin{bmatrix}
P_{11} & P_{12} & \cdots & P_{1n} \\
P_{21} & P_{22} & \cdots & P_{2n} \\
\vdots & \vdots & \ddots & \vdots \\
P_{n1} & P_{n2} & \cdots & P_{nn}
\end{bmatrix}
\begin{bmatrix}
u_1 \\
u_2 \\
\vdots \\
u_n
\end{bmatrix}
= 
\begin{bmatrix}
\phi_1 \\
\phi_2 \\
\vdots \\
\phi_n
\end{bmatrix} \quad (3.7)
\]

with \( \phi_k \) is the sum of flux sources connected to node \( k \) expressed as the right hand side of (3.6c) and \([P]\) is the permeance matrix defined by (3.8)

\[
P_{ij} = \begin{cases} 
-p_{ij} & \text{if } i \neq j \\
\sum_{k=1, k \neq i}^n p_{ik} & \text{if } i = j 
\end{cases} \quad (3.8)
\]
Finally the nodal based system formulation can be expressed as (3.7). By solving this with an appropriate technique, scalar nodal magnetic potentials are obtained. The further iterative process dealing with nonlinear characteristic will be discussed later when applying with the DESM prototype.

3.2 EMCN model of the DESM

Regarding reluctance mesh formulation, two alternatives are proposed: lumped parameter model as in [53, 61, 62] and generalized model [63–65]. Basically, with a lumped parameter model, a small number of reluctances are presented based on main pre-assumed flux paths as a result of prior knowledge of critical flux paths of the machine. Fig. 3.4 is an example of lumped parameter model for stator doubly fed doubly salient machine [53].

![Fig. 3.4: An EMCN model by lumped parameter](image)

Whereas, by mean of generalization as will be presented, each part of the machine is divided into a mesh of elements characterized by a number of rows and columns which will be detailed in the following.

3.2.1 Basic block element

On the contrary to the lumped parameter reluctance network with a basic reluctance block of a single reluctance, with the generalized method, a very basic element of the model is reluctance block which is bi-directional i.e. flux paths in one block are assumed to only flow in 2 orthogonal directions. In this case they are radial and tangential directions. As a result, one block contains four reluctances in two directions and/or MMF depending on the magnetization exists or not the the block’s area and the center of the block is considered as node. Fig. 3.5 shows a basic block without a MMF source having width $w$, height $h$ and length $l$.
Reluctance calculations for individual components in a block are given by (3.9):

\[
R_x = R_y = \frac{w}{2hl\mu_0\mu_r} \tag{3.9}
\]

with \(\mu_r\) is the relative permeability of the block material (air, core or PM). This value is given to all reluctance components of one block.

There are four reluctances included in one block and hence four flux density values. So that there is a need to calculate an equivalent flux density \(B_{eq}\) of the block. As it will be discussed later, this flux density will facilitate the calculation of block’s permeability by using B-H magnetization curve. \(B_{eq}\) is obtained from flux density component by using energy conservation law i.e. the sum of energies in four reluctances equals energy of the block calculated with \(B_{eq}\) as follows:

Energy stored in a reluctance with volume \(V\) is expressed as (3.10):

\[
E = \int \int \int_V H dB dV \tag{3.10}
\]

In the linear case with a rectangular shape, (3.10) is simplified as (3.11)

\[
E_R = \frac{B^2}{2\mu_0\mu_r} V_R \tag{3.11}
\]

with \(V_R\) is the volume of the reluctance \(R\).

Energy stored in the block in Fig. 3.5:

\[
E = \frac{B_{x1}^2}{2\mu_0\mu_r} V_{Rx1} + \frac{B_{x2}^2}{2\mu_0\mu_r} V_{Rx2} + \frac{B_{y1}^2}{2\mu_0\mu_r} V_{Ry1} + \frac{B_{y2}^2}{2\mu_0\mu_r} V_{Ry2} \tag{3.12a}
\]

\[
E = \frac{1}{2\mu_0\mu_r} \frac{w h}{2} (B_{x1}^2 + B_{x2}^2 + B_{y1}^2 + B_{y2}^2) \tag{3.12b}
\]

\[
E = \frac{w h}{4\mu_0\mu_r} (B_{x1}^2 + B_{x2}^2 + B_{y1}^2 + B_{y2}^2) \tag{3.12c}
\]
Energy stored in the block calculated with $B_{eq}$:

$$E = \frac{B_{eq}^2}{2\mu_0\mu_r} whl \quad (3.13)$$

From (3.12c) and (3.13), the equivalent flux density amplitude $B_{eq}$ could be derived as (3.14):

$$B_{eq} = \sqrt{\frac{B_{x1}^2 + B_{x2}^2 + B_{y1}^2 + B_{y2}^2}{2}} \quad (3.14)$$

The equivalent flux density amplitude components in $x$ and $y$ directions could be derived as (3.15a) and (3.15b) respectively:

$$B_x = \sqrt{\frac{B_{x1}^2 + B_{x2}^2}{2}} \quad (3.15a)$$

$$B_y = \sqrt{\frac{B_{y1}^2 + B_{y2}^2}{2}} \quad (3.15b)$$

### 3.2.2 Meshing principle

Although the flux paths in the motor are truly 3-D but in order to simplify the calculations with a smaller number of nodes and reluctances, the whole model will be disassembled into several parts as displayed in Fig. 3.6. In short, three meshes (part 1, 3 and 5) are presented in XY plane which are 2-D and reluctances in Z-direction (part 2 and 4) are added to account for the third dimensional flux direction. In these reluctance meshes, the mesh for part 3 is the most complicated one due to complex and different geometries and material zones. In fact, several layers should be considered for this part to improve accuracy but the total element number and hence computation time would significantly increase.

The basic principle for mesh divisions applied for EMCN follows the general guide as one for FEM i.e. more elements in the critical parts, for example the air-gap region. Meshes used in this generalized model is characterized by a number of rows and columns (radially and tangentially). Row and column divisions are based on material regions. One should be noted that the basic block element is rectangular; therefore, shape approximations should be accomplished since rotary machines basically use cylindrical coordinate where rectangular shapes are rarely presented (except for regions such as PMs) Meshings for each part of the machine are detailed in the following.

#### 3.2.2.1 Main stator meshing

This meshing process is for the main stator which is the part 3 in Fig. 3.6. Row and column division principle in Fig. 3.7 are based on various material regions as follows:

- Three regions in radial direction shown in Fig. 3.7a): stator yoke, stator tooth and stator tooth tip. Each region is then divided into rows. All rows in each region has same heights.
Three types of region in tangential direction in Fig. 3.7b): opening slot, tooth tip beyond the stator tooth and stator tooth. Each region is then divided into columns. All columns in each region has same widths.

It is noted that the numbers of rows and columns in each region are adjustable. Details are given in Table 3.1. With those numbers being chosen, the total number of blocks in stator is 150 (with 5 rows and 30 columns in total). The derived stator mesh is shown in Fig. 3.8 with each small cell is a basic block with four reluctances.

<table>
<thead>
<tr>
<th>Radial region</th>
<th>Tangential region</th>
</tr>
</thead>
<tbody>
<tr>
<td>Yoke</td>
<td>Tooth</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td></td>
<td>Slot opening</td>
</tr>
<tr>
<td></td>
<td>2</td>
</tr>
</tbody>
</table>

As it can be seen in Fig. 3.8, each cell is not perfectly rectangular; therefore, an approximation should be made. To this end, equivalent height and width of each block need to be calculated. The height of each block could be easily derived based on the height of each radial region and the number of rows in that radial region. For example in Fig. 3.9, height $h_s$ of each block in the
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Fig. 3.7: Radial and tangential regions in the stator. a) Radial regions. b) Tangential regions

Fig. 3.8: Block mesh of the stator

Slot opening region equals half of the stator tooth height since there are 2 rows in this region.

For the block width, even though there are three different types of tangential region presented but regarding block width calculation, there are in fact two types of regions: type 1 is the region with parallel edges (tooth tip and tooth regions) and type 2 is the slot opening region. With type 1, the width \( w_1 \) is given by (3.16)

\[
w_1 = \frac{\text{Region width}}{n_1}
\]  

(3.16)

with \( n_1 \) is the number of columns in that region.

An example as shown in Fig. 3.9, the width of block \( B_1 \) (type 1) is the width of stator tooth tip \( w_{tt} \).
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With block in region type 2, the width is approximated as width of an equivalent rectangular
with same block height and area given by (3.17)

\[ w_2 = \frac{S_s}{h_2} \]  \hspace{1cm} (3.17)

with \( S_s \) is the area of one block being considered and \( h_2 \) is the block height. \( S_s \) is calculated
by (3.18)

\[ S_s = \frac{1}{n_2} \left[ \frac{\pi (R^2_{up} - R^2_{low})}{n_s} - \frac{h_t}{n_v} (w_t + 2w_{tt}) \right] \]  \hspace{1cm} (3.18)

with \( n_s \) is number of stator teeth (which is 36 in this study), \( w_t \) is stator tooth width, \( n_2 \) is
number of columns in the slot opening, \( n_v \) is number of rows in the radial stator tooth region
in Fig. 3.7a. \( R_{up} \) and \( R_{low} \) are upper and lower bound radius of the block. For instance, with
the block \( B_2 \) in Fig. 3.9, these radius are calculated as (3.19)

\[ R_{up} = R_{in} + h_{tt} + h_t \]
\[ R_{low} = R_{in} + h_{tt} + 0.5h_t \]  \hspace{1cm} (3.19)

where \( R_{in} \) is inner radius of the stator, \( h_{tt} \) and \( h_t \) are height of stator tooth tip and stator tooth.

3.2.2.2 Rotor meshing

Rotor meshing principle and block dimension calculations follow the ones presented for the
stator part with presence of different material regions and regions with and without parallel
edges. Regions for rotor mesh shown in Fig. 3.10 are:

- Four regions in radial direction: Rotor pole tip, PM, leg and base regions
- Three types of region in tangential direction: Rotor core, rotor pole tip and gap area
  between two poles

Number of rows and columns in each region are given in Table. 3.2. The total number of blocks
in rotor is 96 (with 6 rows and 16 columns in total). The derived rotor mesh is shown in
Fig. 3.11.
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Fig. 3.10: Radial and tangential regions in the rotor (colors are not related). a) Radial regions. b) Tangential regions

Table 3.2: Numbers of rows and columns in each rotor region

<table>
<thead>
<tr>
<th></th>
<th>Radial region</th>
<th></th>
<th></th>
<th>Tangential region</th>
<th>Core</th>
<th>Pole tip</th>
<th>Gap</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pole tip</td>
<td>PM</td>
<td>Leg</td>
<td>Base</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td>1</td>
<td>1</td>
<td></td>
<td>4</td>
<td>1</td>
<td>2</td>
</tr>
</tbody>
</table>

Fig. 3.11: Block mesh of the rotor
3.2. EMCN model of the DESM

3.2.2.3 Air-gap meshing

The air-gap mesh is rather different compared to stator and rotor meshes. It is still based on bi-directional elements; however, the creation is derived from stator and rotor meshes in a manner that: edges of elements of stator and rotor (contiguous with the air-gap) defines edges of elements in the air-gap as shown in Fig. 3.12. Air-gap mesh will be redefined for a new rotor position i.e. taking into account machine’s rotation.

Fig. 3.12: Air-gap meshing principle

Fig. 3.12 shows air-gap mesh principle based on meshes on the boundaries between stator, rotor and the air-gap. Let’s assume all the elements on the stator-air-gap boundary define their edge positions as (3.20):

\[ E_S = [s_1, s_2, ..., s_n] \] (3.20)

Similarly, elements on the rotor-air-gap boundary defines corresponding edge positions as (3.21):

\[ E_R = [r_1, r_2, ..., r_m] \] (3.21)

All edges of two groups \( E_S \) and \( E_R \) are then mixed together and sorted in ascending order. The derived new coordinates group define edges \( E_A \) of elements in the air-gap mesh. For example, if the coordinates of edges in \( E_S \) are \([0\ 2\ 4\ 6]\) and coordinates of edges in \( E_R \) are \([1\ 5\ 7\ 9]\), then coordinates of air-gap element edges are stored in \( E_A = [0\ 1\ 2\ 4\ 5\ 6\ 7\ 9]\). It should be noted that, depending on the nature for stator, rotor geometries and specific rotor positions, some edges of rotor’s elements may coincide with ones of stator’s element, the redundant edges will be removed to have the resulting air-gap edges \( E_A \). Air-gap elements are all bi-directional with the height being the air-gap length \( g \), depth being the machine’s active length and width calculated as (3.22):

\[ w = r_a(a_{i+1} - a_i) \] (3.22)
where $a_i$ and $a_{i+1}$ are two edges defining the element being calculated and $r_a$ is the radius right at the middle of the air-gap. So that an air-gap element takes the average length which is at the middle of the element. This is plausible because in a small deviation (air-gap length), air-gap radius is large and two edges are closed in tangential direction). Because of that, air-gap elements are assumed to be rectangular as the all other basic elements in the model.

With meshes of stator, rotor and air-gap defined, the derived mesh of part 3 is visualized as Fig. 3.13 with 150 blocks for stator, 96 blocks for rotor and 48 blocks for the air-gap.

![Fig. 3.13: Block mesh of part 3](image)

### 3.2.2.4 Outer part meshing

Meshes for parts 1 and 5 (Fig. 3.6) are the same and much simpler compared to one presented for the part 3 due to their simple structures. To simplify, part 1 and part 5 are referred to “outer part”. There are three region types in the radial direction (rotoric flux collector, outer air-gap and end-shield) and only one type in the tangential direction. In order to make a good connection between outer parts and part 3, especially in the rotor region, the number of rows in the rotoric part equals to one in the rotor of part 3 which is 10. On top of the end-shield, one row is dedicated to act as the outer stator core. The same mesh for part 1 and 5 is shown in Fig. 3.14 with 120 blocks in total (10 rows and 12 columns)

It is advised to carefully pay attention to the air-gap permeance calculation due to fringing flux paths demonstrated in Fig. 3.15. Fringing flux paths exist in both main air-gap and outer air-gap regions. The fringing flux paths in the main air-gap region could be neglected since the axial length is much bigger compare to air-gap length i.e. contribution of fringing path
permeance to the total air-gap permeance is neglected. It is, however, not the case for the outer air-gap since axial length of this air-gap (equals end-shield thickness) is much shorter. In addition, the cross section of the flux tube representing this outer air-gap fringing is significant.

The basic shape of fringing flux is shown in Fig. 3.16
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The fringing permeances with quarter-ring and half-ring shapes are expressed by (3.23):

\[
P_{\text{quarter-circle}} = \frac{2\mu_0 L_a}{\pi} \ln \left( 1 + \frac{\pi X_1}{\pi R_1 + 2g} \right)
\]

\[
P_{\text{half-circle}} = \frac{\mu_0 L_a}{\pi} \ln \left( 1 + \frac{\pi X_1}{\pi R_1 + g} \right)
\] (3.23)

In case of fringing flux shown in Fig. 3.15, \( R_1 = 0 \). These permeances are then put in parallel to the permeance of the air-gap under the end-shield. It is shown that by considering these fringing flux paths, the outer air-gap reluctance reduces by 20%

### 3.2.3 Block connection

After having a mesh of elementary blocks with the nodes located at theirs centers, the next task is to make connections to establish reluctances, MMFs between nodes. Two types of connection are possible, namely one-to-one (one block faces one another in a certain direction) and one-to-several connections (one block faces several blocks). The first one which is one-to-one connection is illustrated in Fig. 3.17. In this case, it is very straightforward to have reluctance calculation between node \( i \) and \( j \) as the sum of individual reluctances of each block in the connection as (3.24):

\[
R_{ij} = R_i + R_j
\] (3.24)

![Fig. 3.17: One-to-one block connection](image)

This kind of connection appears quite a lot in the meshes of stator or rotor where they are mostly row-by-column meshes. However, on the boundary between stator and air-gap or rotor and air-gap, it might be different since one block in the stator/rotor possibly faces several blocks in the air-gap as already shown in Fig. 3.12. This introduces one-to-several block connection. Fig. 3.18a) is for an example of a block with node \( i \) is facing three blocks with nodes \( j_1, j_2 \) and \( j_3 \). In the EMCN network, it is compulsory to have connection between every two nodes either zero permeance (not connected) or by a certain value. In Fig. 3.18a), physically there must be a certain flux passing between node \( i \) and node \( j_1 \) therefore a non-zero permeance \( P_{ij_1} \) between these two nodes must be presented. In order to deal with that, block \( i \) could be assumed to be divided into three blocks \( i_1, i_2 \) and \( i_3 \) as in Fig. 3.18b) with magnetic potentials are the same for \( i_1, i_2 \) and \( i_3 \).
By transforming one-to-several connection to several one-to-one connections, the connection is now established, for instance as (3.25):

\[ R_{ij1} = R_{i1j1} = R_{i1} + R_{j1} = 3R_i + R_{j1} \]  

(3.25)

with the note that due to the equal division, \( R_{i1} = R_{i2} = R_{i3} = 3R_i \)

### 3.2.4 EMCN model completeness

In the previous section, using two types of block connection (one-to-one and one-to-several), networks will be defined for parts 1, 3 and 5 in Fig. 3.6. Permeance connection matrices \([P]\) as in (3.7) for these three parts will be computed individually. In order to have a single permeance matrix for the machine, it is necessary to combine these individual matrices and also interconnections between matrices i.e. connection in Z-direction (machine axial direction) should be made. The idea is visualized in Fig. 3.19

Part 1, 3 and 5 are firstly combined together without interconnections i.e. permeance between
any node of a part and one of the other is set zero. After that, matrices for parts 2 and 4 are added to modify interconnections. Main points for Fig. 3.19 based on Fig. 3.6 are summarized as follows:

- Matrices for parts 1, 3 and 5 are all square and symmetric over their diagonals
- Matrices for parts 1 and 5 are the same (due to the same geometries) i.e. \( n_1 = n_5 \)
- All nodes in the model are already presented in parts 1, 3 and 5 i.e. the total number of nodes: \( n = n_3 + n_1 + n_5 = n_3 + 2n_1 \)
- Arrow represents an interconnection existed between parts
- Part 2 and 4 matrices are the same, part 2 is for interconnection between part 1 and 3. Part 4 is for interconnection between part 5 and 3
- The resultant matrix is symmetric over its diagonal

These connecting parts (2 and 4) carry the outer stator yoke (reluctances and MMF from field windings), side PM (reluctances and MMF), rotor solid parts (in Z-direction) and leakage in Z-direction due to side PMs. In order to be more accurate, these connections are distributed along the tangential paths.

![Diagram showing reluctances in axial direction](image)

**Fig. 3.20:** Reluctances in axial direction. a) Due to core b) Due to side PM and leakage

Defining and computing these components will update connections between nodes which were initially set as zero.

The flux source (the right hand side of (3.7)) will also be updated similarly as with the permeance matrix. The MMF sources due to armature windings are placed in the stator teeth with the net value is given by (3.26)

\[
F_{\text{armature}} = N_t(i_1 - i_2)
\]

(3.26)

where \( N_t \) is the number of armature turns, \( i_1 \) and \( i_2 \) are armature current flowing in the winding accommodated two adjacent slots of the tooth. (3.26) is with an assumption that \( i_1 \) and \( i_2 \) are axially flowing in the same direction.
3.2.5 Magnetic saturation consideration

With permeance and flux source matrices are defined, scalar magnetic potentials are obtained by solving (3.7). This equation is simply rewritten as (3.27). In order to solve this equation, it would firstly come up with the nonlinear characteristic of the core material which is represented by a magnetization curve.

\[ PU = \phi \]  

(3.27)

It is noted that most of elements in permeance matrix \( P \) are zero. For example at aligned position, the number of nodes in the whole network is 533 resulting in a \( 533^2 = 284089 \) element matrix \( P \) but there are only 2837 non-zero elements as illustrated in Fig. 3.21 i.e. 1% of the total number of elements.

![Fig. 3.21: Non-zero elements distribution in the permeance matrix \( P \)](image)

3.2.5.1 B-H magnetization curve approximation

In magnetic modelings, there is often a need of an approximate expression for the B-H curve. This will ensure a fast and smooth calculation compared to a direct lookup table using interpolation from the measured magnetization curve. Although several functions could be used to represent the magnetization but if possible, a single function should present the whole range from the origin to the saturation region. This single function would make an easy application and simplify the process from the programming point of view. The choice of an approximation function depends mainly on the range for which the approximation should be valid. For the linear range, the approximate function could be straightforward to handle. However, this becomes more complicated when extending to the saturated region that includes the knee of the characteristic [66].

A very simple approximation with power series either given by a single term as (3.28a) or by
series formula as (3.28b) [66]:

\[ B = aH^n \quad (3.28a) \]
\[ H = a_0 + a_1B + a_nB^n + a_mB^m \quad (3.28b) \]

where \( a_i, n \) and \( m \) are constants. The curve fitting qualities with this formula are efficient for some special materials and applicable for a limited range as \( H \) goes infinitely, permeability \( \mu = B/H \) approaches either infinity or zero instead of permeability of the air \( \mu_0 \).

Another possibility is to replace the curve by hyperbolas using Frölich’s equation given by (3.29) [66]:

\[ |B| = \frac{|H|}{a + b|H|} \quad (3.29) \]

Constants \( a \) and \( b \) can be determined from a plot of \( 1/|B| \) against \( 1/|H| \). The slope of that line gives the coefficient \( a \) and the intercept gives \( b \). However, this approximation is valid only for a maximum value of \( B = 1/b \) and also it often becomes necessary to subdivide the magnetization curve in several regions in order to obtain a good fit in the range of saturation.

In a more complex manner, aiming to describe the magnetic properties of materials, one must know the flux density \( B \), magnetic field strength \( H \), and the intensity of magnetization \( M \) which are correlated by (3.30) [60]:

\[ B = \mu_0(H + M) \quad (3.30) \]

With nonlinear magnetic materials, \( M \) is a complicated function of \( H \) which can be approximated by a second order rational fraction given by (3.31) [67]

\[ M = \frac{a_0 + a_1H + a_2H^2}{1 + b_1H + b_2H^2} \quad (3.31) \]

where \( a_i \) and \( b_i \) are constant coefficients which can generally be determined by curve fitting technique given by (3.32):

\[
\begin{align*}
  a_0 &= 0 \quad a_1 = \chi \quad a_2 = \frac{\lambda M_s + \chi^2}{M_s + \alpha\chi} \\
  b_1 &= \frac{\alpha\lambda + \chi}{M_s - \alpha\chi} \quad b_2 = \frac{\lambda M_s + \chi^2}{M_s(M_s - \alpha\chi)}
\end{align*}
\quad (3.32)
\]

where \( \chi \) is the initial magnetic susceptibility, \( \lambda \) is the Rayleigh material constant [68], \( M_s \) is the saturation magnetization and \( \alpha \) is the Néel constant [69]. From (3.31) and (3.32), it can be observed that at weak fields (\( H \to 0 \)), \( M \) approaches the initial magnetic susceptibility \( \chi \) and and for high fields (\( H \to +\infty \)) \( M \) approaches zero.

In some magnetism problems, for example EMCN which will be discussed later on, an equation for the permeability is given by (3.33) [67]:

\[ \mu_r = \frac{B}{\mu_0H} = 1 + \frac{a_1 + a_2H}{1 + b_1H + b_2H^2} \quad (3.33) \]
From (3.33), at high fields i.e. strong saturation, $\mu_r$ approaches 1 (air medium). However, to obtain this relation, some complex coefficients such as $\chi$, $M_s$ and $\alpha$ needed to be provided leading to a complicated process.

In [70], the permeability function could be more conveniently determined by using fitting curve only from the measurement data. Firstly, the relation between magnetization intensity and field strength is given by (3.34) which differs from (3.31).

$$M = \frac{\alpha H}{1 + \beta H} \quad (3.34)$$

where $\alpha/\beta$ equals to the saturation magnetization, $M_s$. In order to provide additional degrees of freedom in capturing the magnetization characteristic, (3.34) is modified to be (3.35):

$$M = \text{sig}(H) \sum_{k=1}^{K} m_k \left( \frac{|H|/b_k}{1 + (|H|/b_k)^n_k} \right)^{1/n_k} \quad (3.35)$$

with $\text{sig}(.)$ function is to incorporate $H < 0$. Parameter $m_k$, $b_k$ and $n_k$ are then obtained by minimizing the error between the prediction and the measurement.

[70] defines permeability function $\mu_r(B)$ as (3.36)

$$\mu_r(B) = \frac{1}{K} \sum_{k=1}^{K} \left( \left| \frac{B}{m_k} \right|^{n_k} + a_k^n_k \right)^{\frac{1}{n_k}} - 1 \quad (3.36)$$

where $K$ is the approximation order, $a_k$, $m_k$ and $n_k$ are fitting coefficients. For strong fields ($H \rightarrow +\infty$ and hence $B \rightarrow +\infty$), $\mu_r \rightarrow 1$. Any optimization technique could be use to obtain coefficients in (3.36). Although this permeability function proposes a somewhat complex procedure to handle but it is indeed flexible and applicable to a wide variety of materials with an unique closed expression in the whole range of magnetization region.

Using this formula in the thesis, values of coefficients obtained with a fifth order ($K = 5$) approximation are shown in Table. 3.3 with $b_k$ is defined such that: $a_k = b_k/(b_k - 1)$.

<table>
<thead>
<tr>
<th>k</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
</tr>
</thead>
<tbody>
<tr>
<td>$b_k$</td>
<td>1e10</td>
<td>3e6</td>
<td>694.32</td>
<td>722.95</td>
<td>111.25</td>
</tr>
<tr>
<td>$n_k$</td>
<td>6.68</td>
<td>11.82</td>
<td>7.95</td>
<td>12.61</td>
<td>39.97</td>
</tr>
<tr>
<td>$m_k$</td>
<td>19.91</td>
<td>1.85</td>
<td>49.99</td>
<td>21.46</td>
<td>17.55</td>
</tr>
</tbody>
</table>

Fitting curve (3.36) is sketched in Fig. 3.22.

The fitting curve is displayed in Fig. 3.23 in comparison with the original magnetization curve. As it can be seen, a good fitting is made.
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Fig. 3.22: Relative permeability as function of flux density

![Relative permeability as function of flux density](image)

Fig. 3.23: Magnetization curve of the core material

![Magnetization curve of the core material](image)

3.2.5.2 Method to solve nonlinear EMCN equations

Basically, Newton Raphson (NR) method is an efficient method dealing with nonlinear equation solving. The basic form of this method is recalled shortly as follows: For an \(n\)-dimensional set of nonlinear equations:

\[
f(x) = 0
\]

(3.37)

where \(f = [f_1(x) \ f_2(x) \ \ldots \ f_n(x)]^T\) and \(x = [x_1 \ x_2 \ \ldots \ x_n]^T\)

Supposing that \(f(x)\) is differentiable and an iterative process for solving (3.37) by NR method can be defined at iteration \((k + 1)\) as (3.38) [71]:

\[
x^{(k+1)} = x^{(k)} - \left[ J \left(x^{(k)}\right) \right]^{-1} f \left(x^{(k)}\right)
\]

(3.38)

where \(x^{(k)}\) is the solution at the \(k\)th iteration. For the first iteration, an initial guess should be given. For an EMCN model, a constant permeability is often given to all reluctances. \(J\) is the
3.2. EMCN model of the DESM

Jacobian matrix of $f$ defined as (3.39):

$$
J = \frac{\delta f}{\delta x} = \begin{bmatrix}
J_{11} & J_{12} & \cdots & J_{1n} \\
J_{21} & J_{22} & \cdots & J_{2n} \\
\vdots & \vdots & \ddots & \vdots \\
J_{n1} & J_{n2} & \cdots & J_{nn}
\end{bmatrix}
$$

(3.39)

with $J_{ij} = \frac{\delta f_i}{\delta x_j}$

Usually the NR method requires more computational efforts for the differentiating process. Applying this method to EMCN, (3.27) is rephrased as (3.40)

$$
f(U) = PU - \phi = 0
$$

(3.40)

Taking derivative of $f(U)$ with respect to $U$ raises another difficulty since the permeance matrix $P$ and source matrix $\phi$ are unknown and in fact are implicit functions of $U$ as in (3.6c). So that instead of using NR method, another method which is considered as a form of fixed point (FP) method will be used. Even though the drawback of this method is a slow convergence speed generally compared to the NR method.

The original form of FP method is given by (3.41):

$$
f(x) = x
$$

(3.41)

with the iterative process, solution at $(k + 1)$th iteration expressed as (3.42):

$$
x^{(k+1)} = f(x^{(k)})
$$

(3.42)

The iterative process (3.42) could be defined as converged at $k$th iteration if (3.43) is satisfied.

$$
\left\| \frac{x^{(k+1)} - x^{(k)}}{x^{(k)}} \right\|_{\infty} \leq \varepsilon
$$

(3.43)

(3.43) means that the maximum local error between two consecutive iterations is not bigger than a predefined tolerance $\varepsilon$.

Although the objective of (3.27) is to find potential at $n$ nodes of the network but it can be turned into finding permeabilites of $n$ blocks. Initially, a constant permeability $\mu^{(0)}$ is given to all blocks. At $k$th iteration, having known permeabilities $\mu^{(k)}$, node potential $U^{(k)}$ is obtained by (3.44):

$$
U^{(k)} = \left( P^{(k)} \right)^{-1} \phi^{(k)}
$$

(3.44)

From the newly solved $U^{(k)}$, flux density between node $i$ and $j$ is calculated by

$$
B_{ij}^{(k)} = \frac{U_{i}^{(k)} - U_{j}^{(k)} - F_{ij}}{S_{ij}} P_{ij}^{(k)}
$$

(3.45)
with quantities between node $i$ and $j$: $F_{ij}$ is a MMF may present, $P_{ij}^{(k)}$ is the permeance at $k$th iteration and $S_{ij}$ is cross section of the reluctance path. $F_{ij}$ and $S_{ij}$ are unchanged throughout iterations.

From (3.14) and (3.45), flux densities of all blocks will be easily obtained and permeabilities of all blocks $\mu^{(k)}$ could be recalculated by using permeability function (3.36).

The stopping criterion given by (3.46):

$$\left\| \frac{\mu^{(k)}}{\mu^{(k)}} - \mu^{(k)} \right\|_\infty \leq \varepsilon$$

(3.46)

To summarize, Fig. 3.24 displays the block diagram for the EMCN model formulation and solving. There are some main points should be remarked as follows:

- Only the air-gap mesh and armature winding’s MMF are rotor position dependent so all meshes and PM’s MMF are defined at the beginning.

- In order to save computational time, reluctance calculations of linear reluctances (PM, air elements in the slots) could be accomplished right after the preliminary meshes are defined and elements in the air-gap right after air-gap mesh is defined.

- Even though the stopping criterion is set as (3.46), but the maximum number of iterations could be added as a supplementary criterion to prevent an infinite iteration loop when no converged solution found according to (3.46).

### 3.2.5.3 Examination of the proposed method with a simple case

In this part, a simple 2-D electromagnetic field will be used to examine the proposed algorithm. The model to be analyzed will be a C-core being excited by a DC field winding (wrapped inside the C-core) with a wide range of field currents so as to examine saturation level. The quantity to be calculated is the flux flowing in the core.

Fig. 3.25a) shows the dimension of the C-core model and Fig. 3.25b) is for the meshing idea of the model. Accounting for fringing flux of the air-gap, the model is bound by an air volume with a dimension of 20 mm beyond each side. The meshing will be tried with a huge number of elements to examine the performance of the proposed algorithm with the induction map in comparison with FEM. The result will be the flux passing through the red line in Fig. 3.25b).

In detail, the air-gap length $g = 2$ mm. Induction map shown in Fig. 3.26 at highly saturated zone reveals a good accordance between two analyses.

The comparisons between EMCN and FEM are displayed in Fig. 3.27. As it can be seen, good accordance between two analyses even at very high saturation level.
Fig. 3.24: EMCN algorithm block diagram

### 3.3 Results and comparisons with 3-D FEM

Firstly, Fig. 3.28 compares flux linkage at no-load according to field currents in both flux weakening ($I_{dc} = -3$ A) and flux reinforcing ($I_{dc} = 3$ A) modes. As it can be seen, EMCN
reveals very close results versus ones by FEM. This could be explained by the difficulty of a perfect machine’s modeling in 3-D configuration. When the field current is injected (either positive or negative), this adds more influences in the axial direction and other directions rather than tangential and radial ones.

Flux control capability over a wide range of field current is demonstrated in Fig. 3.29. The non-linearity examination is also performed with good agreement except for a very high saturation situation where the modeling imperfection explained above appears.

The tangential and radial components of air-gap flux density distribution for one pole pair at
aligned position, no-load and field current are set to zero ($I_{dc} = 0$ A) are displayed in Fig. 3.30.

A good comparison agreement is seen for radial air-gap flux density; however, bigger difference is seen with tangential components, this could be explained as tangential flux density is very prone to the mesh around air-gap region. The FEM analysis for DESM in this research is 3-D so that a very fine mesh is especially constrained by computer’s memory. As observed in Fig. 3.30a), the radial flux density is asymmetric between first half and second half of one pole pair. This happens owing to the homopolar topology of the studied DESM as explained in 2.4.2.1 in which when field currents are set to zero, air-gap flux densities in the concentrated area are reported to be almost double compared to ones in the unconcentrated region. Also, the flux densities below the slots are substantially reduced.

Electromagnetic torque is again computed by using flux MMF method (calculated with flux-MMF method presented in chapter 2). The instantaneous torque for one example armature current is shown in Fig. 3.31 and Fig. 3.32 is for average torque according to armature current variation. It is noted that the rated armature current is 10 A. Good agreements between EMCN and FEM are reported in these comparisons. Torque comparison is also shown with the linear
Chapter 3. Modeling with Equivalent Magnetic Circuit Network (EMCN)

Fig. 3.30: Air-gap flux density distribution at no-load, $I_{dc} = 0$ A, aligned position. a) Radial component. b) Tangential component

Torque computed by EMCN to visualize the effect of saturation.

Fig. 3.31: Instantaneous electromagnetic torque at armature current of 8A, $I_{dc} = 0$ A

The accuracy and computation time for torque comparison between EMCN and FEM are summarized in Table 3.4.

As it can be seen, the relative maximum error is only 2.2% revealing a very good result of EMCN.
3.3. Results and comparisons with 3-D FEM

![Graph showing generated torque according to armature currents, $I_{dc} = 0$ A](image)

Fig. 3.32: Generated torque according to armature currents, $I_{dc} = 0$ A

<table>
<thead>
<tr>
<th>Armature current [A]</th>
<th>0</th>
<th>2</th>
<th>4</th>
<th>6</th>
<th>8</th>
<th>10</th>
<th>12</th>
<th>14</th>
<th>16</th>
<th>18</th>
<th>20</th>
</tr>
</thead>
<tbody>
<tr>
<td>Error [%]</td>
<td>NaN</td>
<td>1.8</td>
<td>1.3</td>
<td>0.5</td>
<td>0.9</td>
<td>2.2</td>
<td>0.6</td>
<td>0.6</td>
<td>0.2</td>
<td>1.8</td>
<td>1.7</td>
</tr>
</tbody>
</table>

Table 3.4: Comparison between EMCN and FEM based on torque calculation

<table>
<thead>
<tr>
<th>Mesh &amp; Average time</th>
</tr>
</thead>
<tbody>
<tr>
<td>EMCN</td>
</tr>
<tr>
<td>Mesh generation</td>
</tr>
<tr>
<td>Computation time/point</td>
</tr>
<tr>
<td>FEM</td>
</tr>
<tr>
<td>58000 elements</td>
</tr>
<tr>
<td>58 s</td>
</tr>
</tbody>
</table>

compared to FEM. The mesh generation of FEM consists of about 58000 elements which are tetrahedrons while the number of nodes for EMCN is more or less of 530 (varies as air-gap mesh changes) which is 110 times smaller. The computation time per point for EMCN is therefore much faster versus FEM which is 0.2 s compared to 58 s (roughly 290 time faster). From these points, the aforementioned advantage of EMCN is confirmed: accurate enough but much less time consuming compared to FEM.

The mean torque comparison at a wider range of armature and excitation currents are shown in Fig. 3.33. A good accordance between two results are seen with a little more differences lie in the are with high currents due to very strong saturation occur. Since having two surfaces put together, surfaces are kept partly transparent and focuses should be made on the interconnected lines.
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3.4 Iron loss calculation

In order to improve machine’s efficiency itself, the very first step has to accomplish is losses determination. Different losses exist in the machine including core losses, copper losses of armature and field windings and mechanical losses and stray load loss. Among these losses, mechanical and stray load losses are not calculated by electro-magnetic analysis. This part focuses on iron loss calculation since copper loss is straightforwardly calculated as (3.47):

\[ P_{Cu} = \sum_{i=1}^{n} I_i^2 R_i \]  

(3.47)

where \( I_i \) and \( R_i \) is current and resistance of the \( i \)th winding (either armature or field windings) respectively. Winding resistance could be obtained easily based on winding geometry.

3.4.1 Iron losses models

Iron loss calculation is the subject of numerous researches and have gained much attention through years due to its complexity. An accurate computation of core loss must require detail information on microscopic scale behavior of the magnetic domain structure. This task is usually too difficult to handle. Therefore, core losses formulations based on experimental data on sample material with some assumptions are normally utilized. The core loss calculations in this part is for an unit volume.

A simple and common formulation that characterizes core losses is the power equation by Steinmetz [72] given by (3.48):

\[ P_{Fe} = k f^\alpha \hat{B}^\beta \]  

(3.48)

where \( \hat{B} \) is the peak flux density of a sinusoidal waveform with frequency \( f \) and \( k, \alpha \) and \( \beta \) are material dependent coefficients.
This equation is only valid for a limited frequency and flux density ranges. Another limitation is that the flux density in (3.48) must be sinusoidal which is not applicable for almost the cases since material is mostly exposed to distorted flux densities waveform with harmonic contents. Authors of [73] did a research to overcome this limitation by taking into account the fact that the loss due to domain wall motion has a direct dependency of \(\frac{dB}{dt}\). The modified Steinmetz equation given by (3.49) introduces a dependence of core loss on flux density variation i.e. it is able to deal with distorted waveforms.

\[
P_{Fe} = \frac{1}{T} \int_{0}^{T} k_i \left| \frac{dB}{dt} \right|^{\alpha} \left( \hat{B} \right)^{\beta-\alpha} dt
\]  

(3.49)

where \(k_i\), \(\alpha\) and \(\beta\) are material dependent coefficients. It should be noted that coefficients \(\alpha\) and \(\beta\) are the same as ones in (3.48).

The advantages of (3.49) is that it consider multiple peaks occurring in the flux density waveform for example when third or another low-ordered flux density harmonic components becomes significant.

Model proposed by Bertotti [74] expressed as (3.50) is one of the most common model used in core loss calculation. In this model, the core loss is separated into three terms namely hysteresis (\(P_h\)), eddy current (\(P_e\)) and anomalous (\(P_a\)) losses.

\[
P_{Fe} = P_h + P_e + P_a
\]
\[
= k_h f \hat{B}^{\alpha} + k_e f^2 \hat{B}^2 + k_a f^{1.5} \hat{B}^{1.5}
\]

(3.50)

It should be noted that (3.50) cannot estimate accurately eddy current and anomalous losses since it only handles the peak flux densities. (3.51) [75] below presented in time domain is a solution.

\[
P_{Fe} = k_h f \hat{B}^{\alpha} + \frac{k_e}{2\pi^2 T} \int_{0}^{T} \left( \frac{dB}{dt} \right)^2 dt + \frac{k_a}{8.763 T} \int_{0}^{T} \left| \frac{dB}{dt} \right|^{1.5} dt
\]

(3.51)

where \(\alpha\), \(k_h\), \(k_e\) and \(k_a\) are material dependent coefficients. \(f\) is the frequency of flux density with peak \(\hat{B}\) and \(B\) is the instantaneous flux density. \(T\) is a period of flux density.

The eddy current loss coefficient \(k_e\) depends on material’s conductivity \(\sigma\) and its thickness \(d\) as

\[
k_e = \frac{\sigma d^2 \pi^2}{6}
\]

(3.52)

In some cases, anomalous loss could be merged into eddy current loss and therefore eddy current loss coefficient \(k_e\) will be adjusted accordingly by measurement fitting. In fact, all of these loss coefficients are conveniently determined by using measurement fitting based on sinusoidal wave forms of flux densities. However, formulation (3.50) is also valid for non-sinusoidal flux densities which will be detailed later in this section. This extension to non-sinusoidal flux densities of (3.50) is an advantage over (3.48). The core loss formulation based on (3.50) with...
two components: hysteresis and eddy current losses will be used since it is the most widely applied one.

Another formulation which is slightly different from (3.50) was proposed in [76], author agreed to separate core loss into hysteresis and eddy current components, the calculation for eddy current loss is the same as in (3.50) but a new formulation for hysteresis loss is proposed as (3.53)

\[ P_h = f(k_{h1}\Delta B + k_{h2}\Delta B^2) \]  

(3.53)

with \( k_{h1} \) and \( k_{h2} \) are hysteresis coefficients, \( \Delta B \) is peak-to-peak flux density.

In the following parts, detail about eddy current and hysteresis losses based on formulation (3.50) will be discussed especially considering flux density waveforms other than sinusoidal ones.

### 3.4.2 Iron loss with non-sinusoidal flux densities

Core material is rarely exposed to purely sinusoidal flux density, harmonic content usually appears making iron losses computations arduous. This section investigates on how non-sinusoidal flux densities affect the iron loss computation method. Firstly, (3.51) is recalled as (3.54) with a form of two components where anomalous loss is merged to eddy current loss. Coefficients are determined from measurement fitting.

\[ P_{Fe} = k_h f \hat{B}^\alpha + \frac{k_e}{2\pi^2T} \int_0^T \left( \frac{dB}{dt} \right)^2 dt \]  

(3.54)

The very common approach to handle a distorted signal is to decompose it into harmonics. The distorted waveform causes no change in the calculation process for eddy current loss since it directly works on the instantaneous flux densities. Indeed, a simple mathematical work could prove that eddy current loss resulted from a distorted waveform is equal to sum of eddy current losses caused by its separate harmonic components.

However, the summing-up approach is not valid for hysteresis loss because of the fact that this kind of loss simulate the B-H hysteresis loop due to the applied flux density. Depending on the magnitude and phase of the flux density harmonics, the resultant waveform may contain minor loops (flux density reversals). As an example shown in Fig. 3.34, a flux density containing a significant third harmonic causing flux reversals. If the hysteresis loss is calculated base on the peak value \( \hat{B} \) only as \( P_h = k_h f \hat{B}^2 \), the result is inaccurate. The loss calculation must contain additional components characterized by the area bound by these minor loops. The areas of these loops are again proportional to the all components \( \Delta B_i \).

Given that the total loss depend on the magnitude of every local minor loops and their positions. An exact correction may result in a complicated function of these factor. Author of [77] proposed a simplified process assuming that the correction can be correlated with the unweighted algebraic
sum the minor loops. According to that, the hysteresis loss caused by a non-sinusoidal flux density is adjusted as (3.55).

\[ P_{h,dist} = P_{h,sine}(\hat{B}) \cdot CF \]  

(3.55)

with \( P_{h,sine}(\hat{B}) \) is the hysteresis loss caused by a sinusoidal waveform with the same peak flux density \( \hat{B} \) and \( CF \) is a correction factor defined as (3.56):

\[ CF = 1 + \frac{k}{\hat{B}} \sum_{i=1}^{n} \Delta B_i \]  

(3.56)

where \( k \) a coefficient in the range 0.6 to 0.7. \( \Delta B_i \) is the magnitude of \( i \)th minor loop and \( n \) is the number of minor loops. \( \Delta B_i \) are calculated by working on all the local maximum and minimum points in the flux density waveforms.

An example to demonstrate the proposed approach for correction factor is shown below. A flux density waveform is assumed to have only third harmonic component.

\[ B(t) = \sin(\omega t) + B_3\sin(3\omega t + \varphi) \]  

(3.57)

The amplitude ranges from 20% to 100% of the first harmonic amplitude and phase angle \( \varphi \) varies between 0 and 180 electrical degree. Fig. 3.35 gives effects of third harmonic’s phase angle on \( \Delta B_i \) for the case 40% and the correction factors are shown in Fig. 3.34 according to different cases (coefficient \( k \) is chosen as 0.65). As it will be observed, when third harmonic is in phase with the fundamental one, the correction factor gets biggest. At low value of third harmonic’s amplitude and big phase angle, the correction is unity i.e. no correction is made. This is because of no minor loop presented even though the flux density waveform is not sinusoidal.

The hysteresis loss is still computed based on peak flux density only. A maximum of about 65% correction when the third harmonic has same amplitude order as the fundamental one and two components are in phase.

Fig. 3.37 shows flux densities in the stator tooth due to field current variation. As seen at field weakening the minor loop amplitude tend to increase although the one of major loop decrease globally. The corrections for minor loops at is expectedly not much.
Fig. 3.35: Effect of third harmonic’s phase angle on minor loop

Fig. 3.36: Correction factor according to amplitude and phase angle of third harmonic

Fig. 3.37: Flux density in the middle of stator tooth at no-load according to various $I_{dc}$

Core loss calculation according to (3.54) is adaptive to flux densities flowing in a single direction (1-D). The minority of electrical machine have constant axial shapes, a transformer for instance. However, in a rotating electrical machine, there exists some regions where the fields are essentially rotational. A FEM software package usually provides an option to calculate flux densities in orthogonal X and Y components (radial and tangential components are then deduced from
3.4. Iron loss calculation

orthogonal ones by a proper transformation using angular information). The resultant iron loss is commonly calculated by adding loss components together separately as in [78]. With a formation of elementary block in EMCN consisting of four branches which are actually in tangential and radial directions. Iron loss of a block is the sum of all losses component in each branch and the total iron loss of the machine equals the sum of ones in all individual blocks. Some sample points marked in Fig. 3.38 with their flux density loci (a radial component plotted versus a tangential one) are shown in Fig. 3.39.

Fig. 3.38: Sample points in the stator. P1 - Tooth tip side, P2 - Tooth tip middle, P3 - Tooth middle, P4 - Tooth junction, P5 - Yoke middle

Fig. 3.39: Flux density loci at no-load, $I_{dc} = 0$. a) P1 - Tooth tip side. b) P2 - Tooth tip middle. c) P3 - Tooth middle. (d) P4 - Tooth junction. (e) P5 - Yoke middle

One should be pointed out that, due to homopolar flux paths, most of flux density variations consists of DC components as in Fig. 3.37. This actually changes hysteresis loop as demonstrated in Fig. 3.40 and adds more hysteresis losses as in [79].
A factor is introduced to correct for this increase defined as (3.58) [79]

\[ \varepsilon(B_{dc}) = 1 + k_{dc}B_{dc}^\gamma \]  

(3.58)

where \( B_{dc} \) is DC-biased flux density, \( k_{dc} \) and \( \gamma \) are coefficients determined from experiment. In [79], \( k_{dc} = 0.65 \) and \( \gamma = 2.1 \) are expected to approximately applicable to some cases without causing a big difference. Considering the case with \( B_{dc} = 0.3 \), \( \varepsilon \) equals 1.052 i.e. 5.2% increase in the hysteresis loss.

### 3.4.3 Losses in permanent magnets

Since PM has its own electrical resistivity, flux density variations in PMs definitely produce losses as in core regions including eddy current loss and probably hysteresis loss. The present of hysteresis loss depends on whether or not the polarization of the magnet is reversed. If the field strength variation is extremely large and varies between high positive and negative values, a hysteresis loop may be similar as that of a soft magnetic material. Fortunately, in the DESM prototype being considered, PM demagnetization does not strongly occur as mentioned in 2.4.3.1. The flux density in azimuth PM is shown in Fig. 3.41 (This pattern for side PMs is quite the same).

With a very small flux density variation with unchanged magnet polarization, it can be properly assumed that hysteresis losses in PMs are negligible. This shows an advantage of interior PM machines versus surface mounted PM ones in term of low PM loss. In case of surface mounted PM machines, PM may be exposed to a large flux density variation in the air-gap and hence PM losses increase.

Regarding eddy current loss, the most general calculation for a rectangular core with a constant permeability developed by authors of [80] will be used. As shown in Fig. 3.42, a basis rectangular model with the thickness \( d \), width \( W \) being excited by a surface current density:

\[ J_0 = NI e^{j2\pi f t} \]  

(3.59)

where \( N \) is the number of coil turns, \( I \) is current amplitude and \( f \) is applied frequency.
3.4. Iron loss calculation

The magnetic field with a density $B$ will be created perpendicularly to the sample’s surface which is X-Y plane. The calculations are based on solving linear Maxwell’s equations applied to the linear material of PM ($\mu_r = 1$).

Unit volume eddy current loss is given by (3.60) (Refer to [80] for more detail)

\[
 p_c = \frac{16B_m^2 f}{\mu \pi} \sum_{p=1}^{\infty} \frac{1}{(2p-1)^2} \left( \frac{A}{d} + \frac{B}{W} \right) \tag{3.60}
\]

With

\[
 A = \frac{\alpha_m \sinh (\alpha_m r d) - \alpha_m \sin (\alpha_m d)}{\left( \alpha_m^2 + \alpha_m^2 \right)} \left[ \cosh (\alpha_m r d) + \cos (\alpha_m d) \right] \\
 B = \frac{\beta_m \sinh (\beta_m W) - \beta_m \sin (\beta_m W)}{\left( \beta_m^2 + \beta_m^2 \right)} \left[ \cosh (\beta_m W) + \cos (\beta_m W) \right] \\
 \alpha_m = \frac{1}{\sqrt{2}} \left[ \sqrt{\left( \frac{m \pi}{W} \right) - \omega^2 \mu \epsilon} \right]^2 + \omega^2 \mu^2 \sigma^2 + \left( \frac{m \pi}{W} \right) - \omega^2 \mu \epsilon \right] \right]^{1/2} \\
 \alpha_m = \frac{1}{\sqrt{2}} \left[ \sqrt{\left( \frac{m \pi}{W} \right) - \omega^2 \mu \epsilon} \right]^2 + \omega^2 \mu^2 \sigma^2 - \left( \frac{m \pi}{W} \right) - \omega^2 \mu \epsilon \right] \right]^{1/2} \\
 \beta_m = \frac{1}{\sqrt{2}} \left[ \sqrt{\left( \frac{m \pi}{d} \right) - \omega^2 \mu \epsilon} \right]^2 + \omega^2 \mu^2 \sigma^2 + \left( \frac{m \pi}{d} \right) - \omega^2 \mu \epsilon \right] \right]^{1/2} \\
 \beta_m = \frac{1}{\sqrt{2}} \left[ \sqrt{\left( \frac{m \pi}{d} \right) - \omega^2 \mu \epsilon} \right]^2 + \omega^2 \mu^2 \sigma^2 - \left( \frac{m \pi}{d} \right) - \omega^2 \mu \epsilon \right] \right]^{1/2}
\]
with $B_m$ is maximum induction (at the surface), $m = 2p - 1$, $\sigma$ is material conductivity and $\varepsilon$ is material permittivity.

This solution could cope with the case where the field inside the core is not uniform (which is true for the lamination case). If considering skin depth given by (3.61).

$$\delta = \sqrt{\frac{2}{\omega \sigma \mu}}$$

(3.61)

It can be suggested that if one of three factors: frequency - $\omega$, conductivity - $\sigma$ and permeability - $\mu$ becomes small such that skin depth effect is relatively large compared to core thickness, the conventional coefficient $k_e = \frac{\sigma d^2 \pi^2}{6}$ used in eddy current loss calculation is still valid even with the case where $d$ is not in order of a lamination thickness. Moreover, (3.60) is interesting since it treats what we usually call “width” and “thickness” equally.

(3.60) could be approximately applied for the ferrite PM (the electrical conductivity of about $\sigma = 10^{-2}$ S/m) in the DESM model. This excellently low conductivity makes PM eddy current losses approximately zero. However, in circumstances where rare earth magnets are used with the electrical conductivity of about $\sigma = 6.25 \times 10^5$ S/m which is much higher compared to ferrite PMs. The eddy current loss much increases.

It should be noted that, in the DESM model, several parts are solid, the hysteresis loss calculations for these parts are quite the same as others, but the eddy current loss calculation is different. The same approach for calculating eddy current loss in PM above could be suggestively used. However, the difficulty is that the core material is not nonlinear and the shape is not rectangular. Even though the flux density fluctuation in these part are small but due to the solid core, eddy current loss is hardly predicted to be small. So to verify this prediction, next part, core loss due to eddy current will be computed by using FEM.

### 3.4.4 Core loss calculation validations

#### 3.4.4.1 Eddy current loss calculated by FEM

Eddy current losses computations in the solid cores by FEM is conducted for a wide range of field currents. By using FEM, these computations are performed by giving the solid cores a conductivity of $10^7$ S/m. Table. 3.5 shows eddy current losses for solid core parts (refer to Fig. 2.25) in chapter 2 at 1000 rpm, no-load according to field currents.

<table>
<thead>
<tr>
<th>Field current [A]</th>
<th>-7</th>
<th>-5</th>
<th>-3</th>
<th>0</th>
<th>3</th>
<th>5</th>
<th>7</th>
</tr>
</thead>
<tbody>
<tr>
<td>Eddy current loss [W]</td>
<td>0.052</td>
<td>0.223</td>
<td>0.001</td>
<td>0.003</td>
<td>0.009</td>
<td>0.107</td>
<td>1.373</td>
</tr>
</tbody>
</table>

Despite the fact that, in order to have an accurate and reliable result by dynamic eddy current loss calculation, a very fine mesh should be adopted, this is quite challenging to the 3-D FEM
3.4. Iron loss calculation

<table>
<thead>
<tr>
<th>Coefficient</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k_b$</td>
<td>199</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>2</td>
</tr>
<tr>
<td>$k_e$</td>
<td>0.752</td>
</tr>
</tbody>
</table>

Table 3.6: Loss coefficients derived from measurement fitting

due to limits of time and computer resources. But from Table. 3.5, it could arrive at the negligibility of eddy current losses due to solid parts.

3.4.4.2 Core loss comparisons

For the core loss model in (3.54) to be accomplished, loss coefficients must firstly be determined from data-sheets of sample measurements with fitting process as shown in Fig. 3.43. Loss coefficients are detailed in Table. 3.6:

![Curve fitting for the specific loss measurement](image_url)

Fig. 3.43: Curve fitting for the specific loss measurement

The core loss contribution done by EMCN of stator and rotor is shown in Fig. 3.44.

![Core loss by EMCN at 6000 rpm, no-load according to field current](image_url)

Fig. 3.44: Core loss by EMCN at 6000 rpm, no-load according to field current

As seen, rotor loss takes a very small portion of total loss except the flux weakening area where
stator loss reduces and rotor loss increases. This is due to flux densities in the stator tooth is much reduced by negative field current (although it could partly increase harmonic contents as in Fig. 3.37) and flux densities in rotor increase as displayed in Fig. 3.45 for a point in the middle of the solid rotor core.

![Flux density graph](image)

**Fig. 3.45:** Flux density of a point in the rotor according to field current changes

As it will be seen, a good accordance between FEM and EMCN results for a wide range of field current as in Fig. 3.46 (the same core loss coefficients $k_h$, $\alpha$ and $k_e$ are applied to FEM) and between EMCN and experiment demonstrated in Fig. 3.47.

![Core loss graph](image)

**Fig. 3.46:** Core loss comparison according to field current variation at no-load

The core loss comparison according to load variation as in Fig. 3.48 when the field windings are not excited. As it will be observed, EMCN results agree well with ones by FEM and due to armature reaction, flux densities changes their amplitudes as well as harmonics, therefore core loss increases.

### 3.4.5 Core loss calculation using symmetry option

As roughly discussed in chapter 2, using symmetry option could save computation time for torque calculation i.e. torque could be faster calculated using only one sixth of electrical period.
3.4. Iron loss calculation

Fig. 3.47: Core loss comparison with measurement at no-load, $I_{dc} = 0$ A

Fig. 3.48: Core loss according to load variation, $I_{dc} = 0$ A

without any accuracy sacrifice. In this section, a same idea is examined for core loss calculation. The difference is that for torque calculation using flux MMF diagram, the symmetry is based on the phase flux linkages and currents. But for core loss calculation, the local flux density information are the input so the symmetry will be based on the similarities between flux densities at different positions. This approach promises a huge advantage with a 6 times faster gaining while considering a long optimization process. However accuracy examination must be performed.

It is important to remind some of the key characteristics of the machine:

- Symmetry three phase machine
- 6 slots presented in the stator
- Flux density patterns in the rotor repeat six times in one period.
- Core loss in end-shield, rotoric flux collector and outer stator parts are significantly small.
Therefore the idea is to use only one sixth electrical period of one pole pair in the stator and main rotor to retrieve core losses. The flux densities at points $A_1 \div A_6$ (radial component in the stator teeth) and $B_1 \div B_6$ (tangential component in the stator yoke) are shown in Fig. 3.49. It is obvious that the flux densities of all other one sixth electrical periods could be derived from the first one sixth ones as shown in Fig. 3.50.

![Fig. 3.49: Testing points for flux densities calculation](image1)

![Fig. 3.50: Flux density symmetry characteristic. a) Radial flux density in stator teeth. b) Tangential flux density in stator yoke](image2)

The core loss comparisons between full electrical period model and model using only one sixth electrical period are displayed in Fig. 3.51 at armature current of 8 A and difference field currents and speeds. As it will be seen two result are well matched with a slight different due to the numerical error during calculations.

**Conclusion**

This chapter has discussed about the application of EMCN in the modeling of the proposed DESM prototype. The flexible network was introduced to control the detail level of the mesh. Non-linearity of the magnetization curve is taken into consideration by iteratively solving the system nodal equation. The iron loss model has been focused to carefully consider addition losses by flux densities which are not natural either containing harmonics or biased by a DC
3.4. Iron loss calculation

Fig. 3.51: Core loss comparison between models using full and one sixth electrical period. Armature current 8 A, phase angle is zero. a) $I_{dc} = 0$ A. b) $I_{dc} = 4$ A.

component. The good accordance between results performed by EMCN method and ones from FEM has validated the accuracy of EMCN. Moreover, EMCN also reveals its advantageous feature over the FEM candidate in term of computation time. With all things presented, EMCN method applied to the DESM prototype prepares a readiness for a good design stage such as an optimization, where model’s parameters are expected to change and certainly connections with other parts such as an inverter, converter, etc.
This page intentionally left blank
The power of an electrical machine is principally limited by their thermal aspects. Overheating would cause insulation deterioration and consequently reduce machine’s life span. Recently, attentions to thermal designs has been rewarded by major improvements in the overall performance. In comparison with classical machines, a DESM has additional excitation windings i.e. extra heat sources from these winding’s copper losses. This would in one hand require a careful attention to the machine’s efficiency and on the other hand cause thermal problem worse. The main aim of this chapter is to develop a thermal model in transient regime for the studied DESM. This chapter is organized as follows: First, calculations for mechanical losses are briefed since these losses are parts of thermal model. Second, individual lumped thermal resistances and their calculations are addressed. Third, a lumped parameter thermal network and solving technique in transient mode are introduced. Finally, thermal coefficients adjustments by experiments will be presented. The final step is of importance since most of thermal equations are empirical meaning that they are subject to specific structures, assembly process, etc.

4.1 Thermal analysis approach

Heat transfer could be modeled by using a thermal network analogous to an electrical network composing of resistances and capacitors. Thermal resistances in a thermal network consists of conductive, convective and radiative resistances for different parts of the machine. Machine’s thermal analyses could be categorized into two basic types: lumped parameter circuit and numerical methods. No matter what type of method used, a big challenge to thermal analysis is thermal resistances determination which often requires empirical formulations and unfortunately, those values usually have significant impacts on the analysis result.

With numerical method, two available options are FEM method and computational fluid dynamics (CFD). CFD has an advantage that it can be used to predict flow in complex regions, such as around end-winding regions. FEM can only be used to model conductive heat transfer in solid components [81]. FEM method usually provides more accurate results with detailed
local temperature distribution however its long computation time make it less attractive in
the design process. In addition, only temperatures at few local points are sometimes sufficient
to the thermal design (for instance, winding temperature to manage insulation deterioration,
permanent magnet temperature to predict the demagnetization risk). Moreover, as mentioned
above, a thermal analysis requires a lot of empirical formulations. This means that using FEM
analysis has no big advantage in determining critical model’s parameters.

In this work, the lumped parameter thermal method will be utilized. By mean of lumped
parameter, each component of the machine is presented by one or several thermal resistances,
a thermal capacitor representing its heat storage and/or a heat source. A network for transient
analysis will be developed i.e. both thermal resistances and thermal capacitors are presented.
The system solution are obtained by using an iterative method. Aiming at evaluating motor’s
performance at wide operation range, a coupling between thermal and electromagnetic models
are necessarily provided. This is mainly due to the losses dependence on the temperature
and vice-versa. The losses from electromagnetic model are important inputs to the thermal
model. Copper losses of armature and field windings could be easily calculated based on their
geometries. In chapter 3, iron losses has been computed. Mechanical losses including windage
and bearing friction losses will be shortly addressed in the following section.

Fig. 4.1 illustrates the mechanical structure of the studied DESM. This consideration is sup-
portive for the thermal analysis. The thermal processes consider all three types conduction,
radiation and convection. However due to a complex surface geometries inside the machine and
also temperatures are not quite different between these surfaces and air around, radiations are
neglected inside the machine.
4.2 Mechanical losses

Two principal mechanical losses presented in an electrical machine are windage loss in the air-gap due to rotor’s rotation and friction losses in the bearings. Proper calculations of these losses not only help designers have a more accurate value of machine’s efficiency but also provide a good heat source input to the thermal model. At a glance, these losses are expected to be small due to two reasons: first, the machine size is relatively small resulting in a small air-gap diameter and hence roughly small windage loss and light rotor (acting on the bearing) leading to a small bearing friction load as well. Second, machine’s speed is not high (rated speed of about 2000 rpm) further make these losses small.

![Diagram of stator and rotor](image)

Fig. 4.2: Mechanical losses to be considered. a) Windage. b) Bearing friction

4.2.1 Windage loss

Windage loss in a rotating machine is the power absorbed by the air-gap between the rotor and the stator. A conventional approach for windage loss calculation is to compare a proposed machine to a similar machine with a known windage loss [82]. However in the design phase, an analytical calculation method is proved to be useful when various parameters might vary and hence windage loss is conveniently derived. Also, extrapolating the windage loss from commercial machine data is not an easy task. As presented in [82], empirical equations are developed for a cylindrical rotor and a factor considering the effect of salient poles.

4.2.1.1 Windage loss in a cylindrical rotor machine

According to [82], the windage loss of a cylinder rotating in a concentric cylinder is determined based on following assumptions:

- No axial flow exists
- The air-gap length is small compared to the air-gap radius and axial length
- The air in the gap is homogeneous
Chapter 4. Thermal model of the DESMs

With those assumptions, windage loss is expressed as (4.1)

\[ W_{\text{windage}} = \pi C_d \rho R^4 \omega^3 L \quad [\text{W}] \quad (4.1) \]

with \( \rho \) is air-gap density \([\text{kg/m}^3]\), \( R \) is the average air-gap diameter \([\text{m}]\), \( \omega \) is rotor angle speed \([\text{rad/s}]\), \( L \) is axial length \([\text{m}]\) and \( C_d \) is the skin friction coefficient.

This friction coefficient depends on the air flow state in the gap i.e. laminar, transition or turbulence which is characterized by Reynold number given by (4.2)

\[ R_e = \frac{\omega RD}{\nu} \quad (4.2) \]

with \( D \) is the air-gap length \([\text{m}]\) and \( \nu \) is kinematic viscosity of the air \([\text{m}^2/\text{s}]\).

- If \( R_e \leq 2300 \): air flow is laminar
- If \( 2300 < R_e \leq 4000 \): air flow is transition
- If \( 4000 < R_e \): air flow is turbulence

The friction coefficient \( C_d \) is defined as (4.3a) for laminar flow and (4.3b) for transition and turbulence cases.

\[ C_d = \frac{2}{R_e} \quad (4.3a) \]

\[ \frac{1}{\sqrt{C_d}} = 2.04 + 1.768 \cdot \ln \left( R_e \sqrt{C_d} \right) \quad (4.3b) \]

### 4.2.1.2 Windage loss in a salient machine

(4.1) is developed for a cylinder rotor case. In order to take into account saliency aspect which additionally increases windage loss due to its obstacle to the rotation, loss calculate by (4.1) will be multiplied with a factor empirically given by (4.4) [82]:

\[ K = 8.5 \left( \frac{H}{R} \right) + 2.2 \quad (4.4) \]

with \( H \) is the pole depth

As generally stated in [82] that (4.4) is not applicable for the case where \( H/R < 0.06 \). This factor will be examined later with the studied DESM.

Taking the studied DESM’s dimensions, with the air-gap temperature is 50 °C. At the speed of 2000 rpm, the windage loss is estimated to be 0.2 W if the rotor is assumed cylindrical. This loss is quite negligible even if applying a saliency factor, a few times increased would not make it considerable.

The windage loss is therefore neglected in the next analysis.
4.3. Thermal resistances calculation

4.2.2 Bearing friction loss

In a rotating machine, two bearing are usually located in the driving and non-driving ends. The friction loss is apparently subject to the rotor’s properties (rotating speed and weight including shaft) and bearing’s properties (size and friction coefficient). With the bearing using lubricant oil, after a certain time in use, the friction coefficient is usually increase due to the deterioration of lubricant oil. Therefore, it is complicated to obtain an accurate calculation of this friction loss. According to SKF bearing manufacturing [83], the bearing friction could be computed by

\[ W_{\text{bearing}} = 0.525 \cdot 10^{-4} \mu Pdn \]  

(4.5)

with \( \mu \) is friction coefficient, \( P \) is equivalent dynamic bearing load [N], \( d \) is bearing diameter [mm], \( n \) is rotating speed [rpm].

Considering the studied DESM, the bearing loss is approximately 1 W which is again quite small and will be neglected.

After all mechanical losses considered, it would be concluded as expected the beginning that the mechanical losses are negligible (1.2 W at 2000 rpm) due to a small machine size and low/medium speed. One should be noted that in practice, additional mechanical losses would occur due to mechanical tolerance during manufacturing process or one resulted from vibration due to machine’s asymmetry, etc.

4.3 Thermal resistances calculation

Thermal resistance, thermal capacitor and heat source are three component categories of a thermal network. Fig. 4.3 displays a typical node in a thermal network.

Fig. 4.3: A typical node in a thermal network

with \( P \) is heat source, \( \theta \) is node temperature, \( C \) is heat storage capacitor, \( R \) is thermal resistance

Heat sources are derived from electromagnetic and mechanical analyses, heat storage capacitors are determined by (4.6)

\[ C = mc_p \]  

(4.6)
with \( m \) and \( c_p \) are mass [kg] and specific heat capacity [J/kg °C] of the component.

However, it is not straightforward for thermal resistance calculation which normally requires empirical coefficients. In the next part, different types of thermal resistance computation will be discussed in detail.

### 4.3.1 Basic cylindrical component

In a rotating machine, almost components are fully or partly shaped as cylindrical: stator yoke, stator teeth, rotor core etc... Therefore a cylindrical component would be considered as the basic shape for conductive thermal resistance calculation. The basic form for conductive thermal resistance is given by (4.7):

\[
R = \int_0^L \frac{dl}{kS(l)} \quad (4.7)
\]

with \( k, L \) are thermal conductivity and length of the object, \( S(l) \) is cross section at length \( l \).

In [84], a sufficiently complex model was presented as shown in Fig. 4.4

![Cylindrical component](a)

Fig. 4.4: Cylindrical component. a) Physical shape. b) Equivalent thermal model

The \( \theta_1, \theta_2, \theta_3 \) and \( \theta_4 \) are temperatures at inner, outer surface and two sides of the cylinder respectively. Index “a” and “r” represent thermal conduction in the axial and radial directions. The central node of each network gives the mean temperature \( \theta_m \) of the component. \( u \) is the internal heat generation, \( C \) is heat storage capacitor.

This configuration would give a quite accurate result, however it introduces a complexity for both calculations and number of nodes in the network as pointed out in [85]. Authors of [85] had simplified the configuration while still maintaining result accuracy by neglecting the axial thermal flux and also \( R_3 \) resistance since it is always neglected from a practical point of view [86]. The simplified model is demonstrated in Fig. 4.5. As it will be seen, two nodes for one component has been removed.
4.3. Thermal resistances calculation

\[ R_1 = \frac{1}{2\pi k L} \ln \frac{r_m}{r_1} \]  \hspace{1cm} (4.8a)

\[ R_2 = \frac{1}{2\pi k L} \ln \frac{r_2}{r_m} \]  \hspace{1cm} (4.8b)

where

\[ r_m = \frac{r_1 + r_2}{2} \]  \hspace{1cm} (4.9)

with \( r_1, r_2 \) and \( L \) are inner, outer surface radii and axial length of the cylinder. \( k \) is the thermal conductivity of the cylinder’s material.

The total thermal capacitance of the cylinder is found from material density \( \rho \), the specific heat capacitance \( c_p \) and the cylinder’s dimensions as (4.10)

\[ C = \rho \pi \left( r_2^2 - r_1^2 \right) L c_p \]  \hspace{1cm} (4.10)

4.3.2 Outer frame heat transfer

The heat transfer from the frame surface to the ambient is one of the most important problem in thermal analysis since it is the way to evacuate generated heat from the machine. With a relatively low power (about 2 kW rated power), the studied DESM uses natural air cooling causing convective coefficient \( h_c \) small ranging from 5 to 100 w/°C/m². In this case, a portion from radiative heat transfer would be significant.

4.3.2.1 Convective heat transfer coefficient

The convection process depends on the surface area, type of surface (i.e horizontal or vertical) and ambient air temperature \( \theta_a \). The typical outer frame of a horizontal electrical machine could be depicted in Fig. 4.6

In the next calculations, following assumptions are made:

- Surface temperatures \( \theta_s \) are unique everywhere
- Two vertical plates are identical
- Average surface emissivity are used
Chapter 4. Thermal model of the DESMs

Convective heat transfer is derived from a series of calculations expressed in (4.11) [87]

\[ h_c = \frac{kN_u}{L_c} \]

\[ N_u = \left( A + \frac{0.387 \cdot R_a^{1/6}}{1 + (B/Pr)^{9/16}} \right)^2 \]

\[ R_a = \frac{\beta \cdot g \cdot (T_s - T_a) \cdot L_c^3}{\nu \cdot \alpha} \]

with \( N_u, R_a \) and \( Pr \) are Nusselt, Rayleigh and Prandt numbers of the ambient air respectively. \( \beta, \nu \) and \( \alpha \) are expansion, viscosity and diffusivity coefficients of the ambient air. \( L_c \) is the characteristic length of the surface determined by (4.12).

\[ L_c = \begin{cases} D & \text{With a horizontal cylinder of diameter } D \\ \frac{D \sqrt{\pi}}{2} & \text{With a vertical circle plate of diameter } D \end{cases} \]

(4.12)

\( A \) and \( B \) are coefficient depending on type of surface determined by (4.13)

\[ [A, B] = \begin{cases} [0.6, 0.559] & \text{With horizontal surface} \\ [0.825, 0.492] & \text{With vertical plate} \end{cases} \]

(4.13)

Convective resistance due to horizontal cylinder surface \( S_1 \):

\[ R_1 = \frac{1}{h_1 S_1} \]

(4.14)

Convective resistance due to one vertical plate surface \( S_2 \):

\[ R_2 = \frac{1}{h_2 S_2} \]

(4.15)

where \( h_1 \) and \( h_2 \) are convective coefficients of vertical plate and horizontal surfaces respectively. Equivalent convective resistance resulted from a parallel connection of individual convective resistances:

\[ \frac{1}{R_c} = \frac{1}{R_1} + \frac{2}{R_2} = h_1 S_1 + 2h_2 S_2 \]

\[ R_c = \frac{1}{h_1 S_1 + 2h_2 S_2} = \frac{1}{h_{\text{eq}} S} \]

(4.16)

with \( h_{\text{eq}} \) is equivalent convective coefficient and \( S \) is the total surface.
4.3. Thermal resistances calculation

From (4.16), \( h_{ceq} \) could be computed as (4.17):

\[
    h_{ceq} = \frac{h_1 S_1 + 2 h_2 S_2}{S_1 + 2 S_2} = \frac{h_1 \pi \frac{L^2}{4} + h_2 \pi DL}{\pi \frac{D^2}{4} + \pi DL} = \frac{h_1 D + 2 h_2 L}{D + 2L}
\]

(4.17)

4.3.2.2 Radiative heat transfer coefficient

Heat transfer by radiation could facilitate the heat evacuation from the machine especially in natural air convection circumstances. The radiative heat transfer strongly depend not only on the temperature difference between the surface and the ambient but also on the surface property characterized by an emissivity coefficient \( \epsilon \). The surface heat density \( q_r \) evacuated from a body surface is given by (4.18) [87]

\[
    q_r = \epsilon \sigma_c (\theta_s^4 - \theta_a^4)
\]

(4.18)

with \( \sigma_c \) is Stefan-Boltzmann constant \((5.67 \cdot 10^{-8} \text{ W/m}^2/\text{K}^4)\).

The emissivity coefficient of a real surface is not a constant, it rather varies with the temperature, color and material of the surface as well as the wave length and the direction of the emitted radiation [87]. That would make the problem quite complex so that as mentioned, the emissivity is practically assumed to be constant everywhere on the surface.

The surface heat density exchange in (4.18) could be also written in the form of radiative heat transfer coefficient \( h_r \) as (4.19)

\[
    q_r = h_r (\theta_s - \theta_a)
\]

(4.19)

From (4.18) and (4.19), \( h_r \) is obtained derived as

\[
    h_r = \frac{\epsilon \sigma_c (\theta_s^4 - \theta_a^4)}{\theta_s - \theta_a} = \epsilon \sigma_c (T_s + T_a) (\theta_s^2 + \theta_a^2)
\]

(4.20)

And thermal resistance due to radiative heat transfer:

\[
    R_r = \frac{1}{h_r S}
\]

(4.21)

4.3.2.3 Equivalent surface heat transfer coefficient

With corresponding convective and radiative heat transfer coefficients being determined, the equivalent heat transfer coefficient \( h_e \) is derived. The thermal resistance between the machine surface and the ambient (due to both convection and radiation processes):

\[
    R_s = \frac{1}{h_c} + \frac{1}{h_r} = \frac{1}{(h_c + h_r) S}
\]

(4.22)
And $h_e$ could be derived as (4.23)

$$h_e = \frac{1}{R_s} = h_c + h_r \tag{4.23}$$

Therefore, the equivalent coefficient is simply the sum of separate coefficients due to convective and radiative heat transfers. In practice, it is impossible to individually measure each coefficient but the equivalent coefficient instead. However, with (4.23) the contribution of each process can be evaluated. As it will be seen, with natural air convection, the portion of radiation is significant.

A case study with different outer surface temperatures will be shown below to calculate the surface heat transfer coefficient.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Emissivity</td>
<td>0.5*</td>
</tr>
<tr>
<td>Total axial length</td>
<td>115 mm</td>
</tr>
<tr>
<td>Outer diameter</td>
<td>185 mm</td>
</tr>
<tr>
<td>Ambient temperature</td>
<td>22 °C</td>
</tr>
<tr>
<td>Outer surface temperature</td>
<td>$20 \div 100$ °C</td>
</tr>
</tbody>
</table>

* An average value between 0 and 1 is chosen

The coefficients are according to surface temperature variation are demonstrated in Fig. 4.7. As it will be seen, both coefficients (due to convection and radiation) increase as surface temperature goes up. This is explained by (4.20) for the radiative coefficient. For convective coefficient, it is due to the fact that increasing temperature difference between surface and ambient temperature make Rayleigh number increases, as the result, Nuselt number increase and radiative coefficient increases as well. The individual contributions of each coefficient are very close for this case with natural air convection. However, in cases of forced air convection or water cooling systems, the convective coefficient would be few hundreds. In those cases, radiative heat transfer is negligible and its calculation would be omitted.

### 4.3.3 Air-gap heat transfer

The convective heat transfer in the air-gap is different from one on the surface since it is confined in a narrow gap between stator and rotor instead of between the outer surface and a considerably infinite ambient environment. For the studied DESM, there is no internal forced air ventilation, this heat transfer process is affected by temperature, dimensions of the air-gap as well as surface speed of the rotor. As pointed out in [88] which is demonstrated in Fig. 4.8, at low speed only one steady state flow is established. However, a secondary state flow will be
4.3. Thermal resistances calculation

![Graph showing heat transfer coefficient according to surface temperature](image)

**Fig. 4.7:** Heat transfer coefficient according to surface temperature

Formed as speed increases, this introduces a turbulence state in the air-gap and hence increases transferred heat.

![Diagram showing disturbance in the air-gap according to rotor speed](image)

**Fig. 4.8:** Disturbance in the air-gap according to rotor speed. a) Low speed. b) High speed

In order to judge whether the flow in the air-gap is laminar, vortex or turbulent, the Taylor number $T_a$ is used given by (4.24):

$$T_a = \frac{\Omega \cdot r_m^{0.5} \cdot d^{0.5}}{\nu}$$  \hspace{1cm} (4.24)

with $\Omega$ is motor’s angular speed [rad/s], $r_m$ is average air-gap diameter [m], $d$ is air-gap length [m].

Depending on $T_a$, Nusselt number and air-gap state will be determined as (4.25):

$$N_u = \begin{cases} 
2 & T_a \leq 41 \text{ (laminar)} \\
0.212 \cdot \theta_a^{0.63} \cdot P_r^{0.27} & 41 < T_a \leq 100 \text{ (vortex)} \\
0.386 \cdot \theta_a^{0.5} \cdot P_r^{0.27} & 100 < T_a \text{ (turbulent)} 
\end{cases}$$  \hspace{1cm} (4.25)

Convective coefficient in the air-gap is then defined as (4.26) with 10% increased to take into account slotting effect discussed in [89]

$$h_{ca} = \frac{1.1N_u k}{d}$$  \hspace{1cm} (4.26)

Thesis K. HOANG
Air-gap thermal contact is then defined as (4.27)

$$R_{\text{air-gap}} = \frac{1}{h_{ca}S_{\text{air-gap}}}$$

with $S_{\text{air-gap}}$ is cylindrical surface of the air-gap.

Air-gap thermal resistance according to rotor speed and air-gap temperature is displayed in Fig. 4.9

![Graph showing air-gap thermal resistance variation according to rotor speed and air-gap temperature](attachment:image1)

Fig. 4.9: Air-gap thermal resistance variation according to rotor speed and air-gap temperature

As observed in Fig. 4.9, at low speed the Taylor number is small and the Nusselt number stays constant, therefore air-gap thermal resistance does not change as rotor speed varies. Increasing speed creates vortex, turbulence air flow in the air-gap help facilitate heat transfer. As the result, corresponding thermal resistance decreases. The dependence of air-gap thermal resistance on its temperature is also clear that thermal conductivity (strong impact on thermal resistance) of the air increases along with its temperature. Fig. 4.9 also reveals the fact that having a completely passive rotor has an obvious advantage of heat evacuation since heat from the rotor has to pass through air-gap thermal resistance which is pretty big to the stator and then to the ambient. Considering a 200 W energy loss located in the rotor, with an air-gap thermal resistance of $0.5 \degree C/W$ would make a temperature of roughly $100 \degree C$ of rotor higher than that stator. That also agrees well with a general statement that heat sources should be located close to the machine’s surface as much as possible in the thermal point of view. The studied DESM’s topology only has PMs embedded in the rotor while all the windings are on stator side. As analyzed in chapter 3, PMs losses are quite negligible leading to the rotor could be considered passive.

### 4.3.4 Thermal resistances between windings and core

#### 4.3.4.1 Thermal resistance between armature active winding and stator core

Thermal resistance between armature copper and core is of importance because this big resistance is on the main path of evacuating armature copper loss to the ambient. In thermal
domain, armature winding usually presents a complex structure to accurately calculate thermal resistance various layers exist as demonstrated in Fig. 4.10.

![Winding insulation in the slot](image)

Fig. 4.10: Winding insulation in the slot

Authors of [90] proposed an equivalent thermal conductivity between copper and iron $k_{cu,ir}$ of the air and insulation material in the slots. This equivalent conductivity depends on many factors such as material, quality of the impregnation, filling factor, etc. A linear regression from series of tests to determine this equivalent value as function of filling factor $k_f$ is given by (4.28). Fortunately the filling factors for those tests were in range $0.35 \div 0.45$ which is close to the one of studied DESM (0.35), there for the regression model could be applicable.

$$k_{Cu,ir} = 0.1076 \cdot k_f + 0.029967 \quad (4.28)$$

It should be noted that in case of no copper presented ($k_f = 0$), $k_{cu,ir}$ is 0.029967 which is the thermal conductivity of the air at 80 °C.

The thermal resistance between copper and the iron core is determined as (4.29)

$$R_{Cu,ir} = \frac{S_{slot}(1 - k_f)}{k_{Cu,ir} l_{sp}^2 L_s} \quad (4.29)$$

with $l_{sp}$ is the stator slot perimeter, $L_s$ is active stack length and $S_{slot}$ is the stator slot surface.

From (4.28) and (4.29) it is concluded that improving filling factor would lower thermal resistance between copper and the core not only by increasing equivalent thermal conductivity but also decreasing insulation layer thickness. The studied DESM has a pretty low filling factor of 0.35 (due to the distributed winding arrangement) leading to equivalent thermal conductivity of 0.0676 which is only 2.25 times one of the air (at 80 °C).

### 4.3.4.2 Thermal resistance between ending and active parts of armature winding

Heat evacuation from the active part (inside stator slots) of the armature winding could be done conveniently through an insulation contact with stator teeth. However, end-windings faces difficulties since this process must be principally done in axial direction though active winding and then to the stator teeth. With the presence of global excitation windings, an additional path is provided though this winding via small air gap between these windings as shown in
Fig. 4.11. Thermal resistances in these two paths (though active winding and exitation winding) are generally large, therefore, end-winding temperature is predicted to be higher compared to that of the active winding. With an assumption of uniform temperature distribution in each of end-winding and active winding parts, the thermal resistance between end-winding and active winding could be expressed as (4.30):

\[ R_{end-active} = \frac{l_{end}S_{slot}k_f}{\alpha_{ea}} \]  

(4.30)

with \( l_{end} \) is length of the end-winding and \( \alpha_{ea} \) is a coefficient characterizing the heat transfer between end-winding and active winding, this coefficient will be determined by experiments.

### 4.3.4.3 Thermal resistance between field windings and stator core

The double excitation principle presents additional field windings, this makes the machine complicated not only about the electromagnetic analysis but also a thermal one. The main reason is the “non-standard” assembly of these windings. Unlike armature windings where manufacturing and assembly processes would have a standardization and hence formulation for its thermal resistance is available, no similar researches for that of toroidal field winding in the studied DESM. A close look at one field winding of the DESM is shown in Fig. 4.11. As it can be seen, the contact surface between winding and core is smaller than that of a winding located in the slot. Moreover, this contact is not so tight i.e. a big air space is presented between the windings and stator core. These explain why heat evacuation for the field windings of the prototype is more difficult than the one of the armature windings.

![Field winding of the studied DESM](image)

Fig. 4.11: Field winding of the studied DESM

The residual air and contact surface between field winding and motor core (especially to the end-shield side) is difficulty to determine. Despite of these difficulties, formula (4.29) corrected by a factor \( \alpha_f \) will be applied to determine thermal resistance between field winding and outer stator core. Therefore, an experiment is required to determine this correction factor.
4.3.4.4 *Thermal resistance between armature end-winding and field winding*

The thermal resistance between armature end-winding and field windings shown in Fig. 4.11 consists of thermal resistance of the end-winding insulation and one of a small air-gap between these two parts. With the DESM prototype, parameters of these types are not constant along the gap and complicated in shape. Therefore, an equivalent air-gap will be considered for this thermal resistance calculation. With this assumption, formulas from (4.24) to (4.27) could be applied. The air-gap length will be determined experimentally.

4.3.5 *Thermal contact resistance*

In electrical machines, there exists different types of contact, such as between laminations, between stator core and frame, mechanical bearing area, etc. Due to rough surfaces, it cannot be assumed that a thermal short circuit exists between them. Instead, some air presented in the contact area resulting in a thermal resistance. In this section, lamination contacts are neglected since axial heat flows in the core are not considered as mentioned earlier.

The rotor in fact consists of rotor core and PMs, there for thermal contacts appear between them. However, due to a small loss on rotor, the rotor will be considered as a cylindrical component discussed in 4.3.1.

Ball bearing thermal contact resistance calculation also present a difficulty since the balls are in contact with the inner and outer rings just in a very small mechanical spot. Additionally, inside the bearing the presence of lubricant introduces factors of uncertainty for thermal resistance determination. A simple solution is to considered this thermal resistance as an equivalent air-gap of around 0.3 mm [90].

Thermal contact resistance coefficient between inner (laminated) and outer (solid) stator yokes is a function of the surface’s roughnesses and the pressure which is created during the machine’s assembly. An example of the frame contact coefficient as a function of contact pressure is shown in Fig. 4.12 [84].

Unfortunately, information on pressure and surface’s roughnesses are usually unavailable. However, as discussed in [84], even a large variation in the value of this value has surprisingly little effect on the estimates of winding temperatures. Therefore in this thesis, an arbitrary coefficient of 1000 W/m$^2$ °C (a value in the middle of ranges shown in Fig. 4.12 will be adopted).

4.4 *Transient thermal network*

The complete lumped parameter thermal network of the studied DESM is displayed in Fig. 4.13 for the transient analysis with notes as follows:
Fig. 4.12: Frame-core contact coefficient according to contact pressure

Fig. 4.13: Thermal network of the studied DESM

- Two groups of thermal resistance are presented: one using empirical formulations (yellow) and the other could be simply calculated based on object’s geometry only (cylindrical component)

- $R_{\text{ambient}}$, $R_{\text{air-gap}}$ and $R_{\text{end winding - rotor}}$ are temperature dependent and therefore will be updated through iterations
4.4. Transient thermal network

- Only copper losses are temperature dependent loss (Iron losses are assumed constant)
- Mechanical losses (bearing friction and windage) are neglected as discussed in section 4.2
- Residual flux densities of PMs are assumed temperature independent since during transient analysis, numerous iterations will be performed. If these flux densities are subject to temperature, electromagnetic analysis has to be run at the same number of iterations, that would significantly increase computation time
- $P_{\text{ironS1}}, P_{\text{ironS1}}, P_{\text{ironS1}}$ are iron losses in the outer stator yoke, inner stator yoke and stator teeth respectively. $P_{\text{ironR}}$ is iron loss in the rotor. $P_{\text{cuF}}$ and $P_{\text{cuP}}$ are copper losses in field and phase windings

4.4.1 Approach with constant heat sources

Before going with the transient process where the heat sources are temperature dependent, a solution to the process with constant heat sources will be carried out as an easy and basic step. The thermal network could be quite easily solved with MATLAB Simulink, however this will lead to a time consuming process due to each time calling Simulink model when interacting with electromagnetic model (handled by MATLAB script). Therefore, an analytical method could be much more practical.

Firstly, a typical node as in Fig. 4.3 is recalled as Fig. 4.14 with thermal resistances is replaced by s thermal conductance ($G = \frac{1}{R}$)

![Fig. 4.14](image)

Applying Kirchhoff’s circuit law on node 2:

\[-C_2 \frac{d\theta_2}{dt} + (\theta_1 - \theta_2) g_{21} + (\theta_3 - \theta_2) g_{23} + P_2 = 0\]  
\[C_2 \frac{d\theta_2}{dt} + \theta_1 G_{21} + \theta_2 G_{22} + \theta_3 G_{23} = P_2\]  
with $G_{21} = -g_{21}, G_{23} = -g_{23}, G_{22} = g_{21} + g_{23}$

Nodal equation for any node $i$ in a system of $n$ nodes.

\[C_i \frac{d\theta_i}{dt} + \theta_1 G_{i1} + \theta_2 G_{i2} + ... + \theta_i G_{ii} + ... + \theta_n G_{im} = P_i\]  

(4.32)
with \( G_{ii} = \sum_{j=1}^{n} g_{ij}, \quad G_{ij} = -g_{ij} \ (i \neq j) \)

System formulation could be expressed as (4.33):

\[
[C] \cdot \frac{d[\theta]}{dt} + [G] \cdot [\theta] = [P] \tag{4.33}
\]

with \([C], \ [\theta], \ [G]\) and \([P]\) are matrices for nodal capacitors, nodal temperatures, thermal conductances and nodal heat sources respectively. It should be remarked that the establishment of thermal conductance matrix \([P]\) is exactly the same as one performed for magnetic permeance matrix in chapter 3.

It should be noted that capacitor matrix essentially consists of zero components as no thermal storage capacitors are considered at these nodes as shown in Fig. 4.13; therefore, (4.33) includes both linear differential equations and linear equations. As a matter of fact, solving approach to these two equation types are different. Therefore, system equations (4.33) should be divided into two sub-system equations given by (4.34): one includes \(n_1\) nodes where capacitors are presented (subsystem 1) and the other for those without thermal storage capacitor (subsystem 2)

\[
\begin{cases}
[C_1] \cdot \frac{d[\theta_1]}{dt} + [G_1] \cdot [\theta_1] = [P_1] - [G_3] \cdot [\theta_2] \\
[G_2] \cdot [\theta_2] = [P_2] - [G_3]^T \cdot [\theta_1]
\end{cases} \tag{4.34}
\]

\([C_1], [\theta_1], [P_1]\): Capacitors, temperatures, heat sources at nodes of subsystem 1

\([\theta_2], [P_2]\): Capacitors, temperatures, heat sources at nodes of subsystem 2

Thermal conductance matrices \([G_1], [G_2]\) and \([G_3]\) are derived from system matrix \([G]\) as in Fig. 4.15

\[
\begin{array}{c}
1 \\
n_1 \\
n \\
\end{array}
\begin{bmatrix}
| \quad [G_1] \quad | \\
| [G_3] | \\
| [G_2] | \\
\end{bmatrix}
\begin{array}{c}
| \quad [G_3]^T \quad | \\
| [G_1] | \\
| [G_2] | \\
\end{array}
\]

Fig. 4.15: Sub-thermal conductance matrix determination

### 4.4.1.1 Iterative method for differential equations solving

The system equations (4.34) is firstly rewritten in differential form given by (4.35)

\[
\begin{cases}
[C_1] \cdot \frac{\Delta[\theta_1]}{\Delta t} + [G_1] \cdot [\theta_1] = [P_1] - [G_3] \cdot [\theta_2] \\
[G_2] \cdot [\theta_2] = [P_2] - [G_3]^T \cdot [\theta_1]
\end{cases} \tag{4.35}
\]

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with $\Delta t$ is sufficiently small

Solution to (4.35) is found by an iterative method where differential equations are solved by updates from the previous solution and the rest (linear equations) is directly solved from newly updated differential equations. The solution at iteration $(k+1)$ is given by (4.36) with the assumption that thermal conductance matrices are unchanged for this basic step (with constant heat sources).

![R-C network example](image)

$$
\begin{align*}
[\theta_1]^{(k+1)} &= [\theta_1]^{(k)} + \Delta t \cdot [C_1]^{-1} \left( [P_1] - [G_3] \cdot [\theta_2]^{(k)} - [G_1] \cdot [\theta_1]^{(k)} \right) \\
[\theta_2]^{(k+1)} &= [G_2]^{-1} \cdot \left( [P_2] - [G_3]^T \cdot [\theta_1]^{(k+1)} \right)
\end{align*}
$$

(4.36)

It should be noted that solution (4.36) is actually applicable to any transient $R-C$ circuit (with all $C$ should be grounded) with constant current sources.

4.4.1.2 $R-C$ network example

In order to examine the accuracy, effectiveness and general use of this approach as a basic step, a randomly created $R-C$ network will be used as displayed in Fig. 4.16. Values are given as follows:

- $R_1 = 16$, $R_2 = 25$, $R_3 = 4$, $R_4 = 12$, $R_5 = 6$, $R_6 = 5$, $R_7 = 8$ [Ω]
- $C_1 = 200$, $C_2 = 60$, $C_4 = 47$, $C_5 = 100$ [$\mu$F]
- $i_1 = 5$, $i_5 = 10$ [A]

![R-C network example](image)

Fig. 4.16: A freely created $R-C$ circuit with grounded capacitors

All nodal voltages are to be calculated and compared by using (4.36) and MATLAB Simulink. The conditions for analysis are:

- All capacitors are completely discharged

- $\Delta t = 0.1$ ms
The result comparison is shown in Fig. 4.17. As it will be seen, two models reveal exactly same results but analytical is much faster with only 26 ms while the time for Simulink is 2.37 s (mainly due to interacting time between Simulink and script environment).

**Fig. 4.17:** Comparison between analytical and Simulink. Solid - Analytical, dash - Simulink

### 4.4.2 Coupling between thermal and electromagnetic models

Thermal and electromagnetic analyses are hard to reveal accurate results if separate modelings are performed since losses are temperature dependent. Therefore, two systems should be coupled where losses output of electromagnetic model are input to thermal model and vice versa, temperature result from thermal analysis are necessary to electromagnetic one. The coupling is shown in Fig. 4.18.

**Fig. 4.18:** Coupling between thermal and electromagnetic model

The working principle of coupled system in Fig. 4.18 is explained as follows:

- Electromagnetic model is only run whenever there is a change in any of three variables: Speed, field current and armature current (**Condition 1**)
4.5 Thermal coefficient re-determination by experiments

- Losses (copper and iron losses) from electromagnetic analysis and initial temperatures (at the beginning, ambient temperature is taken for every nodes) are input to thermal modal.
- Thermal analysis is run with a local iterative process as presented in 4.4.1 with a pre-defined time period of one iteration. During this time, heat sources (losses) and heat transfer coefficient at the surface are assumed constant. This analysis will output local temperatures.
- These newly updated temperatures will be used for initial temperatures and to re-calculate copper losses in the next iteration of thermal analysis.
- Local iterative process for thermal analysis continues until stopping time is reached or condition 1 is met.
- If condition 1 is met, electromagnetic model will be run with newest updates of windings temperatures.

4.5 Thermal coefficient re-determination by experiments

As shown in Fig. 4.13, many thermal resistance calculations require empirical equations and even that kind of equations does not exist for some, for instance thermal resistance between field windings and the outer stator yoke. Therefore, coefficients verification and re-determination by measurements are necessary.

4.5.1 Experiment approach

In order to more accurately determine thermal coefficients of the machine, various experiments to separately evaluate single contributions of different heat sources will be conducted. Copper loss and core loss are two main heat sources of the machine (since mechanical losses are neglected), however core loss is mainly located in the stator core and is evacuated to the surface by conductive thermal resistance which does not require empirical equations. Therefore, static (i.e. no rotation and hence no core loss occurred) experiments with copper losses (by field and armature windings) will be handled.

As shown in Fig. 4.19, a thermal coupler is used to measure surface temperature, the average temperature of windings are calculated by (4.37)

\[ \theta_{\text{winding}} = \theta_0 + \frac{1}{\alpha} \left( \frac{R}{R_0} - 1 \right) \]  \hspace{1cm} (4.37)

with \( \theta_0 \) and \( R_0 \) are initial temperature and winding electrical resistance at that temperature. \( \alpha \) is winding temperature coefficient at \( \theta_0 \) (\( \approx 0.004 /^\circ\text{C} \) at 20 \(^\circ\text{C} \)). \( R \) is winding electrical resistance simply derived from measured current and voltage of the winding.

Three static measurements will be conducted as follows:

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Case 1: Two field windings (group 1) are connected in series and excited with a DC current of 4 A. Armature windings (group 2) are not excited.

Case 2: Two field windings are not excited. Three armature windings are connected in series and excited with a DC current of 4 A.

Case 3: Two field windings are connected with three armature windings (all 5 windings are in series) and excited with a DC current of 4 A.

For each measurement, following procedures will be taken:

- Voltage $U$ and current $I$ of each winding group (field and armature windings) will be recorded
- Surface temperature $\theta_s$ is recorded
- Recording time interval is 30 mins (decided by several trials based on the thermal transient process)

For each measurement, following data could be retrieved:

- Surface temperature (directly measured)
- Winding temperature as (4.37)
4.5. Thermal coefficient re-determination by experiments

- Surface coefficient is calculated by (4.38)

\[ h = \frac{\sum_{i=1}^{n} U_i I_i}{\Delta \theta \cdot S} \]  

(4.38)

with \( U_i \) and \( I_i \) are final voltage and current of winding group \( i \)th, \( \Delta \theta \) is final temperature difference between surface and ambient and \( S \) is surface area of the machine.

In order to verify predicted coefficients with measurement, the equivalent thermal network for the experiment could be simplified as Fig. 4.20. In this network, the thermal network for the air-gap and rotor part are neglected due to heat from field and armature windings are almost evacuated through stator core to the surface. As it will be seen in Fig. 4.20, there are always two paths for heat evacuation of either field or armature windings. Compared to a classical machine where there is no presence of windings like global field winding in this machine, heat evacuation for the armature windings will hardly pass through air space in the end-winding area to the surface i.e. only the right hand side path in Fig. 4.20.

![Fig. 4.20: Simplified thermal network for the static measurement](image)

4.5.2 Measurement result and thermal coefficient determination

The thermal transient processes for three cases mentioned above are shown in Fig. 4.21. As shown, the transient process takes quite a long time which is approximately 6 hours. This is because of low surface thermal coefficient with natural air convection causing high thermal resistance and hence long thermal constant.

The final value in of the transient process (which could be considered as steady-state values) are reported in Table. 4.2.
Even though the applied current is rather low and at static condition (no rotor movement i.e. zero core losses), the recorded temperature is high due to the natural air cooling. From these measurement results, following coefficients (Fig. 4.20) will be determined:

- Surface heat coefficient
- Coefficient related to thermal resistance between field windings and outer stator yoke: $\alpha_f$
- Coefficient related to thermal resistance between end-winding and active parts of the armature winding: $\alpha_{ea}$
- Equivalent air-gap length between armature end-windings and field windings: $l_e$
4.5. Thermal coefficient re-determination by experiments

It should be noted that thermal resistance between active parts of armature winding and stator core follows (4.29) and thermal contact resistance between inner and outer stator cores is calculated with a fixed contact coefficient of 1000 W/m² °C as mentioned in 4.3.5.

4.5.2.1 Surface heat coefficient determination

The first and easy-to-determine thermal coefficient is the surface heat coefficient which consists of convective and radiative ones. Having accepted that all heat sources will be evacuated through the surface of the machine, the surface heat coefficient $h_s$ is calculated by (4.38) according to different surface temperatures and winding powers (copper losses). These values are listed in Table. 4.3 in comparison with ones calculate by equations from (4.17) to (4.23)

<table>
<thead>
<tr>
<th>Case</th>
<th>Surface temp. [°C]</th>
<th>Measured $h_s$ [W/°C/m²]</th>
<th>Calculated $h_s$ [W/°C/m²]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>50</td>
<td>13.34</td>
<td>10.96</td>
</tr>
<tr>
<td>2</td>
<td>44.3</td>
<td>12.15</td>
<td>10.51</td>
</tr>
<tr>
<td>3</td>
<td>73.2</td>
<td>14.83</td>
<td>12.57</td>
</tr>
</tbody>
</table>

From Table. 4.3, it is obvious that at higher surface temperature, the coefficient increases, this is due to increases in convection and radiation as well. However, there are differences between measured and calculated ones. This could be explained by difference surface emissivities but more importantly the machine in the experiment is coupled with some components which certainly increases equivalent surface for heat evacuation and hence coefficient derived from (4.38) will be higher. Therefore, a correction factor of 1.2 is applied to this coefficient. The measured, calculated coefficient in Table. 4.3 together with the corrected one are displayed in Fig. 4.22

![Fig. 4.22: Surface coefficient according to surface temperature at 20 °C ambient temperature](image-url)
4.5.2.2 Coefficients associated with windings

Coefficients associated with armature and field windings as mentioned above namely $\alpha_f$, $\alpha_{ea}$ and $l_e$ will be determined by a simple optimization to minimize the norm $\|\cdot\|_\infty$ between final steady-state temperatures of calculation and measurement in three cases. A coefficient set chosen is reported in Table. 4.4. The accuracy of these values will be concluded by validations with experiments.

<table>
<thead>
<tr>
<th>$\alpha_f$</th>
<th>$\alpha_{ea}$ [W/m°C]</th>
<th>$l_e$ [mm]</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.5</td>
<td>8.0610^{-5}</td>
<td>3.3</td>
</tr>
</tbody>
</table>

Value of $\alpha_f$ means that thermal resistance between the global field windings and stator core is 2.5 times higher compared to a classical armature winding put in a slot. It clearly shows the low heat transfer capability of global field windings. This could be explained by the fact that the prototype was designed for electromagnetic tests only.

4.5.2.3 Coefficient verification

With all coefficients determined, the whole system will be verified with experiment results displayed in Fig. 4.21. The comparison is shown in Fig. 4.23.

A good accordance is reported in Fig. 4.23 for both final value and transient process (i.e. thermal time constant). It is noted that in this comparison, the calculated temperature of armature winding is uniformed between ending and active parts (derived from total armature winding resistance). Separated temperatures for these two parts are shown in Fig. 4.24. At the steady-state, the temperature of the end-winding is 87.8 °C which is 3 °C higher than that of the active part. The calculated average temperature of armature winding is 85.5 °C which is very close to the measured one (83.7 °C)

In order to further investigate the accuracy of the coefficient fitted, an additional measurement is conducted with higher phase current of 6 A and field current is set to zero. The purpose of this is to avoid windings from burning. The comparison between predicted temperatures and measurement is shown in Fig. 4.25.

As it can be seen, the good accordance verified the determined coefficients and accuracy of the thermal model.
4.5. Thermal coefficient re-determination by experiments

Fig. 4.23: Temperature measurement. a) Case 1. b) Case 2. c) Case 3

Fig. 4.24: Temperature of armature winding

4.5.2.4 Thermal analysis of model in dynamic regime

With the thermal model has been verified by experiment, an analysis will be tested at a dynamic regime i.e. with rotor displacement. Four cases will be considered:
The temperatures in the steady-state at different parts of the machine are reported in Table 4.5. As it will be observed, the temperatures of windings go beyond maximum limit (180 °C with H insulation class). The natural air cooling method appears to be unsuitable. Therefore a new cooling system is supposed to have the surface heat coefficient $h_s$ of 100 W/°C/m$^2$. This is the upper limit for the natural air convection. Temperatures are re-calculated with the new surface heat coefficient shown in Table 4.6, the new temperatures fall below class F (155 °C) which will be set as temperature limit of the windings in design.

### Table 4.5: Predicted temperatures at various parts of machine

<table>
<thead>
<tr>
<th>Case</th>
<th>End-winding</th>
<th>Active winding</th>
<th>Field winding</th>
<th>Stator</th>
<th>Rotor</th>
<th>Surface</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>305</td>
<td>289</td>
<td>225</td>
<td>233</td>
<td>246</td>
<td>206</td>
</tr>
<tr>
<td>2</td>
<td>341</td>
<td>322</td>
<td>313</td>
<td>260</td>
<td>274</td>
<td>231</td>
</tr>
<tr>
<td>3</td>
<td>359</td>
<td>342</td>
<td>265</td>
<td>280</td>
<td>298</td>
<td>244</td>
</tr>
<tr>
<td>4</td>
<td>394</td>
<td>374</td>
<td>358</td>
<td>306</td>
<td>325</td>
<td>267</td>
</tr>
</tbody>
</table>

### Conclusion

This chapter has focused on thermal aspect of the studied DESM. A lumped parameter analytical model has been developed with the objective is to determine overall temperature of
4.5. Thermal coefficient re-determination by experiments

Table 4.6: Predicted temperatures with the new surface heat coefficient

<table>
<thead>
<tr>
<th>Case</th>
<th>End-winding</th>
<th>Active winding</th>
<th>Field winding</th>
<th>Stator</th>
<th>Rotor</th>
<th>Surface</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>119</td>
<td>109</td>
<td>65</td>
<td>72</td>
<td>82</td>
<td>53</td>
</tr>
<tr>
<td>2</td>
<td>130</td>
<td>118</td>
<td>111</td>
<td>79</td>
<td>89</td>
<td>59</td>
</tr>
<tr>
<td>3</td>
<td>145</td>
<td>134</td>
<td>82</td>
<td>95</td>
<td>109</td>
<td>68</td>
</tr>
<tr>
<td>4</td>
<td>158</td>
<td>146</td>
<td>132</td>
<td>104</td>
<td>117</td>
<td>74</td>
</tr>
</tbody>
</table>

the windings which is accurate enough for the optimization process. The main advantage of this approach is fast computation time which is about 86 ns for one iteration in solving linear differential equation system. A well-known feature of a thermal analysis is that a lot of empirical equations was used; therefore, measurements are necessarily required to determine heat coefficients and verify that thermal model. Due to the fact that there is no winding presented in the rotor part while losses due to permanent magnet are quite small, the main heat is evacuated from the windings (in the stator part) though stator core to the surface without passing air-gap area between stator and rotor.

Due to the difficulties of the natural air cooling (applied to the DESM prototype), a new surface heat coefficient is assumed. This assumption only changes heat evacuation on the surface, all determined heat coefficients inside the machine are kept unchanged. In the next chapter, the multi-physics model coupling between electromagnetic and thermal one will be used for the design optimization of the machine based on a driving cycle.
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Chapter 5

Machine Optimization on a Train Driving Cycle

The multi-physics model for the DESM prototype developed in previous chapters will be utilized in this chapter for the design optimization taking into account a train driving cycle. As it will be shown later, performing an optimization considering a huge number of operating points in the driving cycle is a quite challenging task. This is because of considering model’s nonlinearity even though a very fast model (compared to FEM) was used. Instead, a set of representative points will be chosen. These points must represent the region where machine more frequently works on. The objectives of the optimization are to minimize cost and total losses on the driving cycle. The number of objectives would be higher in reality, however in the first phase of design, these two classical objectives which are strongly related to the economy aspect would be quite acceptable. This chapter will firstly study the performance of the DESM prototype on the driving cycle. Then optimizations based on single operating points will be examined. The most important part is to compared the DESM with a classical permanent magnet machine based on the driving cycle will be conducted. Finally, a conclusion and ranges to use DESM machines will be discussed.

5.1 Train driving cycle and design methodology

5.1.1 Train driving cycle

In the transportation domain, vehicles are required to operate at different speeds at given times along their trips. This leads to the requirement of machine’s torque to accelerate/decelerate accordingly. This operation defines a load cycle for specific cases (urban, rural, motor way, railway, etc.). A load cycle is basically torques - speeds combination. There are a couple factors influencing a load cycle:

- Required speed/acceleration (driving cycle) as function of time. As mentioned above, this depends on types of vehicle to be applied
- Route profile i.e. road characteristic, slopes.
These factors help to determine necessary torque to achieve the required speed/acceleration. The driving cycle is a benchmark for machine testing, however, the driving cycle would vary significantly on account of real conditions of route profile, weather, driving behavior, etc.

The train driving cycle is illustrated in Fig. 5.1 [91]. As it will be seen, machine are required to be able to operate in both motor and generator modes. The operating points in the torque vs. speed space does not distribute in whole space but instead, are clustered in some regions. This clustering distribution will be considered in the design approach. Generally there are 1000 operating points at specific times but some points are repeated several times and the number of discrete points is in fact 639.

Another point worth mentioning in the torque - speed characteristic is that the ratio between maximum speed and base speed (transition point between constant torque and constant power regions, red star marked) is $2533/1547 \approx 1.7$ which is relatively small. It means that at high speed operation, the requirement of flux weakening control might not be difficult. This will certainly affect the optimal design. The influence of this ratio will be also examined later on in this chapter.

Fig. 5.1: A train driving cycle. a) Speed profile. b) Torque profile. c) Torque vs. speed characteristic
5.1. Design methodology

This chapter is going to deal with a number of optimizations considering the given driving cycle, therefore a general direction for both model usages and driving cycle will be given as belows:

5.1.2.1 Scale-down load cycle

As shown in the Fig. 5.1, the maximum required torque is about 1000 Nm. However, the prototype for testing purpose was designed with a nominal torque of 10 Nm. Two approaches would be considered: A theoretical redesign process would be considered for the real train application or a modified load cycle with scale-down factor for torque of 1/100 as shown in Fig. 5.2 (speed range is kept unchanged). The first approach will face difficulty of lacking experimental verifications for the modelings. More importantly, the main objective of the research is to examine the double excitation principle and compare with a classical electrical machine therefore having machines with validated modeling accuracy would be more preferable. The scale-down approach is therefore adopted.

![Fig. 5.2: Torque speed characteristic of the driving cycle with torque is scaled down 100 times](image)

5.1.2.2 Sinusoidal armature current assumption

In the motor mode, the machine is practically supplied from a three phase PWM inverter and the armature current is assumed to be sinusoidal. At high speed, this assumption works since high harmonic orders are filtered out by armature winding inductance. But this will be less accurate at low speed, these harmonics may stay at large amplitudes causing the armature current waveform distorted. Equation solving with nonlinear analysis model would much increase the complexity and more importantly making the optimization on driving cycle become impractical. Therefore, the armature currents are assumed sinusoidal in all cases.
5.1.2.3 Steady state or transient thermal analysis

Even though a transient thermal analysis were successfully developed in chapter 4, however this transient model is only applied if all the points on the driving cycle are considered consequently in time domain. If optimal controls are to be found for all of these points i.e. 1000 optimization loops incurred (each loop may take hundreds model evaluations, several driving cycles needed for the stable temperatures and about 5 seconds for one evaluation), the computation would last about few weeks to evaluate one single machine with a core (4) i7, 2.93 Ghz processor computer. Another option is to build surface approximations with the input is control variable set including armature current amplitude and its phase angle, field current, speed and several temperature values from previous points. These would make the problem unfeasible. Due to these reasons, steady state thermal analysis will be used. It should be noted that using steady state approach for temperature calculation will overestimate temperatures since the thermal time constant is much higher than operating time at each point.

5.1.2.4 Optimization algorithm

Non-dominated Sorting Genetic Algorithm (NSGA-II) belonging to Mutltiobjective Evolutionary Algorithm (MOEA) is a popular algorithm solving multi-objective optimization problems. Multi-objective Particle Swarm Optimization (MOPSO) is widely applied as well. Within the scope of this thesis, MOPSO algorithm will be used, the reason is that it is firstly hard to generally decide which algorithm is overwhelming. Second, MOPSO algorithm was developed in SATIE [92, 93] and used conveniently in the laboratory. It would be interesting to examine results by comparisons between these two algorithms. However this comparison is not considered since the optimization needs to run twice and it would take too much time. Instead, some quick comparisons between MOPSO and NSGA-II algorithms with mathematical functions are demonstrated in B.

5.1.2.5 Machine requirement

In this research, machine requirements only focus on the given driving cycle i.e. machine should satisfy only points presented in the cycle. In the motor mode, motor should satisfy constraints for the voltage and temperature limits. In the generator mode, the input mechanical power should overcome all the losses and thermal and voltage limit as well. Basically, machine must satisfy 5 corner points bounding the driving cycle (red circle marked in Fig. 5.2): 2 points in the motor modes including base (maximum torque and hence high current required) and maximum speed (due to voltage limit) points, and 3 points in the generator mode with high torque and low speed i.e. small mechanical input must overcome copper loss incurred by high current. Two other points in the generator mode are at high torques and high speeds i.e. thermal limit might be reached. These two points are in fact quite close in performance.
5.2 Performance of the DESM prototype on the driving cycle

Before going to optimize the machine regarding the driving cycle, the discussed DESM prototype will be examined on this cycle. With dimensions of the machine are fixed, the objective is to find the optimal control to minimize losses at each operating point. It could be a good reference for comparisons later on.

5.2.1 Optimization problem formulation

The objective of finding optimal control set is to minimize the total losses with respect to constraints. With the double excitation principle, the control set consists of three variables: armature current $I_{arm}$, phase angle between armature current and no-load back EMF $\psi$ and excitation current $I_{dc}$. The optimization is expressed as (5.1):

$$\min_{X = \{I_{arm}, \psi, I_{dc}\}} f(X) = P_{Cu} + P_{Fe} + P_{PE} \text{ [W]}$$

s.t. 

$V_{max} \leq 150 \text{ [V]}$

$\theta_{max} \leq 155 \text{ [^\circ]}$

$T = T^* \text{ [Nm]}$

$\Omega = \Omega^* \text{ [rpm]}$

(5.1)

with $P_{Cu}$, $P_{Fe}$, $P_{PE}$ are total copper losses (of both armature and excitation windings), core loss and total losses in the power electronic module, $V_{max}$ is the peak of first harmonic of the phase voltage, $\theta_{max}$ is maximum temperature of both windings, $T$ is the shaft torque and $T^*$ is the torque requirement. $\Omega$ and $\Omega^*$ are speed and speed requirement respectively. With mechanical loss neglected as proved in chapter 4 and taking into account core loss, shaft torque is different from electromagnetic torque expressed by (5.2):

$$T = T_e - \frac{P_{Fe}}{\Omega}$$

(5.2)

with $T_e$ is the electromagnetic torque and $\Omega$ is mechanical speed. At standstill position, shaft torque is exactly the electromagnetic torque and the second term in right hand side of (5.2) are neglected. Therefore, regarding the convenience of numerical computations, the minimum speed is set to 1 rpm without causing any difference since core loss at this speed is almost zero.

For the torque equality constraint $T = T^*$, it is quite challenging to deal with, so this constraint is relaxed by 5% as (5.3).

$$|T - T^*| \leq 0.05|T^*|$$

(5.3)

In the motor mode, machine is supplied from a DC link voltage of 300 V, the inverter is set to work in the linear modulation range to avoid more sideband harmonics centered around the harmonics of switching frequency. As the result, the peak phase voltage could be delivered is $300/2 = 150$ V.
5.2.2 Strategy for optimal control finding

Dealing with a task of finding optimal controls at a large number of operating points, two strategies would be considered:

1. Strategy directly using nonlinear model evaluation:
   At each operating point, the input is the 3 variable control set, this control set is evaluated with objective functions and verified against constraints by the optimization process. The optimal set will be searched and the computation time is proportional to the number of operating points.

2. Strategy using meta-model:
   A large set of control variables is used to generate approximated response surfaces. The optimization to search for the optimal control will be performed based on these surfaces. The optimal control set at each point is then validated against the high fidelity model (in this case is the multi-physics model developed in previous chapters). If big errors exist, this control set will be added to the surface and the process repeats. Frankly, this approach is useful when dealing with a huge number of points and when there is a need to quickly discover performances of any point in the search region. For the case being study, to generate response surfaces including core loss calculation the input variable set should include 5 variables (three for current variables, one for speed and one for operating mode i.e. motor or generator). This large set of variable does not only require much computation time but also actually causes numerical bugs for the post processing with interpolation process. Also, the use of response surfaces is of little interest since they are only for operating points presented in the driving cycle.

Therefore the first approach will be studied in the following.

As mentioned above, this approach uses multi-physics model as functions to evaluate the input variables. With the mono-objective optimization to find the optimal control, it would be suggested using Sequential Quadratic Programming (SQP) method. Normally with a classical machine where there are only two control variables (for armature current only), the objective or constraint surfaces are expected to be smooth. Therefore using gradient method might work effectively. However in case of 3 variable control set as with double excitation machines, multiple objectives and constraint surfaces exist (each surface for one value of excitation current), it means that multiple local optimum points present. As a consequent, gradient methods are likely to trap into local minimums. This point could be illustrated as examples shown in Fig. 5.3 for shaft torque and total loss response surfaces with field currents are -3 A and 3 A. The surfaces are given according to $d-$ and $q-$ axis currents.
5.2. Performance of the DESM prototype on the driving cycle

For this purpose, MOPSO algorithm will be applied. The interesting point with MOPSO is that it certainly could handle mono-objective problems by simply fixing one objective constant. Two important parameters for MOPSO are the numbers of particles $n_p$ and iterations $n_{iter}$ because they directly affect the result accuracy and computation time. For a large number of optimizations it is wished to minimize computation time. Having large numbers will improve the optimality but time consuming and vice versa. These numbers depend on both number of input variables and problem complexity. There is in fact no rule of thumb to choose these numbers. In this part, several combinations between number of particles and iterations will be tested with repetitions. The reason for repetition is due to the heuristic nature of the algorithm so by doing this it could be ensure the good result retrieved. The chosen combination set will be applied later on for all cases to find optimal control sets.

![Graphs showing shaft torque and total loss](image-url)

Fig. 5.3: Response surfaces at the speed 2000 rpm, motor mode. a) Shaft torque. b) Total loss

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The test will be applied for the rated operating point with 7 combinations sets \( \{n_p, n_{\text{iter}}\} = \{5, 5\}; \{5, 10\}; \{10, 5\}; \{10, 10\}; \{20, 10\}; \{10, 20\} \) and \( \{20, 20\} \). These combinations will be repeated 5 times and result will be compared with the case \( \{50, 50\} \) which is expected to have the true optimum.

The results and comparison are summarized in Table. 5.1. With armature current quantities (rms value \( I \) and phase angle \( \psi \)) are converted into \( d \)-axis and \( q \)-axis ones expressed by (5.4):

\[
\begin{align*}
    i_d &= \sqrt{3}I \sin \psi \\
    i_q &= \sqrt{3}I \cos \psi
\end{align*}
\]

The “N/A” note means no solutions found, this is due to a very small number of particles/iterations used. The expected true optimum \( \{i_d^*, i_q^*, i_{dc}^*\} = \{-4.48, 12.38, 3.48\} \) [A] leads to the optimum total loss of 397 W. This result is done with 50 particles and 50 iterations which is quite big enough to make sure a convergence and in fact from results summarized in Table. 5.1, losses through cases and iterations converge to this value. The results shows that same combinations of \( n_p \) and \( n_{\text{iter}} \) repeats several times does not reveal same results due to the heuristic characteristic of the optimization algorithm as mentioned. However if the more number of particle or iteration used, the results become less deviated. Keeping in mind the evaluation of one control set takes about 5 seconds and the total computation should be at least \( 5 \times n_p \times n_{\text{iter}} \) seconds. Summarized in Fig. 5.4, having a good stability and accuracy (about 2% deviated from the optimum) the case \( \{10, 10\} \) is a good compromise between accuracy as shown in Fig. 5.4 and computation time. It should be noted that about 100 functions evaluations for optimization is a very promising number for example a guide for SQP usages in MATLAB, at least few hundred function evaluations should be set as a stopping criteria. Therefore, this combination will be chosen and referred to the name 10-by-10 approach.

<table>
<thead>
<tr>
<th>Trial order</th>
<th>Total loss [W]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1st</td>
<td>350</td>
</tr>
<tr>
<td>2nd</td>
<td>400</td>
</tr>
<tr>
<td>3rd</td>
<td>450</td>
</tr>
<tr>
<td>4th</td>
<td>500</td>
</tr>
<tr>
<td>5th</td>
<td>550</td>
</tr>
</tbody>
</table>

Fig. 5.4: Accuracy comparison between difference \( \{n_p, n_{\text{iter}}\} \) combinations
5.2. Performance of the DESM prototype on the driving cycle

Table 5.1: Different combinations of \( \{ n_p, n_{iter} \} \) comparison

<table>
<thead>
<tr>
<th>Quantity</th>
<th>{5, 5}</th>
<th>{10, 5}</th>
<th>{5, 10}</th>
<th>{10, 10}</th>
<th>{20, 10}</th>
<th>{10, 20}</th>
<th>{20, 20}</th>
</tr>
</thead>
<tbody>
<tr>
<td>( i_d ) [A]</td>
<td>-6.18</td>
<td>-5.58</td>
<td>-3.73</td>
<td>-4.89</td>
<td>-7.69</td>
<td>-5.36</td>
<td>-4.40</td>
</tr>
<tr>
<td>( i_q ) [A]</td>
<td>12.82</td>
<td>12.16</td>
<td>13.72</td>
<td>12.14</td>
<td>13.65</td>
<td>12.25</td>
<td>12.37</td>
</tr>
<tr>
<td>( i_{dc} ) [A]</td>
<td>2.55</td>
<td>2.34</td>
<td>2.68</td>
<td>1.75</td>
<td>2.73</td>
<td>2.95</td>
<td>3.39</td>
</tr>
<tr>
<td>Total loss [W]</td>
<td>411</td>
<td>417</td>
<td>423</td>
<td>402</td>
<td>457</td>
<td>399</td>
<td>398</td>
</tr>
</tbody>
</table>

2nd trial

<table>
<thead>
<tr>
<th>Quantity</th>
<th>{5, 5}</th>
<th>{10, 5}</th>
<th>{5, 10}</th>
<th>{10, 10}</th>
<th>{20, 10}</th>
<th>{10, 20}</th>
<th>{20, 20}</th>
</tr>
</thead>
<tbody>
<tr>
<td>( i_d ) [A]</td>
<td>-0.90</td>
<td>-5.29</td>
<td>-4.16</td>
<td>-4.79</td>
<td>-6.48</td>
<td>-5.16</td>
<td>-5.00</td>
</tr>
<tr>
<td>( i_q ) [A]</td>
<td>14.70</td>
<td>11.67</td>
<td>11.81</td>
<td>12.52</td>
<td>12.36</td>
<td>12.23</td>
<td>12.01</td>
</tr>
<tr>
<td>( i_{dc} ) [A]</td>
<td>4.13</td>
<td>5.00</td>
<td>4.94</td>
<td>3.64</td>
<td>3.26</td>
<td>3.57</td>
<td>3.93</td>
</tr>
<tr>
<td>Total loss [W]</td>
<td>508</td>
<td>439</td>
<td>430</td>
<td>408</td>
<td>413</td>
<td>397</td>
<td>400</td>
</tr>
</tbody>
</table>

3rd trial

<table>
<thead>
<tr>
<th>Quantity</th>
<th>{5, 5}</th>
<th>{10, 5}</th>
<th>{5, 10}</th>
<th>{10, 10}</th>
<th>{20, 10}</th>
<th>{10, 20}</th>
<th>{20, 20}</th>
</tr>
</thead>
<tbody>
<tr>
<td>( i_d ) [A]</td>
<td>N/A</td>
<td>-8.79</td>
<td>-2.35</td>
<td>-5.46</td>
<td>-4.41</td>
<td>-4.94</td>
<td>-4.89</td>
</tr>
<tr>
<td>( i_q ) [A]</td>
<td>N/A</td>
<td>12.42</td>
<td>12.82</td>
<td>12.39</td>
<td>12.47</td>
<td>12.30</td>
<td>11.85</td>
</tr>
<tr>
<td>( i_{dc} ) [A]</td>
<td>N/A</td>
<td>3.32</td>
<td>3.84</td>
<td>3.48</td>
<td>3.52</td>
<td>3.54</td>
<td>4.27</td>
</tr>
<tr>
<td>Total loss [W]</td>
<td>N/A</td>
<td>467</td>
<td>410</td>
<td>406</td>
<td>397</td>
<td>397</td>
<td>406</td>
</tr>
</tbody>
</table>

4th trial

<table>
<thead>
<tr>
<th>Quantity</th>
<th>{5, 5}</th>
<th>{10, 5}</th>
<th>{5, 10}</th>
<th>{10, 10}</th>
<th>{20, 10}</th>
<th>{10, 20}</th>
<th>{20, 20}</th>
</tr>
</thead>
<tbody>
<tr>
<td>( i_d ) [A]</td>
<td>-4.85</td>
<td>-6.00</td>
<td>-9.05</td>
<td>-5.66</td>
<td>-3.58</td>
<td>-6.16</td>
<td>-4.51</td>
</tr>
<tr>
<td>( i_q ) [A]</td>
<td>13.40</td>
<td>13.28</td>
<td>14.12</td>
<td>12.41</td>
<td>12.67</td>
<td>11.91</td>
<td>12.32</td>
</tr>
<tr>
<td>( i_{dc} ) [A]</td>
<td>3.28</td>
<td>2.31</td>
<td>0.97</td>
<td>3.27</td>
<td>3.59</td>
<td>3.65</td>
<td>3.67</td>
</tr>
<tr>
<td>Total loss [W]</td>
<td>437</td>
<td>427</td>
<td>506</td>
<td>403</td>
<td>402</td>
<td>401</td>
<td>397</td>
</tr>
</tbody>
</table>

5th trial

<table>
<thead>
<tr>
<th>Quantity</th>
<th>{5, 5}</th>
<th>{10, 5}</th>
<th>{5, 10}</th>
<th>{10, 10}</th>
<th>{20, 10}</th>
<th>{10, 20}</th>
<th>{20, 20}</th>
</tr>
</thead>
<tbody>
<tr>
<td>( i_d ) [A]</td>
<td>-4.69</td>
<td>-8.85</td>
<td>-5.33</td>
<td>-5.97</td>
<td>-5.26</td>
<td>-4.65</td>
<td>-4.43</td>
</tr>
<tr>
<td>( i_q ) [A]</td>
<td>11.63</td>
<td>11.67</td>
<td>12.68</td>
<td>12.48</td>
<td>12.18</td>
<td>12.24</td>
<td>12.37</td>
</tr>
<tr>
<td>( i_{dc} ) [A]</td>
<td>5.00</td>
<td>3.44</td>
<td>3.00</td>
<td>3.16</td>
<td>3.59</td>
<td>2.35</td>
<td>3.62</td>
</tr>
<tr>
<td>Total loss [W]</td>
<td>431</td>
<td>438</td>
<td>402</td>
<td>407</td>
<td>398</td>
<td>398</td>
<td>398</td>
</tr>
</tbody>
</table>

Table 5.2: Computation time for difference combinations \( \{ n_p, n_{iter} \} \)

<table>
<thead>
<tr>
<th>Cases</th>
<th>{5, 5}</th>
<th>{10, 5}</th>
<th>{5, 10}</th>
<th>{10, 10}</th>
<th>{20, 10}</th>
<th>{10, 20}</th>
<th>{20, 20}</th>
</tr>
</thead>
<tbody>
<tr>
<td>Computation time [mins]*</td>
<td>2.08</td>
<td>4.16</td>
<td>4.16</td>
<td>8.32</td>
<td>16.64</td>
<td>16.64</td>
<td>33.28</td>
</tr>
</tbody>
</table>

* Based on a single thread computation

5.2.3 Result analysis

As mentioned above, equality torque constraint is relaxed as inequality constraint as \( (5.3) \) to facilitate the searching process of optimal control, therefore the comparison between the real
torque and required torque is examined as in Fig. 5.5

Fig. 5.5: Comparison between real torque and required torque on the driving cycle

Generally two torque profiles should match as set in the optimization constraint. However the continuous of real torque profile shows that the optimization algorithm with 10-by-10 approach of MOPSO is able to find optimal control at every operating points (if no solution found the controls are set as N/A).

The total copper loss along the driving cycle displayed together with torque profile is shown in Fig. 5.6. The copper loss is obviously large when high torque is required. Core losses along the driving cycle are shown in Fig. 5.7. Generally, high speed operating points yield big core loss but core loss also depends on the maximum induction which is a consequence of current control adjustment.

Fig. 5.6: Total copper losses along the driving cycle
5.3 Single point optimization

Fig. 5.7: Core loss along the driving cycle

Fig. 5.8 shows current evolutions with respect to time along the driving cycle. It is generally claimed that the contribution of excitation winding provide one more degree for the controlling the air-gap flux and hence it provides more possibilities to optimize the machine’s performance. Therefore at the same time, it makes the controlling strategy somewhat more complex to perceive especially in the context of minimizing total losses with respecting torque, voltage and thermal limits constraints. Additionally, issues with local minimal trapping (optimization algorithm) and multi-optimum points (problem nature) may exist for a certain cases also contribute to the control complexity. As it will be seen in Fig. 5.8, $q$–axis current roughly follows the trend of torque profile but for $d$–axis and excitation currents are more complex to have a clear dependence. Individual losses of the prototype on the driving cycle is summarized in Table. 5.3.

<table>
<thead>
<tr>
<th></th>
<th>Excitation windings</th>
<th>Armature windings</th>
<th>Iron core</th>
<th>Power electronics</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Loss [kW]</td>
<td>10.64</td>
<td>68.01</td>
<td>64.12</td>
<td>20.97</td>
<td>163.74</td>
</tr>
</tbody>
</table>

5.3 Single point optimization

In this section, optimizations of DESM machine will be carried out based one single operating point as done in classical optimization problems. The optimization objective as shown in (5.5) is to minimize both cost and total losses. The cost considered here only account for the raw materials. This cost actually varies regarding to the supplier, period and also material quantities. Therefore in order to accomplish fair comparisons between structures, a normalized cost will be used in which the price per kg for iron is assigned to 1, values for copper and ferrite PM are 7 and 6 respectively [94]. It should be strongly noted that unit price for ferrite PM
is less than copper meaning that regarding the objective (loss and cost minimization), using ferrite PM might gain some advantages over excitation winding but clear performances should be investigated.

$$\text{minimize } f(X) = \begin{cases} P_{Cu} + P_{Fe} + P_{PE} [W] \\ C(X_g) \end{cases}$$

s.t.  
- $V_{max} \leq 150 [V]$ 
- $\theta_{max} \leq 155 [{^\circ}C]$ 
- $T = T^* [Nm]$ 
- $\Omega = \Omega^* [rpm]$ 

(5.5)

with $X_g$ and $X_c$ are geometry and control variables respectively, $C(X_g)$ is the machine cost with geometry $X_g$ and $\Omega^*$ is the operating speed.

The formulation (5.5) is generally applied to either single point or multiple points optimization i.e $T^*$ ($\Omega^*$) could be a set of required torques (speeds).

### 5.3.1 Bi-level optimization approach

The optimization problem formulated as (5.5) leading to two possible solutions:
5.3. Single point optimization

- One level optimization approach:
  This approach is exactly shown as (5.5) where all geometry and control variables are all put in the input variable set. This approach requires a large number of machines to be evaluated because good machines with bad controls will not be feasible. However the biggest challenges is that when dealing with multiple point optimization, the number of constraints will proportionally increase. For instance, if 3 operating points to be optimized at the same time, the number of constraints are 9 including 3 equality constraints and the number of variables would contain 9 control variables (3 for each point). This will absolutely make the optimization problem infeasible (mainly due to the number of constraints)

- Bi-level optimization approach:
  In this approach the variable set is divided into 2 variable sub-set $X_g$ and $X_c$ as in (5.5). The meaning of bi-level is that for each machine (geometry variable) one or several (as the same number of operating points to be optimized) mono sub-optimizations (lower level) are performed to search for the optimal control set, all constraints are handled at this level. At the upper optimization level, the objective is to minimize cost and optimal losses found at lower level. This level does not deal with any constraint since they are all handled in the lower level, only two objectives are considered. With this bi-level approach, the computation time actually increases proportionally with the number of operating points but it effectively overcomes the infeasibility problem with one level optimization approach above since at a time, only 3 constraints are to be handled. (5.5) is reformulated with bi-level approach as (5.6)

\[
\begin{align*}
\text{Upper level:} \\
\text{minimize} \quad f_1(X) &= \begin{cases} \hat{P}_{\text{Loss}} \\ C(X_g) \end{cases} \\
\text{Lower level:} \\
\text{minimize} \quad f_2(X) &= P_{\text{Loss}} \\
\text{s.t.} \quad V_{\text{max}} \leq 150 [V] \\
\quad \theta_{\text{max}} \leq 155 [^\circ C] \\
\quad T = T^* [Nm] \\
\quad \Omega = \Omega^* [\text{rpm}] \\
\end{align*}
\]

(5.6)

with $\hat{P}_{\text{loss}}$ is the optimal loss (minimum loss found in the lower level) and $P_{\text{loss}}$ is the total losses.

The lower level uses optimization strategy for optimal control as presented in 5.2.2. In case no solution found in this lower level either due to bad machine geometries or a small number of trials (as with 10 particles and 10 iterations strategy), to make the process
continue at the upper level, the 3 control variables are set to zero and optimal loss is set to infinity so is to be dominated by any feasible solutions in the upper level. Therefore the temporarily assigned value will not be kept in the final set of solutions.

5.3.2 Geometry variable set

Nine geometry variables are chosen for the upper optimization level as marked in Fig. 5.9

![Fig. 5.9: Geometry variables](image)

This set of variable allow machines to change their sizes in both radial and axial directions. The windows for excitation windings are fixed in size and excitation windings is allowed to only change its height \(x_3\). In case the optimal solution does not want to use excitation windings, \(x_3\) approaches zero but to avoid computation error, the lower limit of this variable is set to 0.05 mm. Due to the model complexity, the number of pole pairs is kept unchanged i.e. 6. Detail ranges of variables are summarized in Table 5.4.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>Range [mm]</th>
<th>Prototype [mm]</th>
</tr>
</thead>
<tbody>
<tr>
<td>(x_1)</td>
<td>Stack length</td>
<td>30 ÷ 60</td>
<td>40</td>
</tr>
<tr>
<td>(x_2)</td>
<td>Bridge thickness</td>
<td>3 ÷ 12</td>
<td>7</td>
</tr>
<tr>
<td>(x_3)</td>
<td>Field winding height</td>
<td>0.05 ÷ 9</td>
<td>9</td>
</tr>
<tr>
<td>(x_4)</td>
<td>Tooth width</td>
<td>3 ÷ 6.5</td>
<td>5.5</td>
</tr>
<tr>
<td>(x_5)</td>
<td>Tooth length</td>
<td>10 ÷ 25</td>
<td>16.5</td>
</tr>
<tr>
<td>(x_6)</td>
<td>Azimuth PM thickness</td>
<td>4.5 ÷ 10</td>
<td>6</td>
</tr>
<tr>
<td>(x_7)</td>
<td>Azimuth PM length</td>
<td>10 ÷ 32</td>
<td>24</td>
</tr>
<tr>
<td>(x_8)</td>
<td>Shaft radius</td>
<td>10 ÷ 20</td>
<td>17</td>
</tr>
<tr>
<td>(x_9)</td>
<td>Side PM thickness</td>
<td>3 ÷ 10</td>
<td>6</td>
</tr>
</tbody>
</table>

Normally the values for the prototype fall in the middle range of their corresponding except for the \(x_3\). The reason is after several trials, 9 mm even seem to be large for the upper limit
5.3. Single point optimization

of this variable so this limit is just kept the same as the prototype. Putting the upper bound unnecessarily large will reduce the chance of finding the optimal set from the optimization point of view.

In order to verify the model’s accuracy when geometry varies, torque surface comparison between EMCN and FEM methods are performed for a wide range of excitation and armature currents. Two extreme models derived from Table. 5.4 as shown in Fig. 5.10: one model with all geometry variables stay at the lower bound (lower bound machine) and the other for the upper bound (upper bound machine). As it will be seen, the lower bound machine is much smaller in size compared to the upper bound one.

Fig. 5.10: Two extreme machines with lower bounds (exterior radius of 60.8 mm) and upper bound (exterior radius of 115.8 mm)

Result comparison displayed in Fig. 5.11 shows a good accordance between EMCN and FEM methods meaning that within the specified range of geometry variables in Table. 5.4, results are reliable.

For the validity of the thermal analysis model, it could be said that the thermal model is reliable since equations used in the thermal network are empirical meaning that it is validated through various measurements with different machine’s dimensions. Moreover, there is no forced fluid

Fig. 5.11: Mean torques of the two extreme geometries. a) Lower bound. b) Upper bound
(either air or water) for the cooling, this make the heat evacuation process stable with heat coefficients are almost constant.

5.3.3 Case study

For the single point optimization, two cases will be examined including the rated operating point which is classically considered and the another is the maximum speed operating point in the motor mode which is also commonly focused. These two points are marked with red in Fig. 5.2 (two upper points). The reasons for this are not just analyze machine design by using single point optimization but more importantly to see how designs change by different design target (i.e. at different single operating points). Detail information of these two points are listed in Table. 5.5

<table>
<thead>
<tr>
<th>Point</th>
<th>Torque [Nm]</th>
<th>Speed [rpm]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rated</td>
<td>10.45</td>
<td>1547</td>
</tr>
<tr>
<td>Max. speed</td>
<td>5.39</td>
<td>2553</td>
</tr>
</tbody>
</table>

Running MOPSO with a choice of 50 particles and 50 iterations (2500 machine evaluations), the pareto front results are shown in Fig. 5.12. The result shows the pareto fronts tends to converge to the final curves after about 20 iterations, further running tries to improve the result distribution along the fronts.

Fig. 5.12: Pareto front convergences through iterations. a) Rated. b) Max. speed

Result comparison between two cases are displayed in Fig. 5.13. There are some points on the top left of the pareto fronts (3 points for max. speed case and 6 points for rated case) could be removed since there is a very little gain for loss saving but big sacrifices for cost. As will be seen, rated operating points require bigger machines with more losses, this is due to the higher
torque requirement for the rated point which is almost twice bigger compared to the max. speed point. The result shows that to have relatively same losses, an optimal machine operating at the rated point is about 1.5 times more expensive than the one for max. speed point.

![Fig. 5.13: Pareto front comparison between rated and max. speed points](image)

In order to see how the excitation winding varies, the thicknesses of this windings are examined through solutions along the pareto fronts as seen in Fig. 5.14

![Fig. 5.14: Excitation winding height through solutions on the pareto front (From left to right in Fig. 5.13)](image)

Both results for two cases reveal that the use of excitation windings are very limited with the height about 2 mm (the one for the prototype is 9.2 mm) which is shown in Fig. 5.15 for a couple of machines marked in Fig. 5.13, this point was mentioned earlier in this section with the reason that PM are more preferable compared to excitation windings. and it is hard to say operating at max. speed require more contribution of excitation winding since the difference are not noticeable.

Detail dimensions of these six machines are reported in Table. 5.6. As it will be seen due to the
little use of excitation winding, the bridge thickness acting as bridge to conduct flux created by this winding tend to stay at the minimum (lower bound) of 3.0 mm.

Table 5.6: Detailed dimensions of extracted machines on the pareto fronts

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>Rated point</th>
<th>Max. speed point</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>R1</td>
<td>R2</td>
</tr>
<tr>
<td>$x_1$</td>
<td>Stack length</td>
<td>58.9</td>
<td>58.7</td>
</tr>
<tr>
<td>$x_2$</td>
<td>Bridge thickness</td>
<td>3.0</td>
<td>3.0</td>
</tr>
<tr>
<td>$x_3$</td>
<td>Field winding height</td>
<td>2.0</td>
<td>1.5</td>
</tr>
<tr>
<td>$x_4$</td>
<td>Tooth width</td>
<td>6.4</td>
<td>6.0</td>
</tr>
<tr>
<td>$x_5$</td>
<td>Tooth length</td>
<td>24.7</td>
<td>13.8</td>
</tr>
<tr>
<td>$x_6$</td>
<td>Azimuth PM thickness</td>
<td>5.8</td>
<td>7.5</td>
</tr>
<tr>
<td>$x_7$</td>
<td>Azimuth PM length</td>
<td>29.4</td>
<td>25.2</td>
</tr>
<tr>
<td>$x_8$</td>
<td>Shaft radius</td>
<td>10.2</td>
<td>10.6</td>
</tr>
<tr>
<td>$x_9$</td>
<td>Side PM thickness</td>
<td>10.0</td>
<td>9.8</td>
</tr>
</tbody>
</table>

5.4 Multiple points optimization and comparisons with a PM machine

In this section, the machine optimization based on multiple points will be addressed. The main objective is to take into account the practical requirement when machine must deal with driving cycle where multiple operating points needed to be considered simultaneously. Dealing
with multiple operating points at various speeds would effectively compromise machine designs. For instance at low speed region, to minimize the losses, machines prefer to use more PMs instead of copper (the price of copper and ferrite PM are quite the same) but when working at the high speed region, this will cause much more core loss and overvoltage might occur. Several multiple point cases will be considered. But it is worth keeping in mind that computation time increases proportionally with the number of points so to handle a big number of points is not practical. In addition, the DESM will be compared with a classical PMSM machine (derived from the DESM with some parts removed).

5.4.1 Corresponding PMSM model and comparison with DESM

In order to evaluate the contribution of double excitation principle on the driving cycle, a PMSM model is built. For a good comparison, this PMSM model is derived from the DESM one with some parts are removed as shown in Fig. 5.16. Two excitation windings, side PMs and rotoric flux collectors are removed. The outer stator and end-shield parts act as the machine housing. In this model the end-shield thickness are kept the same as one of the DESM prototype.

Fig. 5.16: PMSM model derived from DESM

In order to see performance differences between PMSM and DESM machines, the comparison of two machines with the parameters corresponding to the prototype will be investigated. This will help further explain the analysis result on the driving cycle. Based on the prototype configuration, the DESM model is obviously more costly compared to the PMSM counterpart due to the excitation winding and side PMs costs but the most important difference regarding the performance between these two machines is the homopolar flux paths (analyzed in chapter 2) together with leakage flux of the DESM machine reduce its performances. Therefore the flux in PMSM model will be more focused and increased leading to higher torque generation and at the same time, more core loss will be generated but it might benefit from lower copper loss as well.

The comparison between two machines will be performed for torque and loss calculations. Compared to PMSM model, DESM model has two more additional flux sources which are side PMs and excitation windings. Therefore, the comparisons shown in Fig. 5.17 will consider various excitation currents (7 values from 0÷6 A) and side PM thicknesses. It should be noted that
in this comparison all other parameters of two machines are kept the same particularly the azimuth PM dimensions.

As it was predicted before due to the leakage flux in DESM machine, in order to have same torque for DESM model, it must pay more for either excitation current or side PM and hence copper and core losses increase. If the total losses are intended to keep the same as with PMSM, more price should pay for side PMs in the DESM model. For example in Fig. 5.17a) with side PM thickness of 2 mm, to obtain same torque as PMSM, $I_{dc}$ should be around 6 A leading to must higher total losses. In order to save excitation current to lower copper loss at the same level as with PMSM model and in Fig. 5.17c), side PM thickness should increase (as 6 mm) and total losses stay quite the same between two machines in this case.

From this quick comparison based on the prototype dimensions, PMSM machines seems to gain some advantages over the DESM model in term of cost and losses savings. However when operating at high speed region while strong field weakening might be required, the PMSM machine has no methods other than using $d$–axis current. And it therefore might face the high copper loss problem and overheating as well. The comparison for the maximum torque envelop...
between two machines is displayed in Fig. 5.18a, the corresponding total losses are shown in Fig. 5.18b.

![Graphs showing torque envelop and losses comparisons between DESM and corresponding PMSM models](image)

**Fig. 5.18**: Torque envelop and losses comparisons between DESM and corresponding PMSM models

As seen in Fig. 5.18a, double excitation principle allows the machine to operate at higher speed compared to PMSM machine (about 11000 rpm compared to 6500 rpm). The effectiveness of excitation windings are highlighted in this high speed region. Since it together with the \( d \)-axis current helps conveniently reduce air-gap flux, copper losses are shared between these two windings. But in the low speed region (less than few thousands rpm), PMSM model seem to be more advantageous with lower loss.

### 5.4.2 Multiple points optimization on the driving cycle

This part focuses on the machine design with two objectives are to minimize total losses on the driving cycle and machine cost. It would an perfect solution if all operating points are considered regarding the accuracy because the calculated losses are exact which matches correctly the optimization objective. However, the computation time are proportional to the number of points as discussed. The roughly estimated computation time for each point is 60 hours (on the server with parallel computing) making the consideration of all points impossible, even taking into account a dozen of points are hard to be feasible since many optimization trials and comparisons are necessary. In the following, an alternative approach will be presented to shorten the computation time.

#### 5.4.2.1 Representative points

In this research, a set of representative points will be chosen. These points should represent the most frequently operated regions of the machine. They could be chosen by the most solicited points i.e. points with maximum energy on the driving cycle as 3 points shown in Fig. 5.19.
This approach is rational since the designs pay attention to the important operating points in term of energy usage.

![Solicited operating points on the driving cycle](image1)

Fig. 5.19: Solicited operating points on the driving cycle

However this approach does not account for the clustering effect meaning that there are always points closed to each other, energy at each point are not significant but that group of points forms a big energy portion on the driving cycle. A more appropriate alternative is to combine “solicited points” idea with a technique so called “Energy center of gravity” [3]. This technique simply divides the whole driving cycle space into groups and the clustering effect is therefore considered. In this research, the operating space is equally divided with 9 divisions in each dimension (torque and speed) as illustrated in Fig. 5.20, therefore 81 groups are presented. It is obvious that another numbers of divisions and even another splitting techniques should be considered to see the influence on the optimal designs. But once again the time consuming issue currently limits that interesting idea.

![Group division on the driving cycle space](image2)

Fig. 5.20: Group division on the driving cycle space
5.4. Multiple points optimization and comparisons with a PM machine

A representative is then picked for each group with the energy equals total energy of all points in that group and equivalent torque and speed are given by (5.7a) and (5.7b) respectively:

\[ T_{eq}^i = \frac{1}{n_i} \sum_{j=1}^{n_i} T_j E_j \] (5.7a)

\[ \Omega_{eq}^i = \frac{1}{n_i} \sum_{j=1}^{n_i} \Omega_j E_j \] (5.7b)

with \( n_i \) is number of points in the cell “i”, \( E_j, T_j, \Omega_j \) are energy, torque and speed of point \( j \) in the cell “i”.

The equivalent energy loss based on these representatives are given by (5.8)

\[ E_{eq} = \sum_{i=1}^{N} T_{eq}^i \Omega_{eq}^i \Delta t_i \] (5.8)

with \( N \) is number of representative points, \( \Delta t_i \) is the working time duration of the representative point \( i \) as the sum of all operating points in the cell containing that representative point.

After having groups, representative points with maximum energy will be chosen as marked in Fig. 5.20. Due to limit of computation time, strategy with 3 representative points are currently used and detailed in Table. 5.7.

<table>
<thead>
<tr>
<th>Point 1</th>
<th>Point 2</th>
<th>Point 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Torque [Nm]</td>
<td>10.07</td>
<td>7.06</td>
</tr>
<tr>
<td>Speed [rpm]</td>
<td>1559</td>
<td>2150</td>
</tr>
<tr>
<td>Operating mode</td>
<td>Motor</td>
<td>Motor</td>
</tr>
</tbody>
</table>

5.4.2.2 Optimization based on representative points

Due to the removal of excitation windings and side PMs, three related geometry variables will also not be presented in the optimization for PMSM model including: end-shield thickness \( x_2 \), excitation winding height \( x_3 \) and side PM thickness \( x_9 \). Moreover, excitation current variable is also not considered making the optimal control finding is easier compared to DESM model.

As mentioned in 5.1.2.5, machines should additionally satisfy constraints at 5 corner operating points, however incorporating these points into the lower-level optimization would significantly increase computation time few times longer. In order to tackle this issue, the optimization will not take into consideration these points in the lower-level but after the pareto front derived. This approach may reduce the accuracy of the optimal pareto front. Therefore, a compromise
between computation time and diversity (due to removals of several solutions on the pareto front) is actually considered here.

The pareto comparison between two types of machine is shown in Fig. 5.21a. The comparison generally shows that on the basis of a set of 3 specified representative points, PMSM model gains advantages over the DESM counterpart.

Fig. 5.21: Detail comparisons for solutions along the pareto front. a) Volume. b) Mass. c) Copper cost. d) Iron cost. e) PM cost

Fig. 5.21b-f also show an investigation in detail for other quantities including total volume,
mass and individual costs (costs of copper, iron and PMs) along solutions on the pareto front in Fig. 5.21a. It is interesting to realize that even PMSM models are better than DESM ones in term of cost and losses minimization objective but for that same machines, two types of machine are very close regarding both volume and total mass (DESM models, in fact, seem to be a little bit better than PMSM). This is explained by the fact that due to flux leakages in DESM compared to PMSM model, DESM machine needs to use more PMs and copper to compensate that flux to sustain torque capability. More PM and copper materials in DESM model are seen in Fig. 5.21d. and Fig. 5.21e.

The solutions presented in Fig. 5.21a. are for energy losses due to 3 representative operating points. These machines satisfy all constraints for this set of representatives, however this does not ensure that the machine is able to work at all the points in the driving cycle as mentioned in 5.1.2.5. The feasibility examinations at 5 operating points (marked in Fig. 5.2) are performed. Verifying against those points would make some solutions Fig. 5.21a unfeasible and filtered out as shown in Fig. 5.22. It is noticed that points with lower cost i.e. small in size are removed, this is due to the thermal limits are reached.

![Fig. 5.22: Pareto front comparison after verifying against corner operating points](image)

### 5.4.2.3 Result analysis

The ultimate purpose is to minimize total losses in all operating points. To this end, some machines will be extracted and examined their losses on many other operating points as well. Three specific machines (marked in Fig. 5.22) are selected for each type of model (DESM and PMSM): D1, D2 and D3 for DESM type and E1, E2 and E3 for PMSM type. These machines are illustrated in Fig. 5.23 with dimensions are detailed in Table. 5.8. As can be observed, excitation winding thicknesses are pretty small guessing that the use of excitation winding are not really preferable.
Chapter 5. Machine Optimization on a Train Driving Cycle

![Machine D1](image1)

![Machine D2](image2)

![Machine D3](image3)

![Machine P1](image4)

![Machine P2](image5)

![Machine P3](image6)

Fig. 5.23: Specific machines for each model. Upper row is for DESM type and lower row is for PMSM type

Table 5.8: Dimensions of extracted machines in Fig. 5.23. [Unit: mm]

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>Prototype DESM</th>
<th>Prototype PMSM</th>
<th>Optimal DESM D1</th>
<th>Optimal DESM D2</th>
<th>Optimal DESM D3</th>
<th>Optimal PMSM P1</th>
<th>Optimal PMSM P2</th>
<th>Optimal PMSM P3</th>
</tr>
</thead>
<tbody>
<tr>
<td>$x_1$</td>
<td>Stack length</td>
<td>40.0</td>
<td>40.0</td>
<td>50.2</td>
<td>45.2</td>
<td>52.0</td>
<td>60.0</td>
<td>54.6</td>
<td>47.2</td>
</tr>
<tr>
<td>$x_2$</td>
<td>Bridge thickness</td>
<td>7.0</td>
<td>7.0</td>
<td>3.0</td>
<td>3.0</td>
<td>3.0</td>
<td>3.0</td>
<td>3.0</td>
<td>3.0</td>
</tr>
<tr>
<td>$x_3$</td>
<td>Field winding height</td>
<td>9.0</td>
<td>N/A</td>
<td>1.2</td>
<td>1.8</td>
<td>N/A</td>
<td>N/A</td>
<td>N/A</td>
<td>N/A</td>
</tr>
<tr>
<td>$x_4$</td>
<td>Tooth width</td>
<td>5.5</td>
<td>5.5</td>
<td>5.3</td>
<td>5.7</td>
<td>5.1</td>
<td>6.5</td>
<td>5.4</td>
<td>5.9</td>
</tr>
<tr>
<td>$x_5$</td>
<td>Tooth length</td>
<td>17.5</td>
<td>17.5</td>
<td>25</td>
<td>19.5</td>
<td>16.3</td>
<td>24.6</td>
<td>16.6</td>
<td>14.9</td>
</tr>
<tr>
<td>$x_6$</td>
<td>Azimuth PM thickness</td>
<td>6</td>
<td>6</td>
<td>9.0</td>
<td>9.9</td>
<td>9.9</td>
<td>4.5</td>
<td>4.5</td>
<td>5.9</td>
</tr>
<tr>
<td>$x_7$</td>
<td>Azimuth PM length</td>
<td>24.0</td>
<td>24.0</td>
<td>22.8</td>
<td>22.6</td>
<td>17.8</td>
<td>24.5</td>
<td>24.9</td>
<td>25.2</td>
</tr>
<tr>
<td>$x_8$</td>
<td>Shaft radius</td>
<td>10</td>
<td>10.0</td>
<td>10</td>
<td>10.2</td>
<td>10.8</td>
<td>15.1</td>
<td>10.1</td>
<td>10.0</td>
</tr>
<tr>
<td>$x_9$</td>
<td>Side PM thickness</td>
<td>6.0</td>
<td>N/A</td>
<td>2.9</td>
<td>7.3</td>
<td>6.9</td>
<td>N/A</td>
<td>N/A</td>
<td>N/A</td>
</tr>
</tbody>
</table>

The optimization result shows that the bridge thicknesses of DESM machine try to approach the lower bound which is 3.0 mm (3.0 mm is fixed for PMSM type) the reason is mainly due to the fact that increasing bridge thickness will increase machine’s outmost radius resulting in a much increase of iron material.

Machines presented in Fig. 5.23 are then verified against all points in the driving cycle to calculate exactly total losses in the driving cycles which are appropriate values of concern. Machines have to be able to reach required torques at given speeds. Fig. 5.24 compares generated torques (with optimal control set found) and required torques for 6 extracted machines. A very good accordance means that all machines are able to work at all operating points.
Three extracted DESM machines are quickly verified against FEM by flux control examination as shown in Fig. 5.25. As will be seen, a good accordance between two analysis methods (EMCN and FEM). The result also shows that the flux controlling by excitation current are not quite effective, this is due to the bridge thickness stay at its minimum level making magnetic reluctance for flux path from excitation winding significant.

The total energy losses comparison over the given driving cycle of 1000 seconds between extracted machines together with the prototypes are displayed in Fig. 5.26. It is interesting to see that the points extracted from pareto front in Fig. 5.22 still form sets of non-dominated solutions for both model types (DESM and PMSM) and improvements are made compared to the prototypes which are considered as initial designs. This result also supports the idea of the energy center of gravity center principle because this principle only works on representative points and there is no strong foundation for the optimality when verifying against all operating points on the driving cycle (i.e., better machines derived from representatives may become worse when working on the whole driving cycle).
Fig. 5.25: Flux control verification for DESM machines. Circle - by EMCN, star - by FEM

Fig. 5.26: Cost and total losses comparisons between various machines of two models

Individual losses (copper, core and power electronics losses) of each machine are illustrated in Fig. 5.27. The results reasonably shows that copper loss portion increases when machine gets smaller.

Details for the costs and losses of machines in Fig. 5.26 are reported in Table. 5.9. Taking average over the three optimal machines, PMSM configuration has a cost of 27.01 which is almost indifferent from 27.71 for DESM model but it could save about 13% of total energy losses (142.21 kJ compared to 163.7 kJ) and PMSM model gains advantages over the DESM one.
5.4. Multiple points optimization and comparisons with a PM machine

![Pie charts showing power losses](chart)

Fig. 5.27: Individual total losses on the driving cycle of various machines for two models. a) DESM prototype. b) PMSM prototype. c) Machine D1. d) Machine D2. e) Machine D3. f) Machine P1. g) Machine P2. h) Machine P3.

Table 5.9: Costs and individual losses comparison of different machines

<table>
<thead>
<tr>
<th>Machine</th>
<th>Normalized cost</th>
<th>Copper loss</th>
<th>Core loss</th>
<th>PE* loss</th>
<th>Total loss</th>
</tr>
</thead>
<tbody>
<tr>
<td>DESM prototype</td>
<td>39.52</td>
<td>78.65</td>
<td>64.12</td>
<td>20.97</td>
<td>163.74</td>
</tr>
<tr>
<td>PMSM prototype</td>
<td>26.44</td>
<td>64.11</td>
<td>68.14</td>
<td>19.15</td>
<td>151.40</td>
</tr>
<tr>
<td>Machine D1</td>
<td>33.58</td>
<td>65.14</td>
<td>70.68</td>
<td>19.00</td>
<td>154.82</td>
</tr>
<tr>
<td>Machine D2</td>
<td>26.28</td>
<td>81.80</td>
<td>65.94</td>
<td>18.06</td>
<td>165.80</td>
</tr>
<tr>
<td>Machine D3</td>
<td>23.27</td>
<td>96.56</td>
<td>56.62</td>
<td>17.41</td>
<td>170.59</td>
</tr>
<tr>
<td>Machine P1</td>
<td>35.74</td>
<td>40.39</td>
<td>73.11</td>
<td>16.49</td>
<td>129.98</td>
</tr>
<tr>
<td>Machine P2</td>
<td>24.26</td>
<td>61.36</td>
<td>65.43</td>
<td>16.31</td>
<td>143.10</td>
</tr>
<tr>
<td>Machine P3</td>
<td>21.02</td>
<td>71.98</td>
<td>65.79</td>
<td>15.77</td>
<td>153.54</td>
</tr>
</tbody>
</table>

* Power Electronics
Loss unit: kJ
Driving cycle period: 1001 s

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5.4.2.4  Optimization with 6 representative points

In order to examine the influence of the number of representative points on optimal designs, this part presents the design optimization case with 6 representative points. The methodology is exactly the same as done with the case of 3 representative points already discussed in detail above, just more points are considered. Therefore, only some main results will be pointed out for discussion. Fig. 5.28 shows 6 star-marked representatives chosen among representative points of 81 groups. The detailed torque-speed characteristics of these points are listed in Table. 5.10

![Fig. 5.28: Group division and 6 representative points](image)

**Table 5.10: Six representative point characteristics**

<table>
<thead>
<tr>
<th></th>
<th>Point 1</th>
<th>Point 2</th>
<th>Point 3</th>
<th>Point 4</th>
<th>Point 5</th>
<th>Point 6</th>
</tr>
</thead>
<tbody>
<tr>
<td>Torque [Nm]</td>
<td>10.07</td>
<td>7.06</td>
<td>-4.72</td>
<td>10.27</td>
<td>8.87</td>
<td>-9.25</td>
</tr>
<tr>
<td>Speed [rpm]</td>
<td>1559</td>
<td>2150</td>
<td>2563</td>
<td>1013</td>
<td>1821</td>
<td>1883</td>
</tr>
<tr>
<td>Operating mode</td>
<td>Motor</td>
<td>Motor</td>
<td>Generator</td>
<td>Motor</td>
<td>Motor</td>
<td>Generator</td>
</tr>
</tbody>
</table>

The pareto front comparison between DESM and PMSM after verifying against corner points is shown in Fig. 5.29 with several machines illustrated in Fig. 5.30 will be extracted for a more detailed analysis. It is noted that the energy losses much increase compared to ones shown in Fig. 5.22 as there are 3 more points considered. The result yields that PMSM gains advantages over DESM as shown in the case with 3 representative points.

In order to roughly examine influence of having more points on the optimal design, all machines shown in Fig. 5.29 will be recalculated with objectives as for the case of 3 representative points (costs are unchanged but energy loss will reduce since they are for 3 points only) and compared with pareto fronts displayed in Fig. 5.22. This comparison is reported in Fig. 5.31. In this figure, “DESM 6 point” in the legend means DESM machine topologies derived from using 6
5.4. Multiple points optimization and comparisons with a PM machine

Fig. 5.29: Pareto front comparison between DESM and PMSM

Fig. 5.30: Specific machines for each model. Upper row is for DESM type and lower row is for PMSM type

It is clearly seen in Fig. 5.31 that no point in a “6 point” pareto front dominates any point on the corresponding “3 point” curve since the “3 point” curves are the pareto front of its objectives. Generally, there no noticeable difference between 2 cases with same type of model (i.e. DESM or PMSM). So it could state that the number of representative points will not largely matter the optimal designs. Only some differences for the DESM case in the low loss area. It could be due to the fact the DESM case (in Fig. 5.29) did not well converge. It is very possible since in the case of DESM, more optimization variables presented. Rerunning this optimization could improve but in order to get the DESM curve presented in Fig. 5.29, it took almost 2 months
Chapter 5. Machine Optimization on a Train Driving Cycle

Fig. 5.31: Comparison between 6 and 3 representative points with the objectives are for 3 points with a core (4) i7, 2.93 Ghz processor computer.

Energy losses calculations for extracted machines in Fig. 5.30 over the driving cycle are displayed in Fig. 5.32 in comparison with extracted machines in the case with 3 representative points (D1, D2, D3, P1, P2 and P3).

Fig. 5.32: Comparison between various machines in both 6 and 3 representative point cases

As seen, the relative comparisons in Fig. 5.32 are similar to those presented in Fig. 5.31. Therefore, it could be generally stated that the influence of having more representative points consideration mainly makes it harder to converge i.e. more particles or generations in the optimization should be required at the expense of a longer computation time. This could be due to the fact that additional points have less contribution to the total energy and also representative points are not quite different regarding operating speeds.
5.4.3 DESM and PMSM comparison with extended speed range

As discussed in 5.4, DESM machines cannot gain advantages over the PMSM with objectives to minimized both material cost and total losses on the driving cycle. This is mainly due to the ratio $\gamma$ between maximum and base speed are not sufficiently high. In this section, further comparisons between DESM and PMSM models are performed on the extended speed range with $\gamma$ are similar to that of vehicle application. Same objectives (cost and losses minimization) are applied to this case with 2 points as shown in Fig. 5.33. Machines are obliged to reach the rated operating point and maximum speed (no torque constraint at this maximum speed, however it should approach zero to attain minimum losses).

![Fig. 5.33: Two operating points with extended speed range](image)

Two cases will be considered with the maximum speeds are 4 and 5 times of the base speed ($\gamma = 4; 5$). The loss is calculated as the sum of losses at the base and maximum speeds. The pareto front comparisons are given in Fig. 5.34 with some extreme machines extracted displayed in Fig. 5.35. Dimensions of these machines are detailed in Table. 5.11

![Fig. 5.34: Comparison between DESM and PMSM machines considering extended speed range](image)
The speed range characteristic and type of machine (DESM or PMSM) clearly reveal compromises on the machine designs and performances. The following could be observed:

- Higher speed range requirement ($\gamma = 5$) leads to a more total loss and create difficulties
### Multiple points optimization and comparisons with a PM machine

#### Table 5.11: Dimensions of extracted machines in Fig. 5.34. [Unit: mm]

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
<th>D41</th>
<th>D42</th>
<th>P41</th>
<th>P42</th>
<th>D51</th>
<th>D52</th>
<th>P51</th>
<th>P52</th>
</tr>
</thead>
<tbody>
<tr>
<td>$x_1$</td>
<td>Stack length</td>
<td>60.0</td>
<td>51.2</td>
<td>6.0</td>
<td>54.0</td>
<td>60.0</td>
<td>54.8</td>
<td>57.1</td>
<td>52.5</td>
</tr>
<tr>
<td>$x_2$</td>
<td>Bridge thickness</td>
<td>8.8</td>
<td>5.6</td>
<td>3.0</td>
<td>3.0</td>
<td>12.0</td>
<td>5.0</td>
<td>3.0</td>
<td>3.0</td>
</tr>
<tr>
<td>$x_3$</td>
<td>Field winding height</td>
<td>9.0</td>
<td>2.4</td>
<td>N/A</td>
<td>N/A</td>
<td>9.0</td>
<td>3.2</td>
<td>N/A</td>
<td>N/A</td>
</tr>
<tr>
<td>$x_4$</td>
<td>Tooth width</td>
<td>6.0</td>
<td>5.0</td>
<td>4.9</td>
<td>5.7</td>
<td>5.1</td>
<td>5.0</td>
<td>5.5</td>
<td>5.4</td>
</tr>
<tr>
<td>$x_5$</td>
<td>Tooth length</td>
<td>25.0</td>
<td>17.3</td>
<td>25.0</td>
<td>14.8</td>
<td>22.7</td>
<td>15.9</td>
<td>21.3</td>
<td>19.2</td>
</tr>
<tr>
<td>$x_6$</td>
<td>Azimuth PM thickness</td>
<td>7.5</td>
<td>7.2</td>
<td>9.8</td>
<td>6.4</td>
<td>6.4</td>
<td>9.7</td>
<td>5.4</td>
<td>5.0</td>
</tr>
<tr>
<td>$x_7$</td>
<td>Azimuth PM length</td>
<td>14.3</td>
<td>16.6</td>
<td>10.0</td>
<td>18.9</td>
<td>10.0</td>
<td>14.9</td>
<td>13.3</td>
<td>16.5</td>
</tr>
<tr>
<td>$x_8$</td>
<td>Shaft radius</td>
<td>20.0</td>
<td>12.9</td>
<td>20.0</td>
<td>12.4</td>
<td>18.4</td>
<td>12.9</td>
<td>19.1</td>
<td>12.8</td>
</tr>
<tr>
<td>$x_9$</td>
<td>Side PM thickness</td>
<td>6.7</td>
<td>5.7</td>
<td>N/A</td>
<td>N/A</td>
<td>10.0</td>
<td>8.3</td>
<td>N/A</td>
<td>N/A</td>
</tr>
</tbody>
</table>

for machine design.

This is due to the fact that operating at high speed, machines are normally required to have less excitation source to handle both voltage and thermal limit, but this will cause high copper loss at base speed. Therefore having higher and higher maximum speed should increase. In fact, trial was made to extend maximum speed with $\gamma = 6$, PMSM model are unable to find machines.

- **Optimal design of DESM could handle higher speed range without sacrificing much losses compared to PMSM model.**
  This fact can be explained by shared copper loss between excitation and armature windings. For example the lack of excitation source at low speed due to small amount of PMs could be compensated by positive excitation current and hence reduce burden for armature current to satisfy high torque at low speed. But that is not the case with PMSM since the excitation source comes only from PM and fixed.

- **DESM model is able to have much lower loss compared to PMSM one.**
  The same reason with shared copper loss between two types of windings in DESM make this machine able to have very low losses.

The influence of $\gamma$ could be also observed on the field winding height variation along the pareto fronts as shown in Fig. 5.36.

It is clear that field winding heights are much bigger compared to ones obtained in the optimizations in the previous section over the driving cycle with $\gamma \approx 1.7$ and heights with $\gamma = 5$ are bigger than ones with $\gamma = 4$ in overall. It means that field windings are more preferred when DESM operates at very high speed regions.
Conclusion

This chapter has been presented using multi-physics model for design optimization of DESM machine on the driving cycle with the objectives are to minimize both total energy losses and material cost. In order to make the optimization feasible regarding the computation time, a set of representative points was suggested based on the energy center of gravity principle. Some interesting machines was extracted and examined on all the operating points of the driving cycle. The comparison between DESM and corresponding permanent magnet machines was made. Results revealed that under the small range of operating speed \( \gamma = \frac{\Omega_{\text{max}}}{\Omega_{\text{base}}} = 1.7 \) PMSM model yields better performances due to no strong flux weakening required and PMSM machines basically perform better the DESM ones due to a lot of flux leakage presented in DESM model. However, in circumstances with extend speed range (higher \( \gamma \)) the DESM model is expected to be able to overwhelm PMSM especially regarding to loss minimization.
Conclusion and Perspectives

Conclusion

The thesis is dedicated to the optimization design of double excitation synchronous machine (DESM) in railway traction. Overall, multi-physics model with saturation consideration was used in order to attain more accurate results. Five chapters were included and conclusions for each chapters were given. In this final part, a general conclusion linking separate chapters and also future work will be addressed.

Chapter 1 briefly introduced railway traction history and importantly covered several types of electrical machine available in this application. Mainly due to historical reason with the mature development, induction machines are currently the most popular choice. Beside that, permanent magnet synchronous motors (PMSMs) through years appear as a very promising candidate with advantages of PM such as high energy and high power density. Additionally PM cost is being reduced making PMSMs are more attractive. A well-known problem with PMSMs is that the air-gap flux is hard to controlled since it comes from PMs. Therefore, the idea is to maintain advantages of PMSM machines but air-gap flux capability is improved. This introduces the idea of double excitation principle by using excitation windings similarly to ones in would field synchronous machine. With that approach, the main focus is to answer the question whether double excitation synchronous machines (DESMs) could provide better performances compared to PMSMs regarding the railway traction application.

Chapter 2 reviewed a basis on DESMs with a number of topologies in literature. Advantages of DESMs were highlighted in terms of both flux control flexibility and energy efficiency. A prototype realized in SATIE was chosen for further study, it is mainly due to the effective flux control curve i.e. maximum flux versus excitation current. A more detailed analysis of the prototype was given. For the prototype being studied, the topology is truly three dimensional requiring the use of 3D finite element method (FEM) and it leads to a very time consuming process for the early design stage. Therefore a much faster alternative analysis method is needed.
Chapter 3 was dedicated to the modeling of electromagnetic part in DESM using equivalent magnetic circuit network (EMCN). Unlike analytical methods, this semi-numerical method is able to consider saturation effect. The very fast computation time is the main advantages of this method while accuracy is still maintained. The 3D topology with complex magnetic flux paths and different core material (solid and laminated) contribute to the modeling complication. The generalized approach with 4 reluctance block basic elements was used. This enables it to calculate local flux densities and therefore core losses could be computed. Torque and losses and main outputs of this electromagnetic model which are important for the calculations considering a driving cycle. Losses are also prerequisite to the thermal analysis model for temperature calculation and moreover recalculate losses i.e. coupling process. Therefore, a thermal analysis modeling was followed.

Chapter 4 focused on thermal aspect and its coupling with the electromagnetic model for the studied DESM. The thermal model is interconnected with electromagnetic model. A lumped parameter thermal resistance network model has been developed with the objective is to determine overall temperature of the windings which is accurate enough for the optimization process. Generally, two global excitation windings and the natural air convection on the surface of the prototype contribute more to the heat evacuation difficulty. With all windings placed in the stator side and losses from rotor are substantially small reducing overheating issue for PMs. The big challenge of thermal analysis is that many empirical equations are used and therefore some heat coefficients were necessarily determined from experiments. Due to the difficulties of the natural air cooling (applied to the DESM prototype), a new surface heat coefficient was assumed. With all the models developed (electromagnetic, thermal and additionally power electronics and mechanical models), a good tool for optimization considering multiple operating points on the driving cycle.

Chapter 5 has been presented using multiphysics model developed in the previous chapters. The objectives are to minimize both total energy losses and material cost. A full consideration of 1000 operating points and transient thermal model make the design process impractical due to long computation time. Instead, a set of representative points was selected and steady state thermal model was used. The DESM model was compared with a corresponding PMSM one (with some parts removed). The results showed that for the train driving cycle with a small range of operating speed, PMSM model yields better performances due to no strong flux weakening required and PMSM machines basically perform better the DESM ones due to a lot of flux leakage presented in DESM model. However, several trials with extended speed ranges, the DESM model seemed to overwhelm PMSM especially regarding to loss minimization.

Perspectives

The optimization was performed with a DESM prototype on a few representative points. In order to more comprehensively analyze performance of DESM, more work needed to be done:
• Consider various sets of representative points either more points or different cell divisions (it was 9-by-9 grid in the thesis) to see influences on the optimal design

• Develop controlling algorithm for the machines of interest to figure out exactly control variable set (the control set was found by setting generated torque in the range of 5% deviated from required one). Moreover, considering the driving cycle with respect to time, this controlling algorithm is wished to incorporate with transient thermal analysis to have results reflecting real time operation

• It is interesting to consider other DESM topologies and compared with PMSM model. The current DESM topology might not be perfect to support the advantage of double excitation principle
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Appendix A

Losses in power electronics modules

In a variable speed drive system, a motor is usually driven by power electronics modules to control voltage as well as frequency. With a double excitation motor, a DC-DC converter is also necessarily equipped with field current is regulated in both magnitude and direction (for weakening and enhancing regions). The inverter supply to armature winding is displayed in Fig. A.1

![Three phase inverter topology](image)

Fig. A.1: Three phase inverter topology

with \( V_d \) is DC link voltage which is usually fixed depending on available power supply (batteries, electric line, etc.)

The operation of power electronics modules cause some losses including switching and conduction losses (leakage loss is usually negligible). Very basically, switching loss is subject to switching frequency and turn-on and turn-off energies (which is related to rising and falling time). Meanwhile, conduction loss could be simply understood as joule loss as load current passes through on-resistance of the power semiconductors (either IGBT, MOSFET or Diode).

A.1 Inverter losses

The calculations of inverter losses are fundamentally based on the sinusoidal load current assumption. Moreover, linearised loss model is assumed. Switching loss energies \( E_s \) is linearised given by (A.1a) and conduction losses \( P_c \) for a single semiconductor is calculated by (A.1b) [95]
Appendix A. Losses in power electronics modules

\[ E_s = E_{sr} \cdot \frac{V_v}{V_{ref}} \cdot \frac{i_v}{i_{ref}} \]  
(A.1a)

\[ P_c = V_0 \cdot i_v + r \cdot i_v^2 \]  
(A.1b)

with:

\( E_{sr} \) is the rated switching loss energy given for reference commutation voltage and current \( V_{ref} \) and \( i_{ref} \).

\( V_v \) and \( i_v \) indicate the actual commutation voltage and current respectively.

\( V_0 \) and \( r \) are semiconductors threshold voltage and differential resistance respectively.

A.1.1 Conduction loss

Conduction loss on each IGBT switch and on each free-wheeling Diode are expressed by (A.2a) and (A.2b) respectively:

\[ P_{con,I} = \frac{V_{CE,0} \cdot i_L}{2\pi} \left( 1 + \frac{\pi M}{4} \cos \phi \right) + \frac{r_{CE} \cdot i_L^2}{2\pi} \left( \frac{\pi}{4} + \frac{2M}{3} \cos \phi \right) \]  
(A.2a)

\[ P_{con,D} = \frac{V_{F,0} \cdot i_L}{2\pi} \left( 1 - \frac{\pi M}{4} \cos \phi \right) + \frac{r_F \cdot i_L^2}{2\pi} \left( \frac{\pi}{4} - \frac{2M}{3} \cos \phi \right) \]  
(A.2b)

with:

\( i_L \): peak load current (sinusoidally assumed)

\( M \): modulation index

\( \phi \): displacement angle between load current and the fundamental of phase voltage

\( V, r \): threshold voltage and differential resistance of IGBT (Diode)

Total conduction loss for 6 pairs (IGBT and free-wheeling diode) are:

\[ P_{con} = 6(P_{con,I} + P_{con,D}) \]  
(A.3)

With the sinusoidal PWM where control signal is generated by comparing a sinusoidal signal (peak \( \hat{V}_{\text{sin}} \)) with a triangle one (peak \( \hat{V}_{\text{tri}} \)) (shown in Fig. A.2, modulation index \( M \) is defined as (A.4)

\[ M = \frac{\hat{V}_{\text{sin}}}{\hat{V}_{\text{tri}}} \]  
(A.4)

with the constant DC link voltage, the output voltage will be controlled by changing modulation index demonstrated in Fig. A.3 [96]

As seen in Fig. A.3 if the required fundamental output phase voltage is above maximum available value i.e. \( 2V_d/\pi \) then the PWM fails to supply.

The threshold voltage and differential resistance of IGBT and Diode in (A.2a) and (A.2b) could be determined from datasheets as guided in [97]
### A.1 Inverter losses

#### A.1.1 Inverter losses

[Fig. A.2: Sinusoidal and triangle signals used for sinusoidal PWM]

#### A.1.2 Switching loss

Switching loss could be obtained by multiplying sum of turn-on and turn-off energies for one switching event with the number of switching time (proportional with switching frequency). A switching loss formulation is introduced in [95] as (A.5). However this formulation is only correct for the linear modulation range ($M \leq 1$) where sinusoidal signal cuts all edges of triangle signal therefore the number of turn-on, turn-off pairs is essentially the switching frequency $f_s$.

$$P_{sw} = \frac{6}{\pi} \cdot f_s \cdot (E_{\text{On},I} + E_{\text{Off},I} + E_{\text{Off,D}}) \cdot \frac{V_d}{V_{\text{ref}}} \cdot \frac{i_L}{i_{\text{ref}}}. \quad (A.5)$$

with:

- $E_{\text{On},I}, E_{\text{Off},I}$: turn-on and turn-off switching energies associated with IGBT
- $E_{\text{Off,D}}$: turn-off energy in Diode due to reverse recovery current

[Fig. A.3: Normalized peak of fundamental output phase voltage]
Accounting for over-modulation ($M > 1$) where the number of switching event pairs (turn-on and turn-off) is actually less than switching frequency, (A.5) is modified as (A.6):

$$P_{sw} = \frac{6}{\pi} \cdot n_c \cdot \left( E_{On,I} + E_{Off,I} + E_{Off,D} \right) \cdot \frac{V_{d}}{V_{ref}} \cdot \frac{i_{L}}{i_{ref}}$$  \hspace{1cm} (A.6)

with $n_c$ is the actual number of switching event pairs

### A.2 DC-DC converter loss

Double excitation principle with a capability of both flux weakening and flux enhancing modes, field current should be therefore capable of changing either its magnitude or its direction. In order to obtain that purpose, a bidirectional DC power circuit is demonstrated in Fig. A.4

![Bidirectional power circuit for excitation windings](image)

**Fig. A.4:** Bidirectional power circuit for excitation windings

#### A.2.1 Conduction losses

Conduction loss on single Mosfet and diode are given by (A.7a) and (A.7b) respectively [98]

$$P_{con,S} = r_{CE} \cdot I_{S,rms}^2$$  \hspace{1cm} (A.7a)

$$P_{con,D} = r_{F} \cdot I_{D,rms}^2 + V_{F,0} \cdot (1 - D) \dot{i}_{load}$$  \hspace{1cm} (A.7b)

with RMS currents through Mosfet and diode are calculated by (A.8a) and (A.8b) correspondingly

$$I_{S,rms} = \sqrt{D \left[I_{L,\min}^2 + I_{L,\min} \Delta I_L + \frac{\Delta I_L^2}{3}\right]}$$  \hspace{1cm} (A.8a)

$$I_{D,rms} = \sqrt{(1 - D) \left[I_{L,\max}^2 - I_{L,\max} \Delta I_L + \frac{\Delta I_L^2}{3}\right]}$$  \hspace{1cm} (A.8b)

where $I_{L,\min} = \dot{i}_{load} - \frac{\Delta I_L}{2}$, $I_{L,\max} = \dot{i}_{load} + \frac{\Delta I_L}{2}$

$\Delta I_L$ is current ripple through the inductor

$D$ is the duty cycle
A.2. DC-DC converter loss

A.2.2 Switching losses

Switching losses on single Mosfet and diode are given by (A.9a) and (A.9b) respectively

\[ P_{sw,S} = (E_{On,M} + E_{Off,M}) \cdot f_{sb} \]  \hspace{1cm} (A.9a)

\[ P_{sw,D} = E_{Off,D} \cdot f_{sb} \]  \hspace{1cm} (A.9b)

with \( E_{On,M} \) and \( E_{Off,M} \) are turn-on and turn-off energies of Mosfet
\( E_{Off,D} \) is the turn-off energy of the Diode
\( f_{sb} \) is switching frequency of the Mosfet

It should be noted that, when the data for turn-off energy in the diode is not available in the diode’s datasheet, this energy could be calculated according to (A.10)

\[ E_{Off,D} = Q_{rr} \cdot V_d \]  \hspace{1cm} (A.10)

where \( Q_{rr} \) are reversible recovery charge of the diode
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Appendix B

Multi-objective optimization algorithm

The intention of this part is not to go in detail about multi-objective optimization algorithms but focuses on a quick comparison between Multi-objective Particle Swarm (MOPSO) which has been used in the thesis and Non-dominated Sorting Genetic Algorithm (NSGA) - II which is the most common algorithm for multi-objective optimizations.

Mono-objective optimization problem either minimizing or maximizing an interested target is a very classical form of an optimization. The formulation is given by (B.1) with a set of \( m \) inequality constraints \( (g) \) and a set of \( p \) equality constraints \( (h) \). It should be noted that a maximizing \( f(x) \) is equivalent to minimizing \(-f(x)\) and \( g(x) \geq 0 \) is equivalent to \(-g(x) \leq 0\). Therefore all optimization problems could be expressed as minimizing optimization cases without any loss of generality.

\[
\begin{align*}
\min_X & \ f(X) \\
\text{s.t.} & \ g_i(X) \leq 0 \quad (i = 1 \div m) \\
& \ h_j(X) = 0 \quad (j = 1 \div p)
\end{align*}
\]

(B.1)

with \( X = [x_1, x_2, ..., x_n] \) is the design vector.

This kind of optimization will lead to only one single best (optimal) solution with an unique design set (it might sometimes be too challenging to find any feasible solutions if difficult constraints are applied). The designer will then work on that single solution. However in the real world, designers will find many cases where there are \( n \ (n \geq 2) \) objectives (multi-objective) needed to handle. The multi-objective optimization is generally formulated as (B.2)

\[
\begin{align*}
\min_X & \ F(X) = \{f_k(X)\} \quad (k = 1 \div n) \\
\text{s.t.} & \ g_i(X) \leq 0 \quad (i = 1 \div m) \\
& \ h_j(X) = 0 \quad (j = 1 \div p)
\end{align*}
\]

(B.2)

In this multi-objective problem, two solutions are compared to each other to see whether a solution dominates the other. A solution \( F_1 \) dominates solution \( F_2 \) (denoted as \( F_1 \preceq F_2 \)) when both following conditions are satisfied (keeping in mind that minimizing goals is being considered):

---

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1. $F_1$ is smaller than or equal $F_2$ in all objectives

2. $F_1$ is greater than $F_2$ in at least one objective

If any of two above conditions is violated, solution $F_1$ is said to not dominate $F_2$. A set of solutions that there is no solution is dominated by any other one is called non-dominated pareto front. An example of dominance relationship and pareto front is demonstrated in Fig. B.1. In this example, a problem to minimize $F(X) = \{f_1(X), f_2(X)\}$ is considered. As it will be seen, point $A$ dominates points $E, D, C$ and $B$ dominates only $E, D$. Points $A$ and $B$ form the non-dominated pareto front even though $B$ and $C$ are non-dominated solutions compared to each other but $C$ is dominated by $A$ so it is removed from the pareto front.

![Fig. B.1: Non-dominated pareto front illustration](image)

### B.1 Non-dominated Sorting Genetic Algorithm (NSGA)-II

NSGA-II proposed by authors of [99] which belongs to evolutionary algorithm concept. It has been the most common algorithm to deal with multi-objective optimization. This algorithm uses elitism, crowded tournament selection. A non-dominated sorting approach with $O(mN^2)$ computational complexity is introduced, where $m$ is the number of objectives and $N$ is the population size.

Once the population is created, the non-dominated pareto front is extracted. This front will be replaced by individuals of the next generation. Each individual in each front are assigned with rank fitness values and the crowding distance between the individual and its neighbors. The crowding distance help to improve diversity in the population. The parents are selected from the population through binary tournament. Only individual with better crowding distance are chosen to generate off-spring from crossover and mutation. The off-spring and the current population are then combined for next selection based on rank and crowding distance.
B.2 Multi-Objective Particle Swarm Optimization (MOPSO)

This optimization algorithm originated from Particle Swarm Optimization (PSO) which was inspired on the choreography of a bird flock [100]. This algorithm is similar to a genetic algorithm in a manner that systems are initiated with a population of random solutions. Each individual is assigned its own velocity and location in each dimension. In search of the optimal solution through iterations, velocities and locations of each individual are stochastically updated using the best solution it has achieved so far called \( p_{\text{best}} \) and the best global solution by found all individuals called \( g_{\text{best}} \). The approach uses the concept of population and a measure of performance similar to the fitness value used in evolutionary algorithm. Also the adjustments of individuals are analogous to the use of a crossover mutation. PSO algorithm allows individuals to benefit from their past experiences and also experiences of other individuals, therefore this algorithm promotes a cooperative model rather than a competitive model as in evolutionary algorithm.

B.3 Mathematical comparisons

Three bi-objective optimization problems will be tested to compare performance between NSGA-II (codes from MATLAB central) and MOPSO (codes by Judicael [92])

Problem 1: KUR:

\[
\text{Minimize} = \begin{cases} 
  f_1(x) = \sum_{i=1}^{2} \left[ -10e^{-0.2\sqrt{x_i^2 + x_{i+1}^2}} \right] \\
  f_2(x) = \sum_{i=1}^{3} \left[ |x_i^{0.8} + 5\sin(x_i^3)| \right] 
\end{cases} 
\]  

(B.3)

with \(-5 \leq x_i \leq 5, i = 1 \div 3\)

Problem 2: ZDT3

\[
\text{Minimize} = \begin{cases} 
  f_1(x) = x_1 \\
  f_2(x) = g(x) h (f_1(x), g(x)) \\
  g(x) = 1 + \frac{9}{29} \sum_{i=2}^{30} x_i \\
  h (f_1(x), g(x)) = 1 - \sqrt{\frac{f_1(x)}{g(x)}} - \frac{f_1(x)}{g(x)} \sin (10\pi f_1(x)) 
\end{cases} 
\]  

(B.4)

with \(0 \leq x_i \leq 1, i = 1 \div 30\)

Problem 3: Binh and Korn function

\[
\text{Minimize} = \begin{cases} 
  f_1(x) = 4x_1^2 + 4x_2^2 \\
  f_2(x) = (x_1 - 5)^2 + (x_2 - 5)^2 \\
  g_1(x) = (x_1 - 5)^2 + x_2^2 \leq 25 \\
  g_2(x) = (x_1 - 8)^2 + (x_2 + 3)^2 \geq 7.7 
\end{cases} 
\]  

(B.5)
with $0 \leq x_1 \leq 5$, $0 \leq x_2 \leq 3$

Problem 1 is somewhat easy since there is no constraint and the pareto front is continuous, problem 2 also does not have constraints but the number of variables much increases up to 30, also the front pareto is presented with several discontinuous regions. Problem 3 introduces constraints and the pareto front with a small region seems to be difficult to find solutions. These characteristics are observed in Fig. B.2.

Optimality and diversity of two important criteria to evaluate the quality of a pareto front. Optimality is to indicate whether the pareto front converge to the true optimal pareto front or not. Meanwhile diversity is to evaluate the distribution of non-dominated solutions along the front. A diversity quality examination was proposed by [101] which is pretty simple but useful to measure the distance variance of neighboring solutions in the pareto front defined as (B.6) with almost the same convergence quality even though there is explicit criterion for the proof.

$$SP = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (\bar{d} - d_i)^2}$$  \hspace{1cm} (B.6)

With: $d_i = \min_{i,j \neq i} \left( \sum_{k=1}^{K} |f_i^k - f_j^k| \right)$

with $n$ is the number of solutions on the front, $K$ is the number of objectives, $\bar{d}$ is mean of all distance $d_i$, a small value of $SP$ indicates better diversity of the front. The comparison between MOPSO and NSGA-II for 3 mentioned problems are shown in Table. B.1. Due to the stochastic nature of the algorithms, the optimizations are repeated 5 times for each algorithm. Also, difference combinations of numbers of generations ($n_g$) and particles (individuals)($n_p$) are tested. In the table, due to limited spaces, MOPSO is shorted as PS (particle swarm) and NSGA-II is shorted as GA (genetic algorithm). The pareto front comparisons for a case of 50 generations and 50 particles are shown in Fig. B.2.

The average values of $SP$ through runs are reported in Table. B.2

Several remarks on the diversity could be noted as follows:

- MOPSO appears to be better when dealing with continuous pareto fronts as with the problem 1
- It is obvious that increasing numbers of iterations or particles make results more reliable, as seen with less variations of $SP$ through runs. Through many other cases, a combination 50 generations and 50 particles are adopted as personal experience
- With same numbers of function evaluations (same product $n_g \cdot n_p$), having more particles (number of generations decreases as the result) seems to bring better result since it is able to better explore the space
### Table B.1: Pareto front diversity comparison with $SP$ index for various cases

<table>
<thead>
<tr>
<th>$n_g$ &amp; $n_p$</th>
<th>Problem</th>
<th>Run 1</th>
<th>Run 2</th>
<th>Run 3</th>
<th>Run 4</th>
<th>Run 5</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>PS</td>
<td>GA</td>
<td>PS</td>
<td>GA</td>
<td>PS</td>
</tr>
<tr>
<td>20 &amp; 20</td>
<td>1</td>
<td>0.40</td>
<td>1.48</td>
<td>0.38</td>
<td>2.34</td>
<td>0.35</td>
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<tr>
<td></td>
<td>2</td>
<td>0.28</td>
<td>0.32</td>
<td>0.86</td>
<td>0.32</td>
<td>1.62</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>0.14</td>
<td>0.04</td>
<td>0.13</td>
<td>0.09</td>
<td>0.06</td>
</tr>
<tr>
<td>50 &amp; 20</td>
<td>1</td>
<td>0.35</td>
<td>2.07</td>
<td>0.39</td>
<td>1.90</td>
<td>0.21</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>0.20</td>
<td>0.31</td>
<td>0.27</td>
<td>0.30</td>
<td>0.22</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>0.11</td>
<td>0.06</td>
<td>0.11</td>
<td>0.06</td>
<td>0.06</td>
</tr>
<tr>
<td>20 &amp; 50</td>
<td>1</td>
<td>0.27</td>
<td>0.34</td>
<td>0.26</td>
<td>0.44</td>
<td>0.25</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>0.29</td>
<td>0.14</td>
<td>0.29</td>
<td>0.11</td>
<td>0.45</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>0.07</td>
<td>0.04</td>
<td>0.07</td>
<td>0.06</td>
<td>0.06</td>
</tr>
<tr>
<td>50 &amp; 50</td>
<td>1</td>
<td>0.16</td>
<td>0.43</td>
<td>0.16</td>
<td>0.42</td>
<td>0.16</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>0.21</td>
<td>0.15</td>
<td>0.25</td>
<td>0.13</td>
<td>0.26</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>0.07</td>
<td>0.01</td>
<td>0.05</td>
<td>0.01</td>
<td>0.06</td>
</tr>
</tbody>
</table>

Red color indications emphasize smaller values of PS compared to GA.

### Table B.2: Pareto front diversity comparison with mean $SP$ index for various cases

<table>
<thead>
<tr>
<th>$n_g$ &amp; $n_p$</th>
<th>Problem 1</th>
<th>Problem 2</th>
<th>Problem 3</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>PS</td>
<td>GA</td>
<td>PS</td>
</tr>
<tr>
<td>20 &amp; 20</td>
<td>0.42</td>
<td>1.78</td>
<td>0.88</td>
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<tr>
<td>50 &amp; 20</td>
<td>0.30</td>
<td>1.73</td>
<td>0.24</td>
</tr>
<tr>
<td>20 &amp; 50</td>
<td>0.25</td>
<td>0.47</td>
<td>0.32</td>
</tr>
<tr>
<td>50 &amp; 50</td>
<td>0.16</td>
<td>0.44</td>
<td>0.23</td>
</tr>
</tbody>
</table>

These are some quick comparisons between two algorithms, in order to explore more obvious strength of one over the other, intensive comparisons should be done. However, it goes far beyond the subject of this thesis. It is hard to explicitly conclude which one is better than the other even though NSGA-II is generally accepted as the most popular algorithm to handle multi-objective optimizations. Using any of them in engineering optimization problems could just be a matter of a designer’s habit. That explains why MOPSO is used in this thesis as MOPSO was developed in SATIE.
Fig. B.2: Optimal pareto front comparison between MOPSO and NSGA-II. a) Problem 1. b) Problem 2. c) Problem 3
References


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