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^4He optical pumping with intensity modulated laser light

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Résumé. — Les atomes métastables ^4He (2^3S_1) sont pompés optiquement en lumière modulée en intensité. L'utilisation, comme source de pompage, d'un laser monomode LNA pompé par une diode laser permet l'étude de signaux de résonance prédits par la théorie du pompage optique mais non encore observés. Les résonances sont détectées sur le faisceau de pompage transmis à la fréquence de modulation et ses harmoniques. L'application de cette méthode à la réalisation de magnétomètres de haute sensibilité est suggérée.

Abstract. — ^4He (2^3S_1) metastable atoms are optically pumped with intensity modulated light. The use of a single mode diode-pumped LNA laser as the pumping source, allows the study of resonance signals predicted by the optical pumping theory but not yet observed. Resonances are detected on the transmitted pumping beam at the modulation frequency and its harmonics. Application of this method to high sensitivity magnetometers is suggested.

1. Introduction.

In atomic optical pumping experiments, the magnetic resonance experiments have a particularly important place and lead to many applications such as high sensitivity magnetometers. In 1961, Bell and Bloom [1] suggested and published another very attractive method to induce driven spin precession and observe resonances without a radio-frequency magnetic field but only by intensity modulated pumping light at the Larmor frequency of atomic states in the static magnetic field. This fine method gave only few experimental publications certainly because it was rather difficult to obtain a high modulation rate and to modulate the emitted intensity of the vapor lamp at high frequencies.

In Bell and Bloom experiments [1, 2], optical pumping of ground state Cs and Rb atoms and metastable 2^3S_1 He atoms is investigated. Resonance appears as a modification of the average intensity of the modulated pumping beam transmitted through the cell containing the atomic gas when the frequency of the modulation equals the Larmor frequency in a given static magnetic field. Resonances at the modulation frequency and its harmonics were not experimentally investigated. In Corney experiments ([3] and Refs. therein), Cd atoms are excited in the 5^3P_1 state with an intensity modulated discharge lamp. In the particular geometry used, resonance is observed as a modification of the modulation of the fluorescence

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emitted at right angle when the frequency of the modulation is twice the Larmor frequency. Experiments are also reported where a R.F. field and an intensity modulated pumping beam are applied simultaneously [4]

Recently we have developed a diode pumped LNA laser tunable on the $(2^3S_1-2^3P_0)$ ^4He lines. Using an optoelectronic modulator (acoustooptic), it is possible to modulate the laser beam with a modulation rate close to 1

In this paper we present our experiments where the resonances are optically detected. In particular, we detect the modulation induced in the pumping light beam after transmission through He atomic gas. Another interesting method of detection has also been recently published [5], using optogalvanic effect. These signals can be used in ^4He magnetometry. For high modulated pumping power, new resonances appear at multiple harmonics of the Larmor frequency. We systematically study the optical pumping intensity and polarization effects on the resonances and we present an experiment-theory comparison with a model using the density matrix formalism

2. Experimental apparatus.

The block diagram of the experimental apparatus is illustrated in figure 1. The pumping light comes out from a LNA diode pumped laser [L] tuned on the D_0 $(2^3S_1-2^3P_0)$ ^4He transition at $1\,0829\,\mu\text{m}$. This laser has been described in other papers [6, 7] and gives about 10 mW in C.W. single mode emission. The fine selection of the wavelength is provided by two intracavity solid étalons (thickness 200 and $500\,\mu\text{m}$) and a piezoelectric translator [Pz] which modifies the length of the laser cavity

The laser beam is intensity modulated by an acoustooptic modulator [AM] (Intra Action Corp. AOM-4 OR) driven by the signal processor [SP] (Intra Action model ME). The R.F. excitation of the modulator at the frequency N is given by a function generator [G] (PM 5192)

The modulated light is linearly or circularly polarized by the polarizer [P] and propagates through a spherical pyrex cell [C] ($\Phi = 4\,\text{cm}$) containing ^4He atoms at a pressure of 1.5 Torr. The beam diameter inside the cell is close to 5 mm. The atoms are submitted to a weak H.F. electrodeless electric discharge to create metastable 2^3S_1 excited states. This cell is placed inside a cylindrical μ -metal shield [S] (internal diameter $\cdot 50\,\text{cm}$ and length $\cdot 120\,\text{cm}$) to avoid fluctuations of the ambient magnetic field. A pair of Helmholtz coils [b] (diameter $\cdot 40\,\text{cm}$) provides the static magnetic field B .

A photodiode [PD1] detects the transmitted laser light through the helium cell and an electronic detection [D] allows measuring simultaneously the static value of the light intensity and the modulation of the light intensity at the frequency N and at other harmonic components $2N, 3N, \dots$

Another photodiode [PD2] detects the fluorescent light emitted by laser excited He atoms. This photoelectric signal is used to lock the single mode laser frequency on the maximum of D_0 $(2^3S_1-2^3P_0)$ fluorescent light with the help of the piezoelectric translator [Pz]. In order to study in phase and in quadrature components of the modulated resonance signals we use a lock-in amplifier [A] (EGG Mod 5202). A frequency multiplier [M] generates harmonic frequencies nN to monitor the lock-in amplifier reference. The amplitudes of in phase and in quadrature signals *versus* magnetic field B are recorded on a two channel chart recorder.

3. Theory.

The theory of optical pumping with modulated light has been established three decades ago [2, 8]. We recall here the well known equations and discuss the approximations which apply to

Fig 1 — Experimental set up L : LNA tunable laser , AM : acousto-optic modulator , P : polarizer , C : helium cell ; b : Helmholtz coils , S : magnetic shield , PD1, PD2 : photodetectors , D : amplifier ; DC and AC are respectively the average value and the modulated part of the detected signal , G : function generator , SP : signal processor driving the acousto-optic modulator , M : frequency multiplier ; A : lock-in amplifier , R : chart recorder

the case of optical pumping of ⁴He (2 ³S₁) with the 2 ³S₁-2 ³P₀ line. The evolution of the standard irreducible components of the density matrices ρ and ρ_e of a system of ⁴He atoms in the 2 ³S₁ metastable state and 2 ³P₀ state respectively is governed by :

$$\frac{d\rho_q^k}{dt} = -jq\omega\rho_q^k - \Gamma\rho_q^k + \Lambda\delta_{k_0}\delta_{q_0} + \frac{1}{T_p}(\Delta\rho_q^k)_p + \frac{\Gamma_e\rho_e}{\sqrt{3}}\delta_{k_0}\delta_{q_0} \quad (1)$$

$$\frac{d\rho_e}{dt} = -\Gamma_e\rho_e - \frac{\sqrt{3}}{T_p}(\Delta\rho_0^0)_p \quad (2)$$

where ω is the Larmor angular frequency in the magnetic field $\mathbf{B}$, Γ the relaxation constant of the metastable level (we assume a unique constant), Λ is the creation rate of the metastable atoms by the discharge. The last term in (1) represents the repopulation by spontaneous emission from the upper level 2 ³P₀ with Γ_e , the radiative damping constant ($\Gamma_e \approx 10^7 \text{ s}^{-1}$).

$\frac{1}{T_p} (\Delta \rho_q^k)_p$ is the pumping term where T_p is the pumping time. $\frac{1}{T_p}$ is proportional to the power density of the pumping beam and can be expressed as :

$$\frac{1}{T_p} = \gamma (1 + \varepsilon \cos \Omega t) \quad (3)$$

where Ω is the intensity modulation angular frequency ($\Omega = 2 \pi N$) of the beam and ε the modulation rate. The power density is low enough to avoid absorption saturation. However the average pumping constant γ may be larger than the relaxation constant Γ . $(\Delta \rho_q^k)_p$ takes the general form [9] :

$$(\Delta \rho_q^k)_p = \sum_{k', q'} B_{qq'}^{kk'} \rho_q^{k'} \quad (4)$$

with :

$$B_{qq'}^{kk'} = (-1)^{k+k'-q+1} \frac{3}{\sqrt{2k+1} \sqrt{2k'+1}} \sum_{k'', q''} \sqrt{2k''+1} \frac{1 + (-1)^{k+k'+k''}}{2} \times \\ \times \begin{Bmatrix} k & k' & k'' \\ 1 & 1 & 1 \end{Bmatrix} \begin{bmatrix} k'' & k' & k \\ q'' & q' & -q \end{bmatrix} \Phi_{q''}^{k''}(e) \quad (5)$$

where $\begin{Bmatrix} \end{Bmatrix}$ and $\begin{bmatrix} \end{bmatrix}$ are the $6J$ and $3J$ coefficients respectively and $\Phi_{q''}^{k''}(e)$ the irreducible component of the photon density matrix corresponding to the polarization vector e of the pumping beam. The He vapor is supposed to be optically thin.

The first simplification is to consider that the radiative damping constant Γ_e of the 2^3P_0 state is much greater than the average pumping rate γ so that ρ_e is negligible and ρ_0^0 can be considered as constant.

We look for a general solution

$$\rho_q^k(t) = \sum_{n=-\infty}^{+\infty} {}^{(n)}\alpha_q^k e^{jn\Omega t} \quad (6)$$

with ${}^{(n)}\alpha_0^0 = \frac{1}{\sqrt{3}} \delta_{n0}$ (population normalized to 1) and the ${}^{(n)}\alpha_q^k$ ($k \neq 0$) are solutions of the system :

$$[\Gamma + j(n\Omega + q\omega)] {}^{(n)}\alpha_q^k - \gamma \sum_{\substack{k' \neq 0 \\ q'}} B_{qq'}^{kk'} \left[{}^{(n)}\alpha_{q'}^{k'} + \frac{\varepsilon}{2} ({}^{(n-1)}\alpha_{q'}^{k'} + {}^{(n+1)}\alpha_{q'}^{k'}) \right] = \\ = \frac{\gamma}{\sqrt{3}} B_{q0}^{k0} \left[\delta_{n0} + \frac{\varepsilon}{2} (\delta_{n1} + \delta_{n-1}) \right] \quad (7)$$

In the domain of low optical pumping power ($\gamma \ll \Gamma$), the solution is found by taking only into account the equations with $n = 0, 1$ and neglecting all couplings with $|n| > 1$.

For a given modulation angular frequency Ω , resonance occurs if $n\Omega = q\omega$ (q integer). If $\Omega \gg \Gamma$, the different resonances are well separated and can be studied separately. The resonances are monitored by measuring the absorption of the pumping beam through the cell. This absorption is proportional to the quantity L_A :

$$L_A = \frac{1}{T_p} \sum_{k, q} (-1)^{k+q} \Phi_{-q}^k \rho_q^k \quad (8)$$

For a linear polarization vector $\mathbf{e}$ making an angle θ with $\mathbf{B}$, resonances at $\omega = 0$, $\Omega/2$ and Ω take the following form (restricted to the lowest order in average optical power) :

$$L_A^{(0)} = -g^2(1 + \varepsilon \cos \Omega t) \left[2 \sin^2 \theta \cos^2 \theta \frac{1}{1+u^2} + \frac{\sin^4 \theta}{2} \times \frac{1}{1+4u^2} \right] \quad (9)$$

$$L_A^{(\Omega/2)} = -g^2 \varepsilon (1 + \varepsilon \cos \Omega t) \frac{\sin^4 \theta}{4} \left[\frac{\cos \Omega t + (X - 2u) \sin \Omega t}{1 + (X - 2u)^2} \right] \quad (10)$$

$$L_A^{(\Omega)} = -g^2 \varepsilon (1 + \varepsilon \cos \Omega t) \sin^2 \theta \cos^2 \theta \left[\frac{\cos \Omega t + (X - u) \sin \Omega t}{1 + (X - u)^2} \right] \quad (11)$$

Similarly, for a circularly polarized beam with a propagation direction making an angle θ with $\mathbf{B}$, we obtain

$$L_A^{(0)} = -g^2(1 + \varepsilon \cos \Omega t) \left[\frac{\sin^2 \theta (1 + \cos^2 \theta)}{2} \frac{1}{1+u^2} + \frac{\sin^4 \theta}{8} \times \frac{1}{1+4u^2} \right] \quad (12)$$

$$L_A^{(\Omega/2)} = -g^2 \varepsilon (1 + \varepsilon \cos \Omega t) \frac{\sin^4 \theta}{16} \left[\frac{\cos \Omega t + (X - 2u) \sin \Omega t}{1 + (X - 2u)^2} \right] \quad (13)$$

$$L_A^{(\Omega)} = -g^2 \varepsilon (1 + \varepsilon \cos \Omega t) \frac{\sin^2 \theta (1 + \cos^2 \theta)}{4} \left[\frac{\cos \Omega t + (X - u) \sin \Omega t}{1 + (X - u)^2} \right] \quad (14)$$

where $u = \omega/\Gamma$, $X = \Omega/\Gamma$, $g = \gamma/\Gamma$

Resonances appear on the transmitted beam as modulation at null, Ω and 2Ω frequencies. When the pumping constant γ is no longer negligible with respect to the relaxation constant Γ , radiative broadening occurs. The resonances take a more complicated form and the corresponding expressions may be obtained by a development to a higher order in g or numerically evaluated. Modulations of the transmitted beam at higher harmonics are found by including equations with $|n| > 1$. For example, beam modulation at the third harmonic exhibits a resonance at $\omega = \Omega$ and, for a linear polarization vector, the corresponding expression (restricted to the lowest power in g) is given by :

$$L_A = g^3 \varepsilon^3 \frac{3 \sin^4 \theta \cos^2 \theta}{16} \left[\frac{[1 - 2(X - u)^2] \cos 3\Omega t + 3(X - u) \sin 3\Omega t}{[1 + (X - u)^2][1 + 4(X - u)^2]} \right] \quad (15)$$

4. Experimental results.

4.1 RESONANCE POSITIONS. — Figure 2 shows the amplitude of the modulation of the transmitted beam at angular frequency Ω ($N = 250$ kHz) and 2Ω versus magnetic field B cosine component (a) and sine component (b). The beam is linearly polarized with the electric field $\mathbf{e}$ making an angle $(\mathbf{e}, \mathbf{B}) = 45^\circ$ and the modulation rate is $\varepsilon = 0.68$. As expected from relations (9, 10, 11), resonances are observed at magnetic field $B = B_0$ and $B_0/2$ corresponding to Larmor frequencies $\omega = \Omega$ and $\Omega/2$ and as intensity modulation at the two frequencies Ω and 2Ω . At $\omega = 0$ ($B = 0$), a significant resonance is observed only on the cosine component of the modulation at Ω . The small resonances visible at $B = 0$ on the modulation at the frequency 2Ω may be due to a small intensity modulation at 2Ω of the incident beam caused by non-linearity in the acousto-optic modulator. Relative amplitudes of the resonances are in good agreement with the theory.

4.2 RESONANCES AT MULTIPLE HARMONICS. — Modulations of the transmitted beam have been observed up to the tenth harmonic. Some of them at $\omega = \Omega$ are represented in figure 3

Fig 2 — Amplitude of the modulation of the transmitted beam at angular frequency Ω (top) and 2Ω (bottom) *versus* magnetic field B with the cosine components on the left and the sine components on the right. Resonances are observed at field intensities $B = 0, B_0/2, B_0$ corresponding to Larmor frequencies $\omega = 0, \Omega/2, \Omega$ respectively

with the amplitude of the cosine component on the left and of the sine component on the right. In the following, we have analysed the amplitude of the resonances *versus* modulation rate, the amplitude and width *versus* optical power and finally, the angular dependance of the signals

a) Resonance amplitude *versus* modulation rate ε relation (11) shows that for $\omega = \Omega$, the amplitudes of the cosine components $S(\Omega)$ and $S(2\Omega)$ at frequencies Ω and 2Ω are proportional to ε and ε^2 respectively so that

$$S(\Omega) = \frac{2 S(2\Omega)}{\varepsilon}.$$

The two quantities $S(\Omega)$ and $\frac{2 S(2\Omega)}{\varepsilon}$ are plotted *versus* ε in figure 4 in the case of a linearly polarized beam with $\theta = 45^\circ$ and an average power $\bar{P} = 0.55$ mW. As predicted, the experimental values fit well on a straight line. The two lines may be considered as identical: we note that relation (11) is valid only at low optical power. As the optical power increases, we observe that the two quantities $S(\Omega)$ and $2 S(2\Omega)/\varepsilon$ are still represented by straight lines but with different slopes. Similar conclusions are found for a circularly polarized beam.

b) Amplitude and width *versus* optical power: the widths of the resonances at $\omega = \Omega$, observed on the first three harmonics are represented *versus* optical power $\bar{P}$ in figure 5. At zero optical power, the widths at the two frequencies Ω and 2Ω have a

Fig 3 — Resonance amplitudes *versus* magnetic field B of several harmonics of the modulation angular frequency Ω ($N = 250$ kHz). The resonances are observed at the Larmor frequency $\omega = \Omega$. The cosine components (in phase) are represented on the left and the sine components (in quadrature) are on the right. The electric field $\mathbf{e}$ of the linearly polarized laser beam is such that $(\mathbf{e}, \mathbf{B}) = 45^\circ$. Modulation rate $\varepsilon = 0.8$.

common value equal to 2Γ (8 kHz in frequency units). The width at the frequency 3Ω is much larger than expected from relation (15). Actually, the resonance curve is not a pure Lorentzian curve (see Fig 3) and the calculated width of the cosine resonance at zero power is equal to 0.6Γ . The experimental value is somewhat higher and this discrepancy is due to a magnetic field inhomogeneity over the volume of the helium cell.

The widths of the 3 resonances have not the same dependence *versus* $\bar{P}$. This is in fairly good agreement with the result of a numerical resolution of equation (7) represented by solid lines in figure 5. The parameters needed for the calculation are experimentally obtained ($\Gamma = 4$ kHz, $\varepsilon = 0.72$, linear polarization with $\theta = 45^\circ$) and the ratio $\gamma/\bar{P}$ is obtained by fitting experimental and calculated widths for $\bar{P} = 2$ mW on the Ω curve. The physical meaning of the difference between the slopes of the curves corresponding to the frequencies Ω and 2Ω is not evident. This difference is explained by the calculation if we take into account terms with $|n| = 2$ in the expansion of the density matrix elements (6).

The amplitudes of the 3 resonances are represented *versus* $\bar{P}$ in a log-log scale in figure 6 together with the result of a calculation (solid lines) using the same parameters as before. In the zero power limit, the amplitudes at the two frequencies Ω and 2Ω are predicted to behave

Fig 4 — $S(\Omega)$ ($\square$) and $\frac{2S(2\Omega)}{\varepsilon}$ (+) versus modulation rate ε . $S(\Omega)$ and $S(2\Omega)$ are the resonance amplitudes of the Ω and 2Ω harmonics observed at the Larmor angular frequency $\omega = \Omega$ and at constant average optical power $\bar{P} = 0.55$ mW. The laser beam is linearly polarized.

Fig. 5 — Widths (in frequency units) of the resonances at Larmor frequency $\omega = \Omega$, observed on the first three harmonics of the modulation frequency Ω , versus average optical power $\bar{P}$: Ω ($\times$), 2Ω ($\square$), 3Ω (+). The laser beam is linearly polarized and the modulation rate is equal to 0.72. Full lines are calculated (see text for details).

Fig 6 — Amplitudes of the resonances at Larmor frequency $\omega = \Omega$, observed on the first three harmonics of the modulation frequency Ω versus average optical power $\bar{P}$: Ω ($\times$), 2Ω ($\square$), 3Ω ($+$) (Linear polarization, modulation rate $\varepsilon = 0.72$) Full lines are calculated

Fig 7 — Amplitude of the intensity modulation at frequency Ω observed at $\omega = \Omega$ versus angle θ between the electric field $\mathbf{e}$ of the linearly polarized beam and the magnetic field $\mathbf{B}$. The modulation rate is 0.7 Full line is calculated

like $(\bar{P})^2$, while the amplitude at the frequency 3Ω behave like $(\bar{P})^3$. The experimental results agree qualitatively with the calculation. Width and amplitude are important characteristics in magnetometry application: the sensitivity of the magnetometer is proportional to the ratio amplitude over width.

c) Spatial anisotropy figure 7 represents the amplitude of the resonance at $\omega = \Omega$ versus angle θ between the magnetic field and the polarization vector of the beam. At low optical power, spatial anisotropy is described by the geometrical factor in relation (11). As expected, the experimental signal vanishes for $\theta = 0$ and $\theta = \pi/2$ and is maximum for θ close to 45° . The anisotropy profile is lightly modified when optical power increases. The solid line is the result of a calculation with $\gamma/\Gamma = 0.6$. This parameter is estimated from the measurement of the width of the resonance and with the help of figure 5

Similarly, figure 8 represents the amplitude of the resonance at $\omega = \Omega$ in the case of circular polarization. θ is the angle between the magnetic field and the propagation direction of the beam. The solid line is the result of a calculation with $\gamma/\Gamma = 1$. In both cases, theory and experiment are in good agreement.

Fig 8 — Amplitude of the intensity modulation at frequency Ω observed at $\omega = \bar{\Omega}$ versus angle θ between the propagation direction of the circularly polarized beam and the magnetic field $\mathbf{B}$. The modulation rate is 0.9. Full line is calculated.

5. Conclusion.

The recent possibility to use a laser in helium optical pumping allows now the study of interesting theoretically predicted effects difficult to obtain with a lamp. It has been shown that when optical pumping is achieved with only one light beam, the best efficiency is obtained when using one of the three D lines: this can be done only with a laser. Two other advantages of the laser over the lamp are high intensity and high frequency intensity modulation capability with an electrooptic device.

Exploitation of these new resonance signals may be possible in magnetometry and a systematic comparison between the signal to noise ratio related to the magnetometer sensitivity, obtained with magnetic resonance on one hand and with intensity modulated pumping method on the other hand, are in progress. The obvious great advantage of the second method is the absence of R.F. magnetic field. As a consequence, the resonances are free from R.F. broadening.

At the present time, we are studying another new optical pumping method in which the polarization of the beam is modulated. Interesting large signals are also obtained.

References

- [1] BELL W. E. and BLOOM A. L., *Phys. Rev. Lett.* **6** (1961) 280
- [2] BLOOM A. L. and BELL W. E., *Advances in Quantum Electronics* (Columbia University Press, New York and London) 1961, p. 224
- [3] CORNEY A., *J. Phys. B* **1** (1968) 458
- [4] NOVIKOV L. N. and POKAZAN'EV V. G., *Sov. Phys. JETP* **26** (1968) 438
- [5] SCHEARER L. D. and TIN P., *J. Opt. Soc. Am.* **B 6** (1989) 1771
- [6] AUBERT J. J., WYON Ch., CASSIMI A., HARDY V., HAMEL J., *Opt. Comm.* **69** (1989) 299
- [7] CASSIMI A., Thesis, Caen (1989) unpublished.
- [8] POKAZAN'EV V. G., *Opt. Spectrosc.* **24** (1968) 182
- [9] FAROUX J. P., Thesis, Paris (1969) unpublished (microfilm n° AO 3807, CNRS, 15 quai Anatole France, 75007 Paris).