Electronic susceptibility of small particles of silver
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Previously [1], it has been predicted that the electronic properties of sufficiently small metal particles will differ significantly from those of the bulk material. This difference is attributed to the so-called quantum size effect in which a localization of the electronic wavefunction due to the small size of the particle produces a splitting of the electronic energy levels. One of the most interesting predictions associated with this model is that, when the energy difference δ between two adjacent energy levels at the Fermi level is comparable to kT, the magnetic susceptibility is strongly modified. In particular, for particles with an odd number of electrons, Kubo has predicted that for $kT \ll \delta$, the electronic susceptibility will be of the Curie type rather than the temperature independent Pauli type which is characteristic of the bulk metal.

The purpose of this letter is to present the results of measurements of the variation of the susceptibility of silver particles as a function of temperature and to compare this variation with the existing theoretical predictions. The measurements reported here were performed at temperatures between 8 K and 190 K using silver particles which were trapped in a benzene matrix and which had an average diameter of 10 Å. The susceptibility was deduced from the silver conduction electron spin resonance (C.E.S.R.) absorption by calculating the area under the imaginary part of the dynamic susceptibility measured as a function of magnetic field strength. The present results are related to a previous publication in which the observation of C.E.S.R. in small silver crystals was reported [2]. The line width of the observed C.E.S.R. signals for the small silver particles is much narrower than that found for the bulk metal, and this difference can be accounted for by the decrease in the relaxation rate as a result of the quantum size effect [3].

The thermodynamic properties of an ensemble of small metallic crystals are of course directly related to their electronic energy level distributions. If we assume that the shape of a small particle is a perfect sphere, then some of the energy levels will be degenerate. Kubo [1] has proposed that the irregularities in the shape of the particles will lift the degeneracy in the electronic energy levels and thus, in a hypothetical set of particles, each having N atoms, every single small crystal will have its own energy spectrum, which is determined by specific boundary conditions. Kubo also assumed that the levels are randomly distributed with successive energy levels spacings given by a Poisson distribution. Gorkov and Eliashberg [4] have shown that this approach does not take into account the repulsion of the energy levels and they introduced, in the case of weak magnetic fields and low spin orbit coupling, an orthogonal ensemble and, in the case of strong spin orbit coupling, a symplectic ensemble (for a discussion see ref. [4]). Denton et al. [5] have calculated the free energy per particle for these different ensembles. Their results for the electronic susceptibility which were calculated assuming that the function of magnetic field strength. The present results are related to a previous publication in which the observation of C.E.S.R. in small silver crystals was reported [2]. The line width of the observed C.E.S.R. signals for the small silver particles is much narrower than that found for the bulk metal, and this difference can be accounted for by the decrease in the relaxation rate as a result of the quantum size effect [3].

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number of electrons per particle remains constant (canonical statistical distribution) are plotted in figure 1. In the case of particles with an odd number of electrons the susceptibility at low temperature follows closely a Curie law and it is not strongly dependent on the statistical ensemble chosen. Therefore from a measurement of the odd particle susceptibility it is accordingly very difficult to distinguish between the different ensembles. For the even particles susceptibility the Poisson distribution gives a finite susceptibility at zero temperature whereas the orthogonal and symplectic ensembles both give a susceptibility equal to zero.

Experimental evidence for the differing susceptibilities of particles having an odd or an even number of atoms was found first by Taupin [6] from N.M.R. Knight shift measurements on small Li particles in LiF. Similar measurements performed more recently for small Al [7] and Cu [8] particles have shown that the particles with an even number of atoms tend to exhibit a zero Knight shift and hence a zero spin susceptibility. This proves that the distribution of energy levels deduced from the symplectic or orthogonal ensemble is more realistic than the random distribution. Though good measurements of the spin susceptibility have been deduced from the Knight shift in the case of even particles, the size distribution of the particles in the samples has prevented the extraction of precise information about the susceptibility of odd particles.

The susceptibility deduced from the temperature dependence of the E.S.R. absorption is obtained from samples with a size distribution. If we make the reasonable assumption that the number of particles with an odd number of conduction electrons is equal to that with an even number, the low temperature susceptibility is chiefly that of the odd particles. As already pointed out the odd particles susceptibility for the different distributions are close to each other and we cannot expect to determine which one applies to the case of silver.

The samples of small particles used in this experiment were prepared by simultaneously evaporating in a vacuum better than $1.5 \times 10^{-6}$ torr both silver and an inert matrix (C$_6$H$_6$) onto a cold surface (77 K). The reported measurements were performed after annealing the samples at 195 K. Before the annealing process the electron paramagnetic resonance signal was composed of four narrow hyperfine lines due to $^{107}$Ag and $^{109}$Ag atoms trapped in the matrix and a weak signal with an apparent $g$ value approximately equal to 2.007 [9]. During the annealing process the atomic silver hyperfine lines gradually disappear and the weak signal grows. We attribute this behaviour to silver atoms and clusters of atoms diffusing in the matrix to form small particles which are responsible for the signal whose $g$-value is approximately 2.007. If the sample temperature is raised above 195 K the central signal also disappears. We show in figure 2 the size distribution of the small particles, which was obtained with a transmission

![Graph](image-url)
It is well known that the molecular beam technique employed here can produce spurious electron paramagnetic resonance signals due to free radicals which are created during the deposition process. In order to check our results we have reproduced the experimental conditions used to prepare the small particles without silver in the heating basket. No electron paramagnetic resonance signal appeared either before or after the annealing process. We have also trapped silver particles in \( \text{C}_{18}\text{H}_{36} \) or \( \text{CO}_2 \) matrices, the atomic signals were less intense but after annealing the central signal was similar to that observed in \( \text{C}_6\text{H}_6 \). Using the same experimental set up we have evaporated lithium [10] and aluminium [11] metals. In the case of lithium trapped in \( \text{CO}_2 \) matrix the signal observed before annealing is only due to atomic hyperfine lines. After annealing at 160 K these lines disappear and a signal centered at \( g \) equal 2 grows. The intensity of both the atomic signals and the central signal, that we attribute to small lithium particles nucleated during the annealing process, are in agreement with the amount of lithium in the matrix and the assumption of one paramagnetic center per small particle with an odd number of atoms. We thus believe that the above mentioned experimental results give strong support to our identification of the signal at \( g \) around 2.007 as the signal of small silver particles.

The C.E.S.R. measurements were performed with a Varian X-band spectrometer. A flux of cold helium gas blown on the sample permitted a progressive variation of the temperature from 8 K up to 190 K. The temperature was measured with an Au-Fe, Ni-Cr thermocouple with an absolute precision of \( \pm 2 \) K. After completion of the whole series of measurement, a return of the sample to low temperature indicated that the size of the small particles had not changed during the process.

The susceptibility \( \chi \) was measured through integration of the signal and direct comparison with the area under a similarly integrated signal of a reference pitch. The experimental values of \( \chi/\chi_p \) where \( \chi_p \) is the Pauli susceptibility are given in figure 3 as a function of \( kT/\delta \) where the mean energy spacing at the Fermi level is defined by \( \delta = 4 \varepsilon_F/N \) [1]. In this formula \( N \) is the number of atoms per small particle, \( \varepsilon_F \) is the Fermi energy. It should be pointed out that the Curie-like behaviour of \( \chi \) does not depend on the assumptions made in the analysis of the C.E.S.R. spectra, but the numerical comparison between the theoretical and experimental values of \( \chi/\chi_p \) as a function of \( kT/\delta \) does. The detailed analysis was done in the following way. According to the interpretation of C.E.S.R. for small silver particles [2], only particles with a diameter smaller than about 15 Å contribute to the resonance signal.

In a first approximation knowing the size distribution and the total amount of silver in the sample, an estimation can thus be made of the total volume \( V_0 \) of those crystals which are small enough to be observed by C.E.S.R. Together with the absolute value of the integrated signal, this value of \( V_0 \) is used to calculate the ratio \( \chi/\chi_p \). The average number of atoms \( N \) necessary to calculate \( \delta \) is obtained from the absolute value of \( \chi \) assuming that a small odd particle behaves like one paramagnetic center of spin 1/2. This assumption is in agreement with the measured Curie temperature dependence and the fact that for particles of diameter smaller than 15 Å the ratio \( kT/\delta \) remains smaller than 1 at all temperatures lower than 200 K.

It can easily be shown with the previously mentioned definition of \( N \) and \( \delta \), that the graph of \( \chi/\chi_p \) as a function of \( kT/\delta \) is the same irrespective of the exact shape of the size distribution, and it can thus be compared with the theoretical curve calculated for particles of the same diameter. The agreement, as can be seen in figure 3, between the theoretical and experimental curve is good. It should be noted that the agreement does not depend on the estimate of \( V_0 \) since the experimental values of \( \chi/\chi_p \) and \( kT/\delta \) are respectively proportional to \( 1/V_0 \) and \( V_0 \). The \( \delta \) value calculated as noted above is equal to 0.57 eV which corresponds to small particles of approximately 7 Å. This number is smaller than the average from the size distribution, but the discrepancy can be understood if we take into account the fact that the real size distribution may be slightly different from that reported in figure 2, which was obtained after evaporation of the benzene matrix, also it is possible that there are errors in the determination of \( V_0 \).

The primary result of this paper is the observation of a Curie-like susceptibility for small silver particles [12]. This result, together with the measurements of the even particles susceptibility obtained from the
Knight shift measurements, is a confirmation of the lifting of the degeneracy as suggested by Kubo. The transition from the Curie to the Pauli behaviour could unfortunately not be observed since when we increase the temperature above 200 K the C.E.S.R. signal disappears. The observation of such a transition would give a definite proof that the susceptibility reported in this paper is due to small silver particles. We are planning experiments in this direction as well as double resonance experiments on small particles.

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