Large-angle oscillations in heavy ion elastic and inelastic scattering
R. Da Silveira, Ch. Leclerq-Willain

To cite this version:
R. Da Silveira, Ch. Leclerq-Willain. Large-angle oscillations in heavy ion elastic and inelastic scattering. Journal de Physique Lettres, 1975, 36 (5), pp.117-119. <10.1051/jphyslet:01975003605011700>. <jpa-00231167>

HAL Id: jpa-00231167
https://hal.archives-ouvertes.fr/jpa-00231167
Submitted on 1 Jan 1975

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L’archive ouverte pluridisciplinaire HAL, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d’enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.
LARGE-ANGLE OSCILLATIONS IN HEAVY ION ELASTIC AND INELASTIC SCATTERING

R. DA SILVEIRA

Institut de Physique Nucléaire, Division de Physique Théorique (*)
91406 Orsay, France

and

Ch. LECLERQ-WILLAIN (**)

Université Libre de Bruxelles, Physique Nucléaire Théorique
1050-Bruxelles, Belgique

(Reçu le 24 janvier 1975, accepté le 4 mars 1975)

Résumé. — Le comportement oscillatoire observé aux grands angles dans les sections efficaces de diffusion élastique et inélastique d’ions lourds aux énergies supérieures à la barrière de Coulomb, est interprété comme étant dû à un effet d’interférence entre l’amplitude de diffusion dispersive arc en ciel et celle provenant de la branche négative de la fonction de déflexion classique.

Abstract. — The oscillatory behaviour observed at large angles in heavy ion elastic and inelastic scattering cross-sections at energies above the Coulomb barrier, is interpreted as an interference effect between rainbow scattering and the contribution coming from the negative branch of the classical deflection function.

In heavy ion reactions, at energies near and above the Coulomb barrier, the structure of the elastic and inelastic cross-sections, strongly depends on the scattering angle region. On one side of the grazing angle \( \theta_r \) \( (\theta < \theta_r) \) the elastic and inelastic cross-sections present an out of phase oscillatory structure whatever be the parity of the angular momentum transferred [1, 2]. This oscillatory behaviour has already been interpreted as a quantal interference effect between two classical trajectories which contribute to the elastic and inelastic cross-sections at each scattering angle [3, 4].

On the other side of \( \theta_r \) \( (\theta > \theta_r) \) the elastic and inelastic cross-sections drops rapidly to very low values. However, in a recent experiment [5] it appears that in place of this common monotonic decrease, we observe well defined in phase oscillations (see figure 1 and reference [5]).

The aim of the present letter is to show how this oscillatory behaviour can be qualitatively [6] and quantitatively explained in terms of semi-classical arguments.

The contribution of the classical deflection function \( \theta(l) \) to the semi-classical scattering amplitude starts at the \( l \) value (\( l_n \)) for which \( \theta(l) = -\infty \) [7]. For \( l < l_n \), all partial waves are completely absorbed. For \( l > l_n \), \( \theta(l) \) has the shape shown in the upper part of figure 1; one negative branch and two positive ones. The angle \( \theta_r \) is defined by \( \theta'(l) = 0 \).

As long as the incident energy remains slightly above the Coulomb barrier, the negative branch has a negligible contribution to the total scattering amplitude.

For \( \theta > \theta_r \), the contribution of the positive branches, when evaluated in the simplest approximation (the Airy approximation [8]) gives the above mentioned decreasing behaviour or rainbow effect (dotted curve, Fig. 1). When the energy increases, the contribution of the negative branch is no longer negligible, particularly for angles where the rainbow scattering cross-sections has fallen to very low values, i.e. for \( \theta \gg \theta_r \).

Taking into account the negative branch with \( l \) values denoted by \( l_n \), the semi-classical elastic cross-section is defined by [8]

\[
\frac{d\sigma}{d\Omega} = \sigma_n(\theta) + \sigma_{n'}(\theta) - 2(\sigma_1, \sigma_2)^{1/2} \cos(\delta_1 - \delta_2) \tag{1}
\]

where

\[
\sigma_n(\theta) = \frac{l_n}{k^2 \sin \theta | \theta'(l) | l_n} \tag{2}
\]

(*) Laboratoire associé au C.N.R.S.
(**) Maître de Recherches au F.N.R.S.
In the region $\theta > \theta_r$, $\sigma_r(\theta)$ decreases more rapidly than $\sigma_0(\theta)$ and the interference term in (1) produces oscillations whose amplitudes become more pronounced with increasing $\theta$. The wave length of these oscillations, obtained from (4), is $\Delta \theta = 2 \pi/(l_1 + l_2)$, i.e. almost independent of $\theta$.

Now we shall analyse the inelastic scattering cross-section. To do this, we take the semi-classical limit of the D.W.W.A. expression for the reaction amplitude (for details see reference [4] and [9]). The result we obtain is

$$
\frac{d\sigma}{d\Omega_{0-1}} \sim \sum_\mu \left| Y_{l\mu} \left( \frac{\pi}{2}, 0 \right) \right|^2 \left( \sigma_r(\theta) \right| a_r(l_r, I, \mu) \right|^2 + \\
+ \left. \sigma_0(\theta) \right| a_0(l_0, I, \mu) \right|^2 - 2(-1)^\mu (\sigma_r, \sigma_0)^{1/2} \\
\times \left. \left| a_r \right| \left| a_n \right| \cos(\delta_r - \delta_n) \right) 
$$

where $a_r(l_r, I, \mu)$ and $a_0(l_0, I, \mu)$ are the inelastic amplitudes evaluated for $l = l_r$ and $l = l_0$ respectively.

From expression (5) and its comparison with (1) we obtain two important conclusions:

i) The oscillations in the inelastic cross-section of even and odd parities, are out of phase [10].

ii) The oscillations in the inelastic cross-section should be in phase or out of phase with the elastic oscillations, according to whether the parity of the excited state is even or odd. This phase rule between the elastic and inelastic cross-section is just the inverse of the well known Blair phase rule [11] (1).

The results of a numerical calculation with expressions (1) and (5) for the elastic scattering and inelastic $2^+$ (4.43 MeV) excitation of $^{12}_C$ incident on $^{27}_Al$ at $E_L = 46.5$ MeV [5] are presented in figure 1. The classical deflection function (upper part of Fig. 1) has been calculated with a Coulomb plus Woods-Saxon nuclear potential, with the parameters $V_0 = 35$ MeV, $r_0 = 1.15$ fm and $a = 0.55$ fm. The inelastic results are obtained in absolute scale with a deformation parameter $\beta_2 = 0.3$ for the $2^+$ state in $^{12}_C$.

In spite of the crude approximation used in the description of the rainbow scattering, the essential features of the experimental results are quite well reproduced.

References


