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PHYSICAL PROPERTIES OF EuO VERSUS ELECTRONIC CONCENTRATIONS.

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Résumé.– Des monocristaux homogènes d'EuO, EuO riche en Eu, et EuO dopé au gadolinium ont été obtenus et caractérisés par des analyses : aux rayons X, avec des microsondes et par des mesures, en fonction de la température, d'effet Mossbauer, de spectroscopie infra-rouge et de résistivité. Des résultats de photoconductivité, effet Hall, mesures optiques et magnétiques sont apportés. Ils sont interprétés dans le cadre d'un modèle simple tenant compte des énergies de Coulomb, cinétique et d'échange et du degré de compensation d'un niveau donneur, ce niveau étant dû à l'existence de lacunes d'oxygène ou d'atomes de Gd.

Abstract.– Homogeneous single crystals of EuO, Eu rich EuO and Gd doped EuO have been obtained and characterized by X-ray, microprobe analysis, Mossbauer, infrared spectroscopy and resistivity measurements versus temperature. Photoconductivity, Hall effect, optical and magnetic measurements are reported. They are interpreted within a simple model taking into account Coulomb, kinetic and exchange energies and considering the degree of compensation of the donor level due to oxygen vacancies or Gd atoms.

Introduction.– Europium oxide EuO is a magnetic semiconductor which was the subject of many studies due to the following reasons. Its simple crystalline structure (NaCl) simplifies the study of magnetic interactions in this ferromagnetic compound. In addition, by departure from stoichiometry or by doping, a drastic change of the carrier concentration can be achieved resulting in noticeable variations of physical properties; then it is needed to perform the measurements of physical properties on single crystals. For example, with a moderate concentration of oxygen vacancies a Metal Insulator Transition (MIT) appears at about 50 K.1/ Numerous theoretical studies of this transition involving the concept of Bound Magnetic Polaron (BMP)2/ showed that the magnetic interactions have a strong effect on transport properties. Reciprocally, the electronic properties of the material affect the nature of the exchange interaction induced by free carriers. Optical spectra of Eu rich EuO evidence structures which also were correlated to the magnetic interactions. Because of this interdependence between various physical properties it seemed to us that it was interesting to investigate them as a whole with a restricted number of samples. The growing technics of crystals build the first section. The results of characterization measurements not only direct (X-rays, microprobe analysis) but also indirect (infrared absorption spectra, Mössbauer effect, resistivity measurements) are the subject of section 2. We report transport measurements including photoconductivity data in section 3, reflectivity measurements in section 4, and magnetization measurements in section 5. In the last section we present a simple model taking into account a) the contributions of exchange, Coulomb and kinetic energies to the binding energy of the donor state; b) the statistics of free carriers. This model accounts for the experimental properties as a whole.

Growing technics.– EuO single crystals were first obtained by Guerci and Shafer3/ from the reaction of Eu metal on Eu$_2$O$_3$ in a sealed metallic refractory crucibles, followed by a slow cooling of the melt. We have used a similar method: the crucible (Mo) is filled (Eu$_2$O$_3$: 99.99%; Eu: 99.9%) in a glove box under purified argon atmosphere and sealed by arc welding. The sample is twice melted at about 2000°C with intermediate
inversion of the crucible and then slowly cooled at a rate of 3.6°C/h to 1600°C, faster below this temperature. Using this procedure good crystals are obtained and the values of their atomic ratios Eu/O are fairly well correlated with the initial values of this ratio in the charge; thus to obtain crystals with different ratios in the range: 0.98 to 1.01, initial ratios in the charge must be taken from 0.98 to 1.04. But we have noted that if the cooling rate is increased, this relationship changes and the final ratio Eu/O becomes larger, as it can be seen in table I (samples A and 3) and in reference /4/. These results are in agreement with those of Fischer and al./5/. With the double crucible technique, Shafer and al./6/ used a larger ratio range in the initial charge (from 1 to slightly above 2). Solidification temperature values that we have determined agree with the phase diagram established by Shafer and al./6/.

The (Eu,Gd) 0 samples (numbered from 11 to 19) are grown with the procedure used for Eu_x0 crystals. The initial ratio (Eu + Gd)/O is taken equal to 1.02 (except in runs 16 and 17) since in the case of EuO this value led to stoichiometric crystals. We report in table I the Eu/O and Gd/O initial ratios and the Gd weight concentrations in crystals assuming a final ratio Eu + Gd/O of 1.

2. Characterisation.- Micrographic examination shows that the samples are monophase, except samples 1, 18, 19 in which very small amounts of inclusions are present and may be identified to Eu_0.4(1,18,19) and Gd_0.3(18, 19) by microprobe analysis.

A full spectra of crystals impurities are performed with a Ion Analyser (IMS 300 Cernexa), the concentration of all of these are too low (< 500 ppm) to be determined accurately using a MS 46 electronic microprobe analyser.

The repartition of gadolinium in the samples is checked by electron microprobe analysis, figure 1 represents the X ray picture of Gd (La) of a (200 µm)^2 area of sample 16 (2% Gd) showing a good homogeneity. The Gadolinium concentration is given by the mean value of the analyses performed in different points across the whole crystal, and the concentration gradient is given by extreme values of these measurements.

In table I are reported the gadolinium concentration and the gradient expressed as a deviation of the concentration value. Gradient values are small except for sample 15.

The departure from stoichiometry in Eu_x0 samples cannot be determined by direct analysis. In fact, using the method and the results of Shafer and al./6/ assuming the hypothesis that an europium excess appears like oxygen vacancies and europium defect like Eu^3+ appearance, we have estimated the vacancy concentration by indirect physical measurements.

Mössbauer measurements performed between 4.2 and 300 K/7/ reveal the existence of Eu^3+ ions only in the samples 1, 2, 3, among Eu_x0 samples. These samples set on the 0 rich side.

The absorption coefficient a at the wavelength λ = 2 μm measured at room temperature on 200 μm thick polished samples increases from 25 cm⁻¹ in Eu0 n°3 to more than 100 cm⁻¹ in Eu0 n°8. In the samples like 5 and 8 (Fig. 3) the presence of oxygen vacancies can be deduced from the existence of an absorption peak at 2.2μm. Moreover in samples like 8, the high value of a indicated the presence of free carriers. In the sample 3 (Fig. 3), the low value of a indicated that it is near stoichiometry.

The measurements of the resistivity variations versus temperature down to 4.2 K
reported on the figure 4 permit to estimate more accurately the vacancy concentration.

The lattice parameter of the compounds is determined on powdered samples by Debye-Scherrer method. For Eu\textsubscript{1-x}Gd\textsubscript{x}O, the measured values in the whole studied concentration remain constant and equal to $5.143 \pm 0.001$ Å, this value is in agreement with previous measurements \cite{6,8}. For (Eu,Gd)\textsubscript{0} compounds the lattice parameter decreases from 5.143 Å to 5.136 Å when the Gd concentration changes from 0 to about 2%. At these low concentrations, the variation is linear, as it can be seen on figure 2, in a fairly good agreement with Samokhvalov results up to 5 %. (9).

3. Transport properties.- For (Eu,Gd)\textsubscript{0} samples the resistivity curves versus temperature are reported in figures 4 and 5. When the concentration of Gd is small (< 1%) a semiconducting behaviour is observed between 300 K and about 200 K with an activation energy of 0.3 eV.

The activation energy $E_a$ ranging from 0.6 to 0.3 eV indicates a crossing through the stoichiometry from O rich (sample 3) to Eu rich (samples 4,5,6) with the increase of the vacancy concentration. Metal Insulator Transition appears at about 50 K with about 0.3% vacancy concentration. "Metallic" behaviour is observed in samples (7 to 10) for an increase of the concentration from 0.3 to 0.5%.

![Fig 2. Lattice parameter of Eu\textsubscript{1-x}Gd\textsubscript{x}O as a function of x.](image2)

![Fig 3. Absorption coefficient on \# 200 μm thick samples.](image3)

![Fig 4. Resistivity versus temperature on semiconducting EuO samples.](image4)
than 1% the resistivity curves have a metallic character in the whole range of temperatures (Fig 5.)

In particular the resistivity curve of (Eu,Gd)$_0$$_n$$_{12}$ is very similar to the resistivity curve of

<table>
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<th>Nos.</th>
<th>Initial comos. for I &amp; Oxygen</th>
<th>From</th>
<th>Cooling speed</th>
<th>Final comos.</th>
<th>$\rho_{4.2K}$ $\Omega$cm</th>
<th>$\rho_{300K}$ $\Omega$cm</th>
<th>$E_A$ meV</th>
<th>$T_c$ K</th>
<th>$n_{4.2K}$ cm$^{-3}$</th>
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Table I: Characteristic data of the different samples. Final composition of samples A to 10 are estimated by comparison with reference 6. Gd concentrations of samples 11 to 16 are parts by weight. $E_A$ is the activation energy of resistivity $\rho$.

Therefore, we agree with the results of Von Molnar (10) showing that the resistivity depends essentially on the concentration of dopants but is relatively insensitive to the nature of dopants. In particular, the resistivity curve of (Eu,Gd)$_0$$_n$$_{12}$ is very similar to the resistivity curve of Eu$_{1+x}$0$n$ IV-I reported by /6/ in figure 7.

The carrier concentration $n$ was deduced from Hall effect measurements when available, i.e. when the resistivity $\rho$ did
not exceed $10^5 \Omega \text{ cm}$. As an example, we report in figure 6 the temperature dependence of the mobility $\mu$ for the sample no 8, deduced from resistivity and Hall effect measurements. (Fig. 7). In effect, it is commonly assumed that the stationary photocconductivity signals is proportional to $\mu$. The relaxation time $\tau$ of photoexcited carriers is roughly constant in the range $4.2 - 150 K$. It follows that in the critical range $40 - 80 K$, $s$ is proportional to $\mu$. Figure 7 illustrates the similarity between $s$ and $\mu$ vs. temperature. An important feature is the minimum of mobility near $T_c$ which may be imputed to a scattering by spin fluctuations. The ratio between mobilities at high and low temperatures ranging from $10^{-3}$ to $10^{-1}$ is too small to account for the variations of resistivity, so that the MIT is mainly due to a variation of the carrier concentration.

![Fig 5. Resistivity versus temperature on "metallic" EuO samples.](image)

![Fig 6. Resistivity carrier concentration and mobility versus temperature on EuO no8.](image)

For more insulating samples the mobility has been estimated from measurements of the photoconductivity $s$ as a function of temperature (Fig. 7). The relaxation time $\tau$ of photoexcited carriers is roughly constant in the range $4.2 - 150 K$. It follows that in the critical range $40 - 80 K$, $s$ is proportional to $\mu$. Figure 7 illustrates the similarity between $s$ and $\mu$ vs. temperature. An important feature is the minimum of mobility near $T_c$ which may be imputed to a scattering by spin fluctuations. The ratio between mobilities at high and low temperatures ranging from $10^{-3}$ to $10^{-1}$ is too small to account for the variations of resistivity, so that the MIT is mainly due to a variation of the carrier concentration.

![Fig 7. Photosensitivity versus temperature; comparison between signals of photosensitivity and mobility versus temperature near $T_c$. (m: for middle of crucible and b: for bottom).](image)

4. Optical properties.- Torrance et al. first observed two absorption peaks at room temperature, located at 1.85 $\mu m$ and 2.20 $\mu m$, in Eu rich samples. They imputed these transitions to a spin flip of the outer electron of the oxygen vacancy. These peaks were also observed even in the metallic configuration by Helten et al. who challenged this
interpretation since this electron is no longer bound.

To argue this debate, we have performed reflectivity measurements as a function of temperature on the sample No 5. Two dips in the reflectivity spectra at 1.85 \( \mu m \) and 2.2 \( \mu m \) are observed at all temperatures between 4.2 and 300 K (Fig. 8). At 4.2K two other dips are observed at 1.74 \( \mu m \) and 2 \( \mu m \). The location of the 4 dips is not sensitive to the magnetic field up to 30 kG. These results are in good agreement with those obtained on absorption spectra in ref /16/.

![Reflectivity versus wavelength at different temperatures and at different magnetic fields at 4.2 K.](image)

Fig. 8 Reflectivity versus wavelength at different temperatures and at different magnetic fields at 4.2 K.

5. Magnetic measurements.- To investigate the correlation between magnetic and transport properties, we have measured the magnetization of various samples with a vibrating sample magnetometer.

For samples n°5 to 12 the Brillouin law is satisfied with a Curie temperature \( T_C \approx 70 \) K. A tail in the magnetization curve of sample n°13 in the vicinity of 70 K can be assigned to the existence of a small Gd gradient in the sample, due to the fact that in this sample the carrier concentration is near the critical concentration for indirect exchange (see in the discussion). The Curie temperature sharply increases to \( \approx 140 \) K in EuO n°14 with a slightly increased electron concentration, and reaches \( \approx 140 \) K in EuO n°15.

6. Discussion.- The short range superexchange interactions are responsible for the ferromagnetic ordering at \( T_C \approx 70 \) K in insulating EuO.

The introduction of free carriers adds an indirect exchange interaction coupling the spins of the electron and Eu atoms according to the law:

\[
-J_{df} \hat{s}(R_n) \hat{s}(r-R_n)
\]

where \( J_{df} \) is the atomic exchange constant, \( \hat{s}(R_n) \) the spin of the Eu atom on site \( R_n \) and \( \hat{s} \) the spin of the electron. To the second order, in the molecular field approximation, this Hamiltonian leads to the following expression characteristic of the RKKY interaction:

\[
H_{ex} = \sum_{ij} J_{eff}^{(R)} \hat{s}(R_i) \hat{s}(R_j)
\]

\[
J_{eff}^{(R)} = \left( \frac{J_{df}}{2N} \right) \sum_k \Delta E_k (n_k^+ + n_k^-) E^2(\vec{k}) \exp \left( i \vec{q}. \left( \vec{R}_i - \vec{R}_j \right) \right)
\]

where \( n_k^+ \) and \( n_k^- \) are occupation numbers. Further calculations, however, depart from the usual models since they must take into account specific properties of the material arising from the fact that the electron concentration is much smaller than in metals. In particular, the spin splitting of the conduction band, \( J_{df} \hat{s} \), is larger than the Fermi energy at low enough temperatures, so that the Fermi level crosses the bottom of the spin down conduction sub-band at a defined temperature below \( T_C \). This implies a change of the carrier statistics, and then, of the indirect exchange interaction \( J(R_i) \) as given by eq. 2. This effect is responsible for the departure of the magnetization curves from the usual Brillouin law evidenced on thin films /17/ and in ref /18/.

The increase of \( T_C \) as a function of n up...
to 143 K for n = 5 x 10^{20} \text{ cm}^{-3} is in good agreement with the results of the calculations from eq. 2 /18/. For low concentrations (n < 10^{20} \text{ cm}^{-3}) the indirect exchange interaction favours the localization of the free carriers around charge centers to build Bound Magnetic Polarons BMP beyond \# 50 K, owing to the dependence of J(R_{ij}) on temperature and on the Eu spin polarization \( \sigma \). At high temperature, the ionization energy of the BMP is then essentially magnetic in nature, and is then roughly equal to \( J_{df}S/2 \# 0.35 \text{ eV} /18/.

Another typical property of such materials is the shift of the absorption edge with temperature. This effect was first observed by Busch and al. /19/ and experimentally studied by Freiser and al. /20/ for undoped samples. This effect can be imputed to a shift of the bottom of the conduction band due to the exchange interaction /21,22/. For such undoped samples, at \( T = 0 \), the photon energy at the absorption edge is given by:
\[
\hbar \omega = E_y - \frac{1}{2} J_{df} s
\]  
(3)

Such is not the case for Gd doped EuO, as it has been noticed by Schoenes and Wachter /23/, who concluded that the increase of \( \hbar \omega_0 \) with the Gd concentration at \( T = 0 \) was an evidence for a lowering of magnetic interactions. We do not agree, however, with this interpretation, and impute these phenomena to a Burstein effect /24/. More exactly, the photon energy at the absorption edge at \( T = 0 \) in these samples is
\[
\hbar \omega = \hbar \omega_0 + E_F - \Delta E
\]  
(4)

\( E_F \) is the Fermi energy, and accounts for the filling up of the conduction band, when a high concentration of \( \text{Gd}^{3+} \) ions are introduced in the EuO matrix. This doping is also responsible for a deformation energy \( \Delta E \) which, in first approximation, is given by:
\[
\Delta E = \frac{1}{2} B J^2 + \Sigma n J
\]  
(5)

\( B \) is the bulk modulus, \( \Sigma \) the deformation potential, \( n \) the concentration of \( \text{Gd}^{3+} \) ions and \( J \) the elastic deformation which we have assumed to be uniform for simplicity. Minimizing \( \Delta E \) with respect to \( J \), we have:
\[
\hbar (\omega - \omega_0) = E_F - \frac{\Sigma n}{B}
\]  
(6)

Due to the lack of any experimental data relative to the effect of the introduction of Gd on \( B \) and \( \Sigma \), we have taken for these parameters their value measured in undoped EuO /25/, i.e., \( B = 1.1 \times 10^{12} \text{ ergs, } \Sigma = 4.8 \text{ eV} \). This approximation, however, is not expected to be drastic for the present purpose, since \( \Delta E \) is found to be a corrective term in eq. 4 where \( \Delta E \ll E_F \). When the empirical dispersion law of the electrons in EuO given in ref. /26/is chosen to calculate \( E_F \), we obtain for the blue-shift of the absorption edge with Gd doping at \( T = 0 \); \( \hbar (\omega - \omega_0) = 102 \text{ meV for } n = 6 \times 10^{20} \text{ cm}^{-3} \) and 45 meV for \( n = 1.6 \times 10^{20} \text{ cm}^{-3} \). This is in fairly good agreement (within 5 meV) with respect to experimental values of ref. /23/ at \( T = 0 \). We did not attempt to interpret the temperature dependence of the absorption edge, because the strong distortion of the absorption spectra with temperature makes its choice rather arbitrary. We can conclude that both magnetic properties; (such as the deviations of the magnetization from the Brillouin law), and the optical properties, (such as the location of the absorption edge at low temperatures for heavily doped EuO), can be quantitatively explained by our model without referring to any disorder effect.

The spin flip energy of the electron in the BMP is twice as large i.e. 0.6 \text{ eV}, which corresponds to the energy location of the two structures in the optical spectra. That is why some authors /15/ assigned these peaks to a spin resonance of the outer electron of BMP, which reverses its spin with respect to the aligned Eu spins inside the polaron. Due to the existence of these structures at low temperature, when the electron is de-localised, Helten et al /16/ suggested that they might involve a \( F^+ \) center, and not the outer electron of the oxygen vacancy. Nevertheless, the calculation of the Fermi energy and of \( J(R_{ij}) \) according to eq. 2 shows that in the metallic configuration, all the conduction electrons are polarized in the spin up subband split from the spin down subband by an energy which is also about \( J_{df}S \) according to eq. 1. This suggests that the optical transitions may be considered as an
exchange resonance of the outer electron of the vacancy, with respect to the Eu spins inside the polaron in the insulating configuration, and with respect to the Eu spins of the whole crystal in the ferromagnetic and metallic configurations. This interpretation has the advantage of giving an overall understanding of magnetic and optical properties, and does not refer to the existence of a F center which should imply non forbidden optical transitions with stronger intensities.

To study the variation of $n$ induced by the existence of the donor level, we have calculated the carrier statistics from the equation of neutrality:

$$n_d^- + p = n_A^+ + n$$

(7)

where $n_d^-$ is the density of ionized donor states, $p$ is the density of holes in the 4f level, $n_A^+$ is the density of ionized acceptor states and $n$ the density of conduction electron. The results of the calculations depend on the concentration of donor atoms and on their ionization energy $E_d^-$ which we suppose equal to

$$E_d^-=E_{\text{kin}}^+ + E_{\text{Cou}} + 1/2 J_{df} S (1-c)$$

(8)

at all temperatures. The three terms are respectively kinetic, Coulomb and exchange energies. The sum of the two first terms is roughly equal to 17 meV for $T<T_C$ when the donor concentration $N_D$ is smaller than the Mott concentration. At $T=0$, we take into account correlations between donor states according to a law:

$$E_d^-=E_{d,0}^+(1-c N_A^{1/3})$$

(9)

as in the case of non magnetic semiconductors. For $T>T_C$, the radius of the bound orbital is determined by exchange interactions which shrink the orbital; $E_{\text{kin}}^+ + E_{\text{Cou}}$ becomes negative and $E_d^-$ is then smaller than $J_{df} S/2$; $E_d^-$ # 300 meV. Like different authors, we admit the existence of a compensating acceptor level with a concentration $N_A=5 \times 10^{17} \text{cm}^{-3}$ and an ionization energy equal to half of the energy gap. In fact, the energy location of the acceptor level does not change the values of $n$, because it is far below the bottom of the conduction band. The 4f level is considered as a discrete level due to its small width. To calculate the resistivity we have chosen for the mobility a value equal to $100 \text{ cm}^2/\text{V.s}$ at $T<T_C$ and to $1 \text{ cm}^2/\text{V.s}$ at $T>T_C$, which are typical experimental values (figure 6 and ref. /29/). A diagram of the different levels used in the model is drawn in figure 9. A good agreement between experimental and calculated resistivity curves is observed in the whole range 4.2 - 300 K for samples which are not metallic at $T>T_C$, results are plotted in figure 10 for a few of our samples and for 2 samples of ref. /6/.

![Fig 9. Diagram illustrating the model.](image)

In particular, the activation energy $E_a$ at room temperature $\rho(T) \propto \exp \left( \frac{E_a}{kT} \right)$ continuously varies from 300 meV to 300 meV when the degree of compensation $N_A/N_D$ changes from 0.99 to 1.01. This effect is due to the contribution of 4f states in the carrier statistics although the gap # 1.1 eV is large because the density of 4f states is very large. In this simple model, the behaviour of the resistivity of the sample with a vanishing activation energy in the paramagnetic configuration cannot be understood. Nevertheless, an enlargement of this model /30/ taking into account the magnetic entropy connected with a BMP shows that only few BMP are delocalized at $T>T_C$, whereas all the electrons are delocalized at $T<T_C$ when the concentration $N_D$ exceeds the critical concentration of the metal.
insulator transition. This result is in good agreement with the fact that the electron concentration measured at $T < T_C$ is lower than when measured at $T > T_C$ on such samples /29/. This also explains the existence of structures in optical spectra at 1.85 and 2.20 $\mu m$ on an Eu rich EuO sample with a vanishing activation energy at room temperature in ref /16/.

Finally, we can also understand the existence of four structures of low temperature /31/. Due to the fact that the 5d bands build six $t_{2g}$ subbands and with the results of Schoenes and Nolting /32/ (in EuS) showing a crossing of spectral weights at $T < 30 K$, we can expect that extra optical transitions between spin up and spin down subbands appear. The disappearance of the extra structure at 5750 cm$^{-1}$ near 35 K observed by Helten and al. is an argument for this model.

![Diagram](image)

Fig. 10 Experimental and calculated resistivities versus temperature. Samples IV - 1 and IV - 5 are from Ref. 6.

References

7/ Fatseas, G., Thesis Paris VI, mars 1973
/24/ Burstein, E., Phys. Rev. 93 (1954) 632
/25/ Jayaraman, A., Sink, A.K., Chatterjee,
2513.
/26/ Mauger, A., Phys. Status. Solidi 84 b,
(1977) 361.
5195.
/28/ Penney, T., Shafer, M.W., Torrance, J.B.,
and ref /10/
/29/ Shapira, Y., Foner, S., Reed, T.B., Phys.
Rev. B8 (1973) 2299.
/30/ Mauger, A., Godart, C., To be published.
/31/ Godart, C., Mauger, A., Escorne, M., Achard,
J.C., XIV th Proceedings of the Rare Earth
Research Conference, North Dakota, U.S.A.,
June 1979
49 (1978) 1466.