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Spin glasses in amorphous and crystalline RE alloys

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Résumé. --- Nous présentons un sommaire des principaux résultats expérimentaux obtenus sur les verres de spin dans les systèmes cristallins et amorphes contenant des terres rares. Nous nous intéressons plus spécialement aux propriétés magnétiques moyennes dans les verres de spin métalliques contenant du gadolinium. Les effets du Gd dans la limite diluée (x < 1 at. %) sont comparés avec ceux mesurés dans les systèmes avec des impuretés 3d. Le cas des alliages amorphes est discuté. Enfin, nous décrivons en termes d’amas magnétiques les propriétés des verres de spin concentrés (1 < x < 32 at. %) dans le système amorphe La$_{90-x}$Gd$_x$Au$_{20}$.

Abstract. --- Recent experimental results on spin glasses in crystalline and amorphous RE systems are reviewed. Main emphasis of this paper will be on the bulk magnetic properties of metallic spin glasses containing Gd. The effects of Gd in the dilute limit (x < 1 at. %) are compared with those observed in 3d impurity systems. The case of amorphous alloys is discussed. Finally, we present a cluster description of magnetic properties in concentrated (1 < x < 32 at. %) amorphous La$_{90-x}$Gd$_x$Au$_{20}$ spin glasses.

1. Introduction. --- Regardless of the (short- or long-range) forces which are responsible for the spin-glass phenomena [1], both dilute (~ 1 at. %, typically) and concentrated spin glasses are phenomenologically characterized by an ordering temperature below which short-range magnetic order [2] and field cooling effects are observed [3-4]. This ordering or freezing temperature $T_M$ is usually defined by a sharp cusp in zero-field ac susceptibility [5]. Considerable effort has developed among theoreticians to explain this cusp in terms of a phase transition [6-7]. Meanwhile, experimentalists have accumulated evidences for the complex nature of the spin-glass ordering process: namely, both the shape and the position of $T_M$ depend on the strength of a dc applied field and on the frequency of an ac field [8-11]. Moreover, specific heat measurements exhibit no singularity at $T_M$; instead, a broad maximum occurs at a temperature $T$ which varies as a function of applied field [12]. In addition, recent neutron scattering experiments were interpreted as indicating a non-unique freezing temperature depending on the momentum of incident neutrons [13]. Finally, the remanence below $T_M$ is time dependent [4]. All these findings do not favor the phase transition picture for the spin-glass freezing. In contrast, they can be interpreted rather easily within a phenomenological model of superparamagnetic clouds [3-4] inspired from Néel’s studies on fine grains [14]. Such an approach is very appealing for an experimentalist by providing him with a tool for a quantitative analysis of his data. In particular, the scaling behaviour observed in the dilute limit for $T_M$ and for its frequency dependence [9], for the magnetization [15-16] above $T_M$ and for the remanence [3] below $T_M$ allows the experimentalist to decide which forces are responsible (1/$r^3$ interactions). Nevertheless, such a model fails to account for the sharpness of the susceptibility cusp at zero field and low frequency.

In this paper, we review the various manifestations of spin glasses in different systems containing RE. Data on the field-frequency dependence of the freezing temperature or on the relaxation effects in remanence are too scarce yet to be useful for our purpose. In contrast, detailed studies are available concerning the concentration dependence of such quantities as the freezing temperature, the high field magnetization and the remanence in crystalline and amorphous alloys containing Gd for both dilute and concentrated cases. When analyzing these data, we will assume that $T_M$ or remanence were measured over the same reasonable time scale, so that any concentration dependence study in a given system or any comparison between different spin glasses can still be meaningful.

2. Various spin-glass phenomena in different RE systems. --- In table I are listed the different (pseudo) binary alloys containing RE for which some spin-glass properties have been reported. A large number of these alloys and Laves phase compounds were studied within the context of search for coexistence of superconductivity and magnetism. Deviations to the Abrikosov-Gorkov curve, anomalies in the upper critical field and in the specific heat, were attributed to a short-range magnetic order which is now believed to be of spin-glass type. These properties together with...
Table I. — Spin-glass phenomena in RE systems.

<table>
<thead>
<tr>
<th>Matrixes</th>
<th>Impurities</th>
<th>Spin-glass phenomena</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Alloys</td>
<td>Sc, Gd, Ho, Er, Dy</td>
<td>$T_M$ (<em>) [18], $C_v$ (</em>) [19], ME (<em>) [20], N (</em>) [20]</td>
</tr>
<tr>
<td>Y</td>
<td>Gd, Tb, Dy</td>
<td>$T_M$ [18, 21], $C_v$ [19, 22]</td>
</tr>
<tr>
<td>La</td>
<td>Gd, Eu</td>
<td>$sc$ (*) [23], TM [23], $C_v$ [23], ME [24]</td>
</tr>
<tr>
<td>Pr</td>
<td>Nd, Tb</td>
<td>$T_M$ [18]</td>
</tr>
<tr>
<td>La$_{99}$Lu$_2$</td>
<td>Tb</td>
<td>$sc$, $T_M$ [25]</td>
</tr>
<tr>
<td>Th</td>
<td>Er</td>
<td>$sc$, $T_M$ [26]</td>
</tr>
<tr>
<td>2. Compounds</td>
<td>Y$_3$Os$_2$</td>
<td>Gd</td>
</tr>
<tr>
<td>La$_2$Al</td>
<td>Gd, Ce</td>
<td>$sc$ [28], $T_M$ [9, 29-31], $C_v$ [12, 32-33], ESR [34],RMN [35]</td>
</tr>
<tr>
<td>La$_2$In</td>
<td>Gd, Ce</td>
<td>$T_M$, $M_{rm}$ (*) [36, 37]</td>
</tr>
<tr>
<td>La$_2$Ru$_2$</td>
<td>Gd, Ce, Pr</td>
<td>$sc$, $T_M$ [38]</td>
</tr>
<tr>
<td>La$_3$Sn$_3$</td>
<td>Gd, Tb</td>
<td>$sc$, $T_M$ [39, 40]</td>
</tr>
<tr>
<td>CeRu$_2$</td>
<td>Pr, Gd, Tb, Dy, Ho</td>
<td>$sc$, $T_M$ [41, 42]</td>
</tr>
<tr>
<td>ThRu$_2$</td>
<td>Gd</td>
<td>$sc$, $T_M$ [43], N [44]</td>
</tr>
<tr>
<td>SnMo$_6$S$_8$</td>
<td>Eu</td>
<td>$sc$, $T_M$ [45], $C_v$ [46], ME [47-48], $T_M$ [49], N [50]</td>
</tr>
<tr>
<td>Bi$_2$Sr</td>
<td>Eu</td>
<td>$sc$, $T_M$, $C_v$ [51]</td>
</tr>
<tr>
<td>3. Amorphous</td>
<td>Cu</td>
<td>Gd, Dy</td>
</tr>
<tr>
<td>Al</td>
<td>Gd</td>
<td>$T_M$ [53]</td>
</tr>
<tr>
<td>CuZr</td>
<td>Gd, Tb</td>
<td>[56]</td>
</tr>
<tr>
<td>La$<em>{80}$Au$</em>{20}$</td>
<td>Gd</td>
<td>$sc$ [58], $T_M$ [59-60], $M_{rm}$ [61]</td>
</tr>
<tr>
<td>4. Insulators</td>
<td>SrS</td>
<td>Eu</td>
</tr>
</tbody>
</table>

(*) $T_M$ = zero-field susceptibility; $C_v$ = specific heat; ME = Mössbauer effect; N = neutron diffraction; $sc$ = superconducting properties; $M_{rm}$ = saturated remanence.

the results of Mössbauer spectroscopy and neutron diffraction studies in these superconducting spin glasses have been recently reviewed [17].

As can be seen from table I, there exists a large variety of spin glasses containing RE. We should add to the list the spin-glass-like regimes obtained at low temperature in some compounds like GdCo$_2$ after H$_2$ absorption [63]. On the other hand, Chevrel phases like Re$_2$Mo$_6$S$_8$ could be good candidates for a new class of spin glasses [64]. Not included in the list are concentrated amorphous alloys such as REAg [65], where, despite of large hysteresis loops and strong after effects, there exists a long-range magnetic order. This kind of amorphous RE alloys was reviewed recently by Coey [66] and Cochrane et al. [67].

It would be of interest to compare the magnetic properties of Gd spin glasses with those of spin glasses containing other RE elements. Recent calculations [68] investigated the possibility for a local uniaxial anisotropy to induce a spin-glass-like behaviour. Unfortunately, experimental results available so far do not allow to determine unambiguously the effects of the magnetic interactions and those due to crystal field effects. For example, the ac susceptibility maximum is broad in ScTb alloys and it becomes sharper when a dc field is applied. This behaviour, opposite to that observed in ScGd, was attributed to the single ion anisotropy [18]. But this effect does not seem to be the general case, since a sharp cusp was observed in a Y$_{99}$Tb$_2$ alloy [22]. On the other hand, the critical concentration for the onset of long-range magnetic order for Tb in Y is twice that for Gd in Y (5 and 2.6 at. %, respectively) [18]. In contrast, the critical concentration is about the same for Tb and Gd in a Sc matrix (22 and 24 at. %, respectively) [18]. More detailed investigations are needed on non-S state spin-glass systems before one can make a meaningful comparison with the simple case of spin-glasses containing Gd.

3. Crystalline and amorphous Gd spin glasses in the dilute limit. — 3.1 Crystalline Gd and 3d spin glasses. — Influence of RKKY interactions. Are listed in table II the experimental values for $T_M$/x, $V_o$ and $S$ obtained in the dilute limit ($\sim 1$ at. %) for some typical Gd and 3d spin-glasses. The strength of the RKKY interaction $V_o$ was determined from approach to saturation [77]. From table II, it appears at first sight that $T_M$/x scales roughly with $V_o$. This correlation between $T_M$/x and $V_o$ can be expressed in a very naive way as follows. Our starting point is...
Table II. — Values of spin-glass parameters in 4f and 3d systems.

<table>
<thead>
<tr>
<th>Alloy</th>
<th>( T_M/x ) (K/at. %)</th>
<th>( V_0 ) (10⁻³⁷ erg cm⁻³)</th>
<th>( S )</th>
</tr>
</thead>
<tbody>
<tr>
<td>ScGd</td>
<td>0.55 [18]</td>
<td></td>
<td></td>
</tr>
<tr>
<td>YGd</td>
<td>2.30 [18]</td>
<td></td>
<td></td>
</tr>
<tr>
<td>LaGd</td>
<td>0.55 [23]</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( La_{3-x}Gd_x)In</td>
<td>0.60 [39]</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Ce₁₋₃Gd₂Ru₂</td>
<td>0.70 [48]</td>
<td></td>
<td></td>
</tr>
<tr>
<td>( La_{1-x}Gd_Al_x)₂</td>
<td>0.26 [30]</td>
<td>0.24 [30]</td>
<td>3.5 [30]</td>
</tr>
<tr>
<td>( La_{1-x}Gd_B_x)₂</td>
<td>0.09 [36]</td>
<td>0.24 [36]</td>
<td>3.5 [36]</td>
</tr>
<tr>
<td>( La_{80-x}Gd_x)Au_x₀</td>
<td>0.50 [59]</td>
<td>0.3 [60, 69]</td>
<td>3.5 [60, 69]</td>
</tr>
<tr>
<td>AuFe</td>
<td>12 [4]</td>
<td>11 [70]</td>
<td>1.5 [70]</td>
</tr>
<tr>
<td>MoFe</td>
<td>0.55 [71]</td>
<td>2.4-3.8 [72-73]</td>
<td>0.9-1.2 [72-73]</td>
</tr>
<tr>
<td>CuMn</td>
<td>17 [4]</td>
<td>7.5 [74]</td>
<td>2 [74]</td>
</tr>
<tr>
<td>AgMn</td>
<td>(*) (4.5) [75]</td>
<td>3.5 [74]</td>
<td>2 [74]</td>
</tr>
<tr>
<td>AuMn</td>
<td>(*) (5) [75]</td>
<td>2.4 [74]</td>
<td>2.2 [74]</td>
</tr>
<tr>
<td>ZrMn</td>
<td>4.0 [76]</td>
<td>2.7 [76]</td>
<td>2 [76]</td>
</tr>
</tbody>
</table>

(*) Values given for \( T_M/x \) in AgMn and AuMn alloys are only an estimate. The dilute limit for which \( T_M \) should scale with \( x \) has not been reached [75].

the simple derivation given by Sherrington [78] for the order parameter of the Edwards-Anderson model [79]. Sherrington obtains for \( T_M \) an expression which is in fairly good agreement with those deduced from more rigorous treatments [80-81]:

\[
T_M = S(S + 1)/(3 \sqrt{3})k_B^{-1} \left( \sum_{j} J_{ij}^2 \right)^{1/2} \tag{1}
\]

where the average \( \left( \sum_{j} J_{ij}^2 \right)^{1/2} \) is related to the half-width of the molecular field distribution \( \Delta \) by

\[
\Delta = S \left( \sum_{j} J_{ij}^2 \right)^{1/2} \tag{2}
\]

In metallic systems with infinite mean-free-path, the \( J_{ij} \)'s can be expressed by the RKKY function in its asymptotic form. By following the molecular field approach of Souletie [82] inspired from Klein and Brout [83], we can calculate \( \Delta \):

\[
\Delta = 11.85 Q x SV_0 d^{-3} \tag{2}
\]

where \( d \) is the lattice constant of a cubic cell, and \( Q \) equals to 1/4, 1/2 and 1 for the s.c., b.c.c. and f.c.c. structures, respectively. Substituting (2) in (1) yields an explicit expression for the freezing temperature:

\[
T_M = 2.28 Q k_B^{-1} xS(S + 1) V_0 d^{-3} \tag{3}
\]

This expression derived for an Heisenberg model should be multiplied by \( \sqrt{3} \) for an Ising model [78].

The validity of equation (3) is checked on figure 1 by plotting the experimental values for \( T_M/x \) normalized as \( (k_B T_M d^3)/xQ S(S + 1) \) versus strength \( V_0 \) of the RKKY interaction. Theoretical predictions from equation (3) are indicated for an Heisenberg model (full line) and an Ising model (dotted line).

Heisenberg model than to an Ising model might be fortuitous, considering the very crude character of our derivation.

3.2 AMORPHOUS AND CRYSTALLINE Gd SPIN-GLASSES. — It can be seen in table II that the values for \( V_0 \) as determined from approach to saturation are practically identical in amorphous and crystalline Gd spin glasses. In addition, the values for \( T_M/x \) are rather close once the Gd concentration is taken with respect to the whole matrix. From \( V_0 \), we can deduce a value for \( J_s \) which is in good agreement with that obtained from the depression of the superconducting transition in the dilute limit [58]. Such an agreement asserts that the 1/1H contribution in approach to saturation is mainly RKKY in nature. On the
other hand, the initial susceptibility and the magnetization [60] for dilute (x < 1 at. %) amorphous La_{80-x}Gd_{x}Au_{20} were found to follow the Souletie-Tournier scaling laws [16]. This indicates that the RKKY interaction remains basically in its 1/r^3 asymptotic form within this amorphous matrix. A 1/r^2 dipolar interaction is not likely to be predominant for the aforementioned reasons.

This result is rather unexpected. From resistivity measurements, the electronic mean-free-path does not exceed 10 Å in an amorphous alloy. Thus, according to the exponential damping factor of de Gennes [84] and others [85], one should expect a severe modification of the magnetic superconducting properties in an amorphous medium. Our result seems contradicting previous experimental work on the mean-free-path effects in dilute crystalline spin glasses [82, 86-88]. This problem deserves further experimental and theoretical investigations.

4. From dilute to concentrated spin glasses in amorphous La_{80-x}Gd_{x}Au_{20} alloys. — When the Gd concentration exceeds 1 at. % in amorphous La_{80-x}Gd_{x}Au_{20} alloys, the reduced magnetization M/x does not scale anymore with the reduced parameters H/x and T/x. On the other hand, T_M still varies linearly with x up to x = 12, and the departure from linearity is rather small up to x ≈ 30 [59]. Moreover, the reduced saturated remanence M_{r,s}/x was found to scale fairly well with T/x for Gd concentrations as large as 32 at. % [61]. We tried to resolve this apparent contradiction within a model of small interacting clusters [69] which may shed some light on the mechanisms involved in the freezing process of concentrated spin-glasses.

We assume that for concentrations above 1 at. % some ferromagnetic clusters are built up whose spin is S* and concentration x*. These ferromagnetic clusters do not overlap, so that x*S* = xS. The Blandin-Souletie-Tournier scaling argument [15-16] can be extended to magnetic clusters with x*S* as a new invariance, R_{av} being the average distance between clusters. Thus, the scaling law for magnetization modified for clusters reads:

\[ M/x = f(H/x^*, T/x) \]  

A nice scaling behaviour of this type was found in amorphous La_{80-x}Gd_{x}Au_{20} by determining x* graphically for each value of x up to x = 32 at. % (figure 2). Above 32 at. %, the scaling behaviour cannot be recovered any more by simple adjustment of one reduced parameter (figure 2b). This indicates that our simple model fails to describe the magnetization as the clusters start to overlap. Knowing x* allows us to determine the cluster size from S*/S = x/x*. This size can be correlated with the mean environment of a Gd atom in our amorphous matrix. From linear extrapolation of structural studies [89], the Gd-Gd coordination number CN is x/10, so that CN is 8 in Gd_{80}Au_{20}. It can be seen on figure 3 that up to x = 24 at. %, the cluster size S*/S is fairly well determined by a given Gd atom surrounded by its Gd first neighbours, i.e. Z = 1 + (x/10). Above 24 at. %, S*/S is considerably larger than Z, which manifests the emergence of cluster percolation.

The strength V_0* of the effective intercluster interaction can be determined from the Larkin-Khmel'nikit'skii method modified for clusters. V_0* was found to vary in such a way that V_0* S* = V_0 S (figure 3). We believe that this interaction is mainly of the RKKY type, since for x < 32, the ratio M_{r,0}/M_{r,0}(0) is equal to about 5 × 10^{-2}, which provides a measure of the amplitude of the RKKY exchange over the dipolar coupling [4].

Back to the concentration dependence of T_M, our model can explain that T_M remains linear with x in concentrated spin glasses, since equation (3) remains unchanged as long as the relations x*S* = xS and (S* + 1) V_0* ≃ (3 + 1) V_0 are satisfied. Similarly, it can be shown that the scaling behaviour for the remanence is observed provided that T_M versus x does not depart too strongly from linearity.

According to this analysis, the freezing temperature of metallic spin glasses would be determined mainly.

Fig. 2. — Reduced magnetization M/x of La_{80-x}Gd_{x}Au_{20} amorphous alloys as a function of reduced magnetic field for clusters H/x* at different reduced temperatures (a) for 0.5 ≤ x ≤ 6.4 alloys, (b) for 6.4 ≤ x ≤ 32 alloys.
by the strength of the RKKY interaction between isolated spins within the dilute limit. and between small clusters ($S^*/S = 3.75$ for $x = 24$) in concentrated spin-glasses. These clusters behave at high field like single spin entities of concentration $x^* = x/Z$, having a spin $S^* = SQ$; they are coupled by a $1/r^3$ interaction mainly of RKKY type with an amplitude $V_0^* = V/Z$. Let us note that, as in the Soukoulis and Levin model [90], an average size cluster has been used instead of a distribution of cluster size [4]. On the other hand, our small ferromagnetic clusters resemble the superspins in the Monte Carlo simulations of Binder [7]. The remanence phenomena would imply a more complex picture of larger clouds made of 40-50 spins or superspins for our alloys, the size of these clouds being governed by an interplay of RKKY and dipolar interactions between spins or small clusters [4].

5. Conclusion. — Due to highly localized 4f electrons, large Gd moment, negligible crystal-field effects, it appears that the alloys containing Gd provide a simple case to illustrate the importance of the RKKY exchange on spin-glass phenomena and to analyze the magnetic properties of concentrated spin glasses. Much could be learned also from detailed concentration dependence investigations on metallic and insulating spin glasses containing RE elements in a non-$S$ ionic state. This latter area remains almost unexplored.

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