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Excited-state dynamics of the Tm^{3+} ions and $\text{Tm}^{3+} \rightarrow \text{Ho}^{3+}$ energy transfers in LiYF_4

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Résumé. — La dynamique des états excités de LiYF_4 faiblement dopé en ions Tm^{3+} est tout d'abord analysée. Les processus de fluorescence Stokes sont interprétés en tenant compte des nombreuses coïncidences entre les fluorescences émises par les ions Tm^{3+} et en considérant deux types de sites. Plus compliquée, la dynamique de fluorescence anti-Stokes est décrite seulement très brièvement. Les transferts d'énergie $\text{Tm}^{3+} \rightleftharpoons \text{Ho}^{3+}$ sont ensuite étudiés dans des systèmes codopés. Des transferts ${}^3\text{F}_4 \rightarrow {}^5\text{I}_7$ très efficaces à température ambiante sont rapportés alors que le transfert retour ${}^5\text{I}_7 \rightarrow {}^3\text{F}_4$ disparaît complètement aux basses températures ($T < 200$ K). Lorsque les ions Tm^{3+} sont excités dans leur niveau ${}^3\text{H}_4$, on montre que trois voies de désexcitation sont possibles : une désexcitation à l'intérieur d'un même centre Tm^{3+} , une relaxation croisée entre ions Tm^{3+} adjacents du type ${}^3\text{H}_4, {}^3\text{H}_6 \rightarrow {}^3\text{F}_4, {}^3\text{F}_4$ et un transfert direct $\text{Tm}^{3+} \rightarrow \text{Ho}^{3+}$. Le premier mécanisme est très faible et les deux autres sont en compétition, le dernier dominant largement à haute concentration en ions Ho^{3+} .

Abstract. — The excited-state dynamics of the Tm^{3+} ions in a singly doped crystal of LiYF_4 is analysed. The Stokes fluorescence processes are interpreted by taking into account the numerous coincidences between the fluorescences emitted by the Tm^{3+} ions and by considering two kinds of sites. The anti-Stokes fluorescence dynamics which are more complicated are only briefly described. The $\text{Tm}^{3+} \rightarrow \text{Ho}^{3+}$ energy transfers are then analysed in codoped systems. Very efficient ${}^3\text{F}_4 \rightarrow {}^5\text{I}_7$ energy transfers are reported at room temperature whereas the ${}^5\text{I}_7 \rightarrow {}^3\text{F}_4$ back-transfer is completely quenched at low temperatures ($T < 200$ K). When the Tm^{3+} ions are excited in their ${}^3\text{H}_4$ level, it is shown that three channels of de-excitation have to be considered : a Tm^{3+} intra-center de-excitation, a cross-relaxation process between adjacent Tm^{3+} ions of type ${}^3\text{H}_4, {}^3\text{H}_6 \rightarrow {}^3\text{F}_4, {}^3\text{F}_4$ and a direct $\text{Tm}^{3+} \rightarrow \text{Ho}^{3+}$ energy transfer. The former mechanism is very weak while the other two compete, the latter being largely dominant at high Ho^{3+} concentrations.

1. Introduction.

The $2\text{ }\mu\text{m}$ infra-red laser emission of Ho^{3+} activator ions imbedded in single crystals is usually sensitized by Er^{3+} and (or) Tm^{3+} ions. This is the case of the triply doped laser system $\alpha\beta\text{LiYF}_4 : \text{Ho}^{3+}$ in which both the Er^{3+} and the Tm^{3+} ions are sensitizers [1] ; it also

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applies to the codoped system $\text{LiYF}_4 : \text{Tm}^{3+}, \text{Ho}^{3+}$. The first one operates by pumping the material with C.W. or pulsed broad-band lamp sources [2]. The codoped system is proposed as a mid infrared diode-pumped solid state laser [3] because recent progress in this field makes the latter scheme an attractive alternative to lamp-pumped operation and also because a very good spectral match exists between the Ga Al As diode emission and the Tm^{3+} absorption near 795 nm.

In a previous study, we have already considered the sensitization of the $2\text{ }\mu\text{m}$ Ho^{3+} emission by the Er^{3+} ions, in LiYF_4 single crystals [4] and in fluoride glasses [5], and have described the $\text{Er}^{3+} \rightarrow \text{Ho}^{3+}$ energy transfers by using rate equations. The Er^{3+} ions were excited in the visible and the infrared domains and we measured the relative contribution of each channel of deexcitation of the $^5\text{I}_7$ emitting level of Ho^{3+} as a function of the Er^{3+} excitation level. The results show that this sensitization is particularly interesting in the case of pumping in the visible region, for example with a broad-band flash lamp or the 532 nm radiation of a frequency doubled YAG : Nd^{3+} laser.

The complexity of fluorescence dynamics in the rare earth doped materials is now well known. In particular, the occurrence of non-linear processes such as up-conversion and cross-relaxation energy transfers is well established [6-9] and excellent review articles have been devoted to this field in the past years [10, 11]. However, the relative importance of the various processes in the relaxation mechanisms is not very often considered, and what applies for an ion in a given host matrix can be wrong for the same ion in another host. Then each case still needs to be carefully analysed.

As a matter of fact, this paper is dedicated to a detailed study of the excited-state dynamics of the Tm^{3+} and Ho^{3+} ions in LiYF_4 , in order to identify and evaluate the main relaxation mechanisms and to check the assumptions made in the past. Our method of analysis is similar to that used in the above studies [4, 5]. The experimental data and the interpretations of the fluorescence kinetics for a 1 % Tm^{3+} singly doped compound are presented in section 3. The $\text{Tm}^{3+} \rightarrow \text{Ho}^{3+}$ energy transfer mechanisms are then considered in codoped compounds of LiYF_4 containing 7 % Tm^{3+} and x % Ho^{3+} ($x = 0.5, 2$ and 5) and the results are presented in section 4. Particular attention is addressed to the analysis and the interpretation of the Ho^{3+} concentration and the temperature dependences of the fluorescence dynamics. A summary of the results and some concluding remarks are added in section 5.

2. Experimental techniques.

The single crystals were grown using the Czochralsky method by Henry at the L.E.T.I. (Grenoble, France). The optical excitation of the samples was made by using the same pulsed YAG : Nd^{3+} pumped dye laser as that described in one of our articles dedicated to the study of the Er^{3+} fluorescence dynamics in LiYF_4 [12]. We also used a home made pulsed YAG : Nd^{3+} pumped $\text{Al}_2\text{O}_3 : \text{Ti}^{3+}$ solid-state laser tunable in the 680-980 nm region and delivering up to 30 mJ/pulse [13]. The optical techniques used in the fluorescence detection and analysis in the infra-red range and more especially the recording of the lifetime data, are discussed in reference [5]. The fluorescence time constants are measured within 10 % depending on the intensity of the signals and on the theoretical treatment of the data. The absorption measurements were made using a CARY UV - visible - NIR spectrophotometer model 2300, spanning the wavelength range from 185 to 3 152 nm.

3. Excited state dynamics of the Tm^{3+} ions in $\text{LiYF}_4 : 1\text{ }\%\text{ Tm}^{3+}$.

3.1 SPECTRAL ANALYSIS. — The total absorption spectrum of the Tm^{3+} ion in LiYF_4 at room temperature is shown in figure 1. The assignment of the various peaks, as indicated in this

Fig. 1. — Absorption spectrum of the Tm³⁺ ion in LiYF₄ at room temperature (Tm³⁺ concentration : 1 % ; sample thickness : 5.1 mm).

figure, leads to the energy level scheme represented in figure 2. We have reported all the possible emission transitions which can occur between 4 000 and 25 000 cm⁻¹ as a function of their energy. It can be seen that a large number of fluorescences coincide in energy, so that they have to be taken into account in the following.

3.2 STOKES FLUORESCENCE DYNAMICS. — This dynamics describes the downward relaxation following the excitation of a given state. Each of the energy levels in the visible and infrared domains has been excited selectively. The excitation of most of these levels (the lowest ones) leads to simple relaxation processes while the excitation of the ¹G₄ level gives rise to more complex phenomena. Therefore these two cases will be considered separately.

3.2.1 Infrared and red excitations. — The excitation of the ³F₄ state gives rise predominantly to the ³F₄ → ³H₆ emission transition near 1.8 μm. The fluorescence decay is exponential, with a time-constant of 16 ms, the lifetime of the ³F₄ level.

When the Tm³⁺ ions are excited in their ³H₅ state, no fluorescence of this level could have been detected. The ³F₄ → ³H₆ radiative transition, however, is easily observed and the fluorescence decay mode is the same as in the case of direct excitation of the ³F₄ level. The absence of any measurable risetime (the response of our InSb detector was of the order of 0.5 μs) means that the lifetime of the ³H₅ state is short (likely < 0.5 μs), which can be attributed to the small energy gap and the very probable non-radiative relaxation between the ³H₅ and the ³F₄ levels.

The excitation of the ³H₄ level gives rise to a ³H₄ → ³H₆ fluorescence transition between 760 and 830 nm. Its decay is exponential with a time-constant of 1.45 ms, the lifetime of the

Fig. 2. — Energy level scheme of the Tm^{3+} ion and main emission transitions.

$3H_4$ level. The fluorescence of the $3F_4 \rightarrow 3H_6$ transition is also detected and its decay mode (Fig. 3) is well described by the expression :

$$I(t) \propto \exp(-t/16) - \exp(-t/1.45) \quad (1)$$

with time t in ms.

Fig. 3. — Time-dependence of the $3F_4 \rightarrow 3H_6$ infrared fluorescence after $3H_4$ excitation in LiYF_4 : 1 % Tm^{3+} . Curve a : lower scale ; curve b : upper scale.

The built-up reflects the feeding of the ³F₄ level by the ³H₄ level and the decay the lifetime of the ³F₄ level. Thus this time dependence is indicative of a very efficient ³H₄ → ³F₄ energy relaxation. This relaxation process can occur *via* level ³H₅ and/or directly, in which case it could occur with the participation of one and/or two ions transferring their energy from one to the other in a cross-relaxation process of type

This is suggested by the reduced lifetime of 1.45 ms of state ³H₄ in our 1 % Tm³⁺ compound compared to that found in weaker doped materials [14, 15].

The red excitation of the ³F₃ level gives rise to the ³H₄ → ³H₆ emission the decay mode of which is exponential with a time-constant of 1.45 ms. The absence of built-up is due to the short lifetime of the ³F₃ level (< μs), which is explained by the small ³F₃-³H₄ energy difference. The ³H₄ level again de-excites itself in favour of the ³H₅, ³F₄ and ³H₆ lower states according to the same mechanism as described before in case of ³H₄ excitation. The main role played by the ³F₃ level is to quickly transmit the energy to the ³H₄ state. However it will be seen in part 3.3 of this section that it may also induce more complex phenomena.

3.3.2 Blue excitation of the ¹G₄ level. — This excitation leads to several emissions which are considered in succession.

3.2.2.1 ¹G₄ → ³H₆ blue-green fluorescence transition. — The fluorescence decays measured between 460 and 490 nm are not exponential and are described by the expression :

$$I(t) \propto 1.5 \exp(-t/0.120) + \exp(-t/0.570) \quad (2)$$

with time t in ms.

3.2.2.2 ¹G₄ → ³F₄ and ³F₂, ³F₃ → ³H₆ red fluorescence transitions. — This red emission spectrum ranges between 620 and 680 nm. The decay modes are similar to the blue-green fluorescence ones previously obtained. They are assigned to the ¹G₄ → ³F₄ transition. That means that the contribution of the red emission originating from the ³F₂ and ³F₃ levels is very weak because of a fast multiphonon relaxation ³F₂ → ³F₃ → ³H₄.

3.2.2.3 ¹G₄ → ³H₅ and ³H₄ → ³H₆ near infrared fluorescence transitions. — These fluorescences overlap over a wide spectral range from 760 to 830 nm. The short wavelength fluorescence between about 760 and 780 nm seems to be dominated by the ¹G₄ emission and its decay is represented in figure 4a. On the other hand the long wavelength fluorescence ($\lambda > 790$ nm) seems to be dominated by the ³H₄ emission and its decay mode includes a well pronounced built-up at short times (Fig. 4b). However the interpretation of these data is not straightforward and requires to write some appropriate rate equations.

The intensity of each of the two ¹G₄ → ³H₅ and ³H₄ → ³H₆ infrared emissions is proportional to the population of the ¹G₄ and of the ³H₄ emitting state, respectively. According to equation (2) the population N of the ¹G₄ state transforms like :

$$N = \frac{N_0}{2.5} [1.5 \exp(-t/0.120) + \exp(-t/0.570)] \quad (3)$$

This time evolution is represented by the curve a of figure 5.

The population N' of the ³H₄ level varies according to the equation :

$$\dot{N}' = -\frac{N'}{1.45} + AN(t) \quad (4)$$

Fig. 4. — Time-dependence of the $^1G_4 \rightarrow ^3H_5$ and/or $^3H_4 \rightarrow ^3H_6$ fluorescence infrared fluorescences after 1G_4 excitation in LiYF_4 : 1 % Tm^{3+} . Curve a : emission at 770 nm ; curve b : emission at 815 nm.

where 1.45 ms is the lifetime of the 3H_4 level and A represents the total $^1G_4 \rightarrow ^3H_4$ transition probability (direct and *via* 3F_2 , 3F_3). The solution of (4) takes the form given by the curve b of figure 5.

Because of the spectral overlap the observed signal should be the sum of the two emissions

Fig. 5. — Theoretical curves describing the $^1G_4 \rightarrow ^3H_5$ fluorescence decay (curve a), the $^3H_4 \rightarrow ^3H_6$ fluorescence decay (curve b) and the linear combination (curve c) which gives the best fit to the experimental data (+).

and its temporal dependence should depend on their relative intensities, therefore on the fluorescence wavelength considered.

We have tried to fit the corresponding experimental data by a linear combination of the $N(t)$ and $N'(t)$ functions. For example at 815 nm the best fit is represented by the curve c of figure 5. This bad fit proves that the model is unable to describe the observed short-time behaviour (0.120 ms), and therefore is not convenient to explain the dynamics correctly. Another model based on the former can be proposed by dissociating the origins of the two exponential terms of the decay curve of the 1G_4 emission. When a Tm³⁺ ion (1) is excited in the 1G_4 state it can decay (radiatively or non radiatively) on the lower states 3H_5 , 3F_4 , 3H_6 with a probability of $10^3/0.570 \text{ s}^{-1}$. It can also decay with the aid of another Tm³⁺ ion (2) according to the cross-relaxation type energy transfer :

Figure 6 shows the LiYF₄ crystal structure and the positions of the possible nearest neighbours which can be involved in the transfer. Numerical value of the nearest-neighbour distances r are given in table I.

Fig. 6. — LiYF₄ crystal structure and nearest neighbours of a given Y³⁺ ion (0).

By simplification, two types of sites may be considered : either quasi isolated Tm³⁺ ions (1) or Tm³⁺ ions (1) with other Tm³⁺ ions (2) in their vicinity, the latter corresponding to the overall transfer probability :

$$k = \frac{10^3}{0.120} - \frac{10^3}{0.570} \sim 6\,600 \text{ s}^{-1}. \quad (5)$$

The mechanism for these two sites are shown in figure 7.

Table I.

Neighbours	Distance from the reference ion (Å)	Number of equivalent neighbours
1st	3.72	4
2nd	5.16	4
3rd	6.37	4
3rd	6.37	4
4th	6.48	8
5th	7.30	4
6th	8.19	4

Fig. 7. — $^1G_4 \rightarrow ^3H_5$ and $^3H_4 \rightarrow ^3H_6$ infrared fluorescence mechanisms for Tm^{3+} ions occupying sites of type I and type II in $LiYF_4$.

Site I. — The 1G_4 fluorescence decays exponentially with a time-constant of 0.570 ms, so that :

$$N_I = N_0 \exp(-t/0.570) \quad (6)$$

The rate equation describing the time dependence of the 3H_4 population of the sites I then transforms like :

$$\dot{N}'_I = -\frac{N'_I}{1.45} + \frac{\alpha}{0.570} N_0 \exp(-t/0.570) \quad (7)$$

where α is the fractional part of the 1G_4 de-excitation probability which ends directly or *via* 3F_2 and 3F_3 on state 3H_4 . α is considered as a fitting parameter. The solution of equation (7) is :

$$N'_I(t) = \frac{1.45 \times 0.570}{1.45 - 0.570} \times \frac{\alpha}{0.570} N_0 [\exp(-t/1.45) - \exp(-t/0.570)] \quad (8)$$

Site II. — The 1G_4 fluorescence decays with the time-constant of 0.120 ms as :

$$N_{II} = N_0 \times 1.5 \exp \left[- \left(\frac{1}{0.570} + 10^{-3} k \right) t \right]$$

so,

$$N_{II} = N_0 \times 1.5 \exp(-t/0.120) \quad (9)$$

The cross relaxation mechanism feeds the 3H_4 level *via* the strong $^3F_2 \rightarrow ^3F_3 \rightarrow ^3H_4$ multiphonon relaxations, so the rate equation for the 3H_4 population transforms like :

$$\dot{N}_{II}' = - \frac{N_{II}'}{1.45} + \left(\frac{\alpha}{0.570} + 10^{-3} k \right) N_0 \times 1.5 \exp(-t/0.120) \quad (10)$$

which gives the solution :

$$N'_{II}(t) = \frac{1.45 \times 0.120}{1.45 - 0.120} \times \left(\frac{\alpha}{0.570} + 10^{-3} k \right) N_0 \times 1.5 [\exp(-t/1.45) - \exp(-t/0.120)] \quad (11)$$

The overall intensity of the 3H_4 fluorescence then is proportional to $N'_I(t) + N'_{II}(t)$, the best fit to the experimental points being represented by the curve b of figure 8. In agreement with these points a shorter built-up than that predicted by the previous model is obtained so that a linear combination of both the 3H_4 and 1G_4 emissions reproduces very well the experimental results (curve c, Fig. 8).

Fig. 8. — Theoretical curves giving the $^1G_4 \rightarrow ^3H_5$ fluorescence decay of the Tm³⁺ ions in sites I and sites II (curve a), the best fit to the $^3H_4 \rightarrow ^3H_6$ fluorescence decay (curve b) and the linear combination of the 1G_4 and 3H_4 fluorescences (curve c).

3.2.2.4 $^3F_4 \rightarrow ^3H_6$ infrared fluorescence transitions. — The present model should be able to describe the time dependence of the $^3F_4 \rightarrow ^3H_6$ fluorescence. The experimental data are

represented in figure 9. First one observes a short build-up ($\tau \sim 0.1$ ms), then a longer one and finally a long decay with a 16 ms time constant. If we use the rate equation

$$\dot{N}'' = -\frac{N''}{16} + \beta N'_{II}(t) \quad (12)$$

associated with the de-excitation channel $^1G_4 \rightarrow ^3H_4 \rightarrow ^3F_4$ of the Tm^{3+} ions in sites II (N'' stands for the 3F_4 population) to fit the experimental data, one obtains a longer risetime than the one observed (Fig. 9, curve a). On the other hand, if we only consider the direct de-excitation channel $^1G_4 \rightarrow ^3F_4$ of the Tm^{3+} in sites II described by the equation :

$$\dot{N}'' = -\frac{N''}{16} + \gamma \exp(-t/0.120), \quad (13)$$

the rapid risetime is well reproduced but not the longer one (Fig. 9, curve b). This de-excitation channel can be attributed to the cross-relaxation type energy transfer :

a transfer process which gives the same result as that considered above (see Fig. 7).

Fig. 9. — Theoretical curves describing the $^3F_4 \rightarrow ^3H_6$ infrared fluorescence decay of Tm^{3+} ions in sites II.

Naturally, the right time dependence of the 3F_4 fluorescence has been found by considering both the direct and the indirect de-excitation channels of the Tm^{3+} ions in sites II and by solving the rate equation :

$$\dot{N}'' = -\frac{N''}{16} + \gamma \exp(-t/0.120) + \beta N'_{II}. \quad (14)$$

The agreement shown in the curve c of figure 9 between the model and the experimental data is indeed very good. The cross-relaxation mechanism resulting in the direct de-excitation channel $^1G_4 \rightarrow ^3F_4$ thus is clearly evidenced.

3.3 UP-CONVERSION PROCESSES AND EXCITATION OF PARTICULAR SITES. — These complex phenomena give rise to much weaker emissions than those analysed in the previous

subsections and it is why their influence on the Stokes fluorescence dynamics is negligible and was not considered.

However, these processes actually occur and this paragraph is devoted to their study. Their complexity does not always allow to find a clear interpretation of the phenomena so that this part must be considered more as a descriptive study than as an accurate analysis of the experimental results.

3.3.1 760-830 nm *infrared emission*. — We have seen that this fluorescence originates from the ³H₄ and ¹G₄ levels. It can be observed by exciting the Tm³⁺ ions in the ³H₅ state thus resulting from an up-conversion phenomenon. Its time-dependence is peculiar, however : the decay, at λ = 793 nm, shows two short components (2 and 25 μs) and a long one (1.6 ms) without any evidence of risetime. The long component reflects the lifetime of the ³H₄ level and the short components are probably due to the de-excitation of the ¹G₄ state. We have seen that the lifetime of this level depends on the site occupied by the emitting Tm³⁺ ions. In case of ¹G₄ excitation, we have simplified the situation by considering only two types of sites, but it is clear that actually many sites exist, some of which (corresponding to nearest-neighbor Tm³⁺ ions for example) may have very short lifetimes. The latter must not be numerous enough to detect their fluorescence after a direct excitation process such as a ¹G₄ excitation. However it can be more easily detected when it is a consequence, as in the case of a ³H₅ excitation, of an up-conversion process, i.e. an energy transfer mechanism concerning nearby Tm³⁺ ions predominantly.

3.3.2 620-730 nm *red emissions*. — The excitation of the ³H₅ level also leads to a red emission ; its decay, recorded at 700 nm, consists of two short components (2 and 30 μs) which can be assigned to the ¹G₄ → ³F₄ transition.

The excitation of the ³H₄ level gives rise to a weak red emission (Fig. 10, curve c) which is also due to an up-conversion mechanism. Its time-dependence does not show any risetime, but an exponential decay with a time-constant of 1.45 ms. The emission spectrum between 640 and 670 nm (Fig. 10, curve c) is the same as that obtained by exciting the ³F₂, ³F₃ levels at 683 nm (Fig. 10, curve a). It is attributed to ³F₂, ³F₃ → ³H₆ and ¹G₄ → ³F₄ transitions. On the other hand the strongest peak at 695 nm obtained by exciting the ³F₂, ³F₃ levels at 683 nm (Fig. 10a) has completely vanished. This means that the transfers by up-conversion do not involve the particular site in which the ³F₃ emission mainly occurs at 695 nm.

Let us now consider the excitation of the ³F₂, ³F₃ levels, in particular the excitations at 683 and 695 nm, which give rather peculiar results. When the Tm³⁺ ions are excited at 695 nm (Fig. 10, curve b), the spectrum is flat between 640 and 670 nm and shows three weak peaks at 683, 695 and 705 nm. The fluorescence decays recorded at 660, 667, 680, 700 and 710 nm are identical, exponential with a time-constant of 1.45 ms. On the other hand, an excitation at 683 nm (Figs. 10a and 11a) leads to an emission spectrum presenting small structures between 640 and 660 nm and the peak at 695 nm is strongly enhanced compared with the two satellites at 683 and 705 nm. The decay modes at 650 and 667 nm are made essentially of a long component with a time-constant of ~ 2.5 ms while at 683 and 695 nm, the decays involve two distinct components, a short one with a mean time-constant of about 40 μs which may be shared itself into two components (2 and 30 μs), and a long one with a time-constant of 1.55 ms. The contributions of these components to the total red emission were obtained from time-resolved spectroscopy measurements. The time-resolved spectra are shown in figure 11. When the spectrum is resolved at short times after the laser pulse only the emission peak at 695 nm (curve b) appears. When it is resolved at long times, all the other structures appear

Fig. 10.

Fig. 10. — Red emission spectra obtained at room temperature for a 1 % Tm^{3+} doped LiYF_4 crystal after : a) excitation of the $^3\text{F}_2$, $^3\text{F}_3$ levels at 683 nm ; b) excitation of the $^3\text{F}_2$, $^3\text{F}_3$ levels at 695 nm ; c) excitation of the $^3\text{H}_4$ level (antiStokes emission).

Fig. 11.

Fig. 11. — Red fluorescence spectra a) integrated fluorescence spectrum ; b) time-resolved spectrum at short times (gatewidth of signal integration : 100 μs ; delay : 0.5 μs) ; c) time-resolved spectrum at intermediate times (gatewidth : 500 μs ; delay 200 μs) ; d) time-resolved spectrum at long times (gatewidth : 400 μs , delay 1 ms).

progressively (curves c and d), and the intensity of the peak at 695 nm decreases as the delay increases without yet completely disappearing, since it remains the strongest. As a consequence the fluorescence corresponding to the peak at 695 nm is mostly short-lived, while the other fluorescences are essentially long-lived fluorescences. The fluorescence decay measured at 683 nm presents a short component which can be attributed to the influence of the overlapping fluorescence at 695 nm. It comes out from these experimental results that the laser beam at 683 nm excites two kinds of Tm^{3+} luminescent centers : some emit a short-lived fluorescence centered at 695 nm and may be considered as Tm^{3+} ions at normal sites ; others, emitting a long-lived fluorescence and covering the whole range between 640 and 730 nm, are probably perturbed Tm^{3+} ions occupying special lattice sites and acting as traps for the red fluorescence.

We have seen that the red emission between 630 and 680 nm, obtained by exciting the ¹G₄ level, is due to a ¹G₄ → ³F₄ transition. We also have detected a very weak red emission between 680 and 705 nm. As in the case of the previous excitation, the decay of this fluorescence comprises a short component, stronger at 695 nm than at 705 nm, and a long one with a time-constant of 1.45 ms. Therefore this residual fluorescence is attributed again to ³F₂, ³F₃ → ³H₆ transitions within Tm³⁺ ions in different sites.

3.3.3 ¹G₄ → ³H₆ blue-green anti-Stokes emission. — This fluorescence can be obtained by exciting at energies lower than that of the ¹G₄ emitting level and its decay mode depends on the excitation level. Excitation of ³H₅ leads to a short-lived fluorescence decay of a few μs followed by a long one of 1.5 ms. Excitation of ³H₄ gives a decay which is nearly exponential with a time-constant of 1.5 ms. By exciting level ³F₃ one observes at 474 nm a fluorescence decay which consists of two short-lived components with time constants of 2 and 80 μs and at 478 nm a decay made of a short- and a long-lived component with time-constants of a few μs and 1.3 ms, respectively. These experimental results reflect very complicated up-conversion processes which would be difficult to interpret very accurately and that we shall not analyse any further.

4. Tm³⁺ → Ho³⁺ energy transfers.

Three samples were investigated containing 7 % of Tm³⁺ ions and *x* % of Ho³⁺ ions (*x* = 0.5, 2 and 5). The transfer processes were studied in the case of infrared excitation of each of the low-lying levels ³H₄ and ³F₄. The excitation of the Tm³⁺ ions in the ³H₄ excited state is particularly important because it corresponds to the emission range of the laser diodes around 795 nm.

4.1 ³F₄ → ⁵I₇ ENERGY TRANSFERS. — These transfers are analysed by directly exciting the ³F₄ level in the infrared region around 1.68 μm (Fig. 12).

Fig. 12. — Energy transfers ³F₄, ⁵I₈ → ³H₆, ⁵I₇ at room temperature in LiYF₄: 7 % Tm : *x* % Ho (*x* = 0.5, 2, 5).

4.1.1 Transfers at room temperature. — The fluorescence decay of the ${}^3F_4 \rightarrow {}^3H_6$ transition of the Tm^{3+} ions shows first a very strong and short component of a few tens of μs , and then a very long one with a time-constant of 15-19 ms. The time-constants of the two components are so different that it is necessary to use different basetimes to clearly detect them. The time dependence of the fluorescence of the Ho^{3+} ions corresponding to the ${}^5I_7 \rightarrow {}^5I_8$ transition near $2 \mu m$ presents a short built-up of a few tens of μs , and a long decay identical to the one of the 3F_4 fluorescence.

These data are easy to interpret. The short component of the Tm^{3+} fluorescence decay represents the lifetime of the 3F_4 level. Its strong shortening is due to the $Tm^{3+} \rightarrow Ho^{3+}$ energy transfers and also to the fast diffusion among the Tm^{3+} ions, which probably occurs in such concentrated systems (7 % Tm^{3+}). The rapid risetime of the Ho^{3+} fluorescence corresponds to the feeding time of the 5I_7 level via this ${}^3F_4 \rightarrow {}^5I_7$ energy transfer, and this population build-up corresponds well to the decay of the 3F_4 fluorescence observed at short times. However when the 5I_7 level is sufficiently populated, ${}^5I_7 \rightarrow {}^3F_4$ phonon-assisted back-transfers can occur and it follows a population equilibrium between both 3F_4 and 5I_7 levels which decay at long times with the same time constant. This is possible at room temperature since the two excited levels are separated by only a few hundreds of wavenumbers. Thus the transfer mechanisms can be described, using the notation indicated in figure 12, with the following equations :

$$\dot{N} = -\frac{N}{\tau} - kN + k' N' \quad (15)$$

$$\dot{N}' = -\frac{N'}{\tau'} - k' N' + kN \quad (16)$$

Taking into account the initial conditions

$$N(0) = N_0 \quad \text{and} \quad N'(0) = 0 ,$$

the solution of the system is :

$$N = \alpha \exp(r_2 t) + \beta \exp(r_1 t) \quad (17)$$

$$N' = \alpha' [\exp(r_1 t) - \exp(r_2 t)] \quad (18)$$

where α , β and α' are constants and r_1 and r_2 are given by :

$$r_1 = \frac{1}{2} \left\{ - \left(\frac{1}{\tau} + k + \frac{1}{\tau'} + k' \right) + \left[\left(\frac{1}{\tau} + k - \left(\frac{1}{\tau'} + k' \right) \right)^2 + 4kk' \right]^{1/2} \right\} \quad (19)$$

$$r_2 = \frac{1}{2} \left\{ - \left(\frac{1}{\tau} + k + \frac{1}{\tau'} + k' \right) - \left[\left(\frac{1}{\tau} + k - \left(\frac{1}{\tau'} + k' \right) \right)^2 + 4kk' \right]^{1/2} \right\} \quad (20)$$

These relations are complex but can be simplified if one assumes :

$$\frac{1}{\tau} \sim \frac{1}{\tau'} \leq k' \leq k . \quad (21)$$

Then relations (19) and (20) become :

$$r_1 \sim -\frac{1}{\tau'} \quad (22)$$

$$r_2 \sim -k \quad (23)$$

and according to (21), one finds :

$$|r_2| \gg |r_1| \quad (24)$$

in agreement with the experimental observations.

One actually finds experimentally :

$$|r_2| \sim 10^5 \text{ s}^{-1}$$

and

$$\begin{aligned} |r_1| &= \frac{10^3}{15} \sim 67 \text{ s}^{-1} \quad \text{in LiYF}_4 : 7 \% \text{ Tm}^{3+}, 0.5 \% \text{ Ho}^{3+} \\ &= \frac{10^3}{17.3} \sim 58 \text{ s}^{-1} \quad \text{in LiYF}_4 : 7 \% \text{ Tm}^{3+}, 2 \% \text{ Ho}^{3+} \\ &= \frac{10^3}{19} \sim 53 \text{ s}^{-1} \quad \text{in LiYF}_4 : 7 \% \text{ Tm}^{3+}, 5 \% \text{ Ho}^{3+} \end{aligned}$$

$\frac{1}{|r_1|}$ are interpreted as the values of the τ' lifetimes of $^5\text{I}_7$ in the three samples. It should be noted that the τ' value of 16 ms obtained in LiYF₄ : 1 % Ho³⁺ in a previous study [4] agrees well with the trend observed here and indicated in table II. The increase of τ' with the Ho³⁺ concentration, previously observed in LiYF₄ : 50 % Er, x % Ho [4], is confirmed by the present results. This Ho³⁺ concentration dependence of the lifetime of the $^5\text{I}_7$ emitting level is explained by the occurrence of radiative energy transfers among the Ho³⁺ ions.

Table II. — *Time-constants of the $^5\text{I}_7$ fluorescence decays of Ho³⁺ ions.*

τ' (ms)	15	16	17.3	19
x (% Ho)	0.5	1	2	5

4.1.2 Temperature-dependence of the transfers. — An example of the temperature-dependence of the 1.8 μm fluorescence decay of the Tm³⁺ ions in (Tm³⁺, Ho³⁺) co-doped LiYF₄ is represented in figure 13.

According to our model, a few tens of μs after the excitation, both the $^3\text{F}_4$ and $^5\text{I}_7$ levels decay with the same time-constant $\frac{1}{|r_1|}$ which represents the lifetime τ' of the $^5\text{I}_7$ fluorescence. The predominance of the $^5\text{I}_7$ level (which imposes its lifetime to the dynamics) over the $^3\text{F}_4$ level is due to the fact that the $^3\text{F}_4 \rightarrow ^5\text{I}_7$ direct-transfer is more rapid than the $^5\text{I}_7 \rightarrow ^3\text{F}_4$ back-transfer ($k \gg k'$) and consequently the $N'(t)$ population of $^5\text{I}_7$ is higher than the $N(t)$ one of $^3\text{F}_4$ whatever the temperature and the more as the temperature is low.

The linear temperature-dependence of $\text{Ln} \left(\frac{N}{N'} \right)$ with $\frac{1}{T}$ (Fig. 14) confirms the existence of a Boltzmann population equilibrium between the $^3\text{F}_4$ and $^5\text{I}_7$ levels, with an activation energy of about 450 cm^{-1} . This value is in good agreement with the energy mismatch between the two excited states as it can be seen in the right part of figure 14 and is of the same order of magnitude as the maximum phonon frequency in LiYF₄ crystal : 380 cm^{-1} . The long-lived component of the $^3\text{F}_4$ fluorescence decay resulting from the $^5\text{I}_7 \rightarrow ^3\text{F}_4$ back-transfers

Fig. 13. — Temperature-dependence of the $1.8\text{ }\mu\text{m}$ fluorescence decay after excitation of the $^3\text{F}_4$ level.

at room temperature vanishes by $T \approx 200\text{ K}$ and it is completely quenched at liquid nitrogen temperature (Fig. 13).

4.2 $\text{Tm}^{3+} \rightarrow \text{Ho}^{3+}$ ENERGY TRANSFERS IN CASE OF $^3\text{H}_4$ EXCITATION. — In section 3.2.1 we mentioned that a very efficient cross-relaxation type energy transfer among the Tm^{3+} ions could be responsible for the 1.45 ms time-constant observed, in the fluorescence decay of level $^3\text{H}_4$ as well as in the fluorescence rise of level $^3\text{F}_4$, in the singly doped LiYF_4 : 1 % Tm^{3+} compound after excitation in the $^3\text{H}_4$ level. This seems to be confirmed in the codoped systems LiYF_4 7 % Tm^{3+} , x % Ho^{3+} since the decay of the $^3\text{H}_4$ fluorescence and the rise of the $^3\text{F}_4$ fluorescence are now reduced to a few μs . This reduced time-constants however can also be attributed, as sketched in figure 15, by other transfer processes, now between the $^3\text{H}_4$ level of the Tm^{3+} ions and the $^5\text{I}_5$ or $^5\text{I}_4$ level of the Ho^{3+} ions and/or by a cross-relaxation process of type: $^3\text{H}_4, ^5\text{I}_8 \rightarrow ^3\text{F}_4, ^5\text{I}_7$. In this case the rate equation for the $^3\text{H}_4$ population density can be written :

$$\dot{N} = -\frac{N}{\tau_0} - kNN_0 - k'NN'_0, \quad (25)$$

where k and k' stand for the transfer constants involved in figure 15 and where N_0 and N'_0 , the $^3\text{H}_6$ and $^5\text{I}_8$ population densities, respectively, are assumed to be constant

Fig. 14. — Temperature-dependence of the population ratio of the $^3F_4(N)$ and $^5I_7(N')$ energy levels of the Tm^{3+} and Ho^{3+} ions, respectively.

Fig. 15. — The three channels of de-excitation of the Tm^{3+} ions.

(weak excitation density). τ^0 is the fluorescence lifetime of level ${}^3\text{H}_4$ in the absence of transfers. The solution of equation (25) gives rise to an exponential decay with a time-constant τ such as :

$$\frac{1}{\tau} + \frac{1}{\tau^0} + kN_0 + k' N'_0. \quad (26)$$

Instead of studying the ${}^3\text{H}_4 \rightarrow {}^3\text{H}_6$ fluorescence decay, which is difficult to record because the excitation and the fluorescence are in resonance, we have analysed the rise of the ${}^3\text{F}_4$ fluorescence near $1.8 \mu\text{m}$. This fast fluorescence rise, which is interpreted as the lifetime τ of level ${}^3\text{H}_4$ (Tab. III) and the fast decay which follows at short times are strongly dependent on the Ho^{3+} concentration, and this is indicative of the $\text{Tm}^{3+} \rightarrow \text{Ho}^{3+}$ energy transfers from the ${}^3\text{H}_4$ as well as from the ${}^3\text{F}_4$ energy levels as shown in figures 12 and 15.

Table III. — *Lifetimes of ${}^3\text{H}_4$ level and quantum efficiencies of the 3 different channels of de-excitation.*

x (% Ho)	0	0.5	2	5
τ (μs)	12.5	6.5	3	1.2
η_1 (%)	0.33	0.17	0.08	0.03
η_2 (%)	99.67	51.83	23.92	9.57
η_3 (%)	0	48.00	76.00	90.40

The short-time as well as the long-time fluorescence decays of level ${}^3\text{F}_4$ vary with the Ho^{3+} concentration in the same way and for the same reasons as for a ${}^3\text{F}_4$ excitation (see Sect. 4.1.1). The experimental variation of $\frac{1}{\tau}$ with the $N'_0 {}^5\text{I}_8$ ground state population density (proportional to the $x\text{Ho}^{3+}$ concentration) (Fig. 16) can be fitted with a straight line according to equation (26). If we take $\tau^0 = 3.8 \text{ ms}$, which is the experimental value of the ${}^3\text{H}_4$ lifetime measured in a very lightly doped $\text{LiYF}_4 : \text{Tm}^{3+}$ sample [15], it is possible to deduce kN_0 knowing the extrapolated value of τ at $N'_0 = 0$.

Finally, the quantum efficiencies of the three main mechanisms involved in the ${}^3\text{H}_4$ excited state dynamics, namely the Tm intra-center de-excitation, the $\text{Tm}^{3+} \rightarrow \text{Tm}^{3+}$ cross-relaxation and the $\text{Tm}^{3+} \rightarrow \text{Ho}^{3+}$ direct energy transfer, can be evaluated by using the relations :

$$\eta_1 = \frac{\tau}{\tau_0} \quad (27)$$

$$\eta_2 = \tau \times kN_0 \quad (28)$$

$$\eta_3 = 1 - \eta_1 - \eta_2 \quad (29)$$

The calculated values are gathered in table III. As expected, η_1 is very weak whatever the Ho^{3+} concentration. In a singly doped compound with 7 % Tm^{3+} and no Ho^{3+} the dynamics would be completely governed by the $\text{Tm}^{3+} \rightarrow \text{Tm}^{3+}$ cross relaxation process (η_2). In the

Fig. 16. — Inverse time-constant of the ³F₄ fluorescence rise following a ³H₄ excitation of the LiYF₄: 7 % Tm³⁺, x % Ho³⁺ compounds.

codoped systems this process competes with the Tm³⁺ → Ho³⁺ transfer processes η_3 which become highly predominant at high Ho³⁺ concentrations.

5. Summary and concluding remarks.

The study of the excited-state dynamics of the Tm³⁺ ions in a 1 % Tm³⁺ doped crystal of LiYF₄ leads to very particular results. First it shows the existence of numerous coincidences between the various fluorescences that only a careful examination, made in different excitation conditions, allow to distinguish. In addition, the whole dynamics can be interpreted by taking into account the possibility of a Tm³⁺ ion to have other Tm³⁺ ions in closeby positions or to be isolated. The former, that Barthém and Buisson [16] have treated in terms of paired-ions, seem to be the main ones that one should invoke to explain the various cross-relaxation and up-conversion processes observed for certain excitations.

Knowing these results, the energy transfer processes in the systems doped with 7 % Tm³⁺ and x % Ho³⁺ (x = 0.5, 2, 5) are studied in two cases of Tm³⁺ excitation: (i) excitation of level ³H₄ for it is of particular interest for diode-pumping purpose, (ii) excitation of level ³F₄ since it is the excited level which transfers the best its energy to the ⁵I₇ level of the Ho³⁺ ions responsible for the 2 μm laser transition.

The data show very efficient, within a few μs, cross relaxation type Tm³⁺ → Tm³⁺ and direct Tm³⁺ → Ho³⁺ energy transfers followed by diffusion among the Tm³⁺ ions and trapping by the Ho³⁺ ions within a few tens of μs, the latter being strongly influenced, on a longer time scale, by temperature-induced Ho³⁺ → Tm³⁺ back transfers above about 200 K.

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