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To cite this version:
A. Bonnenfant, J.M. Friedt, M. Maurer, J.P. Sanchez. Magnetic and structural properties of iron-based oxide glasses, Fe$_2$O$_3$-BaO-B$_2$O$_3$, from $^{57}$Fe Mössbauer spectroscopy. Journal de Physique, 1982, 43 (10), pp.1475-1487. <10.1051/jphys:0198200430100147500>. <jpa-00209529>

HAL Id: jpa-00209529
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Magnetic and structural properties of iron-based oxide glasses, Fe$_2$O$_3$-BaO-B$_2$O$_3$, from $^{57}$Fe Mössbauer spectroscopy

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(Reçu le 28 janvier 1982, révisé le 6 mai, accepté le 7 juin 1982)

Résumé. — La configuration électronique du fer, l'ordre structural à courte distance et les propriétés magnétiques de verres de composition (Fe$_2$O$_3$)$_x$(BaO)$_y$(B$_2$O$_3$)$_z$ sont établis par spectroscopie Mössbauer de $^{57}$Fe en combinaison avec des mesures macroscopiques. La coordination moyenne du fer est déterminée par le rapport atomique Fe/O dans le milieu tandis que la configuration de valence du fer dépend principalement des conditions de préparation. Un ordre structural à courte distance très strict est mis en évidence autour des atomes de Fe ; il correspond à des fluctuations aléatoires des angles et longueurs de liaison Fe—O. A faible concentration en Fe$_2$O$_3$, le verre reste paramagnétique jusqu'à 1,5 K ; la mesure locale de moment révèle cependant la coexistence d'ions isolés et d'agrégats à l'échelle atomique. A concentration moyenne en Fe$_2$O$_3$ (~ 25 %), le verre présente une transition micromagnétique. A concentration élevée en Fe$_2$O$_3$ (~ 50 %), le verre présente un comportement quasi-superparamagnétique, révélant une inhomogénéité de la répartition du fer dans le milieu. Les phases formées lors de la cristallisation du verre à concentration moyenne en Fe$_2$O$_3$ sont identifiées par spectroscopie Mössbauer.

Abstract. — $^{57}$Fe Mössbauer spectroscopy has been combined with bulk results to determine the electronic configuration of iron, the short-range structural order and the magnetic properties of glasses in the system (Fe$_2$O$_3$)$_x$(BaO)$_y$(B$_2$O$_3$)$_z$. The average coordination of the iron atoms is determined by the Fe/O atomic ratio while the valence state of Fe seems to be affected essentially by the preparation conditions. Structural short-range order around Fe atoms is concluded to be very strong, with random bonding angle and distance fluctuations. At low Fe$_2$O$_3$ content, the glass is paramagnetic down to 1.5 K. Local moment measurements reveal the coexistence of isolated Fe ions and of atomic scale clusters. At intermediate Fe$_2$O$_3$ concentration (~ 25 %), the glass presents a micromagnetic transition. At large Fe$_2$O$_3$ content (~ 50 %), the glass behaves like a superparamagnet, indicating inhomogeneous distribution of the Fe atoms in the solid. Mössbauer spectroscopy is also applied to the investigation of the crystallization of a glass with intermediate Fe$_2$O$_3$ concentration.

1. Introduction. — The investigation of the structural and magnetic properties specific to amorphous systems is of much current interest [1-3]. The understanding of these properties in insulating compounds differs from that in metallic glasses owing to dominant superexchange interactions. Therefore, the magnetic properties of amorphous insulators will reflect rather directly the distributions of bonding angles and distances. The atomic structure is best approximated by a random coordination model with preferred cation-anion bonds in a manner which ensures local charge neutrality [1, 4]. It would be expected that these features should permit an easier theoretical approach of amorphous insulators as compared with metals. Moreover, there are only few amorphous materials which display negative exchange interactions leading to an ordered state with random spin freezing (sperrarnagnetism) [5].

Considerable work has indeed been devoted recently to amorphous insulators [1-8]. Simple ionic compounds are generally difficult to obtain in the amorphous state [9, 10]. Extensive literature exists on binary or ternary oxides, which are easier to prepare but usually cannot be compared to corresponding crystalline systems. Current interest in amorphous oxide glasses primarily concerns the following aspects :

a) The electronic structure and bonding properties of the cations present in the glass. In the case of the widely investigated iron glasses, this corresponds more precisely to the determination of the valence state and the coordination of the Fe ions, in connection with the glass former or glass modifier behaviour [11, 12]. These problems have been extensively studied in many systems, in particular by spectroscopic methods, e.g., Mössbauer, NMR, ESR, etc... In the
Fe$_2$O$_3$-BaO-B$_2$O$_3$ glasses considered here, general trends emerging from previous studies indicate that the coordination of the Fe$^{3+}$ ions is governed by the Fe$_2$O$_3$/BaO ratio (i.e., tetrahedral network when Fe$_2$O$_3$/BaO < 1 and both tetrahedral and octahedral coordination when Fe$_2$O$_3$/BaO > 1) [13]. For comparison, $^{11}$B NMR in alkali-boron oxide glasses demonstrates that tetrahedral coordination of boron is preferred to the 3-coordinate oxygen neighbourhood when the proportion (up to 33 %) of alkali oxide increases, i.e. for increasing O/B atomic ratio [14]. Thus, the metal-oxygen coordination number is governed by the atomic ratio of the elements present in the glass. The presence of Fe$^{2+}$ ions in some glasses is related to the conditions of preparation.

b) The peculiar magnetic transitions and orderings occurring in such glasses are a consequence of frustration connected with topological disorder [5-10]. Speromagnetism has been demonstrated in a few insulating amorphous materials and mictomagnetism or spin glass transitions have been characterized in a variety of concentrated oxide glasses [5-7, 15, 16].

c) Additional problems of interest concern the possibility of chemical short-range order and compositional heterogeneities [17]. In oxide glasses of composition $(1 - x)[0.2$ BaO - 0.8 B$_2$O$_3]$xFe$_2$O$_3$, the occurrence of small iron clusters (dimers, trimers, etc...) has been claimed at low Fe concentration [18], while superparamagnetic behaviour has been demonstrated at high Fe content.

d) The crystallization mechanisms, the phase analysis and the evolution of the magnetic properties on crystallization is of intrinsic interest as well as from the point of view of applications. For example, microcrystalline (possibly monodomain) precipitates of barium hexaferrite evolve within a non-magnetic host; such systems may be considered for permanent magnet applications [19, 20].

2. Experimental. — The amorphous samples were prepared by quenching from the melt between rollers as described previously [19]. The final composition was checked by chemical analysis. The non-crystalline nature of the materials was established by X-ray and electron diffraction halos as well as from crystallization on thermal annealing as investigated by DTA and X-ray analyses. The evolution of the bulk magnetic properties on crystallization has been reported separately [19, 20].

The $^{57}$Fe Mössbauer experiments were performed as a function of temperature between 1.5 and 800 K using a $^{57}$Co/Rh source. Some experiments were performed at temperatures between 4.2 and 300 K in a longitudinal magnetic field up to 100 kOe. Thin absorbers (2-5 mg Fe/cm$^2$) were used for measurements in order to minimize intensity saturation effects [21]. The data were computer analysed for the hyperfine interaction parameters and their possible distributions; in the case of non-collinear quadrupole and magnetic interactions, the calculation of the spectral shape is performed numerically by diagonalization of the full nuclear Hamiltonians rather than using perturbation calculations. A comprehensive discussion of the method of analysis is developed in the text.

3. Experimental results on the amorphous samples. — $^{57}$Fe Mössbauer measurements are reported for amorphous ternary oxides of nominal molar compositions:

- $(Fe_2O_3)_{30}(BaO)_{45}(B_2O_3)_{25}$ sample A
- $(Fe_2O_3)_{30}(BaO)_{17.5}(B_2O_3)_{32.5}$ sample B
- $(Fe_2O_3)_{15}(BaO)_{35}(B_2O_3)_{15}$ sample C
- $(Fe_2O_3)_{5}(BaO)_{24}(B_2O_3)_{11}$ sample D.

They are discussed in combination with previously published [19, 20] static magnetization and susceptibility results. In addition, dynamic susceptibility measurements were performed on sample A (the only one presenting a unique valence state and coordination of the Fe cations) in which the magnetic transition and the nature of the ordered state are investigated in detail [22].

The Mössbauer spectra of sample A reveal a broadened quadrupole doublet in the temperature range from 670 to 42 K (Fig. 1). The isomer shift characterizes Fe$^{3+}$ ion in tetrahedral environment. The average quadrupole splitting ($\Delta_q$), isomer shift ($\delta_{IS}$)
and resonance width ($W_L$) deduced under the assumption of two Lorentzian lines are summarized in Table I. The linewidths are found to be equal for both components and are comparable to those reported previously in other oxide glasses [11–13, 15]. The spectra broaden sharply below 42 K, presenting complex shapes between 42 and 29 K (Fig. 2). Below 29 K, resolved magnetic hyperfine spectra are observed (Fig. 3). For the orientation of the data analysis it is of interest to note that the magnetic spectra appear symmetrical, in apparent contradiction with the quadrupolar splitting at higher temperature. Assuming Lorentzian lineshapes for the individual spectral components, the analysis of the 4.2 K data provides linewidths for the inner, middle and outer lines of 0.75, 1.08 and 1.50 mm/s while the relative areas are almost in the theoretical ratio of $1 : 2 : 3$ for a thin sample ($2$ mg Fe/cm$^2$). Proper analysis of the distribution of hyperfine parameters from these data is discussed below (section 4).

Magnetization curves for this sample (A) are linear down to 4.2 K in fields up to 50 kOe except in the low field region ($< 5$ kOe) where a very weak ferromagnetic component appears [19, 20, 23]. The latter behaviour probably arises from a minor contaminant of ferrimagnetic BaFe$_{12}$O$_{19}$ which is undetected by X-ray, electron diffraction and Mössbauer analyses. Recent high field magnetization ($\leq 150$ kOe) measurements confirm linearity above 80 K and reveal slight curvature below this temperature [24]. It should be noticed that the high field magnetization amounts to only a few percents of the calculated saturation value. The susceptibility deduced from the slope of the linear part of the magnetization curves follows a Curie-Weiss law above 80 K with $C = 1.52$ and $\theta_p = -95$ K. The molar Curie-Weiss constant $C$ is significantly below the value (4.38) predicted for

**Table I.** — Isomer shifts ($\delta_{IS}$), quadrupole splitting ($\Delta_Q$), resonance width ($W_L$) assuming Lorentzian lineshapes. Mean value ($\overline{\Delta}$) and deviation ($\sigma$) assuming Gaussian distribution of quadrupole splitting

$$[P(\Delta) \propto 1/\sigma \exp - (|\Delta - \overline{\Delta}|/2 \sigma)^2]$$

in the paramagnetic spectra of the glass ($\text{Fe}_2\text{O}_3$)$_{30}$ (BaO)$_{45}$($\text{B}_2\text{O}_3$)$_{25}$ (sample A). The isomer shift refers to Fe metal at 300 K.

<table>
<thead>
<tr>
<th>$T$ (K)</th>
<th>$\delta_{IS}$ (mm/s) ± 0.02</th>
<th>$\Delta_Q$ (mm/s) ± 0.02</th>
<th>$W_L$ (mm/s) ± 0.02</th>
<th>$\overline{\Delta}$ (mm/s) ± 0.02</th>
<th>$\sigma$ (mm/s) ± 0.01</th>
</tr>
</thead>
<tbody>
<tr>
<td>673</td>
<td>0.22</td>
<td>0.68</td>
<td>0.53</td>
<td>0.88</td>
<td>0.24</td>
</tr>
<tr>
<td>300</td>
<td>0.25</td>
<td>1.01</td>
<td>0.60</td>
<td>1.00</td>
<td>0.29</td>
</tr>
<tr>
<td>49</td>
<td>0.38</td>
<td>1.05</td>
<td>0.61</td>
<td>1.05</td>
<td>0.30</td>
</tr>
<tr>
<td>44</td>
<td>0.38</td>
<td>1.08</td>
<td>0.77</td>
<td>1.10</td>
<td>0.40</td>
</tr>
</tbody>
</table>

**Fig. 2.** — Temperature dependence of the spectra of sample A in the vicinity of the magnetic transition.

**Fig. 3.** — Mössbauer spectra of sample A at 4.2 K. (a) In the absence of external field; the full line corresponds to a fit as discussed in the text (with equal weights of + and − signs of the $\Delta$ distributions). (b) In the presence of an external field of 45 kOe.
free Fe³⁺ ions; the negative paramagnetic Curie temperature θp and magnetization indicate predominant antiferromagnetic exchange interactions. Below 80 K the reciprocal susceptibility vs. T curve deviates from linearity and reaches a minimum at 12 K [19]. The increase in susceptibility below 80 K may be due to large magnetic moments localized in small clusters [8]. Thermoremanent effects are observed below 14 K for a sample cooled in a field of 18.8 kOe [19, 23]. Unidirectional remanence and displaced hysteresis loops observed at 4.2 K are comparable to those reported for metallic micromagnets [25]. In order to elucidate the discrepancy between the appearance of magnetic hyperfine interactions in Mössbauer spectroscopy at 42 K and the unusual temperature dependence of susceptibility (suggesting a transition temperature of 12 K), dynamic susceptibility measurements were performed in a low field of 6 Oe at a frequency of 70 Hz [22]. They reveal a cusp characteristic of a micromagnetic transition at a temperature of 38 K.

Sample B of nominal molar composition \((\text{Fe}_2\text{O}_3)_{30}(\text{BaO})_{17.5}(\text{B}_2\text{O}_3)_{52.5}\) (i.e. increasing the \(\text{B}_2\text{O}_3/\text{BaO}\) ratio at constant \(\text{Fe}_2\text{O}_3\) content vs. sample A) presents three Mössbauer resonance lines above 24 K (Fig. 4). The deconvolution of these spectra into two broadened quadrupole doublets characterizes the simultaneous presence of Fe³⁺ (∼76 %) and Fe²⁺ (∼24 %) ions (Table II). The onset of magnetic hyperfine splitting occurs at 22 ± 1 K, resulting at 4.2 K in a broadened magnetic pattern which can be resolved into two magnetic sextets (Fig. 4). Because of the coexistence of two valence states of iron, bulk magnetic measurements have not been carried out in detail on this sample.

Sample C, \((\text{Fe}_2\text{O}_3)_{50}(\text{BaO})_{35}(\text{B}_2\text{O}_3)_{15}\), presents at high temperature (200 K < T < 300 K) a broadened and asymmetric doublet (Fig. 5). A magnetic spectrum, coexisting with the doublet, progressively develops below 200 K; the paramagnetic component vanishes below 55 K (Fig. 5). Using Lorentzian line-shapes, the paramagnetic spectra were analysed as a superposition of two symmetrical doublets with different isomer shifts and quadrupole splittings (Table III). The magnetic spectra are represented as a superposition of two sextets with different isomer shifts and hyperfine fields together with vanishing quadrupole effects (see discussion below). Both the \(\delta_{\text{HS}}\) and \(H_{\text{hf}}\) values of these two sites characterize the coexistence of tetrahedral and octahedral coordination of Fe³⁺ ions.

![Mössbauer spectra of sample B](image)

**Fig. 4.** Mössbauer spectra of sample B \((\text{Fe}_2\text{O}_3)_{30}(\text{BaO})_{17.5}(\text{B}_2\text{O}_3)_{52.5}\) in the paramagnetic and ordered phases.

### Table II. — Hyperfine data from the analysis of the Mössbauer spectra of the glass \((\text{Fe}_2\text{O}_3)_{30}(\text{BaO})_{17.5}(\text{B}_2\text{O}_3)_{52.5}\) (sample B). \(H_{\text{hf}}\) and \(\sigma\) are respectively the mean value and the deviation of the Gaussian distribution of the hyperfine field. Other symbols are defined as in table I.

<table>
<thead>
<tr>
<th>T(K)</th>
<th>(\delta_{\text{HS}}) (mm/s)</th>
<th>(H_{\text{hf}}) (kOe)</th>
<th>(\sigma)</th>
</tr>
</thead>
<tbody>
<tr>
<td>80</td>
<td>0.32 ± 0.05</td>
<td>0.56 ± 0.2</td>
<td></td>
</tr>
<tr>
<td>250</td>
<td>0.37 ± 0.05</td>
<td>0.52 ± 0.33</td>
<td></td>
</tr>
</tbody>
</table>

(*) The random orientation of the angle \(\theta\) between the \(EFG\) and \(H_{\text{hf}}\) axes has been taken into account by introducing an uniform broadening of the lines and setting \(\Delta = 0\) (see text, Eq. (2)).

(**) \(\theta = 80^\circ\) (see text).

### Table III. — Hyperfine data from the analysis of the Mössbauer spectra of the glass \((\text{Fe}_2\text{O}_3)_{50}(\text{BaO})_{35}(\text{B}_2\text{O}_3)_{15}\), sample C. Approximately 51 % of the Fe³⁺ are octahedrically coordinated whereas 49 % of the ions are in tetrahedral coordination.

<table>
<thead>
<tr>
<th>T(K)</th>
<th>(\delta_{\text{HS}}) (mm/s)</th>
<th>(H_{\text{hf}}) (kOe)</th>
<th>(\sigma)</th>
</tr>
</thead>
<tbody>
<tr>
<td>250</td>
<td>0.21 ± 0.02</td>
<td>0.52 ± 0.33</td>
<td></td>
</tr>
<tr>
<td>4.2</td>
<td>0.37 ± 0.05</td>
<td>0.52 ± 0.33</td>
<td></td>
</tr>
</tbody>
</table>

(* ) See table II and text, equation (2).
Magnetization and susceptibility results for this sample C indicate a minor ferrimagnetic component (saturated at low field) and show a broad maximum of susceptibility at 70 K. Remanence is observed below 70 K in a field of 18.8 kOe. The high temperature Curie-Weiss parameters are \( C = 4.31, \theta_p = -194 \text{ K} \).

The Mössbauer spectra of sample D, 

\[
\text{(Fe}_2\text{O}_3)_{24}(\text{BaO})_{24}(\text{B}_2\text{O}_3)_{71},
\]

reveal in the temperature range from 300 to 4.2 K three lines which are decomposed into two symmetrical doublets characterizing the presence of \( \text{Fe}^{2+} \) (\(~ 12 \%)\) and \( \text{Fe}^{3+} \) (\(~ 88 \%)\) valence states (Fig. 6, Table IV). At 1.5 K, a broad magnetic spectrum co-exists with the paramagnetic pattern. Isothermal magnetization is linear above 20 K up to fields of 20 kOe and deviates from linearity at higher fields without reaching saturation at 150 kOe. The reciprocal susceptibility vs. temperature shows a Curie-Weiss behaviour \( (C = 3.08, \theta_p = -9 \text{ K}) \) above 20 K and presents no singularity down to 1.5 K.

4. Analysis of hyperfine interaction distributions in the glasses \( \text{Fe}_2\text{O}_3-\text{BaO-B}_2\text{O}_3 \). — The large linewidths observed in the Mössbauer spectra of amorphous materials arise from distribution of hyperfine interactions. The analysis of these distributions is useful for probing the local structure and for establishing the electronic and magnetic properties by reference, for instance, to computer modelling predictions of amorphous structures \([1, 4]\). Let us recall some general features of the \( ^{57}\text{Fe} \) resonance shapes in the presence of such distributions and introduce the computer analysis of the experimental results obtained in this work.

By reference to the systematics of isomer shifts \( (\delta_{is}) \) in crystalline materials \([26]\), the distribution of \( \delta_{is} \) will be small, in comparison to the resonance width, in the case of a single valence state, coordination number, and nature of ligands of the Fe atoms. On the contrary, differing \( \delta_{is} \) are associated with different valence states or coordination numbers and these will be correlated to their quadrupole and magnetic hyperfine interactions. A reliable analysis of distributions of hyperfine interactions from Mössbauer data will be possible only in the former situation of negligible \( \delta_{is} \) distribution. In other cases, some correlations between parameters have to be assumed.
Assuming a unique value for \( \delta_{\text{gs}} \), the distribution function of the quadrupole splitting,

\[
\Delta = \frac{1}{2} e^2 q Q (1 + \frac{1}{2} \eta^2)^{1/2},
\]

can be directly deduced from paramagnetic data. It is noteworthy that quadrupole doublets will be symmetrical under the above assumption, whereas they will be asymmetric in the case of correlated distributions of \( \delta_{\text{gs}} \) and \( \Delta \) [27].

In the presence of additional magnetic interaction and in the absence of single ion anisotropy (e.g. the \( ^6S \) configuration of \( \text{Fe}^{3+} \)) one does not expect any directional correlation between local anisotropy (i.e. electric field gradient, \( E\text{FG} \)) axes and hyperfine field axes. A perturbation treatment of the quadrupole interaction on a magnetic interaction predicts an apparent cancellation of quadrupole effect in the case of random orientation (\( \theta \)) between \( E\text{FG} \) and \( H_{\text{hf}} \) axes. Indeed, the angular average of the quadrupole perturbation of the nuclear magnetic energy levels can be written to first order:

\[
\langle E_Q \rangle = \langle \frac{1}{8} e^2 q Q (3 \cos^2 \theta - 1) \rangle = 0.
\]

(The same result is obtained for non-axial \( E\text{FG} \) tensor.)

This means that the barycentres of the six magnetic resonance components are arranged symmetrically with respect to the isomer shift. However numerical calculation of the spectral shape reveals that each of the six lines actually is asymmetric in the presence of a defined sign of \( \Delta \) and when the asymmetry parameter (\( \eta \)) is small (Fig. 7). Similar conclusions are reached from analytical calculations [28]. The detection of such spectral asymmetry should allow information to be inferred concerning the sign of the principal component of the field gradient and/or the asymmetry parameter. In practice, such asymmetries will unfortunately be difficult to detect, owing to the relatively small field gradients acting at the nucleus of an \( S \)-state ion (\( \Delta(\text{Fe}^{3+}) < 1.5 \text{ mm/s} \)) and to the line broadening which will be induced by the concomitant \( \Delta \) and \( H_{\text{hf}} \) distributions. The latter contributions were neglected in the lineshape calculation of figure 7 in order to illustrate the principal effect of the angular distribution alone.

In summary, the random distribution of \( \theta \) provides to first order a symmetrical arrangement of the barycentres of the six resonance lines, each of these being equally broadened by a value \( \Delta W_{\theta} \) estimated as [29]:

\[
\Delta W_{\theta} = 2\sqrt{\langle E_Q^2 \rangle} = \frac{1}{\sqrt{5}} \Delta.
\]

Adding an isomer shift distribution to the random angular distribution produces a uniform broadening if the two distributions are independent. If they are correlated, asymmetry is induced [27]. An additional distribution in the modulus of the quadrupole splitting gives rise to a broadening which will be equal for all the magnetic components. This contribution sums up to the above-mentioned angular distribution effect. The resulting linewidth can be calculated from the sum of second moments of the two distributions or more simply as:

\[
W = W_L^2 + \Delta W_{\theta}^2
\]

where \( W_L \) is the linewidth observed in the paramagnetic phase.

An additional independent distribution of \( H_{\text{hf}} \) produces non-uniform line broadenings, in the ratio of the average transition energies of the components. Thus, unequal linewidths of the magnetic spectral components unequivocally characterize distribution in \( H_{\text{hf}} \).

The reliability of the analysis of combined distributions of hyperfine interactions is clearly limited and requires data of good statistical quality.

The hyperfine interaction distributions have been analysed numerically from the present experimental data according to the guidelines mentioned above. The Lorentzian component linewidth is constrained to an experimental value of 0.25 mm/s (measured against a thin reference absorber under identical conditions) and spectral shapes are calculated by computer summation according to the relevant hyperfine interaction distribution. For sample A, the paramagnetic spectra (42 < \( T < 670 \text{ K} \)) are very satisfactorily represented when it is assumed that there is constant isomer shift and a Gaussian distribution of the quadrupole splitting (Table I, Fig. 8).
Fig. 8. — Temperature dependence and shape of the distribution of quadrupole splitting in sample A.

The broadening appearing at 42 K corresponds to the onset of magnetic hyperfine effects (Fig. 8).

The nearly symmetric magnetic spectra which are observed at 4.2 K are successfully analysed using the full Hamiltonians of nuclear interaction with:

a) a constant isomer shift,
b) the Gaussian distribution of quadrupole splitting obtained from the paramagnetic phase ($\eta = 0$),
c) a spherical distribution for the polar angle $\theta$ between the EFG and $H_{hf}$ axes,
d) a Gaussian distribution of $H_{hf}$,
e) no correlations between these distributions (Fig. 9, Table V).

In order to lift this ambiguity an experiment was performed under applied field at a temperature which is sufficiently high so that the susceptibility is negligible. The experimental spectrum obtained in a field of 100 kOe at a temperature of 300 K [30] is compared to computer simulations (Fig. 10). These have been performed by numerical integration in order to represent the random orientation between effective field at the nucleus and EFG principal axis. The Gaussian distribution of $\Delta$ is included in the calculations ($\sigma_\Delta = 0.30$ mm/s). The Lorentzian component width is 0.30 mm/s, i.e. slightly broadened owing to the fringing magnetic field occurring at the source. A numerical fit of experimental data to the above model is impracticable because of prohibitive computer time. However, a visual inspection of the calculated spectral shapes reveals that a spectral asymmetry unequivocally demonstrates a weighting in sign of the $\Delta$ distribution and a value of the EFG asymmetry parameter $\eta$ differing significantly from unity (Fig. 10). The present experimental result (Fig. 10a) is adequately represented when assuming a positive sign only for the $\Delta$ distribution and $\eta = 0.5$ (Fig. 10b). Nevertheless, spectral shape simulations illustrate clearly that the deduced weight of the + and - wings in the $\Delta$ distributions is strongly correlated with the value of $\eta$. For instance, an asymmetric distribution in sign of $\Delta$ and a value of $\eta$ differing from unity is certainly consistent with the measurement. Summarizing, it may be pointed out that the external field measurement in the paramagnetic amorphous phase demonstrates unequivocally a significant weighting to positive sign of the $\Delta$ distribution and a value of $\eta$ deviating from unity. This information cannot be extracted reliably from the magnetic hyperfine data in the speromagnetic phase. However, the external field method does not allow simultaneous analyses of the sign distributions of $\Delta$ and of the value of $\eta$.

<table>
<thead>
<tr>
<th>$T$ (K)</th>
<th>$\Delta$ (mm/s)</th>
<th>$q$ (mm/s)</th>
<th>$\Delta$ (mm/s)</th>
<th>$\sigma_\Delta$</th>
<th>$E_{hf}$ (kOe)</th>
<th>$\sigma_B$</th>
</tr>
</thead>
<tbody>
<tr>
<td>4.2</td>
<td>0.34</td>
<td>0.25</td>
<td>1.08</td>
<td>0.3*</td>
<td>425</td>
<td>23</td>
</tr>
<tr>
<td></td>
<td>0.36</td>
<td>0.8</td>
<td>0</td>
<td>431</td>
<td>19</td>
<td></td>
</tr>
</tbody>
</table>

(*) Fixed values.
Fig. 10. a) Mössbauer spectrum of sample A measured at 300 K in an external field of 100 kOe. The solid lines represent spectral lineshapes computed for a random orientation between the EFG and effective field (95 kOe) axes and for a Gaussian distribution of \( \Delta \) (\( \Delta = 1.08 \) mm/s, \( \sigma_\Delta = 0.30 \) mm/s, Lorentzian width of 0.30 mm/s); b) \( \Delta \) distribution of positive sign only, \( \eta = 0.5 \); c) as in b), \( \eta = 0 \); d) as in b), \( \eta = 1 \); e) equal weights of positive and negative signs of \( \Delta \), \( \eta = 0 \).

The Qs distributions are well represented by broadened Lorentzian lines (Table II). The magnetic data at 4.2 K are satisfactorily fitted using a perturbation calculation (Eq. (2)): the \( \delta \) difference between the two components was constrained to the value determined in the paramagnetic phase. For the Fe\(^{3+} \) component the effect of the quadrupole splitting distribution and of the random orientation of the EFG and \( H_{\text{hf}} \) axes was introduced as a uniform line broadening (Eqs. (1) and (2)) (Table II). For the Fe\(^{2+} \) ions, owing to the single ion anisotropy, the EFG and \( H_{\text{hf}} \) axes are strongly correlated; thus \( \theta \) is expected to present a defined value contrary to Fe\(^{3+} \) ions.

A satisfactory fit is achieved (Fig. 4) even with a single Fe\(^{2+} \) magnetic component by letting the angle \( \theta \) for this site as a free parameter (Table II). However, a wide distribution of \( H_{\text{hf}} \) would be expected for Fe\(^{2+} \) ions as a result of the sensitivity of this parameter to orbital effects. Because of the low intensity of this site and the lack of spectral resolution the fit is actually insensitive to such effects. Thus, we believe that the deduced standard deviation of the Fe\(^{3+} \) Gaussian \( H_{\text{hf}} \) distribution is reliable.

The decomposition of the paramagnetic data of the more concentrated sample C into two broadened symmetric quadrupole doublets establishes the occurrence of Fe\(^{3+} \) ions only; these are distributed among octahedral and tetrahedral coordination sites as shown by the 0.13 mm/s difference in isomer shifts. Consistent with the paramagnetic data, the saturation magnetic data (4.2 K) are analysed (using the perturbation calculation (Eq. (2)), in terms of two magnetic subspectra with randomly distributed EFG and \( H_{\text{hf}} \) axes. The average fields are \( H_{\text{hf}}(O_8) \approx 500 \) kOe and \( H_{\text{hf}}(T_d) \approx 445 \) kOe while the deviations of their Gaussian distributions are respectively 23 and 9.5 kOe (Table III, Fig. 5). The values of the hyperfine fields further confirm the attribution of the subspectra to octahedral and tetrahedral coordination of Fe\(^{3+} \).

5. Magnetic transitions and orderings in the amorphous oxides Fe\(_2\)O\(_3\)-BaO-B\(_2\)O\(_3\). — Combining the present Mössbauer data with the published bulk magnetic results [19, 23], three types of magnetic behaviour can be identified, corresponding respectively to low — (sample D), intermediate — (samples A, B) and high — (sample C) concentration range of magnetic ions.

Sample A is most easily discussed since here the iron occurs in a single valence state (Fe\(^{3+} \)) and coordination (tetrahedral). Above 42 K, the Mössbauer spectra reveal paramagnetic behaviour. Between 42 and 29 K, relaxation effects are observed in terms of coexisting unresolved magnetic and central paramagnetic subspectra (Fig. 2), with the relative intensity of the latter decreasing as temperature is lowered. Below 29 K, resolved magnetic spectra appear. Application of an external field up to 45 kOe induces
merely a line broadening both in the intermediate
temperature range (40-34 K, Fig. 11) and at 4.2 K
(Fig. 3). In particular, at the latter temperature, no
polarization of magnetization is induced since the
relative areas of the spectral components are unaf-
affected by the external field (Fig. 3).

Among the conceivable explanations for the measured
temperature dependence, small particle super-
paramagnetism is definitely ruled out on the basis
of the following arguments: electron microscopy
(resolution: ~50 Å) does not reveal small particles
and magnetization data do not show the \( \sigma \) vs. \( H/T \)
superposition behaviour, typical for non-interacting
superparamagnetic particles [20, 23]. In a true super-
paramagnet, the nearly saturated magnetic component
should coexist in the Mössbauer spectrum with the paramagnetic doublet [31], contrary to experiment. Finally, in the temperature range from 35
to 45 K, a large magnetic splitting would be predicted
for small magnetic particles at an external field of
45 kOe, which is not observed (Fig. 11). Paramagnetic
relaxation effects are ruled out because of the narrow
temperature range of the smeared spectra and from
the spectral shape evolution.

Magnetic ordering with a wide distribution in transition temperatures cannot account for the results since the components which would order at the higher temperature (40 K) should already be resolved at 35 K. Distribution of molecular field from site to site according to the near neighbour atomic environ-
ment induces also significant line broadening in the vicinity of a homogeneous ordering temperature [32].

However, in this model, the broadening should extend to reduced temperatures \( T/T_s \) much lower than the experimentally observed value of 0.75. All the above cited Mössbauer results, along with the irreversible magnetization effects, the external field dependence of the dc susceptibility [23] and the ac susceptibility cusp characterize a mictomagnetic transition [25]. The temperature dependence of Möss-
bauer spectra between 40 and 30 K is very similar to
that predicted from a model of spherical relaxation,
with a relaxation rate decreasing at lower tempera-
ture [33, 34]. However, tentative fits with such a model show that a distribution of relaxation rates should be considered.

A spherical relaxation mechanism with a narrow distribution in relaxation rate (or freezing tempera-
tures) has already been concluded from Mössbauer results in an established spin glass system : 
\( \text{Eu}_{1-x}\text{Gd}_x\text{S} \) [35]. The mictomagnetic transition occurring in the present oxide glass is understood in terms of a progressive freezing of magnetic clusters arising from frustration effects, similar to the picture originally introduced by Tholence and Tournier [36]. Contrary to early assumptions [36], strong interactions couple the magnetic clusters via dipolar or (and) frustrated exchange interactions, as indicated by the negligible effect of the external field in the vicinity of the spin freezing temperature (\( T_f \)). The frequency
dependence of \( T_f \) which is revealed by the difference
between the ac susceptibility cusp and the Mössbauer transition temperature, further confirms a freezing
mechanism with significant interactions among clusters. Such interactions between magnetic clusters
have been repeatedly invoked to explain the peculiar properties of the mictomagnetic transition, in particu-
lar to account for the Fulcher law dependence of the relaxation rate in the vicinity of the spin freezing
temperature [37-40].

Because of frustration effects, which are intrinsic
to an amorphous solid with antiferromagnetic exchange, the magnetic structure is speromagnetic,
i.e. random freezing of the spins [3]; antiferromagne-
tic-like order extends at the most over a few inter-
atomic distances. The speromagnetic structure at
4.2 K is revealed by the absence of any detectable
polarization in an external field of 45 kOe. This type
of order is already indicated by the very low induced
magnetization (~ \( 10^{-2} \) of saturation value) and by
the absence of saturation up to 150 kOe.

The magnetic transitions occurring in the other
glasses have been investigated in less detail, owing to the additional complexity introduced by the presence of several coordinations and valence states of the iron ions. The narrow temperature range of the trans-

Fig. 11. — Mössbauer spectra of sample A measured at
35 K without (a) and with an external field of 45 kOe (b).
fication of the two valence states within the amorphous solid.

The temperature dependence of the Mössbauer spectra at high concentration in magnetic ions (sample C) is suggestive of small particle super-paramagnetism (Fig. 5). Indeed, one observes superposed paramagnetic and magnetic spectra over a wide temperature range (60-200 K) and the nearly saturated hyperfine field component appears already at high temperature. The observed temperature dependence is attributed to a progressive freezing of magnetization relaxation, with however much smaller interactions between clusters than in the intermediate concentration range (samples A, B). The latter conclusion contradicts the usual behaviour involving an increase of intercluster interactions with concentration of magnetic ions as found for instance in Eu₂Sr₁₋ₓS [39]. The observation is attributed to amorphous phase segregation in the present oxide glasses, i.e., the iron ions are no longer statistically distributed within the glass in sample C. Clusters of relatively high Fe concentration coexist with regions depleted in this element, so that the interaction among clusters becomes negligible. The broad distribution of relaxation rate (or cluster size) may be connected with the occurrence of both tetrahedral and octahedral coordinations of the Fe³⁺ ions, thus inducing more severe frustration effects than in sample A for instance.

In the less concentrated sample (D), the appearance, at 1.5 K, of a magnetically split component superimposed on the paramagnetic quadrupole doublet in the Mössbauer spectra is attributed to paramagnetic relaxation effects for some of the iron ions (Fig. 6). Measurements at 4.2 K in large external magnetic fields (up to 80 kOe) reveal a magnetic splitting for a fraction of the Fe³⁺ ions (Fig. 12). For one component, the field dependence follows a Brillouin behaviour ($\mu = 5 \mu_B$) indicating that the outer lines correspond to isolated paramagnetic Fe³⁺ ions. Another fraction (the central part of the spectra) does not split at all and merely feels the external field. This component is attributed to antiferromagnetically coupled dimers. The intermediate spectral lines correspond to an effective field of approximately 280 kOe; these are tentatively attributed to antiferromagnetic coupled trimers [18].

The magnetic properties discussed above concern mainly the low temperature data. Little attention has been paid to the high temperature behaviour i.e. the strong reduction of the calculated Curie constant (or effective paramagnetic moment) when compared to the expected free ion value. For sample A, for example, $C = 1.52$ while the Fe³⁺ free ion value amounts 4.38. Ferey et al. [16] explain the lowering of the Curie constant in amorphous FeF₃ under the assumption of a spread in magnitude of the antiferromagnetic exchange interactions as a consequence of frustration effects. It is surprising that in other systems, e.g. the cobalt and manganese alumino-
silicate glasses, the paramagnetic Curie constants are found to be in agreement with the free ion values [41]. We suggest that the reduction of the Curie constant in the present systems arises from short-range antiferromagnetic coupling persisting up to temperatures much higher than the spin freezing temperature, so that some of the Fe³⁺ moments would not contribute to the Curie constant. A similar explanation has been already invoked to account for the magnetic behaviour of CuMn alloys [25] and of the Fe₂TiO₅ spin glass [42].

6. Electronic and structural properties of the amorphous oxides : Fe₂O₃-BaO-B₂O₃. — By comparing the $^{57}$Fe isomer shifts and average hyperfine fields data to those established in crystalline systems [26], it is concluded that sample A contains only Fe³⁺(₄S) ions in tetrahedral coordination. It is of interest to notice that the phase initially crystallized from this sample (BaFe₂O₄) similarly presents a tetrahedral Fe³⁺ coordination unit (See below Section 7). In samples B and D, both Fe²⁺(²D) and Fe³⁺(₄S) valence states coexist. In sample C, one observes the Fe³⁺ valence state only, but in both octahedral and tetrahedral coordinations. The average iron to oxygen coordination number is definitely correlated with the atomic ratio of the elements present in the glass, in agreement with earlier conclusions [13].

The occurrence at low iron concentration (sample D)
of small clusters (dimers, trimers) coexisting with isolated Fe$^{3+}$ ions agrees with previous report [18]. This feature appears to be general for iron-based oxide glasses. The presence of such clusters in glasses with Fe$_2$O$_3$ concentration as low as 0.05 wt. % has also been concluded from the concentration dependence of the linewidth of the Fe$^{3+}$ EPR spectra in sodium silicate glasses [43]. At high iron concentration (sample C), the non-random distribution of Fe ions revealed by the pseudo-superparamagnetic behaviour has already been claimed in other systems [17].

The distribution of quadrupole splitting, observed in all samples is attributed to fluctuations in bond distances and angles. The recent investigation of simple ionic insulating glasses (a-Y$_3$Fe$_2$O$_{12}$ and a-FeF$_3$) has been complemented by computer modelling of their amorphous structure [4]. The computer models were constructed using a random packing of hard spheres (RPHS) with the additional requirement that ions of identical charge be separated as far as possible within the building algorithm [4]. Using a point charge model, this technique permits generation of histograms for the quadrupole splitting distributions [44]. An analytic form for these can be written as:

$$P(\Delta) = (\Delta^{d-1}/\sigma^d) \exp(-\Delta^2/2\sigma^2)$$  \hspace{1cm} (3)$$

with $d = 5$ for the RPHS model [44, 45]. These calculations consistently predict that the $\Delta$ distributions contain approximatively as many positive as negative values and that the marginal distribution, $P(\eta)$ of the asymmetry parameter increases with $\eta$. The function (Eq. (3)) with $d = 2$, which takes into account some degree of short-range order has been successfully applied to amorphous FeF$_3$ for instance [46]. For sample A, where the analysis of the $\Delta$ distribution is performed unequivocally, neither of the functions (Eq. (3)) with $d = 2$ or $d = 5$ provide an adequate description of the data. By contrast, a Gaussian distribution provides an excellent fit (Table I). This indicates more short-range order than in a-FeF$_3$. Also, our results establish significant asymmetry in the sign distribution of the EFG principal component and deviation of $\eta$ from unity, in disagreement with the predictions from the above random models. It is to be noted that in most of the published works the sign of the EFG has not been determined. In summary, the present discrepancies with the RPHS model demonstrate a considerable complexity of the BaO-Fe$_2$O$_3$ phase diagram is taken into consideration [48].

In the measurements performed at successive annealing temperatures up to 843 K, a superposition of several quadrupole doublets was always observed; no significant anomaly in the Debye-Waller factor or in the resonance intensity is observed at any of the selected temperatures of measurement under present experimental conditions.

The phase analysis of the systems obtained on thermal annealing is best performed after quenching at low temperature, by comparing the Mössbauer spectra to those reported in the literature for the crystalline phases of the BaO-Fe$_2$O$_3$ phase diagram [49, 50]. After annealing at 773 K, the 4.2 K Mössbauer spectrum reveals the superposition of a new magnetic hyperfine spectrum ($H_{hf} = 462$ kOe) in addition to the magnetic spectrum of the amorphous phase (Fig. 13). This is attributed to a partial crystallization of BaFe$_2$O$_4$ coexisting with the original amorphous phase. However at a measurement temperature of 77 K, no magnetic hyperfine spectrum is observed. Thus, the resulting BaFe$_2$O$_4$ crystals ($T_N = 880$ K) exist as small particles and show superparamagnetic behaviour. After annealing at 803 K, the amorphous component disappears and all the iron is in the form of superparamagnetic BaFe$_2$O$_4$ microcrystalline particles. After annealing at 823 K, the spectrum measured at 4.2 K shows the superimposition of a central «paramagnetic» doublet and of the BaFe$_2$O$_4$ spectrum. At a measurement temperature of 77 K, a magnetic component coexists.
Fig. 13. Mössbauer spectra measured after crystallization of sample A: a) measured at 4.2 K after annealing at 773 K; b) measured at 300 K, after annealing at 1053 K.

with this doublet, thus demonstrating a growth of the \( \text{BaFe}_2\text{O}_4 \) particle size; the latter progressively lose their superparamagnetic character. The relative intensity of the new "paramagnetic" doublet measured at 4.2 K and 77 K increases upon thermal annealing at 853 K, 873 K and 1053 K at the expense of the \( \text{BaFe}_2\text{O}_4 \) spectrum. At this last annealing temperature, the formation of crystalline barium hexaferrite is clearly proven from the observation of three magnetic subspectra, typical for this phase at 300 K (Fig. 13). The observed behaviour is thus attributed to the progressive transformation upon annealing above 823 K of crystalline \( \text{BaFe}_2\text{O}_4 \) into \( \text{BaFe}_{12}\text{O}_{19} \), which is first formed as small superparamagnetic particles whose size increases on further thermal annealing.

The present conclusion agrees with that suggested previously from X-ray and electron diffraction studies.

8. Conclusion. — The valence configuration and the structural environment of the magnetic ions (Fe) present in the glasses \( \text{Fe}_2\text{O}_3\)-BaO-B\( _2\text{O}_3 \) are identified from Mössbauer spectroscopy. The nature of the valence states (Fe\( ^{2+}, \text{Fe}^{3+} \)) is affected by preparative conditions while the average coordination is determined by the atomic ratio of the elements present in the glass.

The distribution of hyperfine parameters is discussed extensively for one sample in which the magnetic ions occur in single valence state and coordination. The quadrupole splitting \( \Delta \) displays a Gaussian distribution function; in the magnetic state, the magnetic axis is at random with the EFG axis, as expected for an S-state (Fe\( ^{3+} \)) ion without single ion anisotropy. The hyperfine field also presents a distribution of Gaussian shape. The sign distribution of \( \Delta \) should in principle be obtainable from the magnetic hyperfine data; this procedure is unfortunately impracticable when considering the experimental precision and the intrinsically small values of \( \Delta \). High temperature measurement under applied magnetic field unambiguously reveal the strong weighting to positive sign of the \( \Delta \) distribution and a value of \( \eta \) centred around 0.5. The Gaussian distribution function of \( \Delta \), the weighting in sign of the \( \Delta \) distribution and the average value deduced for \( \eta \) demonstrate significant short-range order, for instance, a defined tetrahedral coordination of the Fe\( ^{3+} \) ions, with random fluctuations of bonding angles and distances. This is equivalent to the random coordination model. A random packing of spheres is totally ruled out in the present glasses.

Magnetic exchange is essentially antiferromagnetic in these glasses, as deduced from the large negative Curie-Weiss temperature. The structural disorder is responsible for the distribution in superexchange interactions; therefore, the systems are highly frustrated from a magnetic point of view. A micromagnetic transition is consistently established at intermediate Fe\( _2\text{O}_3 \) concentration (30%) from Mössbauer results, irreversible remanence and a cusp in dynamic susceptibility. This transition is understood in terms of a progressive freezing of strongly interacting magnetic clusters. Consistent with frustration, the low temperature magnetic structure is speromagnetic, i.e. random freezing of the spins. However, the range of antiferromagnetic order cannot be fully specified in absence of neutron spectroscopy data. At small (5%) Fe\( _2\text{O}_3 \) concentration, the glass does not order down to 1.5 K; however, local moments measured in an external field reveal the coexistence of isolated ions along with clusters on the atomic scale (dimers, trimers, etc.). At large Fe\( _2\text{O}_3 \) concentration (50%), the system shows a quasi-superparamagnetic behaviour. This is attributed to heterogeneity of the iron distribution within the glass; therefore, the micromagnetic transition corresponds to the freezing of clusters with weak interactions between them, thus showing up over a wide temperature range in Mössbauer spectroscopy.

The crystallization of the glasses proceeds in a complex sequence. The successive formation of barium ferrites up to the hexaferrite is revealed by Mössbauer spectroscopy, consistent with diffraction results. These phases form first as small particles (revealed by their superparamagnetic characteristics) and subsequently evolve in size.

Acknowledgments. — We thank H. Laville and J. C. Bernier for providing the samples used in this work and for helpful discussions.
References


[29] The collaboration of P. Beuvillaun and J. P. Renard in performing the ac-susceptibility measurements on sample A is gratefully acknowledged.


