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▶ To cite this version:

Christian J Michel, Jean-Sébastien Sereni. Reading frame retrieval of genes: a new parameter of codon usage based on the circular code theory. Bulletin of Mathematical Biology, 2023, 85 (4), pp.24. 10.1007/s11538-023-01129-4 . hal-03788021

HAL Id: hal-03788021 https://hal.science/hal-03788021

Submitted on 26 Sep 2022

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Reading frame retrieval of genes: a new parameter of codon usage based on the circular code theory

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ABSTRACT. Based on the circular code theory, we define a new function f that quantifies the property of reading frame retrieval (RFR) of genes from their codon usage. This RFR function f is computed on a massive scale in genes of genomes of bacteria, eukaryotes and archaea. By expressing f as a function of the mean number \overline{n} of codons per gene, a "universal" property is identified, whatever the kingdom: the reading frame retrieval is enhanced in large genes. By investigating this property according to the theory developed, a Spearman's rank correlation with a strong negative coefficient is observed between the codon usage dispersion d (from the uniform codon distribution $\frac{1}{64}$) and the RFR function f, whatever the kingdom (p-values $< 10^{-180}$ in bacteria, $< 10^{-61}$ in eukaryotes and $< 10^{-159}$ in archaea). Thus, the reading frame retrieval is enhanced with the codon usage dispersion. Furthermore, this approach identifies a "genome center" from which emerge two distinct "genome arms": an upper arm and a lower arm, respectively above and below the linear regression. The RFR function by itself or combined with classical methods (alignment, phylogeny) could also be a new approach to classify the genomes in the future.

1. Introduction

The genetic code is a surjective map between the 64 trinucleotides and the 20 amino acids plus 1 stop signal. Thus, there are codons, called synonymous, coding the same amino acid, except methionine and tryptophan that are encoded by a single codon, ATG and TGG, respectively. Synonymous codons have different frequencies between genomes of different species, as well as between genes within a given genome. This statistical property is known as codon usage bias (CUB). CUB influences different aspects of protein production [11] and codon choice has effects at many biological stages, including transcription [37], translation efficiency [28], mRNA stability [27], protein folding [3] and protein function [2].

A great number of statistical parameters have been defined to analyse CUB, to mention a few: the Effective Number of Codons (ENC) [34], the GC content (GC), the GC content at third codon

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Date: September 26, 2022.

Key words and phrases. circular code theory; reading frame retrieval; codon usage; gene length; codon dispersion.

positions (GC3), the Relative Synonymous Codon Usage (RSCU) [31], the Codon Adaptation Index (CAI) [30], the Frequency of Optimal Codons (FOC) [13], the Relative Codon Bias (RCB) and the Relative Codon Bias Strength (RCBS) [29], the Relative Codon Adaptation (RCA) [10] and the Codon Deviation Coefficient (CDC) [36]. Combination of two parameters allow the creation of 2D plots, for example: ENC plot to investigate codon usage across genes [12], neutrality plot to analyse the effects of natural selection and mutation pressure on codon usage [35] and parity rule 2 (PR2) plot to evaluate the effect of mutation pressure and natural selection at the third codon position of the four-codon amino acids [35]. Factorial statistical methods, such as the Correspondence Analysis (CA) [11], the Principal Component Analysis (PCA) [14], etc., also allow the codon usage to be studied.

The circular code theory has been initiated in 1996 by the identification in genes of bacteria and eukaryotes, of a maximal C^3 self-complementary circular code, a particular set called X of 20 trinucleotides with interesting mathematical properties allowing to retrieve the reading frame and the two shifted frames [1]. In 2017, it has been shown that this circular code X is also found in genes of archaea, plasmids and viruses [16]. The historical context of this result is described in a recent article [17]. We also refer the reader to the reviews [9,15] for the biological context and the main combinatorial studies of circular codes.

This unexpected biological result has led to several mathematical developments since 1996: (i) the flower automaton [1]; (ii) the necklaces LDN (letter diletter necklace) and DLN (diletter letter necklace) [21, 22, 26] extended to (n + 1)LDCCN (letter diletter continued closed necklaces) [20]; (iii) the group theory [5]; and (iv) the recent and powerful approach based on graph theory in 2016 [8]. The graph approach has recently led to two important generalizations: mixed circular codes [6] and k-circular codes [7, 19, 23].

These theoretical results have led to biological applications, to name a few recent ones: identification of "universal" circular code motifs in the ribosome leading to a model of genetic code evolution associating codes, translation systems, and peptide products at different stages from the primordial translation building blocks to the ancestor of the modern ribosome present in the Last Universal Common Ancestor (LUCA) [4]; identification of a circular code periodicity (modulo 3) in a large region of the 16S rRNA including the 3' major domain corresponding to the primordial protoribosome decoding center, containing numerous sites that interact with the tRNA and messenger RNA (mRNA) during translation and surrounding the mRNA channel [24]; potential role of the circular code X in the regulation of gene expression [33]; and characterization of accessory genes in coronavirus genomes using the circular code information [18].

On the genetic alphabet \mathcal{B} , there are $n = 2^{64} - 1 \approx 10^{19}$ (non-empty) trinucleotide codes: 64 codes of cardinality 1: {AAA}, ..., {TTT}, 2016 codes of cardinality 2: {AAA, AAC}, ..., {TTG, TTT}, 41664 codes of cardinality 3: {AAA, AAC, AAG}, ..., {TTC, TTG, TTT} up to 1 code of cardinality 64 (the genetic code): {AAA, ..., TTT}. The recent theory of trinucleotide k-circular codes makes it possible to study the property of reading frame retrieval, called circularity property, of any of these $\approx 10^{19}$ codes [19,23]. Indeed, these codes can be classified into 3 classes according to their circularity property:

 (i) 15 trinucleotide codes with no circularity: no sequence generated by such a trinucleotide code can retrieve the reading frame;

- (ii) n 15 115606988558 trinucleotide codes with a partial circularity: some sequences generated by such a trinucleotide code cannot retrieve the reading frame, but some some other sequences can retrieve the reading frame;
- (iii) 115606988558 trinucleotide codes with a complete circularity (circular codes): any sequence generated by such a trinucleotide circular code can retrieve the reading frame.

The property of reading frame retrieval of trinucleotide codes is analysed with a function defined in [23, Definition 6.1] and recalled below with Definition 2.10. The theoretical work here extends this function to weighted trinucleotide codes with the new Definition 2.12. Such a quantitative parameter to retrieve the reading frame has never been proposed to date. Furthermore, we show here that this RFR function f can be applied in a biological context to the codon usage, of a gene or a set of genes. By computing this RFR function f on a massive scale in genes of genomes of bacteria, eukaryotes and archaea, new properties associated with reading frame retrieval are identified.

This article is organised as follows. The necessary definitions and notations of trinucleotide codes, circular codes and their generalization to k-circular codes are gathered in Section 2.1. The definition of mean number of codons per gene is recalled in Section 2.2. Section 2.3 defines the dispersion function of codon usage and states a proposition about its interval. Section 2.4 defines the reading frame retrieval (RFR) function and states several propositions concerning its interval and its particular value 1 associated with a uniform codon usage. Section 2.5 describes the acquisition of codon usage for the genomes of bacteria, eukaryotes and archaea from the codon statistics database (CSD) [**32**]. As an example, the value of the RFR function for *Homo sapiens* is given in Section 2.6.

The results are presented in three parts. Section 3.1 demonstrates that the reading frame retrieval is enhanced in large genes, in bacteria, eukaryotes and archaea. Section 3.2 shows that the reading frame retrieval is correlated with the dispersion of codon usage and identifies a "genome center" from which emerge two distinct "genome arms", also in bacteria, eukaryotes and archaea. The results previously obtained as well as a study (done by accident) of codon usage in bird genomes suggest that the RFR function could be a new approach to classify genomes (Section 3.3).

2. Method

2.1. Definitions and notations. For the reader's convenience we here recall the most relevant notions, in order to have this article self-contained. The theoretical aspects, with computer results, proofs, examples, remarks, illustrations and refinements are found in the articles [19,23]. We work with the genetic alphabet $\mathcal{B} \coloneqq \{A, C, G, T\}$, which has cardinality 4. An element N of \mathcal{B} is called nucleotide. A word over the genetic alphabet is a sequence of nucleotides. A trinucleotide is a sequence of 3 nucleotides, that is, using the standard word-theory notation, an element of \mathcal{B}^3 . If $w = N_1 \cdots N_s$ and $w' = N'_1 \cdots N'_t$ are two sequences of nucleotides of respective lengths s and t, then the concatenation $w \cdot w'$ of w and w' is the sequence $N_1 \cdots N_s N'_1 \cdots N'_t$ composed of s + t nucleotides.

Given a sequence $w = N_1 N_2 \cdots N_s \in \mathcal{B}^s$ and an integer $j \in \{0, 1, \dots, s-1\}$, the *circular j-shift* of w is the word $N_{j+1} \cdots N_s N_1 \cdots N_j$. Note that the circular 0-shift of w is w itself. A sequence w' of nucleotides is a *circular shift* of w if w' is the circular j-shift of w for some $j \in \{0, 1, \dots, s-1\}$.

The elements in \mathcal{B}^3 can thus be partitioned into conjugacy classes, where the *conjugacy class* of a trinucleotide $w \in \mathcal{B}^3$ is the set of all circular shifts of w.

DEFINITION 2.1. Let \mathcal{B} be the genetic alphabet.

- A trinucleotide code is a subset of \mathcal{B}^3 , that is, a set of trinucleotides.
- If X is a trinucleotide code and w is a sequence of nucleotides, then an X-decomposition of w is a tuple $(x_1, \ldots, x_t) \in X^t$ of trinucleotides from X such that $w = x_1 \cdot x_2 \cdots x_t$.

We now formally define the notion of circularity of a code, i.e. the property of reading frame retrieval.

DEFINITION 2.2. Let $X \subseteq \mathcal{B}^3$ be a trinucleotide code.

- Let *m* be a positive integer and let $(x_1, \ldots, x_m) \in X^m$ be an *m*-tuple of trinucleotides from *X*. A circular *X*-decomposition of the concatenation $c \coloneqq x_1 \cdots x_m$ is an *X*decomposition of a circular shift of *c*.
- Let k be a non-negative integer. The code X is $(\geq k)$ -circular if every concatenation of trinucleotides from X that admits more than one circular X-decomposition contains at least k + 1 trinucleotides. In other words, X is $(\geq k)$ -circular if for every $m \in \{1, \ldots, k\}$ and each m-tuple (x_1, \ldots, x_m) of trinucleotides from X, the concatenation $x_1 \cdots x_m$ admits a unique circular X-decomposition. The code X is k-circular if X is $(\geq k)$ -circular and not $(\geq k + 1)$ -circular.
- The code X is *circular* if it is $(\geq k)$ -circular for all $k \in \mathbf{N}$.

We recall the definition of the graph associated with a trinucleotide code [8].

DEFINITION 2.3. Let $X \subseteq \mathcal{B}^3$ be a trinucleotide code. We define a graph $\mathcal{G}(X) = (V(X), E(X))$ with set of vertices V(X) and set of arcs E(X) as follows:

• $V(X) := \bigcup_{N_1N_2N_3 \in X} \{N_1, N_3, N_1N_2, N_2N_3\};$ and

•
$$E(X) \coloneqq \{N_1 \to N_2 N_3 : N_1 N_2 N_3 \in X\} \cup \{N_1 N_2 \to N_3 : N_1 N_2 N_3 \in X\}$$

The graph $\mathcal{G}(X)$ is the graph associated to X.

The *length* of a directed cycle in a graph \mathcal{G} is the number of arcs of the cycle. We note that every arc of $\mathcal{G}(X)$ joins a nucleotide and a dinucleotide. Thus, the graph $\mathcal{G}(X)$ cannot contain a directed cycle of odd length. A theorem [7, Theorem 3.3] implies that a cycle in $\mathcal{G}(X)$, if any, must have length in $\{2, 4, 6, 8\}$ and, in particular, that a trinucleotide (≥ 4)-circular code must be circular. As noted in a previous article [19], it follows that all trinucleotide codes over \mathcal{B} can be naturally partitioned into 5 classes using the following definition.

DEFINITION 2.4. We define the *circularity* cir(X) of a non-empty trinucleotide code X to be the largest integer $k \in \{0, 1, 2, 3, 4\}$ such that X is $(\geq k)$ -circular.

Thus, the possible values of cir(X) for a trinucleotide code X are 0, 1, 2, 3, 4, which determine the 5 classes.

Next we introduce two new functions, which turn out to be correlated. The first one deals with the dispersion of the codon usage, and the second one, which uses the graph, deals with the property of reading frame retrieval of genes. These two functions are also analysed as a function of the mean number of codons per gene in each genome.

2.2. Mean number of codons per gene in a genome.

DEFINITION 2.5. The mean number \overline{n} of codons per gene in a genome is the total number of codons divided by the total number of genes in the genome.

2.3. Dispersion of codon usage. A codon usage is *uniform* if every codon has the same occurrence frequency. The following function measures the dispersion of codon usage with respect to the uniform one. We write X_g for the genetic code of cardinality 64 (maximal cardinality in \mathcal{B}^3).

DEFINITION 2.6. Given any trinucleotide code X, a weight function on X is a function $\omega \colon X \to [0, 1]$ such that $\sum_{x \in X} \omega(x) = 1$.

DEFINITION 2.7. A weighted trinucleotide code is a pair (X, ω) where X is a trinucleotide code and ω is a weight function on X.

We can now define the dispersion of codon usage.

DEFINITION 2.8. For every weight function $\omega \colon X_g \to [0,1]$, the dispersion of codon usage in (X_g, ω) is the function d given by

(2.1)
$$d((X_g,\omega)) = \sum_{x \in X_g} \left| \omega(x) - \frac{1}{64} \right|.$$

The next proposition gives the extremal values taken by the function d.

PROPOSITION 2.9. For every weight function $\omega: X_g \to [0,1]$, we have

$$0 \le d((X_g, \omega)) \le \frac{63}{32} \approx 1.97$$

Moreover, $d((X_g, \omega)) = 0$ if and only if $\omega(x) = \frac{1}{64}$ for each trinucleotide $x \in X_g$. The upper bound is attained if and only if there is a trinucleotide $x \in X_g$ such that $\omega(x) = 1$ (and hence $\omega(x') = 0$ if $x' \neq x$).

PROOF. The argument is standard. Consider an arbitrary weight function $\omega \colon X_g \to [0,1]$ on X_g and recall that $\sum_{x \in X_g} \omega(x) = 1$. We define

$$X^+ = \left\{ x \in X : \omega(x) > \frac{1}{64} \right\}$$

and

$$X^{-} = \left\{ x \in X : \omega(x) \le \frac{1}{64} \right\}.$$

In particular, $|X^+| + |X^-| = |X_g| = 64$. Now,

$$d((X_g, \omega)) = \sum_{x \in X^+} \left(\omega(x) - \frac{1}{64} \right) + \sum_{x \in X^-} \left(\frac{1}{64} - \omega(x) \right)$$

= $\frac{1}{64} \cdot (|X^-| - |X^+|) + \sum_{x \in X^+} \omega(x) - \sum_{x \in X^-} \omega(x)$
= $\frac{1}{64} \cdot (64 - 2 \cdot |X^+|) + 2 \cdot \sum_{x \in X^+} \omega(x) - 1$
= $2 \cdot \left(\sum_{x \in X^+} \omega(x) - \frac{|X^+|}{64} \right)$

where the third line uses that $|X^-| = 64 - |X^+|$ and $\sum_{x \in X^-} \omega(x) = 1 - \sum_{x \in X^+} \omega(x)$. Now, if $|X^+| = 0$ then $\sum_{x \in X^+} \omega(x) = 0$, and hence $d((X_g, \omega)) = 0$ and moreover ω is constantly equal to $\frac{1}{64}$ (because $\omega(x) \leq \frac{1}{64}$ for every $x \in X = X^-$ and $\sum_{x \in X} \omega(x) = 1$). If $|X^+| \neq 0$ then $|X^+| \geq 1$ and therefore $d((X_g, \omega)) \leq 2(1 - \frac{1}{64}) = \frac{63}{32}$, with equality if and only if $|X^+| = 1$ and $\sum_{x \in X^+} \omega(x) = 1$, which ends the proof.

2.4. Gene reading frame retrieval (RFR) function associated with a codon usage. Theoretical considerations over trinucleotide codes led to the following definition [23, Definition 6.1] as a measure of the reading frame retrieval of genes. Indeed, the number and length of cycles in the graph are associated with ambiguous sequences that do not retrieve the reading frame. Short cycles are associated with short ambiguous sequences, i.e. the reading frame is lost quickly (after 1 trinucleotide), in contrast to long cycles where the ambiguous sequences are long, i.e. the reading frame is lost after several trinucleotides, up to 4 trinucleotides (see [19,23] for details).

DEFINITION 2.10 ([23, Definition 6.1]). The reading frame loss function f of a trinucleotide code X is the mapping $f: \mathcal{B}^3 \to \mathbf{R}$ given by

(2.2)
$$f(X) \coloneqq q_8(\mathcal{G}(X)) + \frac{4}{3}q_6(\mathcal{G}(X)) + 2q_4(\mathcal{G}(X)) + 4q_2(\mathcal{G}(X)) = \sum_{i=1}^4 \frac{4}{i} \cdot q_{2\cdot i}(\mathcal{G}(X))$$

where $q_i(\mathcal{G})$ is the number of directed cycles of length *i* in the graph \mathcal{G} for every positive integer *i*.

Note that f(X) is always a rational number, but not necessarily an integer. The next proposition [23] gives the minimum and maximum values taken by f over all trinucleotide codes.

PROPOSITION 2.11 ([23, Proposition 6.2]). For every trinucleotide code X, we have $0 \le f(X) \le$ 301056. Moreover, f(X) = 0 if and only if X is a trinucleotide circular code, and f(X) = 301056 if and only if X is the genetic code X_g , where

$$q_2(X_g) = 64,$$
 $q_4(X_g) = 1440,$ $q_6(X_g) = 26880,$ $q_8(X_g) = 262080.$

We generalise the function f to the codon usage, where each trinucleotide x has occurrence frequency w(x).

In view of Definition 2.3, one naturally associates to each weighted code the following weighted graph.

DEFINITION 2.12. Let (X, ω) be a weighted trinucleotide code. The weighted graph associated with ω is the pair $(\mathcal{G}(X), \omega')$ where $\mathcal{G}(X)$ is given by Definition 2.3 with respect to X, and ω' is a function assigning to each of the two arcs of $\mathcal{G}(X)$ coming from a trinucleotide $N_1N_2N_3 \in X$ the rational number $\frac{\omega(N_1N_2N_3)}{2} \in [0, 1]$.

In other words, the arcs of the weighted graph $(\mathcal{G}(X), \omega')$ can be written as follows:

$$\left\{N_1 \xrightarrow{\omega(x)/2} N_2 N_3 : x = N_1 N_2 N_3 \in X\right\} \cup \left\{N_1 N_2 \xrightarrow{\omega(x)/2} N_3 : x = N_1 N_2 N_3 \in X\right\}.$$

We are now in a position to define the generalised function f associated with every weighted trinucleotide code.

DEFINITION 2.13. Let (X, ω) be a weighted trinucleotide code and $(\mathcal{G}(X), \omega')$ its associated weighted graph. Let \mathcal{C} be the set of all directed cycles of $\mathcal{G}(X)$. The loss of reading frame retrieval (RFR) function f of a (X, ω) is the mapping f given by

(2.3)
$$f((X,\omega)) \coloneqq \frac{1}{|\mathcal{C}|} \sum_{c \in \mathcal{C}} (2|X|)^{|c|} \prod_{a \in E(c)} \omega'(a)$$

where E(c) is the set of arcs of the directed cycle c.

PROPOSITION 2.14 (Uniform codon usage). Let X_g be the genetic code and let ω the uniform distribution over X_g , that is, $\omega \colon X_g \to [0,1]$ is constant and equal to $\frac{1}{64}$. Then $f((X_g,\omega)) = 1$.

PROOF. We have

$$f((X_g, \omega)) = \frac{1}{|\mathcal{C}|} \sum_{c \in \mathcal{C}} (2 \cdot 64)^{|c|} \prod_{a \in E(c)} \frac{1}{2 \cdot 64}$$
$$= \frac{1}{|\mathcal{C}|} \sum_{c \in \mathcal{C}} 1$$
$$= 1.$$

The next proposition implies that for circular codes, the weight function ω has no significance for f, in the sense that all distributions yield the same value as the uniform one, namely 0. More precisely, the equivalence given by Proposition 2.11 between circular codes and f-value 0 generalises to weighted trinucleotide codes.

PROPOSITION 2.15 (Circular code). Let (X, ω) be a weighted trinucleotide code. Then $f((X, \omega)) = 0$ if and only if X is a circular code.

The function f seems to be maximised by codes obtained from a circular code of maximal size (20) by adding a periodic trinucleotide x (i.e. AAA, CCC, GGG or TTT), with a weight function tending to 1 on x and 0 on all other trinucleotides. The determination of the theoretical maximal values of f is beyond the scope of this article, but we at least make the following observation, obtained by computing f for the aforementioned family of codes.

PROPOSITION 2.16. We have

 $\sup\{f(X,\omega) : (X,\omega) \text{ weighted trinucleotide code}\} \ge 441.$

That is, for every $\varepsilon > 0$, there exists a weighted trinucleotide code (X, ω) such that $f(X, \omega) > 441 - \varepsilon$.

Definition 2.12 can be generalised to codes with words of arbitrary length ℓ on any finite alphabet Σ as a graph can be associated with any ℓ -letter code $X \subseteq \Sigma^{\ell}$ [8].

DEFINITION 2.17. Fix $\ell \in \mathbf{N}$ and let $X \subseteq \Sigma^{\ell}$ be an ℓ -letter code. We define a directed graph $\mathcal{G}(X) =$ (V(X), E(X)) with vertex set V(X) and edge set E(X) as follows.

- (1) $V(X) \coloneqq \bigcup_{i=1}^{\ell-1} \{N_1 \cdots N_i, N_{i+1} \cdots N_\ell : N_1 \cdots N_\ell \in X\};$ and (2) $E(X) \coloneqq \bigcup_{i=1}^{\ell-1} \{N_1 \cdots N_i \to N_{i+1} \cdots N_\ell : N_1 \cdots N_\ell \in X\}.$

The weight function over the arcs then generalises naturally.

DEFINITION 2.18. Fix an integer $\ell \geq 2$. Let $X \subseteq \Sigma^{\ell}$ and let $\omega \colon X \to [0, 1]$ be a weight function over X. For each element $N_1 \ldots N_{\ell} \in X$ and each $i \in \{1, \ldots, \ell - 1\}$, we set

$$w'(N_1 \cdots N_i \to N_{i+1} \cdots N_\ell) = \frac{\omega(x)}{\ell - 1}.$$

2.5. Data. A very interesting codon statistics database (CSD) has recently been developed by the Alvarez-Ponce group [32] (Figure 1). It provides the codon usage for all the species with reference or representative genomes in RefSeq. It is free to access without registration at http://codonstatsdb.unr.edu. From this CSD, we extract (July 2022) the codon usage of genomes of three kingdoms: bacteria, eukaryota and archaea.

Group: Archaea Taxonomy ID: 2157

Genetic code: 11 Mode: RSCU | Count

| Species | #Genes | GCA (Ala) | GCC (Ala) | GCG (Ala) | GCT (Ala) | AGA (Arg) | AGG (Arg) | CGA (Arg) | CGC (Arg) |
|---|--------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|
| <u>Acidianus ambivalens</u> | 2541 | 17018* | 3949 | 3294 | 14257 | 16276* | 9173 | 464 | 310 |
| <u>Acidianus brierleyi</u> | 3076 | 18542 | 4135 | 3582 | 19079* | 22350* | 7768 | 1043 | 385 |
| Acidianus hospitalis W1 | 2420 | 16032* | 3683 | 3008 | 13331 | 15503* | 8663 | 376 | 255 |
| Acidianus infernus | 2365 | 16350* | 3990 | 3460 | 13788 | 15542* | 8739 | 397 | 266 |
| <u>Acidianus manzaensis</u> | 2696 | 18671* | 2546 | 2581 | 18708 | 20642* | 5175 | 550 | 224 |
| <u>Acidianus sulfidivorans</u> <u>JP7</u> | 2279 | 15394* | 2528 | 2728 | 15982 | 17191* | 5217 | 475 | 198 |
| <u>Acidilobus</u> <u>saccharovorans 345-15</u> | 1490 | 5247 | 21461* | 10024 | 6608 | 2663 | 24082* | 201 | 1526 |

FIGURE 1. Partial screen shot of the codon statistics database (CSD) [32] showing the initial data of codon usage.

The Archaea (Id 2157) can be directly extracted. The Bacteria and Eukaryota cannot be directly obtained from CSD, which is restricted to taxa for which the genetic code is homogeneous, i.e. species with the same genetic code. For example, the bacterial Mycoplasmatales uses a different genetic code with only two stop codons TAA and TAG, TGA coding Trp. Thus, the Bacteria are constructed from the union of the 22 following bacterial classes: Acidobacteria (Id 57723), Actinobacteria (Id 201174), Aquificae (Id 187857), Bacteroidetes (Id 976), Balneolia (Id 1853221), Chlamydiia (Id 204429), Chloroflexi (Id 200795), Cyanobacteria (Id 1117), Deferribacteres (Id 68337), Deinococcus-Thermus (Id 1297), Epsilonproteobacteria (Id 29547), Firmicutes (Id 1239), Fusobacteria (Id 32066), Mycoplasmatales (Id 2085), Nitrospirae (Id 40117), Planctomycetes (Id 203682), Pseudomonadales (Id 72274), Spirochaetes (Id 203691), Synergistetes (Id 508458), Thermodesulfobacteria (Id 200940), Thermotogae (Id 200918) and Verrucomicrobia (Id 74201). In a similar way, the Eukaryota are constructed from the union of the 4 following eukaryotic classes: Metazoa (animals, Id 33208), Plants (Embryophyta, land plants, Id 3193; Chlorophyta, green algae, Id 3041; Rhodophyta, red algae, Id 2763), Fungi (Agaricomycotina Id 5302; Pezizomycotina, Id 147538; Saccharomyces, Id 4930; Ustilaginomycotina, Id 452284; Basidiomycota, Id 5204) and Protists (Apicomplexa, Id 5794; Kinetoplastea, Id 5653). The few exceptional genomes in which the codon usage of the stop codons is not given, are not considered. Table 1 gives the basic statistics of genomes in the three kingdoms studied.

| Kingdom | Total number | | | | | |
|-----------|--------------|----------|-------------|--|--|--|
| | Genomes | Genes | Codons | | | |
| Bacteria | 8345 | 34020997 | 11087876805 | | | |
| Eukaryota | 1150 | 20206058 | 10374305634 | | | |
| Archaea | 432 | 1280890 | 367937932 | | | |

TABLE 1. Basic statistics of genomes in the three kingdoms studied with the total numbers of genomes, genes and codons.

2.6. Gene reading frame retrieval (RFR) of Homo sapiens. The codon usage of Homo sapiens obtained from the codon statistics database (CSD) [32] (taxonomy Id: 9606, 19850 genes, 11577026 codons) is given in Appendix Table 3. The gene reading frame retrieval (RFR) function of H. sapiens is equal to f(H. sapiens) = 0.792. This example also allows the reader to easily verify the computation of the RFR function f which does not pose any algorithmic difficulties.

3. Results

3.1. Reading frame retrieval enhanced in large genes. We compute the gene reading frame retrieval (RFR) function f (2.3) as a function of the mean number \overline{n} (Definition 2.5) of codons per gene in the genomes of three kingdoms. A "universal" property is identified: the larger the gene, the lower the reading frame loss, whatever the kingdom. We detail the statistical results for each kingdom.

Figure 2 shows that the mean numbers \overline{n} of codons per gene of the 8345 bacterial genomes all belong to the interval [230, 460]. The overall mean number \overline{n} of codons per gene, over all these bacterial genomes, is 325 (see Table 2). The RFR function f(Bacteria) decreases according to a Spearman's rank correlation coefficient $\rho = -0.07$ with a very strong significant *p*-value $< 10^{-9}$. This property is retrieved in the genes of eukaryotic and archaeal genomes. As their genome numbers are significantly smaller than the bacterial one, the statistical significance of their a values

numbers are significantly smaller than the bacterial one, the statistical significance of their ρ values is obviously smaller compared to the ρ value of bacterial genomes.

Figure 3 shows that the mean numbers \overline{n} of codons per gene of the 1150 eukaryotic genomes all belong to the interval [260, 860]. The overall mean number \overline{n} of codons per gene, over all these eukaryotic genomes, is 519 (see Table 2). Thus, in average, the eukaryotic genes are significantly longer than the bacterial genes. The RFR function f(Eukaryota) decreases according to a Spearman's rank correlation coefficient $\rho = -0.14$ with a strong significant *p*-value $< 10^{-6}$. *Homo sapiens* has a mean number $\overline{n} = 583$ of codons per gene and, as already mentioned, a RFR function f(H. sapiens) = 0.792 (thus, above the linear regression).

Figure 4 shows that the mean numbers \overline{n} of codons per gene of the 432 archaeal genomes all belong to the interval [220, 350]. The overall mean number $\overline{\overline{n}}$ of codons per gene, over all these archaeal genomes, is 287 (see Table 2). Thus, in average, the archaeal genes are the shortest in the three kingdoms. This observation could be a consequence of a fundamental structure of archaeal genomes

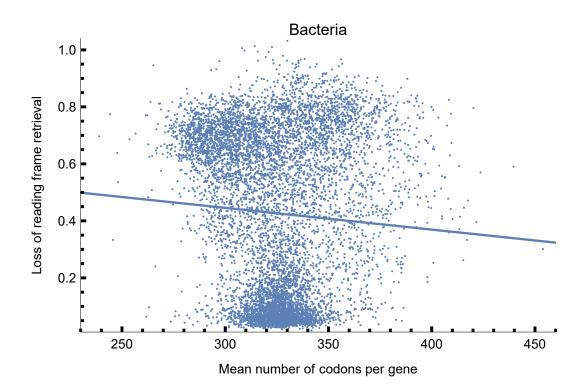


FIGURE 2. Loss of reading frame retrieval in genes of 8345 bacterial genomes. Each point represents all the genes of a bacterial genome. The x-axis shows the mean number \overline{n} (Definition 2.5) of codons per gene, i.e. the total number of codons in a genome divided by its total number of genes. The y-axis shows the reading frame retrieval function f (2.3). The linear regression between \overline{n} and f decreases according to the equation y = -0.000762074x + 0.674293, with a Spearman's rank correlation coefficient $\rho = -0.07$ and p-value $< 10^{-9}$.

or related to its low number of sequenced genomes. The RFR function f(Archaea) decreases according to a Spearman's rank correlation coefficient $\rho = -0.12$ with a significant *p*-value = 0.013. Table 2 gives some additional statistical parameters. Eukaryotic genomes have the highest mean number $\overline{\overline{n}} = 519$ of codons per gene and the archaeal genomes the lowest value $\overline{\overline{n}} = 287$, in agreement with their respective intervals. Concerning the reading frame retrieval function, eukaryotic genomes have the highest value mean(f) = 0.736 and the archaeal genomes the lowest value mean(f) = 0.323. The highest and lowest values for the RFR function are observed with the bacterial genomes: max(f) = 1.032 in *Helicobacter pametensis* and min(f) = 0.016in *Corynebacterium sphenisci DSM*.

3.2. Reading frame retrieval correlated with dispersion of codon usage. We compute the gene reading frame retrieval (RFR) function f (2.3) according to the dispersion function d (2.1) of codon usage in the genomes of the three kingdoms.

Figure 5 is somewhat spectacular for the following reasons. An exceptional correlation with a coefficient $\rho = -0.83$ and *p*-value $< 10^{-180}$ is identified between between the codon usage dispersion and the RFR function. As expected from the theory (see Propositions 2.9 and 2.14), the bacterial RFR function decreases, or equivalently the property of reading frame retrieval increases

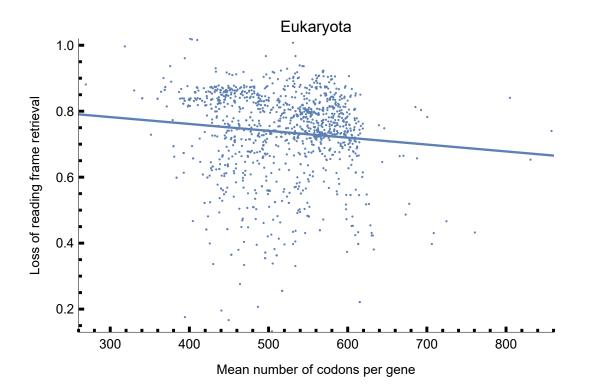


FIGURE 3. Loss of reading frame retrieval in genes of 1150 eukaryotic genomes. Each point represents all the genes of an eukaryotic genome. The *x*-axis shows the mean number \overline{n} (Definition 2.5) of codons per gene, i.e. the total number of codons in a genome divided by its total number of genes. The *y*-axis shows the reading frame retrieval function f (2.3). The linear regression between \overline{n} and f decreases according to the equation y = -0.00020828x + 0.844653, with a Spearman's rank correlation coefficient $\rho = -0.14$ and p-value $< 10^{-6}$.

TABLE 2. Basic statistical parameters of genomes in the three kingdoms studied. The reading frame retrieval function f is given by (2.3).

| Kingdom | Basic statistical parameters | | | | | | |
|-----------|---------------------------------------|---------|-----------|-----------|--|--|--|
| | Mean number $\overline{\overline{n}}$ | mean(f) | $\min(f)$ | $\max(f)$ | | | |
| | of codons per gene | | | | | | |
| Bacteria | 325 | 0.426 | 0.016 | 1.032 | | | |
| Eukaryota | 519 | 0.736 | 0.133 | 1.020 | | | |
| Archaea | 287 | 0.323 | 0.051 | 0.839 | | | |

in bacterial genomes, with the codon usage dispersion ranging from d = 0.36 with high RFR values f > 0.6 to d = 1.1 with low RFR values f < 0.1. However, this RFR increase uses two evolutionary processes. From a bacterial "genome center" ranging approximately from d = 0.36 to d = 0.55, two bacterial "genome arms" emerge. The upper arm (above the linear regression) is

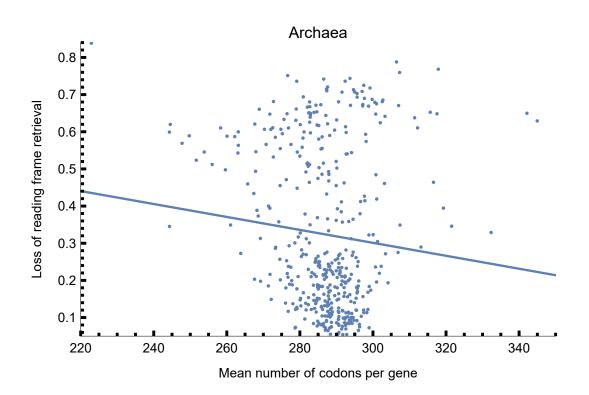


FIGURE 4. Loss of reading frame retrieval in genes of 432 archaeal genomes. Each point represents all the genes of an archaeal genome. The x-axis shows the mean number \overline{n} (Definition 2.5) of codons per gene, i.e. the total number of codons in a genome divided by its total number of genes. The y-axis shows the reading frame retrieval function f (2.3). The linear regression between \overline{n} and f decreases according to the equation y = -0.00174221x + 0.823736, with a Spearman's rank correlation coefficient $\rho = -0.12$ and p-value = 0.013.

ranging from d = 0.55 to d < 1.0. The lower arm (below the linear regression) is longer and ranges from d = 0.55 to d = 1.1.

In order to investigate these two genome arms, we analyse the codon dispersion of each amino acid (AA) with the Spearman's rank correlation coefficient ρ . The 15 AA codons leading to negative ρ values, similarly to the codon usage, are the following ones: Ala codons ($\rho = -0.92$), Arg codons ($\rho = -0.75$), Asp codons ($\rho = -0.66$), Cys codons ($\rho = -0.07$), Gln codons ($\rho = -0.55$), Gly codons ($\rho = -0.84$), His codons ($\rho = -0.44$), Ile codons ($\rho = -0.48$), Leu codons ($\rho = -0.90$), Phe codons ($\rho = -0.31$), Pro codons ($\rho = -0.82$), Ser codons ($\rho = -0.82$, identical value to Pro codons), Thr codons ($\rho = -0.90$), Tyr codons ($\rho = -0.20$) and Val codons ($\rho = -0.86$). The 4 AA codons leading to a positive ρ values, thus not involved in the dispersion of codon usage, are the following ones: Asn codons ($\rho = 0.20$), Lys codons ($\rho = 0.61$), Met codons ($\rho = 0.62$) and Trp codons ($\rho = 0.64$). The Glu codons have a non-significant value $\rho = -0.02$. However, none of the 15 AA codons with negative ρ values has a well-differentiated 2-arm structure (results not shown). This observation suggests that dispersion associated with reading frame retrieval is not associated with a particular amino acid.

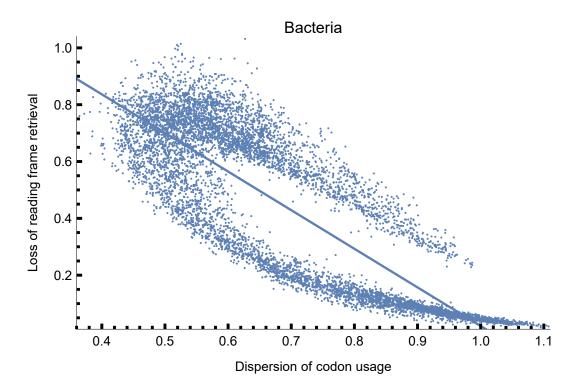


FIGURE 5. Reading frame retrieval correlated with dispersion of codon usage in genes of 8345 bacterial genomes. Each point represents all the genes of a bacterial genome. The x-axis shows the dispersion function d (2.1) of codon usage. The y-axis shows the reading frame retrieval function f (2.3). The linear regression between d and f decreases according to the equation y = -1.35881x + 1.37993, with a Spearman's rank correlation coefficient $\rho = -0.83$ and p-value $< 10^{-180}$.

We continue our dispersion analysis by considering the 3 codes related to the number of different nucleotides in the codons. The set of 1-letter codons, of cardinality 4, is

 $\{AAA, CCC, GGG, TTT\},\$

the set of 2-letter codons, of cardinality 36, is

 $\{AAC, AAG, AAT, ACA, ACC, AGA, AGG, ATA, ATT, CAA, CAC, CCA, CCG, CCT, CGC, CGG, CTC, CTT, GAA, GAG, GCC, GCG, GGA, GGC, GGT, GTG, GTT, TAA, TAT, TCC, TCT, TGG, TGT, TTA, TTC, TTG\},$

and the set of 3-letter codons, of cardinality 24, is

 $\{ACG, ACT, AGC, AGT, ATC, ATG, CAG, CAT, CGA, CGT, CTA, CTG, GAC, GAT, GCA, GCT, GTA, GTC, TAC, TAG, TCA, TCG, TGA, TGC\}.$

The 1-letter codons with a positive ρ value do not contribute to the dispersion associated with reading frame retrieval (Figure 6(A)). In contrast, the 2-letter codons leads to a well-differentiated 2-arm structure (Figure 6(B), similarly to the Figure 5). These two arms are less structured with the 3-letter codons (Figure 6(C)). In summary, the dispersion of codon usage associated with reading frame retrieval in genes is strongly associated with the 2-letter codons and also, to a lesser extent, with the 3-letter codons, i.e. the 60 codons (except the 4 periodic codons).

This correlation between between the codon usage dispersion in the genes of bacterial genomes and the RFR function is retrieved in the genes of eukaryotic and archaeal genomes. Figure 7 shows that the eukaryotic RFR function decreases with the codon usage dispersion ranging from d = 0.3with high RFR values f > 0.8 to d = 0.96 with low RFR values f < 0.4. Two eukaryotic genome arms are observable but the upper arm is very sparse. *Homo sapiens* has a codon usage dispersion d = 0.40 and, as already mentioned, a RFR function f(H. sapiens) = 0.792. He is thus located in the eukaryotic genome center (see Figure 7).

Figure 8 shows that the archaeal RFR function decreases with the codon usage dispersion ranging from d = 0.38 with high RFR values f > 0.8 to d = 0.96 with low RFR values f < 0.1. Two archaeal genome arms are significantly observable.

3.3. A potential evolutionary classification of genomes based on reading frame retrieval. As we have seen in the previous sections with the RFR function according to the codon usage dispersion, the genome center and its two arms could be used to a new and global classification of genomes. Furthermore, at a lower level, by analysing the bird genomes (Aves, Id 8782, 88 genomes, 1318882 genes, 746444944 codons) during the construction process of eukaryotic genomes, the reading frame retrieval function f (2.3) surprisingly identifies 2 groups of genomes (Figure 9). Thus, according to all these observations, this RFR function by itself or combined with classical methods (alignment, phylogeny) could also classify the genomes, a new approach that could be investigated in the future.

4. Conclusion

Codon usage bias depends on a great number of biological factors (described in a recent review [25]). The statistical parameters analysing CUB were mainly developed by considering the coding of amino acids (see Introduction). In contrast to these classical methods and by using the circular code theory, we have defined here a new function f that quantifies the property of reading frame retrieval (RFR) of genes from their codon usage. Furthermore, by expressing f as a function of the mean number \overline{n} of codons per gene, a "universal" property is identified in genes of genomes of bacteria, eukaryotes and archaea: the reading frame retrieval is enhanced in large genes. Then, by expressing f as a function of the codon usage dispersion d (from the uniform codon distribution $\frac{1}{64}$), another property with a strong statistical significance is found whatever the kingdom: the reading frame retrieval is enhanced with the codon usage dispersion. Surprisingly, this approach has revealed a genome center from which emerge two distinct genome arms: an upper arm and a lower arm, respectively above and below the linear regression. As CUB could have evolved through reading frame retrieval, the RFR function by itself or combined with classical methods (alignment, phylogeny) could also be a new approach to classify the genes and the genomes in the future.

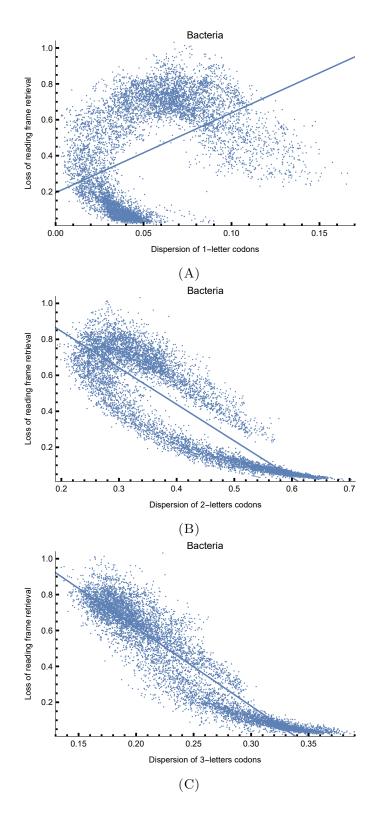


FIGURE 6. Reading frame retrieval correlated with codon dispersion in genes of 8345 bacterial genomes. Each point represents all the genes of a bacterial genome. The x-axis shows the codon dispersion function d (2.1). The y-axis shows the reading frame retrieval function f (2.3). The linear regression between d and f, and the Spearman's rank correlation coefficient ρ with its p-value are given for each code. (A) 1-letter codons: y = 4.45043x + 0.193461, with $\rho = 0.44$ and p-value $< 10^{-180}$. (B) 2-letter codons: y = -2.03092x + 1.25098, with $\rho = -0.85$ and p-value $< 10^{-180}$. (C) 3-letter codons: y = -4.36971x + 1.49, with $\rho = -0.94$ and p-value $< 10^{-180}$.

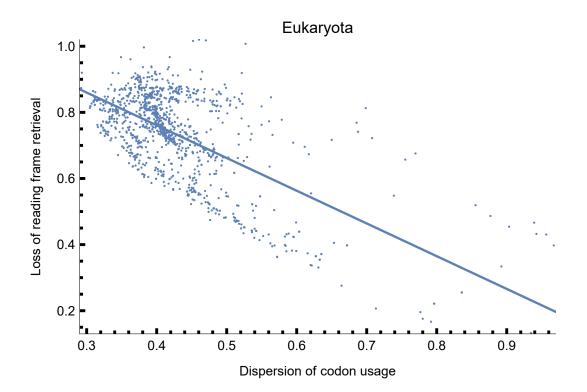


FIGURE 7. Reading frame retrieval correlated with dispersion of codon usage in genes of 1150 eukaryotic genomes. Each point represents all the genes of an eukaryotic genome. The x-axis shows the dispersion function d (2.1) of codon usage. The y-axis shows the reading frame retrieval function f (2.3). The linear regression between d and f decreases according to the equation y = -0.989903x + 1.15688, with a Spearman's rank correlation coefficient $\rho = -0.45$ and p-value $< 10^{-61}$.

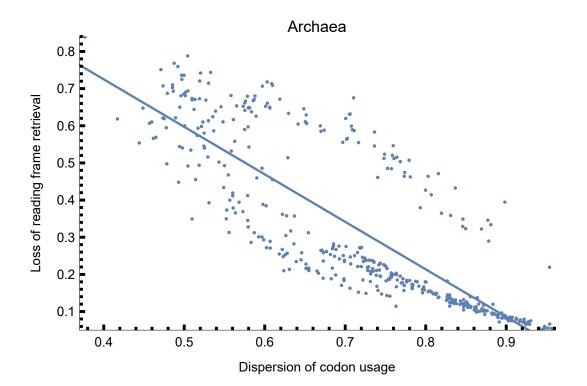


FIGURE 8. Reading frame retrieval correlated with dispersion of codon usage in genes of 432 archaeal genomes. Each point represents all the genes of an archaeal genome. The x-axis shows the dispersion function d (2.1) of codon usage. The y-axis shows the reading frame retrieval function f (2.3). The linear regression between d and f decreases according to the equation y = -1.27828x + 1.23627, with a Spearman's rank correlation coefficient $\rho = -0.86$ and p-value $< 10^{-159}$.

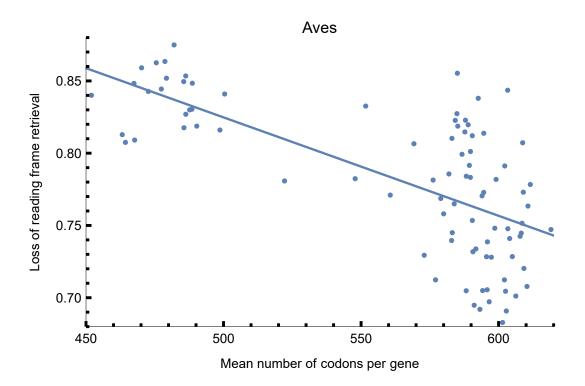


FIGURE 9. Loss of reading frame retrieval in genes of 88 bird genomes (Aves, Id 8782, 88 genomes, 1318882 genes, 746444944 codons) identifying 2 groups of genomes. Each point represents all the genes of a bird genome. The *x*-axis shows the mean number \overline{n} (Definition 2.5) of codons per gene, i.e. the total number of codons in a genome divided by its total number of genes. The *y*-axis shows the reading frame retrieval function f (2.3). The linear regression between \overline{n} and f decreases according to the equation y = -0.000681184x + 1.16537, with a Spearman's rank correlation coefficient $\rho = -0.66$ and *p*-value $< 10^{-12}$.

Appendix A. Codon usage of Homo sapiens

TABLE 3. Codon usage of *Homo sapiens* (Id 9606, 19850 genes, 11577026 codons). The occurrence number and the frequency of each codon are given.

| AAA2923772.53CAA1486031.28GAA3529493.05TAA56360.05AAC2129871.84CAC1747991.51GAC2879742.49TAC1660831.43AAG3650133.15CAG4013643.47GAG4647654.01TAG44360.04AAT1978311.71CAT1296221.12GAT2559332.21TAT1376041.19ACA1777981.55CCA2041981.76GCA1871081.62TCA1500511.30ACC2138471.85CCC2377812.05GCC3232492.79TCC2065501.78ACG687540.59CCG864270.75GCG890970.77TCG530150.46ACT1569041.36CCT2113421.83GCT2135591.84TCT1822881.57AGA1429341.23CGA703190.61GGA1937211.67TGA97730.88AGC2310632.00CGC1199721.04GGC2580402.23TGC1424991.23AGG1404811.21CGG1322751.14GGG1910941.65TGG1243881.07AGG1404811.21CGG521290.45GGT1238811.07TGT1244380.79AGG14 | | | | | | | | | | | | |
|---|-----|--------|------|----------------------|--------|------|----------------------|--------|------|----------------|--------|------|
| AAG3650133.15CAG4013643.47GAG4647654.01TAG44360.04AAT1978311.71CAT1296221.12GAT2559332.21TAT1376041.19ACA1777981.54CCA2041981.76GCA1871081.62TCA1500511.30ACC2138471.85CCC2377812.05GCC3232492.79TCC2065501.78ACG687540.59CCG864270.75GCG890970.77TCG530150.46ACT1569041.36CCT2113421.83GCT2135591.84TCT1822881.57AGA1429341.23CGA703190.61GGA1937211.67TGA1426391.23AGG1404811.21CGG1322751.14GGG1910941.65TGG1424381.07AGG1473881.27CGT521290.45GGT1238811.07TGT1244381.07AGT1473881.94CTC2206011.91GTC830200.72TTA916380.79AGT244051.94CTC2206011.91GTC1613781.39TTC2223731.92AGT2440922.11CTG2206011.91GTC1613781.39TTC2223731.92AGT2 | AAA | 292377 | 2.53 | CAA | 148603 | 1.28 | GAA | 352949 | 3.05 | TAA | 5636 | 0.05 |
| AAT1978311.71CAT1296221.12GAT2559332.21TAT1376041.19ACA1777981.54CCA2041981.76GCA1871081.62TCA1500511.30ACC2138471.85CCC2377812.05GCC3232492.79TCC2065501.78ACG687540.59CCG864270.75GCG890970.77TCG530150.46ACT1569041.36CCT2113421.83GCT2135591.84TCT1822881.57AGA1429341.23CGA703190.61GGA1937211.67TGA97730.08AGG2310632.00CGC1199721.04GGC2580402.23TGC1428591.23AGG1404811.21CGG1322751.14GGG1910941.65TGG1420491.23AGG1404811.21CGG521290.45GGT1238811.07TGT124381.07AGT1473881.27CGT521290.45GGT133811.07TGT124380.79AGT1473890.76CTA830430.72GTA830200.72TTA916380.79AGT2249651.94CTC2206011.91GTC1613781.39TTC2223731.92AT244092 | AAC | 212987 | 1.84 | CAC | 174799 | 1.51 | GAC | 287974 | 2.49 | TAC | 166083 | 1.43 |
| ACA1777981.54CCA2041981.76GCA1871081.62TCA1500511.30ACC2138471.85CCC2377812.05GCC3232492.79TCC2065501.78ACG687540.59CCG864270.75GCG890970.77TCG530150.46ACT1569041.36CCT2113421.83GCT2135591.84TCT1822881.57AGA1429341.23CGA703190.61GGA1937211.67TGA97730.08AGC2310632.00CGC1199721.04GGC2580402.23TGC1428591.23AGG1404811.21CGG1322751.14GGG1910941.65TGG1424381.07AGT1473881.27CGT521290.45GGT1238811.07TGT1244381.07ATA877900.76CTA830430.72GTA830200.72TTA916380.79ATC2249651.94CTG2206011.91GTC1613781.39TTC2223731.92ATG2440922.11CTG449483.88GTG3142232.71TTG1502131.30 | AAG | 365013 | 3.15 | CAG | 401364 | 3.47 | GAG | 464765 | 4.01 | TAG | 4436 | 0.04 |
| ACC2138471.85CCC2377812.05GCC3232492.79TCC2065501.78ACG687540.59CCG864270.75GCG890970.77TCG530150.46ACT1569041.36CCT2113421.83GCT2135591.84TCT1822881.57AGA1429341.23CGA703190.61GGA1937211.67TGA97730.08AGC2310632.00CGC1199721.04GGC2580402.23TGC1428591.23AGG1404811.21CGG1322751.14GGG1910941.65TGG1420491.23AGT1473881.27CGT521290.45GGT1238811.07TGT1244381.07ATA877900.76CTA830430.72GTA830200.72TTA916380.79ATC2249651.94CTC2206011.91GTC1613781.39TTC223731.92ATG2440922.11CTG4494853.88GTG3142232.71TTG1502131.30 | AAT | 197831 | 1.71 | CAT | 129622 | 1.12 | GAT | 255933 | 2.21 | TAT | 137604 | 1.19 |
| ACG687540.59CCG864270.75GCG890970.77TCG530150.46ACT1569041.36CCT2113421.83GCT2135591.84TCT1822881.57AGA1429341.23CGA703190.61GGA1937211.67TGA97730.08AGC2310632.00CGC1199721.04GGC2580402.23TGC1428591.23AGG1404811.21CGG1322751.14GGG1910941.65TGG1420491.23AGT1473881.27CGT521290.45GGT1238811.07TGT1244381.07ATA877900.76CTA830430.72GTA830200.72TTA916380.79ATC2249651.94CTC2206011.91GTC1613781.39TTC2223731.92ATG2440922.11CTG4494853.88GTG3142232.71TTG1502131.30 | ACA | 177798 | 1.54 | CCA | 204198 | 1.76 | GCA | 187108 | 1.62 | TCA | 150051 | 1.30 |
| ACT1569041.36CCT2113421.83GCT2135591.84TCT1822881.57AGA1429341.23CGA703190.61GGA1937211.67TGA97730.08AGC2310632.00CGC1199721.04GGC2580402.23TGC1428591.23AGG1404811.21CGG1322751.14GGG1910941.65TGG1420491.23AGT1473881.27CGT521290.45GGT1238811.07TGT1244381.07ATA877900.76CTA830430.72GTA830200.72TTA916380.79ATC2249651.94CTC2206011.91GTC1613781.39TTC2223731.92ATG2440922.11CTG4494853.88GTG3142232.71TTG1502131.30 | ACC | 213847 | 1.85 | \mathbf{CCC} | 237781 | 2.05 | GCC | 323249 | 2.79 | TCC | 206550 | 1.78 |
| AGA1429341.23CGA703190.61GGA1937211.67TGA97730.08AGC2310632.00CGC1199721.04GGC2580402.23TGC1428591.23AGG1404811.21CGG1322751.14GGG1910941.65TGG1420491.23AGT1473881.27CGT521290.45GGT1238811.07TGT1244381.07ATA877900.76CTA830430.72GTA830200.72TTA916380.79ATC2249651.94CTC2206011.91GTC1613781.39TTC2223731.92ATG2440922.11CTG4494853.88GTG3142232.71TTG1502131.30 | ACG | 68754 | 0.59 | CCG | 86427 | 0.75 | GCG | 89097 | 0.77 | TCG | 53015 | 0.46 |
| AGC2310632.00CGC1199721.04GGC2580402.23TGC1428591.23AGG1404811.21CGG1322751.14GGG1910941.65TGG1420491.23AGT1473881.27CGT521290.45GGT1238811.07TGT1244381.07ATA877900.76CTA830430.72GTA830200.72TTA916380.79ATC2249651.94CTC2206011.91GTC1613781.39TTC2223731.92ATG2440922.11CTG4494853.88GTG3142232.71TTG1502131.30 | ACT | 156904 | 1.36 | CCT | 211342 | 1.83 | GCT | 213559 | 1.84 | TCT | 182288 | 1.57 |
| AGG1404811.21CGG1322751.14GGG1910941.65TGG1420491.23AGT1473881.27CGT521290.45GGT1238811.07TGT1244381.07ATA877900.76CTA830430.72GTA830200.72TTA916380.79ATC2249651.94CTC2206011.91GTC1613781.39TTC2223731.92ATG2440922.11CTG4494853.88GTG3142232.71TTG1502131.30 | AGA | 142934 | 1.23 | CGA | 70319 | 0.61 | GGA | 193721 | 1.67 | TGA | 9773 | 0.08 |
| AGT1473881.27CGT521290.45GGT1238811.07TGT1244381.07ATA877900.76CTA830430.72GTA830200.72TTA916380.79ATC2249651.94CTC2206011.91GTC1613781.39TTC2223731.92ATG2440922.11CTG4494853.88GTG3142232.71TTG1502131.30 | AGC | 231063 | 2.00 | CGC | 119972 | 1.04 | GGC | 258040 | 2.23 | TGC | 142859 | 1.23 |
| ATA877900.76CTA830430.72GTA830200.72TTA916380.79ATC2249651.94CTC2206011.91GTC1613781.39TTC2223731.92ATG2440922.11CTG4494853.88GTG3142232.71TTG1502131.30 | AGG | 140481 | 1.21 | CGG | 132275 | 1.14 | GGG | 191094 | 1.65 | TGG | 142049 | 1.23 |
| ATC2249651.94CTC2206011.91GTC1613781.39TTC2223731.92ATG2440922.11CTG4494853.88GTG3142232.71TTG1502131.30 | AGT | 147388 | 1.27 | CGT | 52129 | 0.45 | GGT | 123881 | 1.07 | TGT | 124438 | 1.07 |
| ATG 244092 2.11 CTG 449485 3.88 GTG 314223 2.71 TTG 150213 1.30 | ATA | 87790 | 0.76 | CTA | 83043 | 0.72 | GTA | 83020 | 0.72 | TTA | 91638 | 0.79 |
| | ATC | 224965 | 1.94 | CTC | 220601 | 1.91 | GTC | 161378 | 1.39 | TTC | 222373 | 1.92 |
| ATT 182397 1.58 CTT 155373 1.34 GTT 127368 1.10 TTT 196707 1.70 | ATG | 244092 | 2.11 | CTG | 449485 | 3.88 | GTG | 314223 | 2.71 | TTG | 150213 | 1.30 |
| | ATT | 182397 | 1.58 | CTT | 155373 | 1.34 | GTT | 127368 | 1.10 | TTT | 196707 | 1.70 |

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