Theoretical and experimental studies of hyperreflective polymer-network cholesteric liquid crystal structures with helicity inversion

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Abstract

Single-layer cholesteric liquid crystals exhibit a reflection coefficient which is at most 50% for unpolarized incident light. We give theoretical and experimental evidence of single-layer polymer-stabilized cholesteric liquid crystalline structures that demonstrate hyper-reflective properties. Such original features are derived by the concurrent and randomly interlaced presence of both helicities. The fundamental properties of such structures are revealed by detailed numerical simulations based on a stochastic approach.

Key words: Cholesteric liquid crystals, photonic bandgap materials, polymer-dispersed liquid crystals, domain structures
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1 Introduction

The cholesteric liquid crystalline (CLC) structure is omnipresent in living matter at various scales and in various tissues, for specific or still unknown functions: condensed phases of DNA [1], cellulose matrix in plant cell walls, chitin matrix in arthropods cuticles [2], collagen network in human compact

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bone [3], virus suspensions [4] or atherosclerosis disease [5]. In technology, the optical properties of the CLC phase are very attractive for numerous applications such as polarizer-free reflective displays [6], polarizers and colour filters [7], mirrorless lasing [8] or smart switchable reflective windows for the dynamical control of solar light [9]. CLCs selectively reflect light due to their helical structure [10,11]; when incident light propagates along the helical axis, selective reflection occurs, if the wavelength λ is of the order of the pitch P of the helix, for circularly polarized light with the same handedness as the CLC helix. At normal incidence, the central Bragg reflection wavelength is given by $\lambda_0 = \bar{n}P$, where $\bar{n} = (n_e + n_o)/2$ is the average refractive index, while reflection occurs within a bandwidth $\Delta\lambda = \Delta nP$, where $\Delta n = n_e - n_o$. This polarization selectivity rule is a unique feature of CLCs, since a normal dielectric mirror inverses the handedness. The maximum reflectance of ambient, unpolarized, light from a CLC structure never exceeds 50% at normal incidence, as only left- or right-circularly polarized light may be reflected. Total reflectance may be achieved by forming a bilayer system where two individual cholesteric layers with the same pitch and inverse helicity sense are stacked together [12]. A multilayer solution is regularly undesired due to the optical losses at the interfaces (reflection, scattering) and the cost of implementation for applications. Recent experimental results have reported the elaboration procedure of single-layer CLC materials that are not restricted by the polarization selectivity rule, as the reflection band applies to circularly polarized light components of both helicities [13].

Photopolymerizable and crosslinkable monomers (RM257 nematic diacrylate 3.8 wt.%, Merck Ltd.) are introduced in the volume of a CLC exhibiting a thermally induced helicity inversion; the blend consists of the nematic LC BL006 (from Merck Ltd., 71.2 wt.%) and a chiral dopant to induce the helicity inversion (propanediol derivative, 25 wt.% [14]). The material is introduced into a 50 ± 10 μm thick glass sandwich-cell with planar anchoring to induce Bragg planar textures. The cell is then cured with ultraviolet light (0.1 mW/cm^2 at 365 nm) at a temperature for which the helix is RH and exhibits a pitch equal to P_0 . The sample is then cooled until a temperature for which, before photopolymerization, the CLC structure was LH with a pitch close to P_0 . The transmittance properties are investigated using a Perkin Elmer IR spectrophotometer coupled with a Mettler hot stage. Whatever the polarization of incident light, the reflectance of the cholesteric film goes over the limit of 50% because of the contribution of both helicities. A fraction of LC molecules is strongly bound to the polymer network and gives rise to a RH helical structure (template effect) and a free fraction far from the polymer surfaces forms a LH helix.

These novel experimental results may open the route to hyper-reflective display applications, for which the 50% reflectance limit is exceeded. Nevertheless, the analysis of such complex structures has not yet been theoretically

addressed; in this context, the present study investigates the optical properties of single-layer polymer-stabilized CLC structures with material regions of both helicities, demonstrating that the existence of alternating domains of RH and LH material can account for an overall reflectance that exceeds the 50% limit. The optical properties of the CLC structures are studied numerically by means of the Finite-Difference Time-Domain (FDTD) method, which is capable of dealing with light propagation problems through anisotropic media [15,16]. Assuming normal incidence, a one dimensional algorithm is sufficient to describe the spatial variation of the CLC's dielectric tensor, while all optical power transmission coefficients presented hereinafter were calculated for the case of unpolarized incident light [17]. The accuracy of the numerical studies was verified by direct comparison of indicative examples with the 4×4 Berreman matrix method [18]; the selection of the FDTD method was due to the fact that it provides significantly faster simulation times for the cases here addressed.

2 Optical properties of cholesteric structures comprising both helicities

As a starting point, the transmission spectra for two ideal structures of homogeneous CLC layers are presented in Fig. 1, for a typical liquid-crystalline compound characterized by $n_o = 1.5$, $n_e = 1.7$ and a pitch value of P_0 . The first one refers to a single layer of RH material with a total thickness of $d_1 = 10P_0$, while the second is a bilayer structure of total thickness $d_2 = 20P_0$, divided equally between two homogeneous layers of RH and LH material. As theoretically predicted, selective reflection for the single layer rises up to 50% within the bandgap forming around the central Bragg wavelength $\lambda_0 = 0.5(n_o + n_e)P_0$, while in the case of the bilayer structure almost all optical power is reflected because of the accumulative effect of the two stacked layers of RH and LH helicity. It should be remarked that the optical simulations presented in this analysis account for no losses whatsoever, e.g. owing to scattering or absorption; thus, wavelength-dependent power transmission levels are attributed solely to the selective reflection properties of the CLC structures. In the case of typical polymer-stabilized CLC structures, i.e. where the photopolymerizable monomer concentration constitutes a small wt. percentage, it is pointed out that the formation of the polymer network does not significantly distort the planar structure and thus no high levels of scattering are induced [19–21,9]. In addition, when present, light scattering in such structures manifests itself primarily as a background wavelength-independent phenomenon; thus, it does not affect their reflective behaviour inside the Bragg bands, which is attributed solely to coherent reflection from the domains that develop in periodical helical configurations of the CLC material. Owing to the absence of loss mechanisms,

Fig. 2. (Color online) Transmittance for a monolayer of thickness $d = 20P_0$ distributed equally among randomly located sublayers of RH and LH material for various values of sublayer thickness d_s . The dotted reference curve corresponds to the bilayer system of Fig. 1. Insets show cross-sectional views of patterns formed by the generated stochastic samples for $d_s = 2P_0$ and $d_s = 0.25P_0$. (Color code - LH:red, RH:blue)

Fig. 3. (Color online) Reflectance quality coefficient for monolayers of thickness $d = 20P_0$ for various values of sublayer thickness d_s and distributions between RH and LH material. Maximum reflectivity is observed for $d_s = 2P_0$ and equal percentages of RH and LH regions. Inset shows typical distributions of the material for increasing percentages of RH material.

curve of the bilayer system of Fig. 1.

Figure 3 provides an overall estimate of the reflective efficiency of the investigated structures, via the assessment for varied values of both d_s and the percentages attributed to RH and LH regions of a reflectance quality coeffi-

Fig. 4. (Color online) Transmittance for a monolayer of thickness $d = 20P_0$ distributed equally among randomly located sublayers of RH and LH material for $d_s = 2P_0$ and various angles of incidence θ . A blue-shift is observed as θ obtains higher values, while the shape of the bandgap transmission spectra remains otherwise practically unaffected.

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$$\tilde{R} \equiv 1 - \frac{1}{\Delta\lambda} \int_{\lambda_1}^{\lambda_2} T(\lambda) d\lambda, \quad \Delta\lambda = \lambda_2 - \lambda_1 \quad (1)$$

which represents the average power reflection coefficient within the bandgap wavelength window ($\lambda_1 = n_o P_0$, $\lambda_2 = n_e P_0$), and $T(\lambda)$ is the power transmission coefficient function, defined as in [17]. It is shown that the reflective performance is enhanced when the percentage of both regions is approximately equal and when the thickness of the sublayer d_s is increased, which corresponds to structures where RH and LH regions exhibit higher homogeneity. In any case, it is clearly demonstrated that CLC layers with randomly distributed areas of alternating senses of helicity are capable of providing enhanced reflectance that exceeds the 50% limit. It is emphasized that this particular study has dealt only with the normal incidence case, both from the experimental as well as from the theoretical point of view. In the case of oblique incidence it is anticipated that the reflection band will experience a blue-shift, while the reflection band $\Delta\lambda$ should remain practically unaffected [24]. As an indicative example, Fig. 4 shows the transmission spectra corresponding to the $d_s = 2P_0$ case of the structure investigated in Fig. 2, obtained for various angles of incidence by the Berreman 4×4 matrix method (still summing over 500 randomly generated samples); apart from the expected blue-shift as θ obtains higher values, the shape of the bandgap reflection windows is not noticeably modified.

Fig. 5. (Color online) (a) SEM image showing a typical network formed in polymer-stabilized CLC structures after the removal of the LC material [25], and (b) material structure and definition of the related parameters used in the model adopted for the numerical study: n_g denotes the polymer's refractive index, d_p the mean thickness of the polymer fibrils, d_b the mean thickness of RH material bound to the polymer network, and P_{0L} , P_{0R} the pitch value for the LH and RH regions, respectively.

3 Optical properties of polymer-stabilized cholesteric structures comprising both helicities

The theoretical model under consideration is next generalized to the case of realistic polymer-network CLC structures, such as the one depicted in the Scanning Electron Microscopy (SEM) image of Fig. 5(a), according to the schematic layout and related parameters shown in Fig. 5(b). The 1-D columns/samples are constructed by randomly placing polymer layers of refractive index n_p and variable thickness around a mean value of d_p . Attached to the polymer network, the RH bound material is assumed to extend for a mean thickness d_b , while the rest of the space is occupied by the free LH bulk material. The pitch value for the LH region is fixed at $P_{0L} = P_0$, whereas in the RH region some shrinkage of the pitch value is allowed ($P_{\min} \leq P_{0R} \leq P_0$) in agreement with experimental findings. Indeed, after photopolymerization the pitch value is slightly decreased as a result of a volume shrinkage effect related to the polymer network formation in the LC matrix [22]; such a behaviour was

Fig. 6. (Color online) Transmittance for a polymer-stabilized CLC monolayer of thickness $d = 50\mu m$, for different distributions of RH, LH, and polymer materials. Structural and material parameters (as defined in Fig. 5): $n_g = 1.5$, $d_p = 150 \sim 250nm$, $d_b = 1.5 \sim 2.2\mu m$, $P_{0L} = P_0 = 2.375\mu m$, and $P_{0R} = 0.93P_0 \sim P_0$. As an example, the inset shows the pattern formed by the generated stochastic samples for a LH/RH/polymer ratio of 22%/66%/12%.

Fig. 7. (Color online) Transmittance for a polymer-stabilized CLC with fixed polymer ratio (3%) and values of d_b ranging from $0.5 \sim 0.7\mu m$ (red curve) to $4 \sim 4.2\mu m$ (orange curve). Other parameters as in Fig. 6. Insets show the pattern formed by the stochastically generated samples for three ratios of LH/RH/polymer distributions.

also observed during the formation of ordered polymer networks with a helical structure [26].

Figure 6 shows the transmission spectra obtained for polymer-stabilized CLCs designed for mid-infrared reflection [13,22], for pitch values $P_{0L} = P_0 = 2.375\mu m$, $0.93P_0 \leq P_{0R} \leq P_0$, polymer index $n_g = 1.5$, polymer strand thickness $d_p = 150 \sim 250nm$ and bound RH material thickness $d_b = 1.5 \sim 2.5\mu m$. The overall distribution among RH, LH and polymer regions is controlled by adjusting the percentage of the polymer in the samples. It can be noticed

Fig. 8. (Color online) Comparison between experimental data [13] and theoretical calculations for a polymer-stabilized CLC structure of thickness $d = 50\mu m$ and a ratio of LH/RH/polymer regions equal to 70%/27%/3%. (The shadowed area marks the chemical absorption bands.)

that as the polymer network becomes denser (more than 10%) and the RH material dominates, the bandgap progressively vanishes and the structure's spectral response is flat, implying a highly scattering state; in contrast, for polymer percentage values of a few percent enhanced reflectivity is demonstrated, which exceeds the 50% limit. These results are in agreement with experimental observations; a polymer concentration threshold exists, above which the free fraction of LC molecules is drastically confined in the dense network resulting, thus, in a polydomain structure that induces high levels of light scattering [22,25].

Assuming a fixed value (3%) for the percentage of the polymer network, which may be directly correlated with experimentally studied structures [9,27], the ratio between RH, LH regions may be associated to the exact value of the thickness d_b of the RH material bound to the polymer network. Figure 7 investigates the transmission spectra obtained for value distributions of d_b ranging from $0.5 \sim 0.7\mu m$ (red curve) to $4 \sim 4.2\mu m$ (orange curve). It is once more demonstrated that for approximately equal percentages of RH and LH material, the reflectivity of the investigated polymer-network CLC structures exceeds 50%, obtaining values as high as $\sim 90\%$ for a LH/RH ratio of 48.7%/48.3%.

As a final elucidating example, Fig. 8 shows a comparison between experimental data for a polymer-stabilized CLC structure obtained as discussed in [13,22] and theoretical results based on the described model. The experiments were conducted for the case of normal incidence, while light was also collected at the output of the sample along the normal direction; numerical simulations were performed according to the following set of parameters: $d = 50\mu m$, $n_g = 1.5$, $d_p = 150 \sim 250nm$, $d_b = 1.5 \sim 2.2\mu m$, $P_{0L} = P_0 = 2.375\mu m$,

and $0.93P_0 \leq P_{0R} \leq P_0$ and RH/LH/polymer ratio equal to 70%/27%/3%. In order to allow for a direct comparison, the theoretical curve was normalized according to the normalization conditions of the experimental findings, i.e. assuming 100% transmittance at the low wavelength limit. Taking into account the stochastic nature of the formation of such structures, the proposed numerical model reproduces with very high accuracy the experimental curve.

4 Conclusions

In conclusion, we have presented a theoretical model that investigates in detail the optical properties of recently proposed hyperreflective polymer-CLC gels based on thermally induced helicity inversion and provides significant insight to questions regarding their structural morphology and properties. Results demonstrate that such structures are particularly promising in terms of the realization of CLC films with exceptionally large fluxes of reflected light that might prove indispensable in polarizer-free reflective displays, tunable glazing panels, smart windows in buildings or vehicles, or temperature-control devices.

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