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Impact of thermal gradients on the geometry correction of a bridge coordinate measuring machine

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Abstract

If the problems related to the parts and measurement strategy of Coordinate Measuring Machines (CMMs) are not taken into consideration, temperature variations become the main source of measurement uncertainties. Indeed, they may cause variations in geometry as well as reference point drift. The effect of drift is sometimes minimized by CMM users and is not well quantified in general. The aim of this paper is to present a physical method to determine the evolution of CMM geometry and drift which is based directly on CMM temperature variations and construction parameters, i.e. the position of the axes measurement scales and reference points of each axis. The method is applied to a Zeiss CMM Contura G2. The consequences of these CMM evolutions are simulated in the measurement of a sphere generated by a Renishaw Machine Checking Gauge. The proposed method falls within the framework of an uncertainty assessment methodology performed by multi-level Monte Carlo simulation, where the first level corresponds to the characterization of the CMM evolution.

Keywords: drift, thermal errors, coordinate measuring machine (CMM), geometry evolution, uncertainty, metrology

1. Introduction

The first Coordinate Measuring Machines (CMMs) appeared in the 1960s [1]. The year 1973 was important in the development of CMMs, with the emergence of both the Zeiss UMM500, which can probably be considered the first modern CMM, as well as the TP1 Renishaw trigger probe. In the 1980s, the market for CMMs grew considerably. The most common type is the bridge CMM [2] consisting of granite rails and air bearings. Indeed, this configuration strikes a very good balance in terms of accessibility, geometric quality, capacity to fix the part directly on the machine and so on. The geometric quality of the CMM, initially obtained by honing the granite elements evolved considerably thanks to the introduction of

numerical geometry correction [3]. Starting in the mid-1980s, the software underwent major improvements in terms of quality [4, 5] and validation of the algorithms [6–8].

The numerical correction of the CMM geometry is based on three assumptions: first of all, for each guideway, the moving part (bridge, carriage, ram) has a rigid body behavior, secondly, the rotation angles are so small that it is possible to write that the cosine is equal to 1 and the sine equal to the angle and, last, the description of geometrical errors of one guideway is independent of the others [9]. In [10], the notations for the description of the geometry are very strictly written and the assumptions for rigid body behavior are studied especially about the stiffness of the granite table. These assumptions work very well for a bridge machine but not, for

example, for a moving ram horizontal-arm machine. For this kind of machine, it is necessary to complete the model. In this article, only bridge machines are considered and the three previous hypotheses are assumed to be valid for these machines.

Under these assumptions, six functions are necessary to describe the geometry of one guideway. In fact, for an horizontal guideway, the CMM defects can be called: linear positioning accuracy, horizontal straightness, vertical straightness, roll, pitch and yaw. Thus, this means that 18 functions are needed to describe the three guideways, to which three parameters (squareness) must be added.

On this basis, Kunzmann and al [11], showed a metrological traceability chain between the realization of the measurement unit (meter) from its definition and the CMM thanks to the correction model and by means of a ball plate.

Since the 1990s, the evaluation of uncertainties has been the subject of a lot of published work [12–19]. Regarding uncertainties, the main ideas are contained in the documents of the Joint Committee for Guides in Metrology, i.e. the GUM (JCGM 100) and supplement 2 (JCGM 102) for an analytical approach and supplement 1 (JCGM 101) [20] for a numerical approach (Monte-Carlo method) [12], and many others proposed the concept of ‘Virtual machine’ which is a practical implementation of JCGM 101 for the CMMs [14], is an approach by constraints, it is a system based on the Maximum Permissible Errors [21].

In the uncertainty budget due to the bridge machine, the geometry is (normally) a small contributor after correction. The most important contributors are thermal problems and (in bad situation) the probe (for example, a very long stylus on a touch trigger probe).

On CMMs and machine tools, thermal drift is a preponderant source of uncertainty and there are some articles addressing this [22–30]. In [30], Balsamo and al. described in six steps a method to correct the thermal effect. The present subject concerns the step B ‘Selection of the thermal model’ in the context of uncertainties assessment. In [25], the authors gave formulas to correct the effect of temperature but a more systematic model is proposed here about the effect of bending guideway, fixed point drift, expansion of scales and so on.

The rules of conception are quite different for a CMM compared with a machine-tool, a major reason is that the effort between the ball tip and the part is in the order of 0.2 N. A CMM must be optimized to achieve excellent repeatability and reproducibility of results. A solution is to use the concept of isostatic coupling. The contact points are designed with an air bearing mounted fixed on a ball joint that provides the equivalent of a point with a frictionless movement. To design a CMM guideway, three contact points are using to make a plane support and two contact points to provide direction. The guideway is completed by a linear scale.

The first objective of this paper is to evaluate the possible and correlated evolution of all the defects of the CMM based directly on the design of the machine studied and thermal variations of the environment.

The second objective is to show that our method is part of a new approach of the concept of virtual machine named Multi Levels Monte Carlo Simulation (MLMCS). This new

approach is intended to describe as precisely as possible the physic behavior of the CMM in order to take into account the covariances as accurately as possible. A summary of the possible complete modeling of a measurement process on CMMs will be presented in this paper.

To summarize, this paper deals with the physical determination of geometry and drift evolution of a CMM. It corresponds to the first level of the MLMCS used to evaluate uncertainties of any measurand on CMMs. The research was performed as part of a French accreditation group for the CETIM (Technical Center for Mechanical Industries).

2. Subject and methods

2.1. Methodology

The methodology, based on MLMCS [31], is described figure 1. The 18 functions and three constants for squareness are determined to calibrate the bridge CMM. During these operations, the temperatures and the gradients are measured. A study of temperatures and gradients is carried out over a long period of time which allow to choose the probability distributions for the Monte Carlo simulations more representative and different to the calibration conditions. A reference correction can be implemented.

For each simulation, the bending and the dilatation of the guideways and of the mechanical structure can be estimated. With these data, the displacements of the aerostatic bearings and the evolution of the scales are calculated and so, the modification of the error components which describe the geometry of the CMM. This means that the drift is directly integrated with the CMM geometrical evolutions during the simulations.

2.2. Definition of the machine coordinate system

ISO 10 360 is the reference standard for the CMM. In 10 360–1 [1], neither the order nor the names of the axes were defined. It is even noted, after the schematic diagram in Annex I, Figure A.2 that ‘The indicated directions are given for information only. Other approaches exist’. In fact, there are several designations for CMM axes according to the manufacturer of the machine.

In France, the classical denomination of the CMM axes was given in the NF E 11–151 [32] standard. This standard, which had the advantage of standardizing the ratings, was suppressed in 2003 due to lack of actual use. Therefore, each manufacturer uses its own conventions. The lack of uniqueness of the notations is a notable constraint for the development of a standard software. The notations of the CMM axes defined in this earlier standard will be used in this paper. It is interesting to note that VCMM developers [12, 13] have made the same choice.

The standard refers to X as the work piece holder (or the slide directly connected to the work piece holder), Z as the probe holder and the Y axis as the complementary axis. The use of X, Y, Z is a direct coordinate system that makes it possible to create a standard system, regardless of the CMM, a noted universal coordinate system.

Figure 1. Schematization of the method.

The coordinate system used by Zeiss on the CMM studied (CONTURA G2) is referenced as the machine tool coordinate system, but it does not correspond to the universal coordinate system defined (figure 2).

To convert any coordinate system to the defined universal coordinate system, one simply has to write the corresponding homogeneous transformation matrix. Thus the transformation from ZEISS coordinates to universal coordinates is

$$\text{written: } \begin{pmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} -y \\ x \\ z \end{pmatrix}.$$

2.3. Geometric evaluation of CMM

2.3.1. Generalities and recommendations To check the 3D geometry of a CMM, there are several well-known methods today, namely:

- Sphere plate artifact.
- Direct interferometry and electronic levels for rotations (conventionally used by manufacturers).
- Laser tracer (currently being evaluated).
- Step gauge and rule (used for French accreditation by the authors for the CETIM for example).

Machine geometry is generally characterized by 18 functions and 3 perpendicularities, schematized in figure 3. Other functions can be added for some machines having, because of their construction, variations of roll or pitch, for example. The objective is to physically represent the defects of the machine. So, it is not conceivable to interpolate each defect of the CMM by too high degree polynomial functions in order to approach the physical geometry of the machine. This must also be decoupled from other aspects related to the automatic control or errors of determination. Therefore, it is optimal to interpolate the variations of the defects of the CMM due to thermal phenomena by a low-level polynomial, a degree of 3 is sufficient [33]. The periodic systematic errors can be taken into account by Fourier series functions calculated on the residues of the function defects of the CMM. Nevertheless, it is important to perform repeatability on each of the geometrical functions of the CMM.

Figure 2. Zeiss coordinate system based on machine tool coordinate system compared to the universal coordinate system.

Indeed, on a CMM, it is conventional to have periodic systematic errors due to, for example, the recirculating ball screw mechanism defects. Nevertheless, not all periodic errors are repeatable, notably linked to stick-slip and hysteresis. These periodic non-repeatable errors are then taken into account in uncertainties.

2.3.2. Setting up geometry and conventions With the definition of the axes presented in §2.2, the machine's geometry can be implemented. So, in figure 2, point Q is at the center of the ball of the working probe. Points O₁, O₂ and O₃ are defined so that point O₃ belongs to the Z probe-bearing axis. Point O₃

Figure 3. Schematic representation of CMM defects.

is, by convention, the center of the ball of a theoretical probe whose lever arm O_3Q is zero, that is to say on the axis of the slide. Point O_2 coincides with point O_3 when the dimension Z is zero. Point O_1 coincides with point O_3 when Y and Z are null. This type of notation has been used by Zhang et al since 1985 [10].

With these notations, rotation and translation vectors for the X -axis could be noted in equation (1) and (2) respectively:

$$\vec{w}_x = (xRx, xRy, xRz) = (\text{roll}, \text{pitch}, \text{yaw}) \quad (1)$$

$$\vec{\varepsilon}_{O_1} = (xTx, xTy, xTz) = (\text{linear accuracy error}, \text{straightness}, \text{straightness}). \quad (2)$$

The same principle applies to Y and Z axes.

The perpendicularity is then corrected and taken into account by adding a constant on the following rotations:

- xRz : perpendicularity between X and Y axes.
- yRx : perpendicularity between Y and Z axes.
- xRy : perpendicularity between Z and X axes.

The basic idea for modeling geometry of a bridge CMM is based on the assumption of the mechanics of the solid body, that is to say that each axis behaves like a solid, moving independently of others. Therefore, with the positions of O_1 , O_2 , O_3 and Q defined in figure 2 and the formalism of torsors, the contribution to displacement of point Q linked to axes X , Y and Z respectively is expressed in the equations (3) and (4).

$$\begin{aligned} \vec{\varepsilon}_x(Q) &= \vec{\varepsilon}_x(O_1) + \vec{w}_x \wedge \overrightarrow{O_1Q} \\ \vec{\varepsilon}_y(Q) &= \vec{\varepsilon}_y(O_2) + \vec{w}_y \wedge \overrightarrow{O_2Q} \\ \vec{\varepsilon}_z(Q) &= \vec{\varepsilon}_z(O_3) + \vec{w}_z \wedge \overrightarrow{O_3Q}. \end{aligned} \quad (3)$$

As a result, the global displacement is:

$$\vec{\varepsilon}(Q) = \vec{\varepsilon}_x(Q) + \vec{\varepsilon}_y(Q) + \vec{\varepsilon}_z(Q). \quad (4)$$

Figure 4. Parametrization for deformation calculation.

2.4. Model for deforming CMM structures

The purpose of this section is to determine the function governing the deformation of a beam subjected to a temperature gradient. In fact, CMM guideways are subject to bending effects related to temperature variations.

So, the equation of heat propagation by conduction, according to Fourier, in stationary thermal conditions, is written: $d^2T/dx^2 = 0$. With this hypothesis, if a beam has a temperature difference ΔT between one face and the other, the temperature distribution is linear.

Assuming that the bottom of the solid is at the reference temperature and corresponds to the length L then, with the notations of the figure 4, the equation (5) can be written.

$$L = 2R\varphi. \quad (5)$$

The equation (6) is written for the upper fiber.

$$L + \alpha L \Delta T = 2(R + h)\varphi. \quad (6)$$

In this equation (6), α is the coefficient of thermal expansion and h the granite height.

The difference between the equation (5) and (6) allows to obtain the equation (7)

$$\alpha L \Delta T = 2h\varphi. \quad (7)$$

In this model, the bending f (figure 4) could be defined by the equation (8)

$$f = (R + h)(1 - \cos(\varphi)). \quad (8)$$

Table 1. Building materials and dimensions of the elements—Zeiss Contura G2.

Axis considered	Dimensions of the axis (mm)			Material of the considered axis	Thermal expansion coefficient of the entity (K ⁻¹)	Thermal expansion coefficient of the scale (K ⁻¹)
	Along X	Along Y	Along Z			
X	$L_X = 1650$	$H_{HX} = 1185$	$H_{VX} = 205$	Granite	$\alpha_x = 6.0 \cdot 10^{-6}$	$\alpha_{Rx} = 5 \cdot 10^{-8}$
Y	$H_{HY} = 76$	$L_Y = 1140$	$H_{VY} = 203$	Ceramic	$\alpha_y = 3,9 \cdot 10^{-6}$	$\alpha_{Ry} = 5 \cdot 10^{-8}$
Z	$H_{DX} = 63$	$H_{DY} = 63$	$L_Z = 950$	Ceramic	$\alpha_z = 3,9 \cdot 10^{-6}$	$\alpha_{Rz} = 5 \cdot 10^{-8}$

aerostatic bearing closest to X_1 . The X-axis guideway is positioned on the right side of the XY granite. The guideway protrudes 60 mm laterally (outer right side).

- P_{3x} corresponds to the aerostatic bearing of normal Z under the left jamb of the bridge.

- P_{4x} and P_{5x} are the 2 lateral bearings of normal Y on the guideway of the conventional X axis of the machine (main driving side of the axis—right jamb of the bridge). P_{4x} is the bearing closest to X_1 .

- P_{6x} is the position of the X-axis scale (reference of the encoder of the scale). This scale is positioned on the guideway along the X-axis.

3.3. Reference entities of the CMM

The same method is used for the Y and Z axis as for the X-axis.

Table 2 summarizes the characteristic points of the CMM studied and the normal vectors associated at these points.

4. Consistent determination of the evolution of machine defects

4.1. Bending effect and axes thermal expansion

The bending and dilatation effects on the axes are summarized in table 3. Hence, the thermal deformations of the machine result from the 9 thermal variations identified (figure 5).

4.2. Effects of thermal variations on the X-axis

The principle involves considering that the displacement of the characteristic points of the axis (the bearings P_{1x} to P_{5x} and the reading head of the scale P_{6x}) corresponds to six small displacements which are expressed with the point considered, that is to say in O_i for the X axis, O_2 for the Y axis and O_3 for the Z axis.

In this way, with the equations defined at §2.3.2., the equation (11) is the expression of the torsor in O_i of the different points P_{ix} for the X-axis.

$$\vec{\varepsilon}(P_i) = \begin{vmatrix} xTx(x) \\ xTy(x) \\ xTz(x) \end{vmatrix} + \begin{vmatrix} xRx(x) \\ xRy(x) \\ xRz(x) \end{vmatrix} \wedge \vec{O_1P_i} \text{ with } i \in \{1, 6\}. \quad (11)$$

4.2.1. Effects of T_{VX} on the X-axis defects With table 3 and the equation (10), it is then possible to solve the series of 6 equations which makes it possible to determine the T_{VX} influence on the defects of the X-axis of the machine. This is

described in the system of equations (12)

$$\left\{ \begin{array}{l} \frac{\alpha_x \cdot L_X^2 T_{VX}}{8H_{VX}} \left(1 - \left(\frac{\vec{X_1P_{ix}} \cdot \vec{n_x} + x - \frac{L_X}{2}}{\frac{L_X}{2}} \right)^2 \right) \\ \quad = \left(\vec{\varepsilon}_{O_1} + \vec{w_x} \wedge \vec{O_1P_{ix}} \right) \cdot \vec{n_{P_{ix}}} \\ \quad \text{with } i = \{1 \text{ to } 3\} \text{ and } \vec{n_{P_{ix}}} = \vec{n_z} \\ 0 = \left(\vec{\varepsilon}_{O_1} + \vec{w_x} \wedge \vec{O_1P_{ix}} \right) \cdot \vec{n_{P_{ix}}} \\ \quad \text{with } i = \{4 \text{ to } 5\} \text{ and } \vec{n_{P_{ix}}} = \vec{n_y} \\ 0 = \left(\vec{\varepsilon}_{O_1} + \vec{w_x} \wedge \vec{O_1P_{6x}} \right) \cdot \vec{n_{P_{6x}}} \\ \quad \text{with } \vec{n_{P_{6x}}} = \vec{n_x}. \end{array} \right. \quad (12)$$

Thus, the T_{VX} effects on the defects xTx , xTy , xTz , xRx , xRy , xRz , calculated with the real data of the CMM studied, are shown in table 4. It is interesting to note that T_{VX} has no influence on the yaw xRz .

4.2.2. Effects of T_{HX} on the X-axis defects From table 3, T_{HX} influence on the defects of the X-axis is obtained by the resolution of the system of equations (13)

$$\left\{ \begin{array}{l} 0 = \left(\vec{\varepsilon}_{O_1} + \vec{w_x} \wedge \vec{O_1P_{ix}} \right) \cdot \vec{n_{P_{ix}}} \\ \quad \text{with } i = \{1 \text{ to } 3\} \text{ and } \vec{n_{P_{ix}}} = \vec{n_z} \\ \frac{\alpha_x \cdot L_X^2 T_{HX}}{8H_{HX}} \left(1 - \left(\frac{\vec{X_1P_{ix}} \cdot \vec{n_x} + x - \frac{L_X}{2}}{\frac{L_X}{2}} \right)^2 \right) \\ \quad = \left(\vec{\varepsilon}_{O_1} + \vec{w_x} \wedge \vec{O_1P_{ix}} \right) \cdot \vec{n_{P_{ix}}} \\ \quad \text{with } i = \{4 \text{ to } 5\} \text{ and } \vec{n_{P_{ix}}} = \vec{n_y} \\ 0 = \left(\vec{\varepsilon}_{O_1} + \vec{w_x} \wedge \vec{O_1P_{6x}} \right) \cdot \vec{n_{P_{6x}}} \\ \quad \text{with } \vec{n_{P_{6x}}} = \vec{n_x}. \end{array} \right. \quad (13)$$

Thus, T_{HX} effects on xTx , xTy , xTz , xRx , xRy , xRz are shown in table 4. It is important to note that only the accuracy error on the axis, the Y-straightness and the yaw are impacted by T_{HX} .

Table 2. Characteristic points of the CMM studied—Zeiss Contura G2.

Axis considered	Reference entities	Conventional local coordinates			Associated conventional normals		
		X (mm)	Y (mm)	Z (mm)	n _x	n _y	n _z
X	Point O_1	−1230	−920	575	−	−	−
	Aerostatic Bearing P_{1x}	−1077,5	0	0	0	0	1
	Aerostatic Bearing P_{2x}	−1547,5	0	0	0	0	1
	Aerostatic Bearing P_{3x}	−1312,5	−1117,5	−120	0	0	1
	Aerostatic Bearing P_{4x}	−1077,5	85	−43	0	1	0
	Aerostatic Bearing P_{5x}	−1547,5	85	−43	0	1	0
	P_{6x} : Scale X	−1205	−67	−100	1	0	0
Y	Point O_2	140	230	−380	−	−	−
	Aerostatic Bearing P_{1y}	−38,5	102	0	0	0	1
	Aerostatic Bearing P_{2y}	−38,5	339	0	0	0	1
	Aerostatic Bearing P_{3y}	0	220,5	−42,5	1	0	0
	Aerostatic Bearing P_{4y}	0	175,5	−160,5	1	0	0
	Aerostatic Bearing P_{5y}	0	265,5	−160,5	1	0	0
	P_{6y} : Scale Y	−76	371	−100	0	1	0
Z	Point O_3	−31,5	31,5	−145	−	−	−
	Aerostatic Bearing P_{1z}	−31,5	0	410	0	−1	0
	Aerostatic Bearing P_{2z}	−15,5	0	215	0	−1	0
	Aerostatic Bearing P_{3z}	−47,5	0	215	0	−1	0
	Aerostatic Bearing P_{4z}	−63	31,5	215	−1	0	0
	Aerostatic Bearing P_{5z}	−63	31,5	410	−1	0	0
	P_{6z} : Scale Z	−31,5	0	270	0	0	1

Table 3. Bending effects and axes dilatations.

Thermal Variations	Bending effect		Dilatation effect on the axis
	Bending Value	Points directly impacted	
T_{VX}	$\frac{\alpha_x \cdot L_x^2 \cdot T_{VX}}{8 \cdot H_{VX}}$	$P_{1x} (\vec{n}_z)$ $P_{2x} (\vec{n}_z)$ $P_{3x} (\vec{n}_z)$	
T_{HX}	$\frac{\alpha_x \cdot L_x^2 \cdot T_{HX}}{8 \cdot H_{HX}}$	$P_{4x} (\vec{n}_y)$ $P_{5x} (\vec{n}_y)$	
T_{RX}			$\propto_{RX} \cdot T_{RX} \cdot x$
T_{VY}	$\frac{\alpha_y \cdot L_y^2 \cdot T_{VY}}{8 \cdot H_{VY}}$	$P_{1y} (\vec{n}_z)$ $P_{2y} (\vec{n}_z)$ $P_{3y} (\vec{n}_z)$	
T_{HY}	$\frac{\alpha_y \cdot L_y^2 \cdot T_{HY}}{8 \cdot H_{HY}}$	$P_{4y} (\vec{n}_x)$ $P_{5y} (\vec{n}_x)$	
T_{RY}			$\propto_{RY} \cdot T_{RY} \cdot y$
T_{DX}	$\frac{\alpha_z \cdot L_z^2 \cdot T_{DX}}{8 \cdot H_{DX}}$	$P_{1z} (\vec{n}_y)$ $P_{2z} (\vec{n}_y)$ $P_{3z} (\vec{n}_y)$	
T_{DY}	$\frac{\alpha_z \cdot L_z^2 \cdot T_{DY}}{8 \cdot H_{DY}}$	$P_{4z} (\vec{n}_x)$ $P_{5z} (\vec{n}_x)$	
T_{RZ}			$\propto_{RZ} \cdot T_{RZ} \cdot z$

4.2.3. Effects of T_{RX} on X-axis defects The T_{RX} effects could be obtained by solving the system of equations (14)

$$\left\{ \begin{array}{l} 0 = (\vec{\varepsilon}_{O_1} + \vec{w}_x \Lambda \overrightarrow{O_1 P_{ix}}) \cdot \vec{n}_{P_{ix}} \\ \text{with } i = \{1 \text{ to } 3\} \text{ and } \vec{n}_{P_{ix}} = \vec{n}_z \\ \\ 0 = (\vec{\varepsilon}_{O_1} + \vec{w}_x \Lambda \overrightarrow{O_1 P_{ix}}) \cdot \vec{n}_{P_{ix}} \\ \text{with } i = \{4 \text{ to } 5\} \text{ and } \vec{n}_{P_{ix}} = \vec{n}_y \\ \\ \propto_{RX} T_{RX} x = (\vec{\varepsilon}_{O_1} + \vec{w}_x \Lambda \overrightarrow{O_1 P_{6x}}) \cdot \vec{n}_{P_{6x}} \\ \text{with } \vec{n}_{P_{6x}} = \vec{n}_x \end{array} \right. \quad (14)$$

However, it is evident that T_{RX} only has an influence on the linear xT_x defect. The result is given in table 4.

4.3. Effects of thermal variations on the Y and Z-axis

The same resolution of the X-axis is performed on the Y and Z axis. The results, applied to the CMM studied, are stored directly in table 4.

4.4. Summary of the effects on the thermal variations

To sum up, in order to characterize the evolution on the CMM, it is necessary to solve nine series of six equations. Table 4 summarizes the different effects of thermal variations on the evolution of the CMM defects. The values in the Table correspond to the polynomial coefficients used to take into account the changes in the geometry of the machine. It is necessary to multiply these coefficients by the term of the corresponding temperature, measured in the area around

Table 4. Impact on the CMM defects and value associated in mm.K^{-1} for each thermal variations.

			Impacted defects taken into account by second degree polynomial functions					
			xTx	xTy	xTz	xRx	xRy	xRz
Thermal Variations on X axis	T _{VX}	0	Drift -4.22287e-2	Drift 4.46935e-4	Drift -5.18832e-2	Constant rotation -7.23195e-7	Perpendicularity -6.2561e-5	
		1	Linear accuracy 1.97561e-5		Perpendicularity 6.01463e-5		Bending X 2.92683e-8	
		2			Vertical bending -1.46341e-8			
	T _{HX}	0	Drift 9.23184e-3	Drift -9.09068e-3				Perpendicularity 1.08228e-5
		1	Linear accuracy -4.31899e-6	Perpendicularity 1.04051e-5				Bending Y -5.06329e-9
		2		Horizontal bending -2.53165e-9				
	T _{RX}	0						
		1	Linear accuracy 5.00000e-8					
		2						
			yTx	yTy	yTz	yRx	yRy	yRz
Thermal Variations on Y axis	T _{VY}	0		Drift 1.88007e-3	Drift 1.8765e-3	Perpendicularity 6.71453e-6		
		1		Linear accuracy -5.37931e-6	Perpendicularity 6.53202e-6	Bending Y -1.92118e-8		
		2			Vertical Bending -9.60591e-9			
	T _{HY}	0	Drift 1.50359e-3	Drift -2.44407e-3	Drift 7.85963e-5		Perpendicularity -4.40316e-7	Constant rotation -1.13151e-5
		1	Perpendicularity 1.18026e-5	Linear accuracy -1.10842e-5				Bending X -5.13158e-8
		2	Horizontal bending 2.56579e-8					
	T _{RY}	0						
		1		Linear accuracy 5.00000e-8				
		2						
			zTx	zTy	zTz	zRx	zRy	zRz
Thermal Variations on Z axis	T _{DX}	0	Drift -1.26982e-3				Constant rotation -1.00595e-5	
		1	Perpendicularity -3.8381e-5				Bending X 6.19048e-8	
		2	Bending 3.09524e-8					
	T _{DY}	0		Drift -1.26982e-3	Drift 3.16875e-4	Constant rotation 1.00595e-5		
		1		Perpendicularity -3.8381e-5	Linear accuracy -1.95e-6	Bending Y -6.19048e-8		
		2		Bending 3.09524e-8				
	T _{DZ}	0						
		1			Linear Accuracy 5.00000e-8			
		2						

the CMM. These terms generate errors in mm.K^{-1} . Four boxes in table 4 have been grayed out because these variations have no impact on the overall geometry of the machine

(constant rotation). All the other variations obtained have been interpreted in terms of corresponding CMM deformations.

Table 5. Thermal variation considered.

Thermal effect	T_{VX}	T_{HX}	T_{RX}	T_{VY}	T_{HY}	T_{RY}	T_{dx}	T_{dy}	T_{RZ}
Maximum thermal variations (°C)	0.3	0.3	0.4	0.05	0.05	0.3	0.05	0.05	0.4

Table 6. Sphere evaluation—Monte Carlo simulation on MCG.

Simulation of the impact of the thermal variations on MCG measurement	Correction of the center position by least square method for each simulation to suppress the drift of reference point

5. Results and analysis

The calibration of the CMM geometry was performed by interferometry and electronic levels for rotations, at least for xRx and yRy . A specific measurement must be made for zRz . The machine was instrumented using temperature sensors (PT 100 wiring in four wires on an Agilent 34972 A power plant) to estimate thermal gradients and axes thermal expansion. The different maximum thermal variations estimated on the CMM are reported in table 5.

So, it is possible to carry out a Monte Carlo simulation in order to estimate the CMM variations. The results are presented in Appendices I, II and III.

Table 6 presents the effects of the CMM geometrical evolution due to thermal variations on the sphere generated by a Machine Checking Gauge (MCG) of 452 mm in diameter. These representations correspond to the experimental measurement of 72 regularly distributed points on which a Monte Carlo simulation is carry out to assess the impact of thermal variations on measurement. The left column shows the simulated errors without treatment. In the right column, a least square refocusing was performed on each of the measurements to remove errors related to the fixed point offset. These thermal drift errors, correspond to the main source of errors during thermal CMM evolutions.

6. Conclusion

This paper presents a physical method for determining the thermal evolutions of the machine's defects based on an analysis of the basic elements of CMM construction. The correction of the bending of the granite table is well-known but this study generalizes the possibilities for the correction of the machines and allows the problem of drift in the points of reference to be better taken into account.

With this method, it is also possible to account for the deformation of the machine caused by the weight of the measured part (deformation of the granite table) in the evaluation of uncertainties. To achieve this, it is sufficient to calculate the bending of the granite support and to carry out similar types of computations. It is also possible to evaluate the impact of the variation of the air film thickness of the aerostatic bearings.

Table 4 identified defects impacted by gradients and thermal variations around the CMM. This analysis is interesting in the design of a CMM. It also provides a better understanding of the evolution of the CMM defects and in particular the problems of drift. These are important and harmful in the context of the use of a rotary table for example over long periods of time.

Finally, this study (carried out for the French CETIM) forms the base of a MLMCS, which allows us to evaluate the uncertainties of any measurand on CMMs [31]. The MLMCS is carrying out on two levels, namely:

Appendix I. Geometrical evolution on the CMM – X-axis.

Appendix II. Geometrical evolution on the CMM – Y-axis.

Appendix III. Geometrical evolution on the CMM—Z-axis.

-The first level takes into account CMM defects and their evolutions caused by thermal variations (the principle topic of this paper) or other reasons. Dynamic effects and defects in the probing system are also added at this level.

-The second level concerns the part and the evaluation of the measurands. This level takes into account the effects related to reference entities, resolutions, repeatability, roughness, uncertainties on the determination of CMM defects.

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