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Terahertz pulse generation by multi-color laser fields with linear versus circular polarization

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We study the influence of the polarization state of multi-color femtosecond laser pulses ionizing air or noble gases on the emitted terahertz radiation. A local-current model and plane-wave evaluations predict a cross-over in the THz energy yields with increasing number of pump harmonics, for which circular laser polarization is more efficient for few harmonics and linear polarization is favourable for more than six pump colors. Comprehensive 3D numerical simulations of gas jet experiments confirm this property for singly- and multiply-ionized gases. Rotation of the THz polarization ellipse in the case of circular laser polarization is explained by phase shifts that may alter the phase angle between the harmonics. © 2021 Optical Society of America

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THz radiation refers to the range of electromagnetic waves associated with $\sim 0.01 - 10$ ps-scaled oscillation periods, nowadays covered by emitter devices employing ultrafast lasers [1]. Their applications are numerous, spanning from medicine with cancer detection [2], remote identification [3], to greenhouse gas detection and plant life monitoring [4]. Besides overcoming water absorption in atmospheric remote spectroscopy, the need of intense THz fields is in constant increase, as the most recent applications require high field strengths, e.g., to probe the dynamics of water molecules [5], to drive matter into metastable states [6], or for atom probe tomography [7].

An efficient method to generate intense THz radiations consists in focusing a two-color ultrashort light pulse composed of the fundamental (FH) and its second harmonic (SH) frequency into a gas. Near focus the pulse creates an electron plasma that produces, through photocurrents, low frequencies belonging to the THz domain. Such is the case with air or noble gases ionized by two-color laser pulses with $\sim 10^{14}$ W cm⁻² intensities, which can radiate broadband, strong (≥ 0.1 GV/m) THz fields with $\sim \mu$ J energies [8]. This technique has several advantages, as it is free of any material damage and can benefit from the laser filamentation process to produce terahertz pulses remotely [9]. Let us recall that much higher THz energies ~ 1 -10 mJ can be obtained by relativistic laser gas-jet [10, 11] and laser solid interactions [12, 13], but they need TW to PW laser systems delivering

Joule energies and intensities larger than 10^{18} W cm⁻².

At moderate laser intensities $\sim 10^{14-15}$ W/cm², several techniques to increase the THz yield by photocurrents have been reported. Using longer FH wavelengths from 0.8 to 2.2 μ m can already augment the radiated energy by one order of magnitude [14, 15]. The recent advent of sub-mJ, ultrafast mid-IR (3.9 μ m) and CO₂ (10.6 μ m) lasers also allowed to reach records of $\sim 2\%$ in conversion efficiency and ~ 0.1 mJ THz energies for pump energies < 10 mJ [16, 17]. Alternative ways may employ gases with higher ionization energies, trigger multiple ionization events [18], or play on the pump duration and plasma dimensions [19].

For a given FH wavelength, higher THz performances were attained by increasing the number of colors [20–22] or modifying the polarization state of the FH and SH components [23, 24]. On the one hand, Gonzalez de Alaiza Martinez *et al.* [20] suggested that, with multiple-color pulses arranged in sawtooth-like wave-shape, THz energy could be dramatically increased by a factor ~ 10 at constant ionization yield compared with a classical two-color arrangement. On the other hand, Meng *et al.* [24] experimentally evidenced from helium gas jets that circularly-polarized two-color pulses with same helicity (CP-S) could deliver ~ 5 times higher THz powers than their linearly-polarized, parallel (LP-P) counterparts. Dai *et al.* [23] earlier reported THz field polarization remaining linear in CP-S pump configuration, with power invariant to any change in the FH-SH relative phase. Meanwhile, the effects of the pump polarization states were also investigated numerically [25, 26]. Increase in the THz power was attributed in [27] to a direct dependency of the drift velocity acquired by photo-ionized electrons on the dominant FH pump amplitude and longer ionization sequences.

Combining the two previous techniques remains to be explored and may considerably increase the energy of the emitted THz pulses. In the present Letter we investigate THz performances of pulse profiles containing up to 10 harmonics (or colors) being either linearly or circularly polarized. We report, by means of an analytical approach and local-current (LC) estimates, a major change in the radiated THz energies when passing from 2 to more than 6 harmonics between LP-P and CP-S sawtooth-like pump pulses at saturated ionization yield. LP-P pulses with large enough number of colors deliver the highest energy yields compared with their CP-S counterpart. This is a generic feature for singly-ionized air molecules or multiply-ionized noble gases

Fig. 1. Left-hand side axis: normalized electron density N_e (black curves), laser field components $E_{x,y}$ (blue and red curves), electron drift velocity at ionization times (blue and red dots) as a function of time for 2-color (a) LP-P; (b) CP-S pulses, and 10-color (c) LP-P and (d) CP-S pulses ionizing O_2 molecules with 200 TW/cm² intensity, 1600 nm FH with 60 fs FWHM [see Eq. (2)]. Right-hand side axis: THz energy (green curves). All quantities are normalized with respect to their maximum value achieved in the 2-color LP-P configuration.

able to produce few tens of μJ radiated energies with modest laser pulse parameters. Rotation of the THz polarization ellipse for CP-S pump configurations is finally addressed and identified as phase shifts induced by nonlinear propagation effects.

According to the LC model [28] and assuming negligible contributions from the Kerr response, the THz emission is proportional to the time derivative of the current density $\vec{J}$:

$$\partial_t \vec{J} + \nu_c \vec{J} = \frac{e^2}{m_e} N_e \vec{E}, \quad (1)$$

where e and m_e are the electron charge and mass, respectively, and $\nu_c = 1/350 \text{ fs}^{-1}$ denotes the electron-neutral collision rate. The growth in the free electron density N_e from neutrals' density $N_a = 2.7 \times 10^{19} \text{ cm}^{-3}$ is, at leading order, modeled by the electron source equation $\partial_t N_e = W(E)(N_a - N_e)$, where $W(E)$ is the ionization rate only depending on $E(t) \equiv |\vec{E}_L(t)|$. This rate is given, in a first approximation, by the quasi-static tunneling (QST) rate, $W[E(t)] = (\alpha/E(t))e^{-\beta/E(t)}$, where the constants (α, β) can be found in [28]. It is applied to the O_2 molecules of air (20 % of N_a) with ionization potential $U_i = 12.1 \text{ eV}$ irradiated by the transverse vectorial Gaussian multi-color field:

$$\vec{E}_L(t) = E_0 \sum_{j=1}^N \frac{\mathcal{E}_j}{2^{\rho/2}} e^{-2 \ln 2 \frac{t^2}{\tau_j^2}} \begin{pmatrix} \sin[j\omega_0 t + \varphi_j] \\ \rho \cos[j\omega_0 t + \varphi_j] \end{pmatrix}, \quad (2)$$

where $\mathcal{E}_j = (-1)^{j+1} / \left(j \sqrt{\sum_{k=1}^N k^{-2}} \right)$ for sawtooth-shaped input fields composed of N colors and $\mathcal{E}_1 = \sqrt{1-r}$, $\mathcal{E}_2 = \sqrt{r}$ for two-color setups in LP-P configuration for which $\rho = 0$. CP-S pulses are similarly described with $\rho = 1$. The parameter r , here always fixed to 0.2, is the two-color SH intensity fraction. The phase φ_j is a constant phase shift. We shall assume same FWHM duration $\tau_j = 60 \text{ fs}$ for all colors if not stated otherwise.

In the plane wave approximation, quasi-DC components of the photocurrents produced by two-color fields ($N = 2$) lead to THz fields behaving as $\vec{E}_{\text{THz}} \propto (\cos \phi, 0)^T$ in LP-P and $\vec{E}_{\text{THz}} \propto (\cos \phi, \sin \phi)^T$ in CP-S [27], where $\phi = \varphi_2 - 2\varphi_1$ is the

effective phase angle between FH and SH. This simple expression justifies the expected linear polarization of THz radiation and invariance of the THz energy with respect to ϕ when using CP-S pump pulses. Following [28], the local THz electric field can be evaluated by the low-frequency filtering of $\partial_t \vec{J}$ [Eq. (1)] in which $N_e(t)$ increases stepwise through elementary steps δN_n at the ionization times $t = t_n$ defined by the extrema of the laser electric field. By using $N_e(t) = \sum_n \delta N_n H_n(t - t_n)$ where $H_n(t)$ is close to the Heaviside function, the current density expresses as $\vec{J}(t) = -e \sum_n \delta N_n [\vec{v}_f(t) - \vec{v}_f(t_n) e^{-\nu_c(t-t_n)}] H_n(t - t_n)$ where $\vec{v}_f(t) = -(e/m_e) \int_{-\infty}^t \vec{E}_L(t') e^{-\nu_c(t-t')} dt'$ describes the net drift velocity which free electrons born at $t = -\infty$ would acquire from E_L . The low-frequency (second) term of this expression highlights that electron acceleration at $t = t_n$ is proportional to $v_f(t_n)$. Approximated in the limits $\omega/\omega_0, \nu_c/\omega_0 \rightarrow 0$ [20], this term provides an estimate of the THz energy as $\eta_{\text{THz}} \propto [\sum_n \delta N_n v_f(t_n)]^2$. This approach is expected to supply qualitative features of direct numerical integrations of Eq. (1), which in turn supplies approximate results to 3D comprehensive propagation models.

Figure 1 displays examples of field patterns and their THz yields for two- and 10-color, 60-fs Gaussian pulses with 200 TW/cm² intensity ionizing O_2 with FH wavelength $\lambda_0 \equiv 2\pi c/\omega_0 = 1600 \text{ nm}$. The blue (red) curve refers to the x (resp. y) component of the laser electric field. With $\varphi_j = 0$ the relative phase between harmonics in Eq. (2) promotes an optimally-emitting plasma in the LP-P case [20]. THz yields are computed for a 90-THz large frequency window. Comparing the 2-color configurations [Figs. 1(a,b)], the THz energy curve numerically computed from Eq. (1) appears larger in the CP-S case compared with the LP-P one. Both pulse configurations fully ionize O_2 to O_2^+ . However, even though the CP-S pulse reaches saturation later in time, the electron drift velocity $v_f(t_n)$ acquired at each ionization instant t_n (see blue dots) is much higher for CP-S than for LP-P pulses, explaining the superiority of the CP-S pulses. Surprisingly, an opposite conclusion follows for a 10-color sawtooth pulse ($N = 10$) as the LP-P configuration yields more THz energy than the CP-S one. Here, the contribution from $v_f(t_n)$ is more important in the LP-P case compared with the CP-S one.

To clear up this inversion of performances, Fig. 2(a) details the THz yield numerically evaluated from the LC model by increasing the number of harmonics in Eq. (2). Trends in the radiated energy indeed become reverted between LP-P and CP-S pulses for a number of colors close to 6. This property can directly be found from the analytical expressions $\eta_{\text{THz}}^{\text{LP-P}} \sim (\sum_{j=1}^N \cos(j\pi/(N+1))/j^2)^2$ and $\eta_{\text{THz}}^{\text{CP-S}} \sim \frac{1}{2} (\sum_{j=1}^N 1/j^2)^2$, assuming constant ionization steps δN_n and same maximum electron density. The former constraint overestimates the photocurrent efficiency over each electron density step for $N > 2$ and CP-S configurations. The latter one is easily satisfied for 200 TW/cm² intensity using the QST tunnel rate because ionization saturates. It is also fulfilled for other ionization rates, e.g., the Perelomov-Popov-Terent'ev (PPT) rate [29] with effective charge numbers $Z_{O_2}^* \sim 1$ [see Fig 2(b)]. In contrast, for $Z_{O_2}^* = 0.53$ [30], the ionization yield strongly varies below saturation between the two pump polarizations and our analytical estimates no longer hold.

The previous properties are now checked by direct 3D numerical computations based on a vectorial version of the unidirectional pulse propagation equation (UPPE) [31]. This numerical model governs the forward-propagating transverse electric field components E_x, E_y of elliptically-polarized pulses subject to linear dispersion and diffraction, together with third-order

Fig. 2. (a) THz energy yields normalized to their LP-P two-color counterpart and computed from the LC model using Eq. (2) for unchirped 2- and 10-color 60-fs pulses with QST ionization rate (blue/red) and 10-color pulses undergoing the PPT rate with $Z_{\text{O}_2}^* = 1$ (purple/cyan curves). Dashed curves refer to analytical expressions (η_{THz}) also normalized to the LP-P 2-color case (see text). (b,c) Peak electron density and conversion efficiency as functions of the input intensity. Vertical dotted curves indicate the minimum intensity value from which singly-ionized charge states are completed.

nonlinear polarization, photo-ionization and related losses [32]. More details about this vectorial model can be found in [27] while the physical parameters for air are taken from [33]. We first validate our theoretical expectations using the simple QST model for singly-ionizable oxygen (20% of N_a) at input intensity $\sim 200 \text{ TW}/\text{cm}^2$. Figures 3(a,b) display for this configuration an ionization yield clamped to saturation during early propagation with two and ten colors. Results from Fig. 2 should thus apply and, indeed, we observe that, unlike the basic 2-color configuration, THz energy increases more in LP-P polarization with 10 colors [Fig. 3(b)]. In Fig. 3(a) fluence patterns reveal a net conical emission for two colors at $z = 500 \mu\text{m}$ forming an angle close to $\sim 4 - 5^\circ$ in agreement with Yu *et al.* [34]. Conical emission here occurs earlier for LP-P pulses ($\sim 5^\circ$) compared to CP-S ones ($\sim 4^\circ$), from the middle of the optical path. Similar features follow from a more realistic ionization model for air [30], encompassing ionization of both O_2 (20%, $Z_{\text{O}_2}^* = 0.53$) and N_2 (80%, $Z_{\text{N}_2}^* = 0.9$) molecules with a PPT rate by 10-color pulses [Figs. 3(c,d)]. Note the sudden increase in the electron density driven by the LP-P pulse, which follows from local phase shifts between the harmonics strongly affecting the peak electric field value (see inset). This enhances the ionization response at $z \approx 20 \mu\text{m}$ and the electron density accordingly. Consequently, this pulse configuration takes over its CP-S counterpart along the remaining propagation range. Interestingly, conical emission patterns with 10 colors remain comparable with those produced by two colors [compare Figs. 3(a) and 3(d)]. Finally, we also tested in Figs. 3(e,f) a multi-ionization (ADK-driven) module detailed in [35] for gas jets of argon (blue/red curves) and of helium (purple curve) at 0.2 atm pressure ($N_a = 5.4 \times 10^{18} \text{ cm}^{-3}$) and for different pump energies. It is clear that, even with higher charge states N_e/N_a close to 2, the major tendencies remain, i.e., LP-P pulses with $400 \text{ TW}/\text{cm}^2$ intensity in argon deliver THz radiation with highest energy, close to $\sim 10 \mu\text{J}$. Helium with larger ionization potentials promote the highest yields, above $40 \mu\text{J}$, reached with $5 \text{ PW}/\text{cm}^2$ intensity. We checked that accounting for avalanche ionization does not change these qualitative behaviors.

Fig. 3. (a,c,e) Peak electron densities and (b,d,f) THz energies computed with a 3D UPPE code for 2-color (dashed curves) and 10-color (solid curves) pulses. Blue/red curves stand for LP-P/CP-S configurations. (a,b) O_2 ionized with a QST rate. (c,d) Realistic air with 20% O_2 and 80% N_2 ($U_i = 15.6 \text{ eV}$) ionized with PPT rate using Talebpour et al.'s charge numbers $Z_{\text{O}_2}^* = 0.53$, $Z_{\text{N}_2}^* = 0.9$ [30]. (e,f) 10-color-driven multiply-ionized argon (blue/red curves) and helium in CP-S configuration (purple curve) at 0.2 atm pressure employing the multi-ionization scheme of [18]. The LP-P pulse triggers density ratio N_e/N_a varying from 1.41 to 2.02; CP-S pulses achieve density ratios of 1.99 and 1.89 in Ar and He, respectively. In (a) and (d) fluence patterns illustrate conical emissions at $z = 500 \mu\text{m}$ in the transverse plane $-100 \leq x, y \leq 100 \mu\text{m}$.

Finally, visual inspection of the UPPE3D results revealed a generic rotation of the THz polarization angle along 0.5 mm propagation ranges for the CP-S pump configuration. As recalled above, in a 2-color CP-S setup the THz polarization angle is determined by the effective phase angle between the two harmonics. Figure 4(a) reports in this respect an anticlockwise rotation that continuously follows the growth of THz emission [see Fig. 3(b)] for singly-ionizable oxygen (20% of N_a , QST rate). As observed from Fig. 4(b) the same property occurs with 10 colors, i.e., the THz radiation globally remains almost linearly polarized, but with slightly larger rotation angle. After testing several potential processes causing this rotation, we inferred that nonlinear propagation effects (e.g., plasma dispersion, distortions induced by local plasma defocusing etc.) introduce phase shifts into the harmonics that cannot preserve a constant relative phase along the pulse oscillations [see Fig. 4(c) detailing FH and SH components of a 2-color pulse at $z = 500 \mu\text{m}$]. This can be approached by considering a time dependent phase function $\varphi_j(t)$ including now linear or quadratic chirp contributions. Figure 4(d) tends to confirm this property when one evaluates from the LC model the THz field produced by a Gaussian pulse acquiring different phase shifts, e.g., from a constant phase angle to linear and quadratic chirps that break the constancy of the 2-color relative phase for equal pulse durations $\tau_2 = \tau_1$.

In conclusion we numerically explored the possibility to enhance the THz energy yield by multi-colored sawtooth pulses arranged in optimum polarization states. Surprisingly, circularly-polarized pulses with 6 or more harmonics do not maximize

Fig. 4. (a) Angular polarization diagrams (energy flux transmitted by a polarizer) extracted from UPPE3D simulations for 2-color Gaussian pulses at the distances: $z = 10 \mu\text{m}$ (dashed), $z = 250 \mu\text{m}$ (dash-dotted) and $z = 500 \mu\text{m}$ (solid curve); (b) same information for a 10-color sawtooth pulse; (c) FH and SH components corresponding to (a) at $z = 500 \mu\text{m}$ and displaying a chirped phase. (d) Polarization rotation induced by a constant phase angle $\phi = 0.19 \text{ rad}$ (red curve) reproducing (a), by a linear chirp with $\phi_j(t) = -1.38t/\tau_j$ (green curve) and by a quadratic chirp with $\phi_j(t) = 5.54t^2/\tau_j^2$ in Eq. (2) for two colors with various pulse durations: no chirp (dashed), $\tau_2 = \tau_1/\sqrt{2}$ (dash-dotted) and $\tau_2 = \tau_1$ (solid blue curve).

the THz energy performances, as linearly-polarized pulses still supply the highest electron density, from singly- or multiply-ionized species. LP-P pulses appear more sensitive to local phase shifts that increase the ionization yield. Our analysis provided evidence that multiple color arrangements deliver the highest energy yields, up to $50 \mu\text{J}$ in He at moderate intensities, in a more efficient way than changing the pump polarization state. However, for few-color sources, passing to circularly polarized pumps (CP-S) remains beneficial for the THz yield. We finally attributed the rotation of the THz field for CP-S pump polarization to the introduction of phase shifts between the harmonics along propagation. With the increasing progress in combining various laser frequencies, we believe that our results will be useful in the all-optical generation of strong THz fields and their applications.

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DISCLOSURES

The authors declare no conflicts of interest.

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