Influence of elastic anisotropy on measured sound velocities and elastic moduli of polycrystalline cubic solids

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Abstract

Cubic solids such as NaCl, crystalline argon, or H₂O-ice VII exhibit significant elastic anisotropy strongly increasing upon compression. As earlier recognized for solid argon and H₂O-ice (both exhibiting Zener ratio $A > 1$), longitudinal sound velocities of their polycrystals, V_{Lav} , measured using Brillouin light scattering (BLS) or pulse-echo ultrasonics are much closer to $V_{\text{L}(111)}$ than to $V_{\text{L}(100)}$, the V_{L} -extremes in any cubic single crystal. Here, we experimentally confirm, using the technique of time-domain Brillouin scattering, the same tendency for NaCl exhibiting the opposite anisotropy type, $A < 1$. To understand this tendency, we modelled orientational distribution and the frequency of occurrence of V_{L} values in texture-free polycrystalline samples of NaCl and solid argon. We found a remarkable and predictable asymmetry of the V_{L} distributions with maxima at $V_{\text{L}(110)}$ which is always much closer to $V_{\text{L}(111)}$. This asymmetry persists in BLS peaks but can be obscured in experiments. In the case of solid argon at 49 GPa, the asymmetry can lead to a moderate deviation of experimental V_{Lav} from V_{LH} (obtained from elastic-stiffness constants C_{ij} applying the Hill approximation) by $\sim 7\%$. The latter can cause, however, a significant overestimation of the aggregate shear modulus by $\delta G/G \sim 50\%$ or of the bulk modulus by $\delta B/B \sim 20\%$ if just one BLS peak of longitudinal modes is detectable. A similar analysis, performed for transverse sound velocities, V_{T} and V_{Tav} , has shown that, by use of a BLS spectrum showing peaks of both longitudinal and transverse modes, overestimation of B is similarly high but that of G is much less dramatic.

1. Introduction

Elastic anisotropy is a quantity describing non-uniformity of response of a single crystal to deformations along different directions, e.g., propagation of sound waves. While description of a single crystal under stress/deformation is straightforward, if the independent elastic-stiffness constants C_{ij} are known, description of response of a dense polycrystalline solid can be done only within of an approximation. The existing ones (e.g. Voigt, Reuss, Hill, Hashin-Shtrikman) were developed in order to take into account the influence of elastic anisotropy on distribution of strain and stress in adjacent grains of a deformed polycrystalline body.¹⁻⁴ They involve assumptions about uniformity of strain and stress as well as of grain shapes and orientations. These approximations are used in various technical application such as engineering or building construction but are of exceptional importance for understanding of propagation of seismic waves in the deep Earth and, as a consequence, of its composition e.g..⁵ According to earlier reports, a significant part of rock-forming minerals exhibits a moderate or decreasing with pressure elastic anisotropy.^{6,7} However, there are also cubic solids showing a strong increase of elastic anisotropy on compression, as recognized earlier^{8,9} and in the present work. For the latter type of cubic solids, a reliable recovery of elastic properties from experimental signals remains a subject of continuous efforts, e.g. when Brillouin light scattering (BLS) is applied to examine polycrystalline samples compressed in a diamond anvil cell (DAC).¹⁰

In the case of a cubic crystal, just three C_{ij} 's (namely, C_{11} , C_{12} and C_{44}) are nonzero and the elastic anisotropy can be quantified using the Zener ratio $A = C_{44}/C'$, the ratio of the two principal shear moduli, C_{44} and $C' = (C_{11} - C_{12})/2$. The first one, C_{44} , is related to simple shear along one of the symmetry directions while the second one, C' , to the tetragonal shear.¹¹ Cubic crystals can be classified with respect to the value of this Zener ratio, namely whether it

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is greater or smaller than unity. As demonstrated below, orientationally isotropic polycrystals of these two classes of cubic solids show distinct signals by measurement of their averaged longitudinal and transverse sound velocity, $V_{L\text{av}}$ and $V_{T\text{av}}$, respectively. As a consequence, a careful signal analysis is required in order to avoid inconsistent $V_{L\text{av}}$ and/or $V_{T\text{av}}$ values as well as of bulk and/or shear moduli (B and/or G , respectively). Special attention should be paid not only to methods of measurement of $V_{L\text{av}}$ and/or $V_{T\text{av}}$, e.g. BLS or pulse-echo ultrasonics (PEUS), but also to procedures used to derive B and G from the collected signals taking into account grain sizes.

Until very recently, PEUS and BLS were the most common techniques used to measure $V_{L\text{av}}$ and $V_{T\text{av}}$ of densified polycrystalline solids. The latter technique is predominantly used to examine small/microscopic objects such as thin films or polycrystals compressed to ultrahigh pressures in a DAC. We show below, that shapes and widths of BLS peaks are controlled by elastic anisotropy, which can strongly increase with pressure and this in different ways for $A>1$ and $A<1$. Possibilities to experimentally analyze shapes of BLS peaks collected from microscopic samples, especially for transverse modes (T-modes) which peaks are much weaker than those of longitudinal modes (L-modes), are limited because it is difficult to compensate low signal-to-noise ratios by extending counting times: In some cases, measurement of only one BLS spectrum can last several days to just extract a peak from the background not to mention its shape.^{10,12} Apparently, $V_{L\text{av}}$ - and $V_{T\text{av}}$ values recovered from such spectra require independent verification. Application of PEUS for measurement of $V_{L\text{av}}$ at ultrahigh pressures is, however, rare because its accuracy is strongly limited by sample sizes. Also, elastic anisotropy biases in a different way (depending on A with respect to unity) $V_{L\text{av}}$ - and $V_{T\text{av}}$ values recovered using the two techniques (see below).

In the last years, an alternative technique of time-domain Brillouin scattering (TDBS) was demonstrated to have significant advantages by examination of elastic behavior of microscopic polycrystalline samples due to its ability to measure longitudinal sound velocities with a high 3D-spatial resolution. This provides V_L variations for differently oriented crystallites or their groups and, as already described in earlier publications, access to the maximal and minimal V_L values, $V_{L\text{max}}$ and $V_{L\text{min}}$, along the fastest and the slowest directions in a single crystal. For cubic crystals, these are always $\langle 111 \rangle$ and $\langle 100 \rangle$, respectively, for $A>1$ and vice-versa for $A<1$. Combined with independently measured bulk modulus and density, knowledge of $V_{L\langle 111 \rangle}$ and $V_{L\langle 100 \rangle}$ provides access to the complete set of C_{ij} of any cubic solid.^{8,9} The $V_{L\text{av}}$ - and $V_{T\text{av}}$ values can then be derived using one of the approximations mentioned above.

In this work, we performed the first TDBS measurements on a polycrystalline sample of NaCl (having $A<1$) compressed to 24 GPa in a DAC using the approach developed earlier.^{8,9,13-15} Our $V_{L\langle 111 \rangle}$ and $V_{L\langle 100 \rangle}$ data confirmed, within experimental uncertainties, the previous unique BLS data-point for a NaCl single crystal compressed to a similar pressure of $P=26$ GPa,¹⁰ as well as the experimental $C_{ij}(P)$ derived from XRD examination of polycrystalline NaCl samples non-hydrostatically compressed in a DAC.¹⁶ Comparison of the existing and of our $V_{L\langle 111 \rangle}$ and $V_{L\langle 100 \rangle}$ values with earlier experimental dependences $V_{L\text{av}}(P)$ for NaCl polycrystals revealed a significant shift of the latter towards $V_{L\langle 111 \rangle}(P)$. In order to understand nature of this shift, recognized earlier for anisotropic cubic solids with $A>1$ where $V_{L\text{av}}(P)$ was also found to approach $V_{L\langle 111 \rangle}(P)$,^{8,9} we performed a detailed analysis of possible origins. For this aim, we modelled shapes of BLS peaks of strongly anisotropic polycrystalline cubic solids with $A<1$ (NaCl) and $A>1$ (solid argon). We have found a remarkable but predictable asymmetry of the peak shapes which make determining of both $V_{L\text{av}}$ and $V_{T\text{av}}$ and of the isotropic elastic moduli B and G ambiguous. We show that ambiguities in determining of $V_{L\text{av}}$ and $V_{T\text{av}}$ are different for the two classes of elastically anisotropic cubic solids ($A<1$ or $A>1$) and for the classical measuring techniques, BLS and PEUS, especially when an operator is involved in the decision about positions of the detected BLS peaks. However, some systematics have also been recognized.

II. TDBS measurements of C_{ij} of NaCl at 24 GPa

In our experiment, NaCl powder was compressed in a DAC between beveled diamond anvils and radially supported by a pre-indented steel gasket. A thin metallic film (Ti, 350 nm in thickness), facing the sample on one of the sides, served as a photo-acoustic transducer which absorbed ultrashort pulses of a pump laser and launched coherent acoustic pulses (CAPs) into

the sample (Fig. 1).¹³⁻¹⁵ Ruby grains placed near the transducer were used for pressure measurement. 3D-spatially resolved velocity of propagation of the CAPs along the DAC axis was measured using a probe laser which pulses could be continuously delayed in time with respect to the pump-laser pulses: The probe laser light, scattered by a moving CAP, interfered on a photodetector with that reflected from stationary optical inhomogeneities and thus produced a signal oscillating as a function of the delay-time between the pump- and probe pulses (Δt) and, accordingly, as a function of the distance from the transducer to the CAP.^{13-15,17} Figure 1a shows one of raw TDBS signals collected in our experiments which shows oscillations due to the propagation of a CAP (named Brillouin oscillations¹⁸⁻²⁰) superimposed with non-oscillating background, caused by a transient dissipation of heat from the sample area hit by the pump laser pulse. Frequencies of the oscillations obey the same equation as in classical BLS measurements: $f_B = 2nV_L/\lambda$, where f_B is the Brillouin frequency, λ wavelength of the probe light in vacuum and n refractive index of the sample material. Accordingly, CAPs propagating through differently oriented elastically anisotropic crystallites generate oscillations of the scattered probe light with f_B proportional to the local V_L (in the crystallites or their groups) along the CAP propagation direction (parallel to the sample axis).^{14,15} In order to axially resolve the V_L values, the short-time Fourier transform (STFT) was applied with a narrow temporal window Δt equal to one oscillation which defined the axial/depth resolution to be ~ 250 nm. Our measurements have been performed on three different samples compressed to $P=24(1)$ GPa and, for each sample, TDBS signals were collected from typically 2 different places. Considering that each TDBS signal provided up to two dozens of independent f_B values (see Brillouin oscillations in Fig. 1), more than 100 independent locally resolved V_L values were measured for differently oriented grains or group of grains. To derive V_L values from the Brillouin frequencies we used here the refractive index $n=1.698$ from our *ab-initio* calculations (to be reported separately²¹). From all the V_L values we extracted the maximal and the minimal ones, V_{Lmax} and V_{Lmin} , respectively. For cubic solids, the latter pair represents, with a high degree of confidence, $V_{L\langle 111 \rangle}$ and $V_{L\langle 100 \rangle}$ or vice-versa, even though the sample is textured.

FIG. 1. (a) TDBS raw signal: relative change of transient reflectivity, as a function of the pump-probe delay, recorded for a polycrystalline NaCl sample compressed to 24(1) GPa. (b) Brillouin oscillations after subtraction of the thermal background from the raw TDBS signal shown in (a). Amplitude of the oscillations was magnified for better visibility. (c) Schematic of the sample inside the DAC and of paths of the pump and probe laser beams.

The V_{Lmax} and V_{Lmin} extracted here for NaCl correspond, respectively, to $V_{L\langle 100 \rangle}$ and $V_{L\langle 111 \rangle}$ (Fig. 2). Using the obtained $V_{L\langle 100 \rangle}=9.0(6)$ km/s and $V_{L\langle 111 \rangle}=7.0(3)$ km/s, we recovered all single-crystal elastic moduli $C_{11}=266(24)$ GPa, $C_{12}=49(12)$ GPa and $C_{44}=28(11)$ GPa applying $B(P)=119.5$ GPa from the Decker's equation of state, $\rho(P)$.²² Then we calculated $V_{L\langle 110 \rangle}=7.6(3)$ km/s (Fig. 2), shear modulus $G_H=50(13)$ GPa and the anisotropy ratio $A=0.27(10)$. To do this, we used the following equations²³:

$$V_{L\langle 100 \rangle} = \sqrt{\frac{C_{11}}{\rho}} ; V_{L\langle 110 \rangle} = \sqrt{\frac{C_{11}+C_{12}+2C_{44}}{2\rho}} ; V_{L\langle 111 \rangle} = \sqrt{\frac{C_{11}+2C_{12}+4C_{44}}{3\rho}} = \sqrt{\frac{B}{\rho} + \frac{4C_{44}}{3\rho}} \quad (1)$$

$$B = \frac{C_{11}+2C_{12}}{3} ; G_H = \frac{1}{2}(G_V + G_R) = \frac{1}{2}\left(\frac{C_{11}-C_{12}+3C_{44}}{5} + \frac{5(C_{11}-C_{12})C_{44}}{4C_{44}+3(C_{11}-C_{12})}\right) \quad (2)$$

where G_V , G_R and G_H represent shear moduli according to the Voigt-, Reuss- and Hill approximation, respectively. Our experimental $V_{L\langle 100 \rangle}$ and $V_{L\langle 111 \rangle}$ of NaCl at $P=24$ GPa agree, within the experimental errors, with results of the unique classical BLS measurement on a single crystal of NaCl at a similarly high pressure of $P=26$ GPa¹⁰ (Fig. 2). They also agree reasonably well with results of a rarely used approach based on radial-XRD measurements on powders compressed in a DAC¹⁶ (Fig. 2). In the latter approach, nonhydrostatic compression causes a systematic difference in the interplanar distances $d(hkl)$ due to the presence of uniaxial stress which permits to derive, making some assumptions, all $C_{ij}(P)$ of cubic solids. Earlier reported $V_{L\text{av}}$ values of polycrystalline NaCl, measured using the conventional BLS- and PEUS techniques, are located between our $V_{L\langle 100 \rangle}$ and $V_{L\langle 111 \rangle}$ and show the tendency to approach $V_{L\langle 111 \rangle}$ (Fig. 2).

FIG. 2. Pressure dependences of longitudinal sound velocities of NaCl measured using different methods. The $V_{L\langle 100 \rangle}$ and $V_{L\langle 111 \rangle}$ derived from our TDBS measurements on a polycrystalline sample of NaCl at $P=24$ GPa are shown by solid red circles with error bars. They agree with the earlier measurements on NaCl single crystals using classical BLS (solid blue diamonds¹⁰ and solid blue squares²⁴) and pulse-echo ultrasonics (solid green circles²⁵) as well as with $V_{L\langle 100 \rangle}$ and $V_{L\langle 111 \rangle}$ derived from the radial-XRD examination of NaCl polycrystals compressed nonhydrostatically (crosses¹⁶). The open red circle with error bars indicates $V_{L\langle 110 \rangle}$ calculated from our $V_{L\langle 100 \rangle}$ and $V_{L\langle 111 \rangle}$ (see Eq. (3) below) while the open blue diamond shows $V_{L\langle 110 \rangle}$ from the classical BLS measurement at 26 GPa.¹⁰ The earlier experimental $V_{L\text{av}}(P)$ for polycrystalline NaCl are shown as follows: classical BLS results - open blue squares²⁶; ultrasonic measurements - open green triangles²⁷ and open green circles.²⁸

III. V_L distribution in elastically anisotropic cubic crystals

The fact that $V_{L\text{av}}$ obtained in classical BLS measurements and, in particular cases considered below, in PEUS measurements are much closer to $V_{L\langle 111 \rangle}$ than to $V_{L\langle 100 \rangle}$ was first recognized in high-pressure experiments on H_2O ice⁸ and argon⁹ crystallizing on compression in cubic structures. The important difference of these two solids from NaCl is the inverse ratio of the velocity extremes: In H_2O ice and cubic argon, $V_{L\langle 111 \rangle}$ is not the slowest but the fastest direction of sound propagation in a single crystal. In the present and in the previous works, first application of high-pressures permitted to reveal this particular tendency for $V_{L\text{av}}$ because

elastic anisotropy of these compounds grew on compression to the levels where the tendency surpassed experimental uncertainties.

In order to understand this tendency, we performed a detailed analysis of distribution of sound velocities in NaCl (at 24 GPa and 1 atm.) and in solid argon (at 49 GPa and 2.4 GPa) which were selected as the representatives of cubic solids with $A < 1$ and $A > 1$, respectively. The pressure of 24 GPa was chosen for NaCl because its elastic anisotropy approached the maximum but the transition to the high-pressure B2 phase at ~30 GPa not yet commenced.²⁹ The reason for choosing $P=49$ GPa for solid argon is the same: at this pressure its elastic anisotropy approaches the highest measured value.⁹ The pressure of $P=2.4$ GPa is just above the value where condensed argon solidifies.³⁰ Another reason for the above selections is a similarly high value of A , in the case of solid argon, and of its inverse, $1/A$, in the case of NaCl.

At the first step, we calculated V_L -histograms representing the probability to measure each of the possible V_L 's along a fixed direction in space when a single crystal of NaCl (Fig. 3a-b) or of solid argon (Fig. 3d-e) is uniformly rotated in the 3D space. Such a histogram is equivalent to statistical distribution of V_L in a texture-free polycrystalline sample and, accordingly, to the ideal shape of its BLS peak collected for a particular scattering direction if the instrument function, background and noise of the experimental set-up are neglected. This statement is valid when wavelengths of longitudinal waves, λ_{ac} , scattering the incident laser radiation are shorter than typical size of crystallites constituting the sample. The latter is usually the case in classical BLS measurements on common polycrystalline samples free of intentionally added nm-sized grains (typically <100 nm) which elastic properties can, in addition, deviate from those of sub- μ m- and μ m-sized grains in common polycrystalline solids. More precisely, such histograms can be attributed to BLS peaks collected in the backscattering geometry, $\theta=180^\circ$, if the examined polycrystalline NaCl sample is composed of grains larger than ~160 nm. The latter value is similar to or above the wavelength $\lambda_{ac}=\lambda_L/(2n\sin(\theta/2))$ of acoustic waves probed using a typical laser with the wavelength of $\lambda_L=532$ nm. In the case of the $\theta=90^\circ$ scattering geometry, the grain-size limitation increases to ~250 nm, which is still small.

Figures 3a and 3b show V_L -histograms calculated for NaCl using C_{ij} measured for a single crystal at $P=1$ atm.²⁵ and those measured here at $P=24$ GPa, respectively. Figures 3d and 3e show histograms calculated for solid argon using earlier reported experimental C_{ij} at $P=2.4$ GPa³⁰ and at $P=49$ GPa,⁹ respectively. For both solids, it is the increase of anisotropy on compression which causes broadening of the histograms over significant V_L -ranges and, more importantly, their asymmetric shapes with sharp maxima: For NaCl at $P=1$ atm. and $P=24$ GPa, the peak maximum is located at $V_L=4.5$ km/s and $V_L=7.6$ km/s, respectively, closer to the lower end of the histograms limited by $V_{L\langle 111 \rangle}$ (Figures 3a and 3b). For solid argon at $P=2.4$ GPa and $P=49$ GPa, the peak maximum is located at $V_L=3.3$ km/s and $V_L=8.2$ km/s, respectively, closer to the upper end of the histograms limited, again, by $V_{L\langle 111 \rangle}$ (Figures 3d and 3e). Maxima of these peaks correspond, for each of the solids, to $V_{L\langle 110 \rangle}$ exactly, as followed from our direct calculations of $V_{L\langle 110 \rangle}$ using the same experimental C_{ij} 's (Fig. 3). Appearance of such clear local maxima in the histograms is due to the fact that (i) orientations along and close to $\langle 110 \rangle$ are highly populated in cubic crystals and (ii) variation of V_L with orientation is monotonous. The latter can be recognized from 3D representations of orientational distribution of V_L in a single crystal of NaCl at 24 GPa (Fig. 3c), and in a single crystal of solid argon at 49 GPa (Fig. 3f). For both solids, the distribution of V_L is of the same character except the directions corresponding to the maximal and minimal V_L are inversed. Moreover, the position of $V_{L\langle 110 \rangle}$ between $V_{L\langle 100 \rangle}$ and $V_{L\langle 111 \rangle}$ is not arbitrary but defined by the equation:

$$V_{L\langle 100 \rangle}^2 - V_{L\langle 110 \rangle}^2 = 3(V_{L\langle 110 \rangle}^2 - V_{L\langle 111 \rangle}^2) \quad (3)$$

which can be easily verified by substitution of squares of $V_{L\langle hkl \rangle}$ (given in Eqs. (1)) in the present Eq. (3). In the case of a weak elastic anisotropy, when A approaches unity, $|V_{L\langle 111 \rangle} - V_{L\langle 100 \rangle}| \ll V_{L\langle hkl \rangle}$ (for any h , k and/or l) and $(V_{L\langle 100 \rangle} + V_{L\langle 110 \rangle}) / (V_{L\langle 110 \rangle} + V_{L\langle 111 \rangle})$ is close to unity. Then Eq. (3), rewritten as:

$$(V_{L\langle 100 \rangle} - V_{L\langle 110 \rangle})(V_{L\langle 100 \rangle} + V_{L\langle 110 \rangle}) = 3(V_{L\langle 110 \rangle} - V_{L\langle 111 \rangle})(V_{L\langle 110 \rangle} + V_{L\langle 111 \rangle}) \quad (3a)$$

can be simplified to:

$$V_{L(100)} - V_{L(110)} \approx 3(V_{L(110)} - V_{L(111)}) \quad (4)$$

The latter result indicates that the difference $|V_{L(110)} - V_{L(111)}|$ makes only ~25% of the maximal possible spreading of V_L 's in a cubic single crystal, equal to $|V_{L(100)} - V_{L(111)}|$.

Further, we calculated V_{Lav} values applying the Voigt-, Reuss-, and Hill approximations (V_{LV} , V_{LR} , and V_{LH} , respectively) using the same C_{ij} as by establishing of the histograms and compared them with $V_{L(110)}$ in Fig. 3a-b and 3d-e. Here, V_{LH} can be attributed to sound velocity in an isotropic polycrystalline solid when λ_{ac} is greater than grain sizes. The latter is usual in PEUS measurements and could be the case in particular BLS measurements with small scattering angles θ when polycrystals contain grains of intermediate sizes, between about 100 and 250 nm. We also derived the value V_{LC} indicating center of mass of the histogram which can be attributed to V_{Lav} in rare PEUS measurements where λ_{ac} is smaller than grain sizes. Common for such case is a higher value of V_{LC} when compared with V_{LH} , independent of A (see Fig. 3a, b, d, e).

Applying the Voigt approximation to estimate sound velocity in an isotropic polycrystalline solid:

$$V_{LV} = \sqrt{\frac{9C_{11} + 6C_{12} + 12C_{44}}{15\rho}} \quad (5)$$

and Eq. (1) for $V_{L(110)}$, we found, in addition, that:

$$V_{L(110)}^2 - V_{LV}^2 = \frac{(A-1)C'}{5\rho} \quad (6)$$

This indicates that, for all cubic solids with $A > 1$ (such as argon), $V_{L(110)}$ is always higher than V_{LV} and, consequently, than V_{LH} and V_{LR} (Fig. 3d-e). Accordingly, maxima of ideal BLS peaks, if selected by an operator, will provide overestimated V_{Lav} (similar to $V_{L(110)}$) when compared with V_{LH} from, for example, PEUS measurements. In the case of solids with $A < 1$ (e.g. NaCl), $V_{L(110)}$ is always smaller than V_{LV} but V_{LR} can be either smaller or greater than $V_{L(110)}$ but V_{LH} appears to be always similar to $V_{L(110)}$ (Fig. 3a, b).

Another interesting observation valid for both cubic solids considered here, e.g. for $A > 1$ and for $A < 1$, is an apparent growth with pressure of the difference between the approximations of velocity in polycrystalline solids V_{LR} , V_{LH} and V_{LV} , on one hand, and V_{LC} , on the other. In order to verify this statement, we evaluated the distance between V_{LV} (representing the group V_{LR} , V_{LH} and V_{LV}) and V_{Lmax} representing V_{LC} . The latter replacement, needed because V_{LC} cannot be expressed analytically, is plausible because, for each of the considered two solids, V_L 's redistribute towards the histogram part with higher velocities (see Fig. 3b, e) and V_{LC} moves, accordingly, towards V_{Lmax} . For NaCl having $A < 1$, $V_{L(100)}$ is the upper extreme (Fig. 3b) and the distance to V_{LV} changes according to the relation:

$$V_{L(100)}^2 - V_{LV}^2 = \frac{4(1-A)C'}{5\rho} \quad (7)$$

From 1 atm. to 24 GPa, this difference increases with pressure because $(1-A)$ increases by 2 times (Fig. 3a and 3b) and the basic shear modulus C' increases also. On the other hand, the denominator ρ increases in this pressure range by 12% only.²² In the case of solid argon having $A > 1$, $V_{L(111)}$ is the upper extreme and the distance to V_{LV} changes according to the equation:

$$V_{L(111)}^2 - V_{LV}^2 = \frac{8(A-1)C'}{15\rho} \quad (8)$$

From 2.4 GPa to 49 GPa, this difference increases too because A increases from ~3 to ~18 and $(A-1)$, accordingly, by more than eight times while C' also grows. The denominator ρ increases, in the same pressure range, by two times only.³¹ Consequently, the difference between V_{LV} (representing the group V_{LR} , V_{LH} and V_{LV}) and V_{Lmax} (representing V_{LC}) increases with pressure for both $A < 1$ and $A > 1$ if pressure dependence of elastic anisotropy is stronger than that of the ratio ρ/C' .

FIG. 3. Histograms of the frequency of occurrence of V_L values in a cubic single crystal of NaCl (a and b) and of solid argon (d and e), and 3D representations of V_L values (color scales) along different directions in single crystals of NaCl (c) and of solid argon (f). The histograms are equivalent to statistical distributions of V_L in texture-free polycrystalline samples measured, at the indicated pressure, for a selected sound propagation direction. The histograms for NaCl (red bars) were calculated using the earlier reported experimental C_{ij} at 1 atm.²⁵ (a) and our experimental C_{ij} at 24 GPa (b). The histograms for solid argon (red bars) were calculated using earlier published experimental C_{ij} at 2.4 GPa³⁰ (d) and 49 GPa⁹ (e). $V_{L(100)}$ and $V_{L(111)}$ are the maximal and the minimal V_L values for NaCl having $A < 1$, while the case is opposite for solid argon having $A > 1$. Vertical dashed lines in (a, b, d, e) indicate the velocities V_{LV} , V_{LR} and V_{LH} obtained using the three well-known approximations, Voigt, Reuss, and Hill, respectively. Solid curves represent modelled shapes of BLS-peaks for isotropic densified polycrystalline samples obtained via convolution of the histograms with Gaussian distributions having widths of 0.25 GHz (gray lines) and of 1 GHz (black lines). The vertical dashed lines labeled with V_{LC} indicate positions of mass-centers of the histograms while V_{LW} indicate positions of FWHM-middles of the BLS peaks modelled using the wider Gaussian distribution.

As mentioned above, the histograms shown in Fig. 3 can be considered as ideal representations of intensity distribution in BLS peaks collected from polycrystalline texture-free samples if grains composing them are sufficiently large (above 160-250 nm, depending on the BLS geometry), background, noise and all line-broadening effects are negligible. In order to take line-broadening into account, we modelled shapes of experimental BLS-peaks by convolution of the histograms with Gaussian distributions having widths of 0.25 GHz and of 1 GHz. The latter value was taken from a BLS spectrum collected from a NaCl single-crystal compressed to $P=26$ GPa (see figure 10 in Ref. 6). It appears to be mostly caused by a significant numerical aperture of the optics used to collect the scattered light because it exceeds the instrument function of a typical BLS spectrometer. The latter we estimated to be ~ 0.25 GHz or $\sim 1\%$ of the range of frequencies (proportional to V_L) covered by the spectrum in the same figure 10 in Ref. 6. As shown in Fig. 3, the peak shapes modelled using the narrower Gaussian distribution resemble shapes of the histograms. However, the peak models obtained using the wider Gaussian distribution obscure the histogram asymmetry, especially for the weaker anisotropy. Apparently, the BLS peak asymmetry will further be obscured by electronic noise, background, not to mention texture in the examined polycrystalline sample. If texture is not pronounced then middle of the full width at half maximum (FWHM) of the recorded BLS-peak, V_{LW} , is usually attributed to V_{Lav} . In the particular cases of NaCl compressed to $P=24$ GPa and of solid argon compressed to $P=49$ GPa, V_{LW} values are ~ 5 -7% higher when compared with the corresponding V_{LH} values (Fig. 3b and 3e, respectively). In general, the extracted V_{Lav} will depend, for such signals, on the

method used to determine the BLS-peak position. These could be the peak maximum, its center-of-mass, or middle of the FWHM given by $V_{L(110)}$, V_{LC} or V_{LW} , respectively. Agreement of $V_{Lav}(P)$ of polycrystalline NaCl from PEUS measurements²⁷ with that from the BLS measurements²⁶ suggest that BLS-peak maxima and not V_{LW} were preferred in the latter work. However, we cannot exclude that texturing of the NaCl samples upon compression between opposed anvils even stronger promoted the mutual agreement and the tendency of V_{Lav} to approach $V_{L(111)}$ (Fig. 2).

In the case of solids having $A > 1$, such as argon, the values of V_{LC} , V_{LW} and $V_{L(110)}$ are similar and the derived V_{Lav} will not depend on the BLS-peak quality and the operator choice (Fig. 3e). On the other hand, all established approximations of sound velocities provide lower values of V_{LV} , V_{LH} and V_{LR} . Accordingly, $V_{Lav} = V_{LH}$ obtained using PEUS will disagree with the BLS result, where V_{LW} should be selected. Thus, BLS measurements on polycrystals with $A > 1$ are expected to overestimate V_{Lav} and cause the tendency of approaching of $V_{L(111)}$ by V_{Lav} .

Summarizing, attributing of maximum of a BLS-peak (located at $V_{L(110)}$), measured for any polycrystalline sample of an elastically anisotropic cubic solid, to V_{Lav} will always lead to the recognized approaching of $V_{L(111)}$ by V_{Lav} . For solids with $A < 1$, V_{Lav} attributed to $V_{L(110)}$ would agree with V_{LH} and thus with PEUS data. For solids with $A > 1$, V_{Lav} attributed to $V_{L(110)}$ would be systematically higher than V_{LH} . The case where V_{Lav} is attributed to V_{LW} is less straightforward: For solids with $A < 1$, such $V_{Lav} = V_{LW}$ will deviate from V_{LH} and provide overestimated values. For solids with $A > 1$, such $V_{Lav} = V_{LW}$ will provide a value similar to $V_{L(110)}$, thus been closer to $V_{L(111)}$ than to $V_{L(100)}$ and, again, higher than V_{LH} . With other words, V_{Lav} recovered from BLS measurements on polycrystalline elastically anisotropic cubic samples using any of the approaches will be either equal to or higher than V_{LH} , independent of the Zener ratio A .

IV. V_T distribution in elastically anisotropic cubic crystals

In this section, we examine theoretically distribution of velocities of T-modes (V_T) in polycrystalline orientationally isotropic samples of elastically anisotropic cubic solid. In contrast to BLS peaks of L-modes, those of T-modes are difficult to measure due to a low scattering power as well as due to less favorable scattering geometries at which transverse modes can be detected.³² This could be one of the main reasons why high-pressure BLS measurements of V_{Tav} at elevated pressures are not available for NaCl, and those for solid argon resulted in $G(P)$ deviating by 100%.^{32,33} Accordingly, discussion of a relation between the experimental V_{Tav} data and the modelled-here V_T -histograms and BLS peaks would be premature.

To obtain V_T -histograms and to model BLS peaks of T-modes in polycrystalline NaCl and solid argon, we first calculated histograms for the slow (V_{T1}) and fast (V_{T2}) transverse modes in their single crystals and then summed them (Fig. 4). The calculations were performed at the same pressure conditions as above for the L-modes: For NaCl, the V_T histograms were calculated at $P = 1$ atm and $P = 24$ GPa. In the latter case the C_{ij} 's derived from our TDBS measurements were used. For solid argon, the V_T histograms were calculated at $P = 2.4$ GPa and $P = 49$ GPa using C_{ij} values reported elsewhere.^{30,9} To model the corresponding BLS peaks, the histograms were convoluted, as above, with Gaussian distributions having widths of 0.25 GHz and 1 GHz (Fig. 4).

As can be recognized in Fig. 4, the histograms of T-modes spread over much wider V_T ranges (relative to the absolute V_T values) when compared with the corresponding V_L histograms in Fig. 3. Also, the V_T histograms exhibit two local maxima on different sides of the covered V_T range and the local maximum at the extreme $V_{T1(100)} = V_{T1(110)} = V_{T2(100)}$ is almost one order of magnitude higher than the second one near but not coinciding with $V_{T1(111)} = V_{T2(111)}$. In the case of NaCl, the dominant maxima of the V_T histograms are located at V_{Tmin} and contain mostly contributions of the V_{T1} modes (green lines in Fig. 4a, b). In the case of solid argon, the dominant maxima are located at V_{Tmax} and contain mostly contributions of the V_{T2} modes (blue lines in Fig. 4c, d). However, convolutions of the histograms with the Gaussian distributions (representing, respectively, an ideal and a typical instrument function of a BLS set-up) strongly suppress intensities of the dominant peaks: In the BLS signals modelled using the narrower Gaussian distribution with FWHM = 0.25 GHz, the two local maxima can be

recognized (gray solid curves in Fig. 4). Convolution with the wider Gaussian distribution obscured the two local maxima especially when the elastic anisotropy is not extremely high (black solid curves in Fig. 4), only the modelled BLS peaks become asymmetric. It seems to be very difficult to recognize these local maxima in real peaks of T-modes because they will be further obscured by noise, background and, eventually, sample texture. However, in some high-pressure experiments on polycrystalline samples of cubic H_2O ice, splitting of BLS peaks of T-modes was reported.³² Authors of the work attributed the additional peak(s) to the polycrystalline nature of their samples without further specifications.

FIG. 4. Histograms of the frequency of occurrence of V_T values (comprising V_{T1} and V_{T2}) in a cubic single crystal of NaCl (a and b) and in solid argon (c and d). The histograms were calculated using the same C_{ij} 's as by calculation of the V_L histograms in Fig. 3. Histograms for the slow (V_{T1}) and fast (V_{T2}) transverse modes are shown by green and blue solid lines, respectively. Their sums are shown by red bars. Vertical dashed lines indicate the velocities V_{TV} , V_{TR} and V_{TH} obtained using the three well-known approximations, Voigt, Reuss, and Hill, respectively. Gray and black solid lines represent modelled shapes of BLS-peaks for isotropic densified polycrystalline samples. They were obtained via convolution of the histograms with Gaussian distributions having widths of 0.25 GHz and of 1 GHz, respectively. The vertical dashed lines labeled with V_{LC} indicate positions of mass-centers of the histograms while V_{LW} indicate positions of FWHM-middles of the BLS peaks modelled using the wider Gaussian distribution.

Although the V_T distributions in Fig. 4 are very wide, especially when elastic anisotropy becomes pronounced (e.g. on pressure increase), the difference between V_{TW} and V_{TH} is less significant when compared with that between V_{LW} and V_{LH} . Even though, V_{TW} shifts faster towards V_{Tmax} with increasing anisotropy than V_{TH} , the overestimation of $V_{Tav}=V_{TW}$ recovered from a classical BLS measurement with respect to $V_{Tav}=V_{TH}$ measured using a PEUS technique appears to remain moderate (see also below). Finally, our results in Fig. 4 suggest that increase of elastic anisotropy is accompanied by a systematic shift of V_{TW} and V_{TC} to V_{Tmax} , independent of the anisotropy type, $A>1$ or $A<1$.

V. Uncertainties in isotropic elastic moduli B and G due to elastic anisotropy

As recognized above, elastic anisotropy can lead to a systematic overestimation of V_{Lav} and V_{Tav} recovered from BLS- and, in some cases, from PEUS measurements on dense orientationally isotropic polycrystalline samples even though the sample materials exhibit cubic structure. The deviation is systematic and can be predicted if C_{ij} values are known. The latter are, however, often not known for new materials not available or not accessible as single crystals. New compounds and phases forming at high pressures are just two examples

of such materials. Below, we estimated deviations in determining of B and G when such overestimation of V_{Lav} and/or V_{Tav} takes place.

Firstly, we consider the frequent case when only one BLS peak of L-modes is detectable. Applying the equation relating V_{Lav} in an isotropic polycrystalline solid to B and G :

$$V_{\text{Lav}} = \sqrt{\frac{3B+4G}{3\rho}} \quad (9)$$

and assuming that B was determined correctly in an independent measurement, e.g. from an equation of state $\rho(P)$, we estimated the error for G to be:

$$\frac{\delta G}{G} = \left(\frac{3B}{2G} + 2\right) \frac{\delta V_{\text{Lav}}}{V_{\text{Lav}}} \quad (10)$$

To provide a quantitative example, we consider here the realistic differences in V_{Lav} discussed above for solid argon at $P=49$ GPa. Here, independent of the BLS peak quality, the operator will select, most probably, the value $V_{\text{LW}} \approx V_{\text{L(110)}} \approx V_{\text{LC}}$ as that corresponding to V_{Lav} while V_{LH} is $\sim 7\%$ lower. Applying the earlier published $B=190$ GPa^{31,33,35} and $G=57$ GPa^{9,33} at $P=49$ GPa, we obtained the relative deviation of the shear modulus to be $\delta G/G \approx 50\%$.

In the opposite case, when G is correctly measured but B is not known, the error in determining of B is given by the equation:

$$\frac{\delta B}{B} = \left(\frac{8G}{3B} + 2\right) \frac{\delta V_{\text{Lav}}}{V_{\text{Lav}}} \quad (11)$$

For the same case of solid argon at $P=49$ GPa, the overestimation of V_{Lav} by the same $\sim 7\%$ results in a deviation of the bulk modulus by $\delta B/B \approx 19.6\%$. Thus, the overestimation caused by use of V_{Lav} recovered from classical BLS measurements can be significant for B but less dramatic than for G .

The second frequent case is a BLS spectrum showing two peaks due to L- and T-modes. In the case of orientationally isotropic polycrystalline sample of solid argon at $P=49$ GPa, these peaks should have asymmetric shapes as shown in Fig. 3e and 4d, respectively. Applying the equation relating transverse sound velocity in a polycrystalline solid, V_{Tav} , and the isotropic shear modulus G :

$$V_{\text{Tav}} = \sqrt{\frac{G}{\rho}} \quad (12)$$

we obtained for solid argon at $P=49$ GPa the relative overestimation $\delta G/G = (V_{\text{TW}}^2 - V_{\text{TH}}^2)/V_{\text{TH}}^2 = 9.7\%$. To estimate deviation of B of solid argon, we used an equation similar to Eq. (11):

$$\frac{\delta B}{B} = \left(\frac{8(G+\delta G)}{3B} + 2\right) \frac{\delta V_{\text{Lav}}}{V_{\text{Lav}}} \quad (11a)$$

and obtained almost the same $\delta B/B \approx 20.2\%$ as above for single BLS peak of the L-modes. Summarizing, both B and G can be overestimated if classical BLS spectra collected from polycrystalline orientationally isotropic samples of elastically anisotropic cubic solids contain two peaks of the T- and L-modes. However, the overestimation of G is much less dramatic than by use of the V_{Lav} peak position in a BLS spectrum with a single L-peak and an independently measured B .

Finally, we consider uncertainty in the above systematic deviations of isotropic moduli if C_{ij} values from TDBS measurements are biased by an uncertainty in the used refractive index. As already mentioned in Section II, we used theoretical refractive index $n=1.698$ at $P=24$ GPa to derive the local V_{L} values in our polycrystalline NaCl sample. Here we apply, in addition, the earlier reported $n=1.68$ measured upon shock compression of NaCl³⁶ in order to quantify influence of the 1%-uncertainty in n on V_{L} - and C_{ij} values of NaCl obtained from TDBS signals. For this aim, we used both n -values to derive first $V_{\text{L(111)}}$ and $V_{\text{L(100)}}$, then C_{ij} 's, and, finally, the values V_{LH} and V_{LW} . Applying our theoretical $n=1.698$, we obtained $V_{\text{LH}}=7.61$ km/s, $V_{\text{LW}}=8.05$ km/s and the ratio $(V_{\text{LW}}-V_{\text{LH}})/V_{\text{LH}}=5.75\%$. Applying the previously reported experimental $n=1.68$, we obtained $V_{\text{LH}}=7.70$ km/s, $V_{\text{LW}}=8.11$ km/s and the ratio $(V_{\text{LW}}-V_{\text{LH}})/V_{\text{LH}}=5.32\%$. For the value of interest, $\delta G/G$, we obtained, applying Eq. (10), 32.3% and

28.7%, respectively. Thus, the degree of elastic anisotropy derived from TDBS measurements is relatively sensitive to the used refractive index. However, our findings on systematic deviation of sound velocities and elastic moduli of polycrystalline samples of elastically anisotropic cubic solids, if derived from classical BLS and PEUS techniques, are not affected by the latter outcome in no way.

In classical BLS measurements, determining of V_{Lav} and V_{Tav} depends on the spectrum quality and its interpretation by the operator.¹⁰ Furthermore, in such measurements on microscopic samples compressed in a DAC, “averaged” sound velocity is sometimes derived from weak and noisy peaks overlapping with flanks of strong BLS-peaks of diamond anvils and, eventually, of a pressure transmitting medium. Background scattering and electronic noise make determining of V_{Lav} and V_{Tav} even more demanding and counting times, for a single BLS spectrum, up to 72 hours are not rare.^{10,12} Even if all above considered aspects are taken into account and the experimental procedure optimized, sample texture can further bias the BLS-peak shapes and positions, or duration of propagation of acoustic pulses in PEUS measurements. It appears that, in the case of NaCl, the much stronger approaching of $V_{\text{L}(111)}$ by V_{Lav} (see Fig. 2), when compared with that predicted by Eq. (3), is caused by a strong sample texture during the classical BLS- and PEUS measurements.²⁶⁻²⁸ Pronounced texturing of polycrystalline NaCl samples upon compression between opposed anvils was already documented.³⁷

Some of the experimentalists who applied classical BLS to examine solids compressed in a DAC, including NaCl,¹⁰ considered various sources of experimental uncertainties and limitations of this technique. However, the systematic tendency of $V_{\text{Lav}}(P)$ to approach $V_{\text{L}(111)}(P)$, in the case of orientationally isotropic samples having cubic structures but exhibiting elastic anisotropy, was recognized and evaluated in the present work for the first time.

VI. Conclusion

In this work, we extracted $V_{\text{L}(111)}$ and $V_{\text{L}(100)}$ in a single crystal of NaCl at $P=24$ GPa from the TDBS signals collected during propagation of narrow CAPs through a polycrystalline NaCl sample compressed in a DAC. Applying the Decker's EOS of NaCl, considered as the reference for the primary pressure scale, we derived C_{ij} 's of NaCl at this pressure. We have confirmed the earlier recognized tendency of experimental V_{Lav} (for polycrystalline cubic solids with $A>1$) to approach $V_{\text{L}(111)}$ but this time for a solid, NaCl, exhibiting $A<1$. We have shown that this tendency is promoted by asymmetry of V_{L} distribution in a cubic single crystal because (i) the directions close to $\langle 110 \rangle$ have the highest multiplicity and thus the strongest contribution to the BLS peak intensity and (ii) $V_{\text{L}(110)}$ is always closer to $V_{\text{L}(111)}$ than to $V_{\text{L}(100)}$ independent of the anisotropy type, $A>1$ or $A<1$. For cubic solids with $A>1$, both BLS peak maximum and middle of the FWHM provide a higher V_{Lav} when compared with V_{LH} . We have shown that influence of grain sizes, anisotropy type and degree, as well as of the method of signal analyses should be considered when V_{Lav} is derived from classical BLS- and PEUS measurements on polycrystalline elastically anisotropic cubic samples. If such V_{Lav} is used alone to derive either the aggregate shear- or bulk modulus, then a moderate deviation of the V_{Lav} from V_{LH} can cause a strong error in elastic moduli while that in G can be much greater than the error in B . A similar analysis of distribution of V_{T} in a cubic single crystal was also performed for solids having $A>1$ (solid argon) and $A<1$ (NaCl) and a much wider spreading of V_{T} velocities was revealed. Shapes of V_{T} histograms are different from those of V_{L} histograms but the characteristic features seem to be difficult to extract in real BLS measurements due to a low scattering intensity of T-modes, insufficient resolution and low signal-to-noise ratios of available experimental set-ups which cannot be compensated by long counting times. The latter explains, at least partially, why $V_{\text{Tav}}(P)$ for the considered here solids, argon and NaCl, are not available (the case for NaCl) or are inconsistent (the case for solid argon). Another outcome of our analysis of the V_{T} distribution in cubic single crystals is a moderate difference between G derived from $V_{\text{Tav}}=V_{\text{TW}}$ and G_{H} , when compared with the case where the BLS peak of L-modes is used to derive G . Accordingly, errors in B and G obtained from classical BLS spectra containing both transverse- and longitudinal peaks are nearly independent and controlled by asymmetry of each of the peaks.

In contrast to BLS and PEUS, the applied here TDBS technique is much less sensitive to the elastic anisotropy sample material and its homogeneity: A large number of the depth- and

laterally resolved measurements of local V_L values permits detecting, with a high degree of confidence, of the extremes $V_{L(111)}$ and $V_{L(100)}$ even when single crystals are not accessible and the examined polycrystalline sample is textured. If combined with independently measured bulk modulus and density, e.g. from an EOS, a complete set of C_{ij} and thus the true $V_{Lav}=V_{LH}$ and $V_{Tav}=V_{TH}$ can be determined for any solid exhibiting cubic structure.

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Data Availability

The data that support the findings of this study are available within the article. The raw TDBS signals can be provided on request by F. Xu.

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