Graph-space optimal transport concept for time-domain full-waveform inversion of ocean-bottom seismometer data: Nankai Trough velocity structure reconstructed from a 1D model

Andrzej Górszczyk^{1,2}, Romain Brossier¹, Ludovic Métivier^{1,3}

¹ISTerre, Univ. Grenoble Alpes, F-38000 Grenoble, France

²Institute of Geophysics, Polish Academy of Sciences, Warsaw, Poland

³Univ. Grenoble Alpes, CNRS, LJK, F-38000 Grenoble, France

Key Points:

- Time-domain FWI
- Alternative misfit function
- Cycle-skipping mitigation
- High-resolution crustal-scale imaging

Corresponding author: Andrzej Górszczyk, agorszczyk@igf.edu.pl

Abstract

Detailed reconstruction of deep structures with full-waveform inversion (FWI) of wide-angle ocean-bottom seismometer (OBS) data remains challenging and unconventional. The complexity of the long-offset waveforms increases the nonlinearity of the inverse problem, while the sparsity of the OBS deployments leads to a poorly constrained model reconstruction. Consequently, for such a FWI setting it is difficult to derive an initial model that satisfies the cycle-skipping criterion. Searching for a remedy to this issue, we investigate the graph-space optimal transport (GSOT) technique, which can potentially overcome the cycle-skipping problem at the initial FWI stage. The key feature of the GSOT cost function is the convexity with respect to the patterns in the two seismograms, which allows for correct matching of the arrivals shifted in time for more than half of the wavelet. This in turn shall allow FWI to handle the large kinematic errors of the starting model. We test this hypothesis by applying the time-domain acoustic FWI to the synthetic and field data from the subduction zone environment. We show that despite the complexity of the geological structure, the GSOT misfit function is able to guide the FWI toward the precise velocity model reconstruction and data fitting starting from a simple 1D model. The improved convexity of the GSOT misfit function allows FWI to converge even when mismatches between the observed and synthetic signals reach a few cycles. This ability reduces the constraint on the kinematic accuracy of the initial model and makes the FWI from the OBS data more feasible.

1 Introduction

Full-waveform inversion (FWI) has proven to be a powerful tool able to reconstruct high-resolution velocity models of the subsurface. Rapid development of this technology during past decades has led to its successful application in imaging of various geological targets, from near-surface to global-scale endpoints (see Tromp (2019) for a recent review). In particular, the oil & gas industry (stimulated by the hydrocarbon market) is currently routinely applying FWI at the exploration scale for high-resolution imaging of reservoirs (Plessix & Perkins, 2010; Stopin et al., 2014; Operto et al., 2015; Borisov et al., 2019). Such an increase in FWI applications has not yet been observed when considering regional-scale academic imaging case studies based on wide-angle ocean-bottom seismometer (OBS) acquisitions. Although these kinds of data have a great potential to efficiently constrain the subsurface velocity at depths beyond the range of typical reflection seismic data, so far, only a few attempts have been performed to combine them with FWI (Operto et al., 2006; Kamei et al., 2012; Morgan et al., 2013; Górszczyk et al., 2017; Davy et al., 2017; Górszczyk et al., 2019). Instead, the routine wide-angle data processing still relies mainly on ray-tracing and traveltimes inversion, utilizing the arrival times of pre-interpreted phases (Nakanishi et al., 1998; Korenaga et al., 2000; Yu et al., 2016; Czuba, 2016). This fact is partially due to the limited availability of dense seismic datasets (preferably 1-2 km OBS spacing) required for the stable application of FWI. Indeed, one of the major challenges for crustal-scale FWI is related to the large volumes of the models constituting the geological targets, which, in turn, are recovered from relatively sparse OBS acquisitions. Moreover, the ultralong-offset data contain a full-range of various arrivals associated with different propagation regimes and resolution powers, further increasing the nonlinearity of the inverse problem. The simultaneous inversion of seismic information collected along the long-offset diving and refraction wavepaths additionally enriched with wide-angle reflection arrivals is therefore highly nontrivial. This challenge is all the more severe when the standard form of FWI is considered, namely, FWI relying on a nonlinear least-squares minimization. The fact that the L^2 misfit function is nonconvex with respect to large kinematic errors between observed and calculated data (larger than a half-period of the dominant inverted wavelet), makes the FWI prone to cycle-skipping; that is, due to the inaccurate starting model, the inversion converges toward a geologically unreliable local minimum.

A solution to the cycle-skipping problem can rely either on building more accurate starting models or looking for more convex misfit functions. Regarding FWI from wide-angle OBS

data, the initial velocity model is usually built with first-arrival tomography (FAT, e.g., Zelt and Barton (1998)). As a consequence, it strongly relies on the ability to precisely pick and accurately invert the traveltimes of first breaks. However, the picking procedure might be subjective in the areas of the seismogram where the arrivals are mixed, dominated by noise, or for far-offset data. In such a case, significant human interaction and subsequent quality control of the tomographic model is required (Górszczyk et al., 2017). Even with precisely picked first-breaks, the long-offsets data still imply a long time of wavefield propagation and therefore a potential accumulation of kinematic error along the wavepath, namely higher risk of cycle-skipping (Pratt, 2008). Furthermore, the resolution of the final FAT model is limited to the first Frenel’s zone, which does not guarantee that the model accurately predicts the later arrivals. The problem can be partially mitigated through the joint refraction and reflection traveltime tomography (e.g., Gras et al. (2019)) or through the simultaneous inversion of first-arrival traveltimes and their slopes (horizontal derivatives, e.g., Sambolian, et al. (2019)). The latter approach has the potential to better constrain the model structure, although it requires a proper weighting between the update coming from the first-break traveltimes and from their slopes.

Another approach to mitigate the cycle-skipping problem relies on the design of alternative ways to measure the discrepancy between observed and calculated data to enhance the convexity of the misfit function with respect to the model parameters. Such methods should make it possible to start the inversion from cruder initial models while still converging toward the global minimum. Different families of misfit function with better convexity have been proposed over the past decade. Some of them still compare the data in the L^2 sense; however, they incorporate additional constraints (coming, for example, from the traveltime information (Treister & Haber, 2017)) or modify the data, for example, taking their envelope (e.g., J. Luo and Wu (2015); Borisov et al. (2017); Bozdağ et al. (2011)) or instantaneous/unwrapped phase (e.g., Choi and Alkhalifah (2011); Alkhalifah and Choi (2012); Kamei et al. (2014)). Other misfit functions are based on the cross-correlation measurement (Y. Luo & Schuster, 1991; van Leeuwen & Mulder, 2010) or a deconvolution operation (S. Luo & Sava, 2011; Warner & Guasch, 2016; Zhu & Fomel, 2016). Further promising approaches rely on extending the model space by means of wavefield reconstruction (van Leeuwen & Herrmann, 2013; Aghamiry et al., 2018), although time-domain applications of this strategy still seems a challenging problem.

Recently, misfit functions relying on the optimal transport (OT) distance have been proposed for FWI leading to a new family of promising misfit functions (Engquist & Froese, 2014; Qiu et al., 2017; Y. Yang et al., 2018; Y. Yang & Engquist, 2018; Métivier et al., 2016a, 2019a). In spirit, unlike the L^2 misfit function - which compares the field and the synthetic seismic data sample by sample - the OT distance searches for the best fitting (mapping) between the field and the synthetic data. Each such mapping is attributed with a cost, which increases/decreases if the mapping operation requires larger/smaller modification of the synthetic data to fit their observed counterpart. The distance between field and synthetic data is the cost produced by the best mapping operator. The appealing property from OT distance is its convexity with respect to translation and dilation, which makes it a very good candidate to produce a convex misfit function for FWI. To date, various OT-based misfit function implementations have been applied, mainly to different benchmark datasets from the oil & gas exploration field (e.g. Métivier et al. (2016b); Poncet et al. (2018); Chen and Peter (2018); He et al. (2019); Sun and Alkhalifah (2019); Pladys et al. (2020); Provenzano et al. (2020)).

In this study, we investigate the potential of the OT distance to mitigate the problem of the high nonlinearity and nonconvexity of FWI when applied to ultralong-offset OBS data. As described above, the sparsity of the OBS stations, large size of the models or wide range of different arrivals in the wavefield, make this acquisition setting fundamentally different than the one used in exploration-scale seismic imaging. Therefore the robustness of OT-based crustal-scale FWI has yet to be proven. We follow the graph-space optimal transport (GSOT) implementation of Métivier et al. (2019a) that compares the discrete graphs of the signals instead of the signals themselves. Due to the graph-space transformation, the

oscillatory seismic data are converted into positive values and can be compared without losing the convexity of the OT misfit function - even when the data are shifted by more than half a cycle. The ability of the GSOT to compare data samples within a given time window shall in principle relax the constraints related to the kinematic accuracy of the initial velocity model. As such, the GSOT misfit function provides a possibility to reduce the burden related to the accurate tomographic inversion of the first-arrival traveltimes as well as their precise picking for the sake of building the initial FWI model. We confront this hypothesis against synthetic and real 2D OBS datasets from a subduction zone environment. In both cases, the GSOT misfit function combined with a progressive data selection (from early to late arrivals) makes it possible to run FWI starting from a crude 1D model. Despite the significant kinematic error (a few cycles mismatch between the field and synthetic data) at the initial FWI stage, the GSOT misfit function makes the convergence of the inversion possible and leads to successful velocity model reconstruction.

In the following section we outline the formulation of our forward and inverse problem and introduce the GSOT misfit function definition. Then, we illustrate with a synthetic FWI case study based on the GO_3D_OBS model (Górszczyk & Operto, 2021) how GSOT makes it possible to apply the FWI starting from a 1D initial velocity model that linearly increases in depth. We describe our inversion workflow and present the convexity analysis, followed by the evolution of the velocity model and the data fitting during the inversion. Further, we apply a similar FWI workflow to the SFJ-OBS field data from the Tokai area of the Nankai Trough, Japan. We show how we are able to make FWI converge starting from a 1D initial model and recover the velocity structure consistent with that obtained during a frequency-domain FWI study performed by Górszczyk et al. (2017) on the same dataset. Finally, we discuss some aspects of the presented work and summarize the article with a conclusion.

2 Methods

2.1 Forward modeling

In this study, we use a 2D finite-difference (2^{nd} order in time and 4^{th} order in space) visco-acoustic isotropic time-domain modeling. It is derived from the 3D visco-acoustic VTI modeling and inversion formulation proposed by P. Yang et al. (2018). The intrinsic attenuation mechanism that we use is based on the generalized Maxwell body including three standard linear solid attenuation mechanisms (P. Yang et al., 2016a). As it is common for wide-angle studies, we process the shots in a reciprocal manner, taking advantage of the spatial reciprocity of the Green's functions. In such a configuration, we treat the vertical geophone at the OBS location as a vertical force source (vertical derivative of the pressure), and we extract the pressure wavefield at the air-gun shot position. Each OBS is processed independently, taking advantage of MPI parallelism over the sources, which translates to good scalability of the modeling step, especially for large-scale applications. We impose a free-surface boundary condition at the sea/air interface and absorbing sponge layers on the lateral sides and at the bottom of the model (Cerjan et al., 1985). Sources and receivers are accurately positioned in the finite-difference grid using the windowed sinc interpolation (Hicks, 2002).

2.2 Inversion

In the standard FWI formulation, the mismatch between observed and synthetic seismograms is measured as an L^2 distance. This L^2 distance between two datasets ($\mathbf{d}_1$) and ($\mathbf{d}_2$) with N_s sources and N_r receivers is expressed as:

$$J(\mathbf{d}_1, \mathbf{d}_2) = \frac{1}{2} \sum_{s=1}^{N_s} \sum_{r=1}^{N_r} \int_0^T (\mathbf{d}_1(\mathbf{x}_r, t; \mathbf{x}_s) - \mathbf{d}_2(\mathbf{x}_r, t; \mathbf{x}_s))^2 dt, \quad (1)$$

and the associated L^2 FWI misfit function is:

$$\mathcal{C}(\mathbf{m}) = J(\mathbf{d}_{cal}[\mathbf{m}], \mathbf{d}_{obs}). \quad (2)$$

Here, the model properties are denoted by the vector $\mathbf{m}$. The total recording time for the seismogram is denoted by T . The observed and synthetic trace computed in the model $\mathbf{m}$, associated with source $\mathbf{x}_s$ and receiver $\mathbf{x}_r$, are denoted by $\mathbf{d}_{obs}(\mathbf{x}_r, t; \mathbf{x}_s)$ and $\mathbf{d}_{cal}[\mathbf{m}](\mathbf{x}_r, t; \mathbf{x}_s)$, respectively.

The associated inversion is formulated as the minimization of the misfit function $\mathcal{C}$. Due to the size of the corresponding discrete problem, the inversion is performed through the local optimization techniques. Starting from an initial model $\mathbf{m}_0$, those are based on the following iteration:

$$\mathbf{m}_{k+1} = \mathbf{m}_k + \Delta\mathbf{m}_k, \quad (3)$$

where k is the iteration number and the model perturbation $\Delta\mathbf{m}_k$ is given by:

$$\Delta\mathbf{m}_k = -\alpha_k Q_k \nabla_{\mathbf{m}} \mathcal{C}_k, \quad (4)$$

In equation (4), $-\nabla_{\mathbf{m}} \mathcal{C}$ is the steepest-descent direction and α_k is the step length magnitude at iteration k estimated through a line search process (Nocedal & Wright, 2006). The gradient $\nabla_{\mathbf{m}} \mathcal{C}$ is determined with the adjoint-state method (Plessix, 2006). The operator Q_k is an approximation of the inverse Hessian operator at iteration k . It is computed following the l -BFGS approximation (Nocedal, 1980; Byrd et al., 1995) and combined with a diagonal preconditioning operator based on a pseudo-Hessian strategy (Shin et al., 2001; Choi & Shin, 2008). This diagonal preconditioning compensates for the amplitude decay at depth in the gradient due to the geometrical spreading associated with the surface acquisition configuration we are using. Our implementation uses the SEISCOPE optimization toolbox (Métivier & Brossier, 2016). A Gaussian smoothing operator is also applied to the gradient, with a correlation length defined as a fraction of the local wavelength. The latter is estimated through a reference frequency and the current local velocity.

2.3 GSOT misfit function

The FWI methodology introduced in the previous section suffers from a severe limitation, namely, the nonconvexity of the L^2 misfit function with respect to the velocity model. If the starting model m_0 generates synthetic data shifted in time by more than half the dominant period from the observed signal, then the L^2 misfit function will guide the inversion toward a wrong solution. This key issue is known as the cycle-skipping criterion (Virieux & Operto, 2009), and to overcome it in this study we consider a GSOT-based misfit function. The concept of OT dates back to the French engineer Monge (1781), who first formulated the OT problem in an attempt to minimize the effort of workers transporting sand on a bridge building site. This originally ill-posed OT problem was later re-explored by Kantorovich (1942) who provided a well-posed relaxation of the original Monge's problem. Based on the Kantorovich OT problem, it is possible to properly define an OT distance in the space of probability distributions. An important property of the proposed OT distance is the convexity with respect to translation and dilation. This means that for seismic signals, the OT could be convex with respect to time shifts, which is a very good proxy for convexity with respect to velocity perturbations.

However, the oscillatory nature of the seismic signals makes them impossible to be represented as a probability distribution. Several strategies have been proposed so far to overcome this issue. Some approaches rely on a prior nonlinear transformation of the signal to make it positive (square, exponential, softmax) followed by a normalization (Engquist & Froese, 2014; Qiu et al., 2017; Y. Yang et al., 2018; Y. Yang & Engquist, 2018). Another method consists of considering a specific instance of OT distance (1-Wasserstein distance), which can be extended to oscillatory signals (Métivier et al., 2016b, 2016a).

However, the nonlinear transformation of the data does not appear to us as a satisfactory option. This is because the chase for a robust misfit function shall not only focus on the improved convexity, but also on the ability to exploit all of the signal attributes for the sake of

better model reconstruction. Nonlinear signal transformation can cause loss of information, or might induce uncontrolled emphasis on particular phases. This is especially true in the case of long-offset OBS data that contain a wide variety of phases with different amplitudes and time signatures. The alternative approach based on the 1-Wasserstein distance has shown interesting properties, especially because it is possible to apply it to multi-D shot gathers and account for the lateral coherency of the data in this shot-gather representation (see, for instance, successful applications to the exploration-scale field data by Poncet et al. (2018); Messud and Sedova (2019); Sedova et al. (2019); Carotti et al. (2020); Shutova et al. (2020)). However, one identified drawback of this approach is the loss of convexity with respect to large time shifts (Métivier et al., 2018): the valley of attraction of the misfit function is only slightly larger than that of the L^2 norm. In other words, the convergence of FWI towards global minimum still strongly relies on the kinematic accuracy of the initial model. The interest of this approach thus relies more on its ability to better extract low-frequency information from noisy data by exploiting the lateral continuity of events in shot-gather representations rather than being resilient to large kinematic errors.

In this study, we employ an alternative OT approach based on the comparison of the discrete graph of seismic traces, following the original idea of (Thorpe et al., 2016). Mathematically, this GSOT variant of OT represents each seismic trace as a sum of Dirac delta functions in a 2D space with the time and amplitude dimensions. Comparison of the discrete graphs of the observed and synthetic seismic data (instead of the data themselves) ensures the positivity of the considered quantities and maintains the convexity of the distance with respect to time and amplitude shifts (Métivier et al., 2019a). Compared with 1-Wasserstein distance, this is a trace-by-trace approach and therefore does not exploit the lateral coherency of seismic event.

The formulation for GSOT we use has been introduced in Métivier et al. (2019a). First, we define a seismic trace $d(t)$ discretized as $(d_1, \dots, d_n)$. We denote its discrete graph by $(t, d) = ((t_1, d_1), \dots, (t_N, d_N)) \in \mathcal{R}^{2N}$. Let d_{cal} and d_{obs} be a calculated and observed trace respectively. With (t, d_{cal}) and (t, d_{obs}) we denote their discrete graphs consisting of N delta Dirac functions in a 2D space. The GSOT distance between d_{cal} and d_{obs} is given by solving the linear sum assignment problem:

$$h_2(d_{cal}, d_{obs}) = \min_{\sigma \in S(N)} \sum_{i=1}^N c_{i, \sigma(i)}(d_{cal}, d_{obs}), \quad (5)$$

where $S(N)$ denotes the space of permutation of $\{1, \dots, N\}$, and c_{ij} is the distance between the points i and j of the discrete graph of d_{cal} and d_{obs} :

$$c_{ij}(d_{cal}, d_{obs}) = |t_i - t_j|^2 + \left| \frac{\tau}{A} (d_{cal,i} - d_{obs,j}) \right|^2. \quad (6)$$

In Equation 6, A is the maximum peak amplitude difference between observed and calculated data, while τ is the maximum estimated time shift between d_{obs} and d_{cal} . This ensures the convexity of the GSOT distance for time up to approximately τ . The assignment problem is efficiently solved using the auction algorithm (Bertsekas & Castanon, 1989; Métivier et al., 2019b). The final cost function we use for the purpose of FWI application with N_s shots containing N_r receivers is defined as:

$$\min_m f[m] = \sum_{s=1}^{N_s} \sum_{r=1}^{N_r} w^{s,r} h_2(d_{cal}^{s,r}[m], d_{obs}^{s,r}), \quad (7)$$

where $d_{obs}^{s,r}$ and $d_{cal}^{s,r}[m]$ are the observed and synthetic (calculated in model m) traces respectively, which are associated with source s and receiver r . The $w^{s,r}$ is a trace-by-trace weighting factor, typically used to restore the AVO trend in the data. This trend is removed from the trace-by-trace GSOT approach, and the amplitude of each trace is treated separately through the normalization factor $\frac{\tau}{A}$.

Regarding the gradient computation, we refer to (Métivier et al., 2019a). Let us however state the main result. Due to the adjoint-state strategy, the only modification in the gradient computation compared with the L^2 misfit function is related to the computation of the

adjoint source. The latter can be expressed, in the GSOT approach, as a generalized residual between synthetic and field data. For a given trace, this generalized residual is equal to the difference between synthetic and field data at time samples connected by the optimal permutation σ solution of the problem (5). Mathematically, this generalized residual is defined by:

$$r_i = d_{cal,i} - d_{obs,\sigma(i)} \quad (8)$$

189 with σ being the solution of (5). We also see immediately that when σ is equal to the identity,
190 we recover the conventional L^2 misfit function with the conventional residual (difference between synthetic and observed data).

Figure 1. (a)-(b) True V_p and ρ models; (c) Initial V_p model; (d) Velocity perturbations - difference between (a) and (c); (d) OBS gather recorded at 70 km of model distance (red triangle in (a)-(d)). Every 20 traces generated in the true model are interleaved with the following 20 traces generated in the initial model. Green/red lines mark the first breaks in true/initial data.

3 Synthetic test

In this section, we illustrate how the GSOT misfit function can lead FWI from long-offset OBS data into the correct velocity reconstruction of deep crustal targets starting from a crude 1D model. We use the 2D P-wave velocity and density (V_p and ρ) models extracted from the GO_3D_OBS (Górszczyk & Operto, 2021) crustal-scale model of a subduction zone (see Figure 1a-b). This model has been designed to benchmark different tomographic and inversion approaches with a special emphasis on FWI of long-offset stationary-receiver data. Our test assumes modeling of the acoustic data within the target model and subsequent inversion of these data starting from the kinematically wrong initial model.

3.1 Experiment setup

The acquisition settings that we design comprises 72 receivers distributed along the seabed with 2 km spacing intervals, as presented in Figure 1a, and 1500 shots distributed every 100 m (10 m depth) between 5 km and 155 km of model distance. To generate the synthetic dataset, we use a 2D time-domain acoustic isotropic modeling with a 1.5 Hz Ricker source wavelet. We consider a 20 s propagation time.

During the inversion we focus mainly on the ability of GSOT to overcome the problem of the kinematic inaccuracy of the initial velocity model. For this purpose, we consistently keep the true ρ model that was also used for synthetic data generation. Alternatively, we could use constant density model for both forward modeling and FWI steps. This could theoretically make the problem simpler for GSOT-based FWI, since in our setting the velocity update has to take into account spatially varying density parameter. Moreover, the presence of density contrasts can create the arrivals (especially short-spread reflections and less produced wide-angle reflections) originating at the interfaces, that are not existing in the velocity model at the initial stage. As a starting V_p model, we use the 1D model that linearly increases in depth, presented in Figure 1c. The difference between the true and initial models is presented in Figure 1d. Note the significant velocity perturbations reaching ~ 3000 m/s. In Figure 1e, we present in an interleaved manner the corresponding data generated in the true and initial models. The complexity of the structure from the true model is clearly reflected by the various interfering arrivals. Large velocity differences from Figure 1d are reflected by a significant kinematic mismatch between the first-arrival traveltimes marked by the green (true) and red (initial) lines in Figure 1e. This clear cycle-skipping revealed in the OBS gather example makes it impossible to run FWI with the standard L^2 misfit function which is stuck from the first iteration.

We perform time-domain acoustic FWI with the *l*-BFGS optimization scheme and the

	STAGE1	STAGE2	STAGE3	STAGE4
τ value	4.0 s	4.0 s	4.0 s	4.0 s
Time window	0.2 s + 0.5 s taper	0.2 s + 0.5 s taper	0.2 s + 10 s taper	Full data
Amplitude	NO AVO	AVO	AVO	AVO
Smoothing	2.0×2.0	1.6×0.8	0.8×0.4	0.8×0.4
Iterations	50	20	50	150

Table 1. Summary of the inversion steps in the synthetic test

preconditioning strategy described previously. We invert for the synthetic data without applying any band-pass filter, and we follow the 4-stage multiscale strategy presented in Table 1. The workflow is based on progressively extended time windows and reduced gradient smoothing realised by the means of the Gaussian filter with correlation lengths matching to the local wavelength. The time-window of length of 0.2 s starts at the first-arrival time and is extended from one FWI stage to another with progressively longer taper. This makes it possible to limit the volume of the data used at the beginning of the inversion. In Table 1,

the time window that we use at the initial FWI stages is narrow and focused mainly around the first arrivals. Consequently, the volume of the data that must be compared by the GSOT misfit function is reduced. Muting of the secondary arrivals and wide-angle reflections from the observed data reduces the risk of matching them with the first arrivals from the synthetic data. Such a mismatch may likely occur taking into account the large time shifts between the observed and initial data in Figure 1e. Moreover, progressive introduction of the later arrivals translates to the narrowing of the scattering angles associated with smaller scale of perturbations. Combined with the tuned correlation lengths of the smoothing operator, this approach makes it possible to keep control of the spatial scale of the model update at each FWI stage. In addition, to re-estimate the maximum peak amplitude difference between the observed and calculated data (A in Equation 6), we restart the inversion after every 10 FWI iterations.

At the initial FWI stage, we use constant $w^{s,r}$ equal to 1; namely, we compare trace-normalized seismograms to increase the contribution of the far-offset data in the gradient. Those data correspond to the waves penetrating in the deeper subsurface and have typically much smaller amplitudes than the near-offset data. Trace normalization at the initial FWI stage mitigates this issue at the price of the loss of the amplitude trend with the offset. For the consecutive FWI stages the $w^{s,r}$ is calculated as a trace-by-trace RMS value of the observed seismogram to restore the amplitude vs offset (AVO) trend in our misfit function.

3.2 Convexity analysis

To analyze the convexity of the GSOT at stage 1 of our inversion, we generate a population of 10 V_p models V_α according to the formula:

$$V_\alpha = (1 - |\alpha|)V_{true} + |\alpha|V_{init} \quad (9)$$

where $\alpha = [-1.0, -0.9, \dots, 0.9, 1.0]$. For each of the models we calculate the initial misfit function values using $\tau = 0.005$ s and $\tau = 4$ s. The first value of τ mimics the L^2 norm, since the data sampling in our test equals 0.005 s. For this scenario the convexity of the GSOT-misfit function is reduced to the L^2 norm convexity. The second value of τ is empirically selected to account for significant time shifts between the early arrivals in the true and initial data. Consequently, the convexity of the GSOT misfit function is increased. The normalized values of the misfit functions for both scenarios are plotted in Figure 2. One can observe that for $\tau = 0.005$ s, the global minimum valley is in between $\alpha \sim -0.3$, and $\alpha \sim 0.3$. Starting from an initial model that is farther from the true model would result in converging toward a local minimum. Conversely, for $\tau = 4$ s, we obtain a convex misfit function with a single global minimum for the whole range of α values, including the case $|\alpha| = 1.0$ which corresponds to taking the 1D model as an initial model. Note, that the absolute value of α in Equation 9 is used only to create the apparent symmetry of the misfit function with respect to $\alpha = 0.0$ in Figure 2. Namely, the initial models for a given $\pm\alpha$ values are exactly the same and so are the values of the misfit functions.

Notably, with the broadening of the global minimum valley, it also becomes less sharp, which is an indication of potential resolution loss. As a consequence, keeping large values of τ can lead to less resolved velocity model reconstructions. For the synthetic test presented here, we however keep a constant $\tau = 4$ s at each stage of the inversion. For the field data application, various factors such as presence of noise, acoustic approximation of the wave propagation and simplified subsurface parametrization, or imperfect source wavelet, can further broaden the null space of the misfit function. Therefore, in such a case, we shall keep the τ value according to the kinematic errors of the model and as small as possible to narrow the global minimum valley.

3.3 Results

The final recovered V_p model is presented in Figure 3a. Figure 3b-e show the velocity perturbations recovered at each of inversion stage. Each of the panels is overlaid with

Figure 2. GSOT cost-function convexity for $\tau = 0.005$ s and $\tau = 4$ s at the first stage of our test.

three transparent masks that change the saturation of the underlying color according to the relative error ϵ of the resolved velocity model calculated as follow:

$$\epsilon = \left| \frac{m_{true} - m_{fwi}}{m_{true}} \right| * 100\%. \quad (10)$$

In Equation 10 m_{true} and m_{fwi} are the true model and the model recovered at given FWI stage respectively. We introduce three ϵ intervals: (1) $\epsilon \leq 2.5\%$ (light saturation); (2) $2.5\% < \epsilon \leq 5.0\%$ (intermediate saturation); (3) $5.0\% < \epsilon$ (strong saturation, see arrows in Figure 3b). Note how from one stage to another the resolution of the recovered structure is increased, and how the area of light-saturated colors ($\epsilon \leq 2.5\%$) is progressively expanding. Despite, the fact that we invert for low frequency band (below 4.5 Hz) (although assuming no noise and known source signature), the complex velocity perturbations in Figure 3e were recovered in the details (compare with true perturbations in Figure 1d). In particular, on the landward part the steeply dipping faults marking the old backstop at approximately 30-40 km distance as well as the thin subduction channel on top of the oceanic crust between 40 and 55 km distance are clearly imaged. In the central part, the accretionary wedge containing a sequence of deformed thrusts is clearly reconstructed and also includes the low-velocity zone at 12 km depth between 60 and 80 km distance. In the deep water part, the rapid increase in velocity is properly recovered, and the sharp contrast of velocity between sediments deposited in the trench and the top of the oceanic crust is imaged. Furthermore, the signatures of the faults cutting through the subducting crust and the upper mantle are also imaged. In the deeper parts of the mantle, we start observing some velocity mismatches that possibly result from the limited and mainly subhorizontal illumination of those segments. This is confirmed by Figure 3f where we show the perturbation logs (marked in Figure 3e with black-dashed lines) representing true (red line) and reconstructed (green line) V_p perturbations (difference between true/initial and reconstructed/initial V_p models). One can observe that the logs remain in very good agreement even for the most complex structures down to approximately 20 km of the model depth. In Figure 4a-b, we show the initial and final data-fitting comparison for the OBS marked with a red triangle in Figure 3a. The red-blue color scale corresponds to the calculated data, while the black-colored phases denote the observed data. The presence of large time shifts between the observed and initially predicted data in Figure 4a are a clear indication of the cycle-skipping. Despite it, the fact that there is no red color in Figure 4b indicates that the GSOT-based FWI approach we have designed leads to precise data and model reconstruction.

4 Field data application

In this section we present the GSOT-based FWI application to the TKY-21 field OBS data from the subduction zone located in the eastern Nankai Trough (Tokai segment, Figure 5a). This region was historically a subject of numerous studies investigating its geodynamical background in the context of devastating earthquakes frequently occurring in the

Figure 3. (a) Final V_p model after FWI stage 4; Red triangle marks the position of the OBS from Figure 4; (b)-(e) Recovered perturbations - difference between the initial and the final model after each FWI stage; Each panel is overlaid with three transparent masks that modify the color saturation and correspond to three intervals of model reconstruction error ϵ : (1) $\epsilon \leq 2.5\%$; (2) $2.5\% < \epsilon \leq 5.0\%$; (3) $5.0\% < \epsilon$. See the arrows in (b), which mark the respective saturation levels. (f) True (red) and reconstructed (green) V_p perturbation logs (see vertical black-dashed lines in (e) for locations);

311 Nankai Trough. Among different research efforts, the detailed velocity model reconstruction
 312 via frequency-domain FWI of the TKY-21 OBS line was first performed by Operto et
 313 al. (2006) and later revisited by Górszczyk et al. (2017) with Laplace-Fourier FWI. These

Figure 4. Comparison of the data fitting at the initial (a) and the final (b) FWI stage. Observed

Figure 5. (a) The tectonic settings of the Nankai Trough area. The solid red line represents the seismic profile of the TKY-21 experiment. (b) Zoomed view of the TKY-21 survey area, with bathymetry variations. The black and dashed red lines represent the shot and the receiver lines respectively.

frequency-domain results gave us a good reference point for the time-domain GSOT-based FWI application we present here.

4.1 Data preprocessing

The OBS TKY-21 dataset was acquired by JAMSTEC in 2001 during the KY0106 cruise of R/V Kaiyo within the framework of the French-Japanese project SFJ-OBS. The acquisition consisted of 100 OBS stations (facilitated with 4.5-Hz three-component geophones and hydrophones) deployed within 1 km intervals and 1404 air-gun shots (total array volume of 196 l) spaced 100 m apart. This acquisition geometry leads to a relatively dense spatial sampling of the target by the propagating wavefield which is at least sufficiently redundant for FWI to be applied.

Before running the inversion we perform an elementary data preprocessing procedure. We

remove the DC component before applying 3D to 2D amplitude-spreading correction (scaling factor equal to the square root of time). We then apply a spectral whitening to partially mitigate the bubble effect, and we bandpass filter the data between 1.5 and 3.5 Hz. Finally, we normalize the OBS gathers with their amplitude RMS value to compensate for differences in the instrument response and seabed coupling.

4.2 Workflow

Our field data FWI application relies on the workflow designed during the synthetic study previously presented. The analogous 4-stage FWI scheme is summarized in Table 2. The parameters are tuned to meet the real data conditions, namely, possible elastic effects, rapid amplitude decay with offset, inaccuracy of source wavelet, and presence of noise. In particular, we reduce the value of τ as the model accuracy increases from one stage to another. We set the time windows to proceed from first arrivals to the later ones. We use a maximum time window of ~ 2 s after the first arrival to limit the amount of energetic elastic arrivals (mainly from near and intermediate offsets) in our acoustic inversion. In stage 2, we introduce an intermediate misfit function weighting based on the square root of the AVO. This is due to the large amplitude variations between near- and far-offset traces (several orders of magnitude) observed in this dataset. We run the inversion until no significant model updates are observed. We pre-estimate one source wavelet for all OBS gathers from the short-offset water wave (Pratt, 1999), and we keep it the same for all FWI stages. Figure

	STAGE1	STAGE2	STAGE3	STAGE4
τ value	4.0 s	1.0 s	1.0 s	0.2 s
Time window	0.1 s + 0.5 s taper	0.1 s + 1.0 s taper	0.1 s + 2.0 s taper	0.1 s + 2.0 s taper
Amplitude	NO AVO	SQRT(AVO)	AVO	AVO
Smoothing	2.0 $\times$ 2.0	1.6 $\times$ 0.8	1.6 $\times$ 0.8	0.8 $\times$ 0.4
Iterations	80	40	40	140

Table 2. Summary of the inversion steps in the field data application

6a presents the initial velocity model (1D velocity profile) derived as a horizontal average of the initial FWI model used by Górszczyk et al. (2017) which was obtained with FAT. To illustrate the kinematic mismatch between the field and the synthetic data generated in this initial model, we show in Figure 6b the gather from the OBS marked by the red triangle in Figure 6a. Every 20 traces of the field data are interleaved with subsequent 20 traces of the synthetic data (blue shading). It is clear that with the increasing offset, the time shifts between trace intervals become larger and locally reach few cycles. Moreover, one can observe the local change in the time shifts sign depending on the offset. This indicates that the initial model lacks large-scale low and high velocity perturbations.

To obtain a better insight into the kinematic inaccuracy of the initial model, we estimate the order of the cycle-skipping for the whole dataset. Figure 6c presents the map of the skipped cycles between the observed and synthetic first-arrivals for each trace used during inversion. The number of skipped cycles was calculated as a difference between the first-break traveltimes picked from the observed data and the synthetic traveltimes calculated in the initial FWI model from Figure 6a. This difference was further divided by the dominant period of the data (assuming a 3.5 Hz dominant frequency). One can observe, that there are just a few regions where the observed first-arrival phases match the synthetic ones (white color), while the majority of the synthetic traces are shifted with respect to their field equivalent by at least two cycles. Not surprisingly, with such an initial model, FWI with the L^2 misfit function is unable to converge from the very first iteration of stage 1. In contrast, the FWI with the GSOT-based misfit function provides a consistent model and data update along the different stages of the inversion.

4.3 Results

Figure 7a-d and Figure 8 illustrate, respectively, the model and the data evolution after each FWI stage. One can observe that after stage 1 we recover long-wavelength positive (red) and negative (blue) perturbations (see the inset in Figure 7a) which leads to a smooth model exhibiting the general trend of the subduction zone. However, the synthetic data in Figure 8a (blue-shaded traces) are still locally significantly cycle-skipped. This mismatch effects most likely from the strong smoothing of the gradient at this stage, which hampers the intermediate- and small-scale perturbations needed to explain the data more precisely. Therefore, in stage 2, we use a smaller τ value to improve the convergence of inversion, and simultaneously, we increase the resolution of the introduced perturbation by means of reduced smoothing and a slightly extended time window. Importantly, we switch to a data weighting according to the square root of the AVO. In this way, we put more weight into the energetic short- and intermediate-offset data that carry rich information about the underlying geological features. It is clear that after stage 2, the reconstructed model (Figure 7b) has much higher resolution. One can observe the signature of the complex structures building the accretionary prism. The shape of the oceanic crust and the Moho is also reconstructed. This increase in the model resolution is reflected by the improved data fitting presented in Figure 8b. There is no clear evidence of cycle-skipping within the first arrivals which indicates a significant improvement of the model with respect to the previous stage. In the inset, one can observe that the synthetic data exhibit a complex package of wide-angle reflections - although their kinematics and dynamics are not precisely reconstructed yet. The model after stage 3 (Figure 7c) shows mostly improvement of the resolution of the shallow and intermediate structures. This result is due to the weighting of the misfit function applied according to the true AVO. At this stage, we further improve the continuity of the phases between the synthetic and field data panels, as seen in Figure 8c, as well as for later arrivals. The final model is presented in Figure 7d. A smaller τ value and a smaller

Figure 6. (a) 1D initial FWI model. Triangles mark the OBS positions. Red triangle mark the position of the OBS in (b). Green triangles mark the position of the OBS in Figure 9. (b) Gather extracted from the OBS 23. Every 20 traces of the observed data (white and black phases) are interleaved with the following 20 traces of the synthetic data (light blue and black phases) generated in the initial FWI model from (a). Inset present the zoom on the heavily cycle-skipped data. (c) Map showing the number of skipped cycles for each trace in the dataset - arranged in the source-receiver coordinates. Blue/red color indicates that the first breaks of the synthetic data arrive later/earlier than their observed counterparts. Black color marks the traces excluded from the inversion.

Figure 7. (a)-(d) Model evolution after each FWI stage. (e)-(f) Results from Górszczyk et al. (2017). Initial model derived with FAT and the model derived with frequency-domain FWI (frequency range up to 4 Hz). Insets show the difference between the presented and the initial model from Figure 6a. The color-scale is ± 2000 m/s.

smoothing make it possible to sharpen the structure within the accretionary prism. Shallow sedimentary basins, as well as sequences of thrusts of various scales are clearly visible now. The characteristic undulations of the subducting oceanic crust in the Tokai region, coupled with a wavy nature of the underlying Moho are also made evident. The final velocity perturbations presented in the inset exhibit a wide range of introduced structures varying both in terms of spatial scale and magnitude. In Figure 8d one can observe further improvement of the continuity of phases and amplitude trends between synthetic and field data traces.

We can also compare the model evolution (Figure 7a-d) with the results obtained by (Górszczyk et al., 2017). Figure 7e-f shows the initial model (derived with FAT) and the model from Laplace-Fourier FWI after inverting frequency groups between 1.5 Hz and 4.0 Hz. Direct and detailed judgement of the final models (Figure 7d and f) is not straightfor-

Figure 8. (a)-(d) Comparison of data fitting (OBS 23, Figure 6b) after FWI stages 1-4 respectively. Every 20 traces of the observed data are interleaved with the following 20 traces of the synthetic data (blue-shaded traces). Insets show the zoom on the complex waveform package.

ward due to the different parametrizations used in both workflows. However, we can observe a good agreement between the two velocity structures despite the fact that the time-domain FWI results were obtained starting from a simple 1D model. One can observe that the tomographic model in Figure 7e has higher resolution than the model after FWI stage 1 (Figure

7a, still producing the cycle-skipped data) and lower resolution than the model after FWI stage 2 (Figure 7b). We may therefore argue, that using possibly inaccurate tomographic model (e.g. equivalent of the model in Figure 7a) as a starting point for GSOT-based FWI, shall allow us to start the inversion from stage 2 and still converge towards global minimum. Together with a notable data fitting obtained with the GSOT-based FWI, this justifies the accuracy of the model reconstruction. We will come back to the time- versus frequency-domain FWI in the Discussion section.

To obtain a better insight into the final data fitting in Figure 9, we present another 4 observed/synthetic OBS gathers recorded at different locations along the profile (green triangles in Figure 7). The presented waveforms cover a broad range of arrivals that might be recorded in the subduction zone environment. One can observe the good continuity of the phases not only in terms of the first arrivals but also in terms of later wide-angle reflections and free-surface multiples appearing at various offsets. The amplitude trends of the synthetic data also follow those from field data - although the acoustic approximation of our FWI causes limited amplitude reconstruction in particular for later arrivals. It is noteworthy again here that for our inversion, we use only the data from the 2 s time window starting at the first arrival. Such a time window makes it possible to incorporate the majority of the P-wave arrivals constraining the velocity model, and at the same time, it limits the amount of waveforms related to elastic effects that we cannot handle properly due to the simplified approximation of physics we are using here.

5 Discussion

5.1 Application of FWI to OBS data

FWI proved to be a powerful technique able to recover velocity models of the subsurface with the theoretical resolution limit reaching half of the wavelet. This resolution can be indeed obtained assuming that the target is illuminated by the wavefield propagating at different angles and spanning wide range of wave-vectors at this target. Such a illumination can be obtained with the dense long-offset OBS deployments, which record the data that contain various waveforms - including those travelling in the deep subsurface and undershooting the target structure. Additionally, the OBS experiments provide 4C data, opening the perspective for decoupling the crosstalk between physical parameters during multiparameter FWI (Operto et al., 2013). In practice, however, the wavefield associated with a surface seismic acquisition, provides only limited sampling of the model-space by the wave-vectors. The issue becomes even more severe in case of the academic 2D OBS deployments, where the OBS spacing is often larger than 10 km and the low-frequency content of the data is missing. Application of FWI to such a dataset leaves major doubts about the geological correctness of the reconstructed model - even if one is able to fit the data. Unfortunately, the number of the OBS stations available for a given seismic experiment is always limited. It is therefore necessary to optimize the acquisition setting, if the aim is to process the resulting data using FWI. Below we mention some of the acquisition-related factors and dependencies, which from the practical point of view, can have a crucial impact on the successful application of FWI to the OBS data.

5.1.1 Complexity and depth of the target

With decreasing number of the OBS stations the spatial aliasing in the shallow part of the model increases (Brenders & Pratt, 2007a). However, the sampling of the intermediate and deeper parts of the model (e.g. crust or upper mantle) can be sufficient to retrieve a meaningful structural information with the resolution higher than in case of FAT. Of course this might be possible assuming that there is no large kinematic errors in the shallow part of the model (e.g. resulting from the shallow high-velocity layers, which are difficult to reconstruct without dense receiver coverage). On the other hand, the sampling of the deeper parts of the model will most likely rely on the sub-horizontal wavefield propagation, which

Figure 9. (a)-(d) Comparison of data fitting after stage 4 of FWI - the OBS positions are marked by the green triangles in Figure 6a. Every 20 traces of the observed data are interleaved with the following 20 traces of the synthetic data (blue-shaded traces).

will translate to the reconstruction based only on the limited range of wave-vectors. This issue could be partially stabilised if the various types of arrivals (i.e. reflections, wide-angle reflections, diving waves, refraction) originate at the same target and feed the FWI with

more seismic information. In other words, if the recorded wavefield contains clear arrivals that represent different propagation regimes and sample the same subsurface area, then the precise reconstruction of such a waveforms can potentially mitigate the sparsity of the OBS acquisition and stabilise the inversion. The drawback in turn, will be the increased nonlinearity of the inverse problem related to the more complex input to FWI.

5.1.2 Availability of the multichannel streamer (MCS) data

Incorporating MCS data into the model building process can significantly constrain the velocities down to the depths approximately equal to the streamer-length. This makes it possible to partially compensate for the undersampling of the shallow subsurface related to the sparse OBS deployment. The constrain from the MCS data can rely either on the building more accurate initial model, either on updating the final FWI model from the OBS data. Depending on the length of the streamer and frequency content of the data, one can aim on updating the velocity model with tomography (based on reflections, slopes or waveforms (Sambolian, Operto, et al., 2019; Takougang & Calvert, 2011)) or FWI (Qin & Singh, 2017). In case of deep-water environment, re-datuming of the data to the seafloor with downward continuation approach (Gras et al., 2019) can also be considered to extract the diving waves for FWI. Moreover MCS data can be used for depth-migration with the model derived from the OBS data as background velocity field (Gorszczyk et al., 2019). This can bring additional high-resolution geological information, but also validate the correctness of the velocity model, which shall flatten reflections in the common image gathers.

5.1.3 Frequency content of the data

One of the main issue for robust FWI is deficiency of the low-frequencies in the active seismic data. This results form the difficulty of generating and recording of the signal energy below ~ 2 Hz. Although some enhancement of the low-frequency content in the data can be done at the preprocessing stage (e.g. spiking deconvolution, Yilmaz (2001)), the presence of noise (typical for the OBS data) can hamper the processing and lead to the FWI application without access to the low-frequency data. In the first line, this translates to the cycle-skipping issue, which can be solved with building an accurate starting model - difficult to derive from the sparse data. Alternatively, one can use more convex misfit functions, which are able to introduce a tomographic-like model update and fill the resolution gap between the long-wavelength structure of the initial model and the short wavelength perturbations resulting from the FWI of high-frequency data. Secondly, even when the cycle-skipping problem is solved, the spatial aliasing resulting not only from the coarse OBS sampling, but also from the lack of low-frequency content, can lead to the artefacts in the model update - in particular in the shallow subsurface. MCS data can be utilised to mitigate this issue in the manner mentioned above. One can also consider more robust gradient regularisations, which are able to produce a broadband wavenumber update of the model, or which can utilise a priori information about the underlying structure (Aghamiry et al., 2019; Peters & Herrmann, 2017; Trinh et al., 2017).

5.1.4 2D or 3D OBS deployment

Most of the active seismic OBS experiments conducted up to now were performed along the 2D profiles. The SFJ-OBS 2001 dataset, which we processed here was acquired with 100 OBS stations deployed with 1 km spacing. Such a setting can be consider as a very dense deployment for the academic surveys. However, with 100 receivers one can perform a 3D OBS acquisition, covering $100 \text{ km} \times 20 \text{ km}$ area assuming $\sim 5 \text{ km}$ OBS spacing. This will still be considered a dense academic acquisition setting. Which of those two is more optimal form the point of view of FWI application? Can the 3D deployment with few shooting lines compensate for the sparser OBS spacing - taking advantage form narrow-azimuthal coverage? Was SFJ-OBS experiment oversampling the underlying structure? Or maybe the

3D setup will undersample the model space? Perhaps some of those issues might be clarified, if we will start performing more routinely the realistic numerical studies, to optimize the active seismic OBS experiments for the purpose of further FWI processing. This might lead to the development of the leading-edge acquisition approaches which will allow to fully exploit the potential of the crustal-scale FWI from the OBS data.

5.2 Initial model-building

We have presented how the GSOT misfit function can guide FWI into a correct solution starting from a crude 1D model. This raises the question of whether we still need to build accurate initial models, for example, with FAT. From a practical point of view, there are a few aspects to consider. In terms of computational time, traveltimes tomography is cheap. However, precise picking of the first breaks might be uncertain and time consuming when the interpretation of the first-arrival phases is ambiguous. This, in turn, might require iterative refinement of the picked traveltimes and repetitive FAT inversion (Górszczyk et al., 2017). On the other hand, time-windowing of the data during our FWI still requires the first-arrival traveltimes to be provided. There is, however, a fundamental difference here. The precision of the traveltimes defining the time window that we are using can be significantly lower compared to what would be usually required to design a correct (in the sense of satisfying the cycle-skipping) velocity model through FAT (even when uncertainty of picks is taken into account). From these premises, we could envision a workflow that would consist of first running a computationally cheap FAT with potentially inaccurate first-arrival picks to obtain a first smooth velocity model. This smooth velocity model, even if it were not to satisfy the cycle-skipping criteria could serve as an initial velocity model for a GSOT-based FWI. In such a way, one could start FWI with a better initial model than a simple 1D profile and still benefit from the improved convexity of the GSOT misfit function and less expanded FWI workflow comparing to what we presented. Such an approach might be especially important from the perspective of large-scale 3D FWI.

5.3 Computational cost of the GSOT approach

The computation of the GSOT misfit requires the solution of an optimal assignment problem for each trace. By virtue of the auction algorithm, the solution of such a problem can be relatively fast (less than 1 s on a single core), for instances of a problem with a number of discrete point N inferior to 1000. This is approximately the order of magnitude we attain for FWI applications at crustal scale, considering a resampling of the data in time. For our field data application, we decimate the data in time by a factor of 3. This leads to N equal to 1334 discrete points per trace and the time step equal to 0.015 s. Such a data-sampling is still much denser than that required by the Nyquist law (for the frequency range we consider here) and introduces negligible differences into the gradient compared to the original sampling. In addition, to speed up the solution of the optimal assignment problem, we have implemented a localization of the algorithm that depends on the maximum expected time shift (defined by the parameter τ). We thus observe that the computation time for a gradient using the GSOT misfit function is between 93 s and 66 s depending on whether τ is taken equal to 4 s or 0.2 s. With a reference time of 49 s in the L^2 case, this represents an additional cost between 89% and 34%. Let us also mention that a complexity analysis reveals that the computational cost of GSOT scales with $\mathcal{O}^3$, where $\mathcal{O}$ is the reference frequency of the data, while the incident and adjoint modeling steps required for the FWI gradient building scale with $\mathcal{O}^4$. This indicates a favorable trend for the higher costs associated with the GSOT strategy for larger-scale applications.

5.4 Acoustic vs visco-acoustic modeling

Unlike frequency domain modeling, for which the implementation of the attenuation is done through the introduction of a complex-valued velocity, the time-domain visco-acoustic

Figure 10. (a)-(b) True V_p and Q_p models; (c) Velocity perturbations - difference between true and initial V_p model; Reconstructed velocity perturbations after FWI with visco-acoustic modeling using (d) true Q_p model; (e) constant $Q_p=100$ in solid part and $Q_p=10000$ in the water column; (f) constant $Q_p=10000$.

modeling comes at an extra computing cost. In our implementation we use the checkpoint-assisted reverse forward simulation (CARFS) strategy proposed by P. Yang et al. (2016b). Despite the fact that this approach is more computationally efficient than conventional checkpointing our visco-acoustic modeling is still approximately 3 times more expensive than its acoustic counterpart. On the other hand, previous studies report that better FWI results can be obtained, even when using a crude attenuation model for field data FWI applications (e.g. Kurzman et al. (2013); Górszczyk et al. (2017); Operto and Miniussi (2018)). This might be especially true for the ultralong-offset data inversion where number

of propagated wavelets is large.

Since the GO_3D_OBS model (Górszczyk & Operto, 2021) also contains the definition of the Q_p parameter, we can easily run a synthetic analysis of the FWI with different attenuation scenarios. We consider the same acquisition parameters as for the synthetic study presented before. Figure 10a-b shows the true V_p and Q_p models used to generate the data. Note that the Q_p values span between 15 and 275 in the solid part and are constant ($Q_p=10000$) for the water column. Figure 10c shows the difference between the true and the initial V_p model (smooth version of the true model) used in this exercise. We run 3 different GSOT-based FWI tests (200 iterations) where we aim at the V_p reconstruction using visco-acoustic modeling with different Q_p models. We also keep the true ρ model (not presented here) both for the modeling and the inversion step. In the first scenario we use the true Q_p model (Figure 10b), and not surprisingly, the reconstructed perturbations in Figure 10d match well with those from Figure 10c. In the second test, we use a simple Q_p model where we set the $Q_p=100$ in the solid part and $Q_p=10000$ in the water column. The corresponding perturbation model is presented in Figure 10e. We start observing an indication of an acquisition footprint in the shallow sedimentary part for which low Q_p values are present in the true model. Moreover generally faster perturbations are observed in the deeper model part. Despite those differences, the reconstructed structure is still close to the one presented in Figure 10d. In the third test we use the constant $Q_p=10000$ model (approximately no attenuation). The resulting velocity structure in Figure 10f is clearly damaged due to the lack of accounting for the viscous effect during the waveform modeling. In our field data study, even though we invert the data within a relatively low frequency band we use a constant Q_p model in the solid part ($Q_p=200$). The final results from FWI with visco-acoustic modeling show less artifacts in the reconstructed velocity model and provide better data fitting (from 5% to 15% depending on the OBS) than the FWI with acoustic modeling. One can expect that this difference might be even more significant when moving to higher frequency ranges and/or strongly attenuating media. Therefore, considering a simple attenuation model during FWI - even as a passive parameter - clearly improves the final inversion results.

5.5 Time- versus frequency-domain crustal-scale FWI

Since our GSOT misfit function relies on the comparison of seismograms in the time domain, we consequently apply the time-domain implementation of FWI. Indeed, the computational efficiency of frequency-domain crustal-scale FWI for processing the 2D stationary receiver data was exploited in previous studies (e.g. Sirgue and Pratt (2004); Brenders and Pratt (2007b); Ravaut et al. (2004); Operto et al. (2006); Kamei et al. (2012); Malinowski et al. (2011); Górszczyk et al. (2017)). Furthermore, the development of more robust direct solvers coupled with low-rank techniques currently allows undertaking 3D imaging problems at the exploration scale with frequency-domain FWI (Operto et al., 2015; Li et al., 2019). However, their extension to the large 3D imaging problems is still prohibitive in terms of memory demand, volume of computation and communication. Moreover, the typically sparse OBS deployments translate to a limited number of reciprocal sources that have to be processed within the large computing domain. Consequently, efficient parallelism over the sources and over the subdomains can be implemented to speed up the processing in the time domain. Therefore, while the frequency-domain FWI is still contemporaneously easily utilized for 2D crustal-scale OBS data, the perspective of changing the seismic imaging paradigm toward the 3D high-resolution model reconstruction requires robust FWI schemes designed in the time domain.

6 Conclusions

We have illustrated how the GSOT misfit function can relax the initial model design for crustal-scale FWI from OBS data. In both cases of synthetic and field studies, we were able to guide GSOT-based FWI toward a correct solution starting from a simple 1D model.

Significantly better convexity of the GSOT than that of the L^2 misfit function makes it possible to handle the kinematic errors in the initial model that are of the order of a few cycles. Consequently, this approach allows for saving efforts related to the precise picking and inversion of the first-arrival traveltimes from the ultralong-offset data, when the initial FWI model is obtained with FAT.

Prospectively, the development of the misfit functions with improved convexity, such as the GSOT, can be expected to stimulate the more routine FWI applications to the wide-angle OBS data. Indeed, with the mitigation of the cycle-skipping problem, the feasibility of the regional FWI would rely more on the ability to use a more realistic physics approximation, more robust regularization techniques, as well as the availability of the seismic data recorded by the sufficiently dense OBS deployments. In particular, the 3D areal OBS acquisitions would essentially improve the illumination of the deep structures, thus making the whole inversion process better constrained. Therefore, the step forward regarding the way that we image the lithospheric targets entails investigating further challenges within the framework of the 3D crustal-scale FWI.

Acknowledgments

This study was partially funded by: (i) the SEISCOPE consortium (<http://seiscope2.osug.fr>), sponsored by AKERBP, CGG, CHEVRON, EQUINOR, EXXON-MOBIL, JGI, SHELL, SINOPEC, SISPROBE, and TOTAL, and (ii) the Polish National Science Center (grant no: 2019/33/B/ST10/01014). The study was granted access to the HPC PL-Grid Infrastructure (grant id: 3dwind2). The access to SFJ-OBS field dataset can be negotiated with JAMSTEC agency and is accessible through their database (http://www.jamstec.go.jp/obsmcs_db/e/index.html). The GO_3D_OBS synthetic model can be accessed through the official data portal of IG PAS (https://dataportal.igf.edu.pl/dataset/go_3d_obs).

References

- Aghamiry, H., Gholami, A., & Operto, S. (2018). Improving full-waveform inversion based on wavefield reconstruction via Bregman iterations. In *Expanded abstracts, 80th annual eage meeting (copenhagen)*.
- Aghamiry, H., Gholami, A., & Operto, S. (2019). Admm-based multi-parameter wavefield reconstruction inversion in VTI acoustic media with TV regularization. *Geophysical Journal International*, 219(2), 1316–1333. doi: <https://doi.org/10.1093/gji/ggz369>
- Alkhalifah, T., & Choi, Y. (2012). Taming waveform inversion non-linearity through phase unwrapping of the model and objective functions. *Geophysical Journal International*, 191, 1171–1178.
- Bertsekas, D. P., & Castanon, D. (1989). The auction algorithm for the transportation problem. *Annals of Operations Research*, 20(1), 67–96. doi: 10.1007/BF02216923
- Borisov, D., Gao, F., Williamson, P., & Tromp, J. (2019). Application of 2d full-waveform inversion on exploration land data. *Geophysics*, 85(2), 1–57.
- Borisov, D., Modrak, R., Gao, F., & Tromp, J. (2017). Spectral-element based 3D elastic full-waveform inversion of surface waves in the presence of irregular topography using an envelope-based misfit function. *Geophysics*.
- Bozdağ, E., Trampert, J., & Tromp, J. (2011). Misfit functions for full waveform inversion based on instantaneous phase and envelope measurements. *Geophysical Journal International*, 185(2), 845–870.
- Brenders, A. J., & Pratt, R. G. (2007a). Efficient waveform tomography for lithospheric imaging: implications for realistic 2D acquisition geometries and low frequency data. *Geophysical Journal International*, 168, 152–170.
- Brenders, A. J., & Pratt, R. G. (2007b). Full waveform tomography for lithospheric imaging: results from a blind test in a realistic crustal model. *Geophysical Journal International*, 168, 133–151.
- Byrd, R. H., Lu, P., & Nocedal, J. (1995). A limited memory algorithm for bound constrained optimization. *SIAM Journal on Scientific and Statistical Computing*, 16, 1190–1208.
- Carotti, D., Hermant, O., Masclet, S., Reinier, M., Messud, J., Sedova, A., & Lambaré, G. (2020). Optimal transport full waveform inversion - applications. In *82th Annual EAGE Meeting (Amsterdam)*. European Association of Geoscientists & Engineers. Retrieved from <https://www.earthdoc.org/content/papers/10.3997/2214-4609.202011288> doi: <https://doi.org/10.3997/2214-4609.202011288>
- Cerjan, C., Kosloff, D., Kosloff, R., & Reshef, M. (1985). A nonreflecting boundary condition for discrete acoustic and elastic wave equations. *Geophysics*, 50(4), 2117–2131.
- Chen, F., & Peter, D. (2018, June). Constructing Misfit Function for Full Waveform Inversion Based on Sliced Wasserstein Distance. In *80th EAGE conference and exhibition 2018*. EAGE Publications BV. doi: 10.3997/2214-4609.201801030
- Choi, Y., & Alkhalifah, T. (2011). Frequency-domain waveform inversion using the unwrapped phase. *SEG Technical Program Expanded Abstracts*, 30(1), 2576–2580.
- Choi, Y., & Shin, C. (2008). Frequency-Domain Elastic Full Waveform Inversion Using the New Pseudo-Hessian Matrix: Experience Of Elastic Marmousi 2 Synthetic Data. *Bulletin of the Seismological Society of America*, 98(5), 2402–2415.
- Czuba, W. (2016, November). 3-d seismic tomographic modelling of the crustal structure of northwestern svalbard based on deep seismic soundings. *Geophysical Journal International*, 208(1), 508–520. doi: 10.1093/gji/ggw418
- Davy, R. G., Morgan, J. V., Minshull, T. A., Bayrakci, G., Bull, J. M., Klaeschen, D., . . . Cresswell, D. (2017, October). Resolving the fine-scale velocity structure of continental hyperextension at the Deep Galicia Margin using full-waveform inversion. *Geophysical Journal International*, 212(1), 244–263. Retrieved from <https://doi.org/10.1093/gji/ggx415> doi: 10.1093/gji/ggx415
- Engquist, B., & Froese, B. D. (2014). Application of the Wasserstein metric to seismic signals. *Communications in Mathematical Science*, 12(5), 979–988.

- Górszczyk, A., & Operto, S. (2021). GO_3D_OBS: The multi-parameter benchmark geomodel for seismic imaging method assessment and next-generation 3D survey design (version 1.0). *Geoscientific Model Development*, 14(3), 1773–1799. doi: <https://doi.org/10.5194/gmd-14-1773-2021>
- Górszczyk, A., Operto, S., & Malinowski, M. (2017, June). Toward a robust workflow for deep crustal imaging by FWI of OBS data: The eastern nankai trough revisited. *Journal of Geophysical Research: Solid Earth*, 122(6), 4601–4630. doi: 10.1002/2016jb013891
- Górszczyk, A., Operto, S., Schenini, L., & Yamada, Y. (2019). Crustal-scale depth imaging via joint FWI of OBS data and PSDM of MCS data: a case study from the eastern nankai trough. *Solid Earth*, 10, 765–784. doi: <https://doi.org/10.5194/se-10-765-2019>
- Gras, C., Dagnino, D., Jiménez-Tejero, C. E., Meléndez, A., Sallarès, V., & Ranero, C. R. (2019, October). Full-waveform inversion of short-offset, band-limited seismic data in the alboran basin (SE iberia). *Solid Earth*, 10(6), 1833–1855. doi: 10.5194/se-10-1833-2019
- He, W., Brossier, R., Métivier, L., & Plessix, R.-É. (2019). Land seismic multi-parameter full waveform inversion in elastic VTI media by simultaneously interpreting body waves and surface waves with an optimal transport based objective function. *Geophysical Journal International*, 219(3), 1970–1988. doi: 10.1093/gji/ggz414
- Hicks, G. J. (2002). Arbitrary source and receiver positioning in finite-difference schemes using Kaiser windowed sinc functions. *Geophysics*, 67, 156–166.
- Kamei, R., Pratt, R. G., & Tsuji, T. (2012). Waveform tomography imaging of a megasplay fault system in the seismogenic Nankai subduction zone. *Earth and Planetary Science Letters*, 317–318, 343–353.
- Kamei, R., Pratt, R. G., & Tsuji, T. (2014, April). Misfit functionals in Laplace-Fourier domain waveform inversion, with application to wide-angle ocean bottom seismograph data. *Geophysical Prospecting*, 62(5), 1054–1074. doi: 10.1111/1365-2478.12127
- Kantorovich, L. (1942). On the transfer of masses. *Dokl. Acad. Nauk. USSR*, 37, 7–8.
- Korenaga, J., Holbrook, W. S., Kent, G. M., Kelemen, P. B., Detrick, R. S., Larsen, H. C., ... Dahl-Jensen, T. (2000). Crustal structure of the southeast greenland margin from joint refraction and reflection seismic tomography. *Journal of Geophysical Research*, 105, 21591–21614.
- Kurzmann, A., Przybindowska, A., Kohn, D., & Bohlen, T. (2013). Acoustic full waveform tomography in the presence of attenuation: a sensitivity analysis. *Geophysical Journal International*, 195(2), 985–1000.
- Li, Y., Brossier, R., & Métivier, L. (2019). 3D frequency-domain elastic wave modeling using spectral element method with a parallel direct linear solver. In *Expanded abstracts, 81th annual EAGE conference & exhibition, london* (p. Th R06 05). EAGE. doi: 10.3997/2214-4609.201901534
- Luo, J., & Wu, R.-S. (2015). Seismic envelope inversion: reduction of local minima and noise resistance. *Geophysical Prospecting*, 63(3), 597–614.
- Luo, S., & Sava, P. (2011). A deconvolution-based objective function for wave-equation inversion. *SEG Technical Program Expanded Abstracts*, 30(1), 2788–2792. Retrieved from <http://link.aip.org/link/?SGA/30/2788/1> doi: 10.1190/1.3627773
- Luo, Y., & Schuster, G. T. (1991). Wave-equation travelttime inversion. *Geophysics*, 56(5), 645–653.
- Malinowski, M., Operto, S., & Ribodetti, A. (2011). High-resolution seismic attenuation imaging from wide-aperture onshore data by visco-acoustic frequency-domain full waveform inversion. *Geophysical Journal International*, 186(3), 1179–1204.
- Messud, J., & Sedova, A. (2019). Multidimensional optimal transport for 3d FWI: Demonstration on field data. In *Expanded abstracts, 81th annual eage meeting (london)*.
- Métivier, L., Allain, A., Brossier, R., Méridot, Q., Oudet, E., & Virieux, J. (2018). Optimal transport for mitigating cycle skipping in full waveform inversion: a graph space transform approach. *Geophysics*, 83(5), R515–R540. Retrieved from <https://doi.org/10.1190/geo2017-0807.1> doi: 10.1190/geo2017-0807.1

- Métivier, L., & Brossier, R. (2016). The SEISCOPE optimization toolbox: A large-scale nonlinear optimization library based on reverse communication. *Geophysics*, *81*(2), F11-F25.
- Métivier, L., Brossier, R., Méridot, Q., & Oudet, E. (2019a). A graph space optimal transport distance as a generalization of L^p distances: application to a seismic imaging inverse problem. *Inverse Problems*, *35*(8), 085001.
- Métivier, L., Brossier, R., Méridot, Q., & Oudet, E. (2019b). Graph space optimal transport for FWI: Auction algorithm, application to the 2d valhall case study. In *Expanded abstracts, 81th annual EAGE conference & exhibition, london* (p. Tu R08 03). EAGE. doi: 10.3997//2214-4609.201900870
- Métivier, L., Brossier, R., Méridot, Q., Oudet, E., & Virieux, J. (2016a). Measuring the misfit between seismograms using an optimal transport distance: Application to full waveform inversion. *Geophysical Journal International*, *205*, 345–377.
- Métivier, L., Brossier, R., Méridot, Q., Oudet, E., & Virieux, J. (2016b). An optimal transport approach for seismic tomography: Application to 3D full waveform inversion. *Inverse Problems*, *32*(11), 115008.
- Monge, G. (1781). Mémoire sur la théorie des déblais et des remblais. *Histoire de l'Académie Royale des Sciences de Paris*.
- Morgan, J., Warner, M., Bell, R., Ashley, J., Barnes, D., Little, R., . . . Jones, C. (2013). Next-generation seismic experiments: wide-angle, multi-azimuth, three-dimensional, full-waveform inversion. *Geophysical Journal International*, *195*, 1657–1678.
- Nakanishi, A., Shiobara, H., Hino, R., Kodaira, S., Kanazawa, T., & Shinamura, H. (1998). Detailed subduction structure across the eastern Nankai Trough obtained from ocean bottom seismograph profiles. *Journal of Geophysical Research*, *103*(B11), 27151–27168.
- Nocedal, J. (1980, September). Updating quasi-Newton matrices with limited storage. *Mathematics of Computation*, *35*(151), 773–773. doi: 10.1090/s0025-5718-1980-0572855-7
- Nocedal, J., & Wright, S. J. (2006). *Numerical optimization* (2nd ed.). Springer.
- Operto, S., Brossier, R., Gholami, Y., Métivier, L., Prioux, V., Ribodetti, A., & Virieux, J. (2013). A guided tour of multiparameter full waveform inversion for multicomponent data: from theory to practice. *The Leading Edge, Special section Full Waveform Inversion*(September), 1040-1054.
- Operto, S., & Miniussi, A. (2018). On the role of density and attenuation in 3D multiparameter visco-acoustic VTI frequency-domain FWI: an OBC case study from the North Sea. *Geophysical Journal International*, *213*, 2037–2059. doi: 10.1093/gji/ggy103
- Operto, S., Miniussi, A., Brossier, R., Combe, L., Métivier, L., Monteiller, V., . . . Virieux, J. (2015). Efficient 3-D frequency-domain mono-parameter full-waveform inversion of ocean-bottom cable data: application to Valhall in the visco-acoustic vertical transverse isotropic approximation. *Geophysical Journal International*, *202*(2), 1362-1391.
- Operto, S., Virieux, J., Dessa, J. X., & Pascal, G. (2006). Crustal imaging from multifold ocean bottom seismometers data by frequency-domain full-waveform tomography: application to the eastern Nankai trough. *Journal of Geophysical Research*, *111*(B09306), doi:10.1029/2005JB003835.
- Peters, B., & Herrmann, F. J. (2017, 01). Constraints versus penalties for edge-preserving full-waveform inversion. *The Leading Edge*, *36*(1), 94-100. Retrieved from <https://www.slim.eos.ubc.ca/Publications/Public/Journals/TheLeadingEdge/2016/peters2016cvp/peters2016cvp.html> doi: 10.1190/tle36010094.1
- Pladys, A., Brossier, R., & Métivier, L. (2020). Graph space optimal transport based FWI: 3D OBC valhall case study. In *Seg technical program expanded abstracts 2020*.
- Plessix, R. E. (2006). A review of the adjoint-state method for computing the gradient of a functional with geophysical applications. *Geophysical Journal International*, *167*(2), 495-503.
- Plessix, R. E., & Perkins, C. (2010). Full waveform inversion of a deep water ocean bottom

- seismometer dataset. *First Break*, 28, 71-78.
- Poncet, R., Messud, J., Bader, M., Lambaré, G., Viguier, G., & Hidalgo, C. (2018). Fwi with optimal transport: a 3D implementation and an application on a field dataset. In *Expanded abstracts, 80th annual eage meeting (copenhagen)*.
- Pratt, R. G. (1999). Seismic waveform inversion in the frequency domain, part I: theory and verification in a physical scale model. *Geophysics*, 64, 888-901.
- Pratt, R. G. (2008). Waveform tomography - successes, cautionary tales, and future directions. In *Presented at the 70th annual EAGE conference & exhibition, roma* (p. WO11 - Full-Waveform Inversion: current status and perspectives).
- Provenzano, G., Brossier, R., & Métivier, L. (2020). Joint FWI of diving and reflected waves using a graph space optimal transport distance: synthetic tests on limited-offset surface seismic data. In *Seg technical program expanded abstracts 2020*.
- Qin, Y., & Singh, S. C. (2017, apr). Detailed seismic velocity of the incoming subducting sediments in the 2004 great sumatra earthquake rupture zone from full waveform inversion of long offset seismic data. *Geophysical Research Letters*, 44(7), 3090-3099. Retrieved from <https://doi.org/10.1002/2016gl072175> doi: 10.1002/2016gl072175
- Qiu, L., Ramos-Martinez, J., Valenciano, A., Yang, Y., & Engquist, B. (2017). Full-waveform inversion with an exponentially encoded optimal-transport norm. In *Seg technical program expanded abstracts 2017* (p. 1286-1290).
- Ravaut, C., Operto, S., Improta, L., Virieux, J., Herrero, A., & dell'Aversana, P. (2004). Multi-scale imaging of complex structures from multi-fold wide-aperture seismic data by frequency-domain full-wavefield inversions: application to a thrust belt. *Geophysical Journal International*, 159, 1032-1056.
- Sambolian, S., Górszczyk, A., Operto, S., Ribodetti, A., F., B. T., , & Virieux, J. (2019). Building initial model for FWI from ultra long-offset obn data by first-arrival travel-time + slope tomography. In *81th annual eage meeting (london)*.
- Sambolian, S., Operto, S., Ribodetti, A., Tavakoli, B., & Virieux, J. (2019). Parsimonious slope tomography based on eikonal solvers and the adjoint-state method. *Geophysical Journal International*, 218(1), 456-478. doi: 10.1093/gji/ggz150
- Sedova, A., Messud, J., Prigent, H., Royle, G., & Lambaré, G. (2019). Acoustic land full waveform inversion on a broadband land dataset: the impact of optimal transport. In *Expanded abstracts, 81th annual eage meeting (london)*.
- Shin, C., Yoon, K., Marfurt, K. J., Park, K., Yang, D., Lim, H. Y., ... Shin, S. (2001). Efficient calculation of a partial derivative wavefield using reciprocity for seismic imaging and inversion. *Geophysics*, 66(6), 1856-1863.
- Shutova, S., Carotti, D., & Hermant, O. (2020). Extending the potential of acoustic optimal transport fwi in the south of oman. In *82th Annual EAGE Meeting (Amsterdam)*. European Association of Geoscientists & Engineers. Retrieved from <https://www.eearthdoc.org/content/papers/10.3997/2214-4609.202012113> doi: <https://doi.org/10.3997/2214-4609.202012113>
- Sirgue, L., & Pratt, R. G. (2004). Efficient waveform inversion and imaging : a strategy for selecting temporal frequencies. *Geophysics*, 69(1), 231-248.
- Stopin, A., Plessix, R.-E., & Al Abri, S. (2014). Multiparameter waveform inversion of a large wide-azimuth low-frequency land data set in Oman. *Geophysics*, 79(3), WA69-WA77.
- Sun, B., & Alkhalifah, T. (2019). The application of an optimal transport to a pre-conditioned data matching function for robust waveform inversion. *GEOPHYSICS*, 84(6), R935-R957. Retrieved from <https://doi.org/10.1190/geo2018-0413.1> doi: 10.1190/geo2018-0413.1
- Takougang, E. M. T., & Calvert, A. J. (2011). Application of waveform tomography to marine seismic reflection data from the Queen Charlotte Basin of western canada. *Geophysics*, 76(2), B55-B70.
- Thorpe, M., Park, S., Kolouri, S., Rohde, G., & Slepčev, D. (2016, sep). A transportation l^p distance for signal analysis. *ArXiv e-prints*.
- Treister, E., & Haber, E. (2017). Full waveform inversion guided by travelttime tomography.

- 861 *SIAM Journal on Scientific Computing*, 39(5), S587-S609.
- 862 Trinh, P. T., Brossier, R., Métivier, L., Virieux, J., & Wellington, P. (2017). Bessel smooth-
 863 ing filter for spectral element mesh. *Geophysical Journal International*, 209(3), 1489–
 864 1512. Retrieved from <http://dx.doi.org/10.1093/gji/ggx103> doi: 10.1093/gji/
 865 ggx103
- 866 Tromp, J. (2019). Seismic wavefield imaging of earth’s interior across scales. *Nature Reviews*
 867 *Earth & Environment*, 1–14.
- 868 van Leeuwen, T., & Herrmann, F. J. (2013). Mitigating local minima in full-waveform
 869 inversion by expanding the search space. *Geophysical Journal International*, 195(1),
 870 661–667. doi: doi:10.1093/gji/ggt258
- 871 van Leeuwen, T., & Mulder, W. A. (2010). A correlation-based misfit criterion for wave-
 872 equation traveltime tomography. *Geophysical Journal International*, 182(3), 1383–
 873 1394.
- 874 Virieux, J., & Operto, S. (2009). An overview of full waveform inversion in exploration
 875 geophysics. *Geophysics*, 74(6), WCC1-WCC26.
- 876 Warner, M., & Guasch, L. (2016). Adaptive waveform inversion: Theory. *Geophysics*,
 877 81(6), R429-R445.
- 878 Yang, P., Brossier, R., Métivier, L., & Virieux, J. (2016a, October). A review on the system-
 879 atic formulation of 3D multiparameter full waveform inversion in viscoelastic medium.
 880 *Geophysical Journal International*, 207(1), 129-149. doi: 10.1093/gji/ggw262
- 881 Yang, P., Brossier, R., Métivier, L., & Virieux, J. (2016b). Wavefield reconstruction in
 882 attenuating media: A checkpointing-assisted reverse-forward simulation method. *Geo-*
 883 *physics*, 81(6), R349-R362. doi: 10.1190/geo2016-0082.1
- 884 Yang, P., Brossier, R., Métivier, L., Virieux, J., & Zhou, W. (2018). A Time-Domain
 885 Preconditioned Truncated Newton Approach to Multiparameter Visco-acoustic Full
 886 Waveform Inversion. *SIAM Journal on Scientific Computing*, 40(4), B1101-B1130.
 887 doi: 10.1137/17M1126126
- 888 Yang, Y., & Engquist, B. (2018). Analysis of optimal transport and related misfit functions
 889 in full-waveform inversion. *GEOPHYSICS*, 83(1), A7-A12. doi: 10.1190/geo2017-
 890 -0264.1
- 891 Yang, Y., Engquist, B., Sun, J., & Hamfeldt, B. F. (2018). Application of optimal transport
 892 and the quadratic Wasserstein metric to full-waveform inversion. *Geophysics*, 83(1),
 893 R43-R62. Retrieved from <https://doi.org/10.1190/geo2016-0663.1> doi: 10.1190/
 894 geo2016-0663.1
- 895 Yilmaz, O. (2001). *Seismic data analysis*. Society of Exploration Geophysicists: processing,
 896 inversion and interpretation of seismic data.
- 897 Yu, Z., Li, J., Ding, W., Zhang, J., Ruan, A., & Niu, X. (2016, October). Crustal structure
 898 of the southwest subbasin, south china sea, from wide-angle seismic tomography and
 899 seismic reflection imaging. *Marine Geophysical Research*, 38(1-2), 85–104. doi: 10
 900 .1007/s11001-016-9284-1
- 901 Zelt, C., & Barton, P. J. (1998). Three-dimensional seismic refraction tomography: a com-
 902 parison of two methods applied to data from the Faeroe basin. *Journal of Geophysical*
 903 *Research*, 103(B4), 7187–7210.
- 904 Zhu, H., & Fomel, S. (2016). Building good starting models for full-waveform inversion
 905 using adaptive matching filtering misfit. *Geophysics*, 81(5), U61-U72. doi: 10.1190/
 906 geo2015-0596.1