Comprehensive characterization of sooting butane jet flames, Part 1: soot, soot-precursor, and reaction zone

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Abstract

The present work examines the effect of Reynolds number (Re) on n -butane jet flames, ranging from laminar to turbulent regime ($Re = 2100$ to 21500). n -butane is chosen since it can represent the oxidation of larger paraffins contained in practical fuels. Several quantities are measured, and various data analysis approaches are employed. Soot volume fraction (f_v) was measured using a laser-induced incandescence technique, whereas polycyclic aromatic hydrocarbons (PAH) and reaction zone (OH) were imaged using laser-induced fluorescence (LIF) tool. The mean and instantaneous images of OH, PAH, and soot volume fraction are examined. The reaction zone is the least affected by the turbulence, while the PAH-LIF signal is moderately affected. A strong effect of turbulence is observed on the soot concentration and intermittency. Soot and PAH concentration decreased with Re due to reduced residence time, increased strain rate, and likely increase in a scalar dissipation rate. In the turbulent regime, f_v decreases with PAH at a sharper rate, possibly due to reduced local time scales associated with turbulent eddies. Soot structure complexity is quantified through a fractal dimension (D_f). D_f increased with Re ; however, in a turbulent regime D_f becomes insensitive to Re . A semi-global correlation between f_v and sheet thickness is also analyzed. A power-law trend is noted in the

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f_v vs. thickness plot. Coefficients of power-fit are found to be Re -dependent. Additionally, the local correlation between f_v and sheet thickness is examined, which revealed a non-monotonic trend. f_v peaks at a preferred soot sheet thickness. These analysis-derived insights can contribute towards the understanding of soot-turbulence interaction. Furthermore, the reported database will facilitate the validation of soot chemistry models intended for practical fuels.

Keywords: jet flames, turbulent sooting flames, soot, butane, PAH

1. Introduction

Combustion-generated soot emission adversely affects our health and the environment. Therefore, a fundamental understanding of soot formation is essential to control soot emission. However, soot formation is a complex process that depends on the fuel type, air/fuel mixing, flow field, temperature, and residence time. The influence of such parameters has been elucidated to some extent, both experimentally and numerically. For numerical studies, large-eddy simulations (LES) along with sub-grid models are usually used to predict soot concentration. In LES, two interlinked phenomena, namely turbulence and chemistry, are modeled for sub-grid small scales. For practical devices such as gas turbines or diesel engines, it is necessary to develop computationally feasible and yet reasonably accurate models. Such turbulence-soot chemistry sub-grid models need to be validated against detailed measurements. Therefore, an experimental database with a well-controlled boundary condition is required. Several past works have reported phenomenon-focused soot investigations, while a few aimed at generating the database suitable for validating models of practical interest. Both of such past works are summarized next.

Since combustion in many practical devices is accompanied by turbulence, soot investigations in turbulent flames are desired. Most of the experimental studies in turbulent sooting flames have been carried out in a jet flame configuration. For instance, Lee et al. [1] investigated the relation between soot, polycyclic aromatic hydrocarbons (PAH), and OH distributions, along with var-

ious analyses. Qamar et al. [2] reported the soot volume fraction in a turbulent non-premixed jet flame with natural gas fuel. Shaddix et al. [3] reported measurements and numerical modeling results in turbulent non-premixed jet flames with ethylene and kerosene-based JP-8 fuels. The data [3] included soot volume fraction, OH, and PAH fields. This database has been used recently to validate LES results in [4]. To meet the particular needs of modelers, Köhler et al. [5] devised a flame configuration. A lifted ethylene jet flame without any pilot flame anchoring was chosen. The DLR database [5, 6] containing various parameters was used to assess simulations [6]. Gu et al. [7] reproduced the soot concentration measurement in the DLR flame [5] with an excellent agreement. The authors [7] report simultaneous measurements of temperature, soot volume fraction, and soot size. The authors examined correlations between these quantities. Similar multi-scalar measurements in turbulent toluene flame are reported recently by Kruse et al. [8]. The authors [8] showed that soot may not always completely oxidize across the OH-layer.

Apart from the database-oriented studies, parameters influencing soot in turbulent flames are also investigated by a few research groups. The correlation between gas temperature and soot concentration has been examined in laminar [9] and turbulent flames [10–12]. Soot concentration was noted to peak within a preferential temperature range. Park et al. [12] performed simultaneous measurements of the soot and mixture fraction in the soot-inception region. They [12] concluded that soot preferentially forms in a region of low scalar dissipation rate. Narayanaswamy and Clemens [13] have investigated the effect of strain rate on soot formation. Soot was found to exist at a preferred velocity and local strain rate, independent of the jet exit velocity. Mahmoud et al. [14, 15] reported soot volume fraction trends in turbulent jet flames as a function of exit strain rate at a constant Reynolds number (Re). The total soot yield was observed to vary linearly with the nozzle diameter and fuel flow rate. In recent work [16], a global relationship (power-law trend) between soot sheet width (i.e., thickness) and soot concentration is reported. Time-resolved spatial correlations between the soot, PAH, and OH distributions were examined by Franzelli et al.

[17]. Although these simultaneous measurements were qualitative, it provided
55 insights into the spatio-temporal evolution of soot, soot-precursor, and reaction
zone. Soot concentration and particle size in buoyancy-dominated jet flames
have been measured by Crosland et al. [18]. Besides the jet configuration, the
soot formation has also been investigated in a more complex swirl stabilized
flames [19–23].

60 In jet flames, both the lifted and attached flames have been studied. The
flame lift-off leads to leakage of oxidizer in a fuel zone, which consequently leads
to partial premixing. The effect of such premixing has been investigated in
detail by Grader et al. [24] in a recent LES study. The authors quantified the
extent of premixed and non-premixed combustion regimes through a flame-index
65 [25] approach. It was suggested that the upstream (near flame base) partial
premixing could influence soot evolution. Soot formation and growth processes
were observed to occur dominantly in the premixed regime, while soot oxidation
was postulated to occur mainly in the non-premixed combustion regime.

The effect of Re on soot volume fraction (f_v) has been investigated by a few
70 researchers in non-premixed jet flames [1, 15, 26]. The fundamental, indepen-
dent parameters that govern the soot formation are - the mixing field (mixture
fraction and scalar dissipation rate), temperature, and residence time. Several
soot-influencing quantities change simultaneously with the variation of jet ve-
locity (to alter Re). The key variables are strain rate, residence time, level of
75 premixing (or mixture fraction) owing to the flame lift-off and turbulent mix-
ing, and scalar dissipation rate which is a function of mixture fraction gradient.
The increase in Re (through velocity) is generally accompanied by a decrease
in the residence time and an increase in the strain rate. The level of premixing
and scalar dissipation rate are expected to increase with Re . Therefore, the
80 observed change in f_v with Re is a manifestation of the combined influence of
several parameters. Note, though these parameters are interdependent, they
may not be used interchangeably while examining their impact on soot. The
relative dominance of these soot-influencing parameters is complex to assess,
especially in a turbulent flame.

85 As noted from the above overview, a wide body of literature exists in soot-
ing flames. The international sooting flame workshop [27] has consolidated data
from various groups (Sandia, DLR, Adelaide, TUDelft) to facilitate database ac-
cess to the modeling community. In most of the works reported so far, ethylene
[1, 3, 5, 7, 10] or ethylene-based mixtures [13–16, 28] were used as a fuel. The
90 choice of ethylene has been primarily motivated by the considerable soot yield,
which enables accurate measurements. Additionally, chemical kinetic mecha-
nisms for ethylene are well-established [14]. A few studies used methane [17] or
methane-based mixtures [2, 18].

The combustion study of larger alkanes is also necessary since they are im-
95 portant constituents of practical fuels. Therefore, *n*-butane has been used as
a surrogate fuel in spark-ignition engines since it is the smallest paraffin that
mimics oxidation of larger paraffins contained in a gasoline [29]. *n*-butane is
complex enough to mimic the practical fuels while offering simplicity to facil-
itate the development of chemical kinetics mechanisms. Thermochemical and
100 combustion properties of *n*-butane are similar to the fuels of practical interest
[30, 31]. Yet, there is no detailed database of turbulent butane jet flames in the
literature. Such a database is needed to validate the simulations developed to
predict soot formation with fuels of practical interest. The present contribution
fills this database gap by providing information on soot volume fraction, soot
105 particle size, soot-precursor (PAH), reaction zone (based on OH distribution),
temperature (in a low-sooting region), velocity field and fuel concentration (in
a non-reacting lifted part), and burner wall temperature. To summarize the
findings effectively, the paper is divided into two parts. The present article
(Part 1) discusses soot, soot-precursor, and reaction zone characteristics. The
110 companion paper (Part 2) [32] focuses on the soot-temperature correlation and
soot particle size.

The objectives of the present paper are to report the soot volume fraction in
n-butane flames and assess the effect of turbulence on soot characteristics. An
additional objective is to investigate the correlation between soot concentration,
115 soot-precursor (PAH), and reaction zone (OH). Further contributions include

fractal and thickness analyses of soot sheets.

2. Experimental methods

2.1. Burner and flame conditions

The jet configuration was chosen since it provides an axisymmetric flame
120 with excellent reproducibility owing to well-controlled boundary conditions.
Figure 1 shows the schematic of the burner along with the overall dimensions.
The fuel (*n*-butane) was injected through a tube of 2.4 mm inner diameter and
3.1 mm outer diameter. The fuel tube was surrounded by the co-flowing air,
which was issued through a square duct of 400 mm width. The upstream part
125 of the co-flow duct accommodates flow conditioning devices to enhance uniformity.
The flame was confined up to 750 mm height above the burner (HAB).
The quartz windows provide optical access for laser diagnostics. The optically
accessible regions are shaded in Fig. 1 along with dimensions. Although the
confinement limits the optical access, it is necessary to avoid flame perturba-
130 tions caused by ambient currents. The confinement also ensures well-defined
boundary conditions. A square exhaust hood of 750 mm size extracts the com-
bustion gases. The flame perturbation due to entrainment of ambient air from
the co-flow exit plane (at HAB = 750 mm) was mitigated by a square annular
shield of airflow.

135 The air and fuel flow rates were regulated with thermal mass flow controllers
(Bronkhorst) that were calibrated using a Coriolis calibration bench. Based on
this calibration, the uncertainty in flow rates is estimated to be within $\pm 1\%$.
Four *n*-butane jet flames were established by varying the fuel flow rate. The
mass flow rate of co-flow air was kept constant and high enough (5 g/s) to
140 achieve over-ventilated flames. The corresponding bulk velocity of air co-flow is
26 cm/s. These flame conditions are listed under Table 1 along with Re , lift-off
height (h_{lift}), flame length (L_f), mean flame width (W_f), bulk velocity (U_j),
and exit strain rate (U_j/d). Flame length determined from the photographs is
likely to have higher uncertainty in turbulent or unsteady flames. Thus, L_f in

145 this work is deduced from the OH presence probability map. Such a map is
 obtained based on a certain presence threshold applied to the imaged OH signal
 (detailed subsequently in Sec. 3.6). L_f is obtained by defining the flame-tip at
 10% OH probability. This criterion marks the external edge of the flame-brush.
 For $Re = 21500$, flame-tip was beyond the imaged data. Nevertheless, L_f is
 150 estimated by locating the PAH-tip (which was well-imaged for all Re) from the
 PAH probability map. The ratio of the lengths of OH-tip to PAH-tip remained
 nearly constant (with a value of 1.16 ± 0.01) for $Re = 2100, 5000$, and 7200 .
 Thus, the identical scaling factor (ratio) was used to estimate L_f for $Re = 21500$
 flame. The OH probability map is also used to deduce the mean flame width
 155 (W_f) by considering the radial location of peak OH probability. This criterion
 provides the centerline of the flame brush in the radial direction. The lift-off
 height (h_{lift}) is determined by locating the flame base in instantaneous OH
 fields. The mean and standard deviation of h_{lift} are indicated in Table 1. At
 $Re = 21500$ in turbulent flame, strong fluctuations of the flame base leads to
 160 higher σ_h . Since the lift-off height is a sensitive parameter, it can be used for a
 stringent validation of simulation models.

Figure 2 shows the flame photographs acquired using a digital camera (D70s,
 Nikon) at three following exposures: $1/20$ s to image the blue flame base, $1/500$ s
 to visualize soot inception regions, and $1/8000$ s to qualitatively visualize large-
 165 scale soot structures, especially in a turbulent case. In the $Re = 2100 - 7200$
 range, the flame is entirely contained within the co-flow duct. At $Re = 21500$,
 the flame-tip exceeds the confinement of the duct. Some regions were optically
 inaccessible, as indicated earlier in Fig. 1. Investigated four flames represent an
 unsteady laminar case (Fig. 2a), transient flow attached flame (Fig. 2b), and
 170 low-turbulence lifted flame (Fig. 2c), and a fully turbulent lifted flame (Fig.
 2d). The laminar, transient, and fully-turbulent terminologies are based on the
 exit Re for round jets. These four cases provide modelers an opportunity to
 validate simulations at different flow regimes.

2.2. Boundary conditions

175 To aid LES validations, the following boundary conditions are measured:
wall temperature for all the flames, and velocity and mixing fields upstream of
Re 21500 flame. For brevity, the velocity and mixing boundary conditions are
provided in the Supplement (Sections S1.2 and S1.3). An appreciable partial
premixing is noted at the base of *Re* 21500 flame.

180 Confined sooting flames could alter the duct wall temperature (T_w) through
radiative heating. Therefore, T_w was measured using thermocouples (Type-K
#397-1488, RS Components). Thermocouples were flush-mounted on the wall
at nine axial locations. For thermocouple mounting, quartz-window space was
replaced by steel plates. The data was acquired over 10 minutes at a 2 *Hz*
185 rate. The mean temperature was obtained by time-averaging the values. To
reduce the transient heating bias, measurements were acquired 45 minutes after
the flame ignition. An approximately similar approach was adopted for other
laser-based measurements. Figure 3 shows the mean wall temperature (T_w) for
flames at different *Re*. The wall temperature differs from ambient conditions
190 by as much as 140 *K* for the highest *Re*. T_w increases with *Re* due to increased
total soot yield, flue gas volume, and flame vicinity to the wall. The maximum
 T_w is observed for turbulent flame (*Re* 21500). For laminar flame (*Re* 2100),
the wall does not heat up significantly due to the slender flame. For *Re* 5000
and 7200 flames, T_w remains appreciable even near the exit plane of the co-flow
195 duct.

Temperature profiles follow the axial f_v trends until peak- f_v location. Be-
yond this height, convective heating is likely to be dominant due to increased
flame vicinity to the wall. A slope discontinuity in the T_w profile appears after
every three data points. Note, a gasket was used between the thermocouple-
200 mounted steel plate and the co-flow duct wall. This gasket acts as a conduction
insulator. Since three thermocouples were mounted on each plate, the corre-
sponding slope discontinuity is observed across different plates (or thermocouple
sets).

2.3. Laser diagnostics

205 2.3.1. Laser-induced incandescence (LII)

In the LII technique, soot particles are heated well beyond flame temperature. The resulting broadband incandescence signal is acquired at a certain wavelength. Once calibrated, the LII signal provides the soot volume fraction. To heat soot particles, infrared wavelength (1064 nm) of the Nd:YAG laser
210 (Brilliant, Quantel) was used since this avoids PAH interferences in the LII signal [33–35]. The laser was operated at a 10 Hz repetition rate. The laser beam was formed into a sheet to obtain the planar LII signal. The light-sheet (LS) was obtained by using a set of cylindrical ($f = -33$ mm) and a spherical ($f = 1000$ mm) lenses. The LS measured 90 mm in height $\times$ 0.3 mm in thick-
215 ness. Laser energy was 105 mJ/pulse, which translates to an average fluence of 0.4 J/cm². The LS thickness and profile were determined using a beam profiler (WinCam, DataRay Inc.). The LS intensity was found to be uniform within 70% of the peak. This extent of non-uniformity is acceptable if the LII is performed in a plateau regime (of LII signal vs. laser fluence plot). To verify the
220 plateau, the fluence curve was deduced by measuring the LII signal as a function of laser fluence. Laser energy was controlled using a variable attenuator (containing polarizer and half-wave plate), which facilitated energy variation at a constant laser pulse width (~ 7 ns). The derived fluence curve is provided in Fig. S7a of the Supplement. Typically, the plateau regime commences around
225 0.3 J/cm². The present energy choice ensured that the fluence in the entire light-sheet remains within a plateau regime with a range of 0.35 to 0.45 J/cm². At this fluence, the signal-to-noise ratio (SNR) of the instantaneous LII signal is nominally around 12, while the f_v detection limit is approximately 0.015 ppm.

The LII signal was collected normal to the light-sheet using an intensified
230 CCD (ICCD) camera (PI-MAX: 512, Princeton Instruments). The camera was equipped with an imaging lens (105mm f/4.5, UV-Nikkor) that provided the magnification of 5.75 pixels/mm and corresponding square field-of-view (FOV) of 89 mm in width. The signal was collected through a 400 nm filter with

FWHM of 25 nm (#86664, Edmund Optics). The blue spectral region (400 nm) mitigates the background noise from soot radiation (at flame temperature). A short prompt gate is needed to avoid signal biases towards larger soot particles that cool down at a slower rate. Thus, the prompt gating was used with a short gate width of 50 ns. The data was acquired at a 10 Hz rate. The number of acquired images were 1000 for $y < 150$ mm, and 2000 for higher height ($y > 150$ mm) to ensure statistical convergence. The LII signal was calibrated using the laser-extinction method at 1064 nm. Details of the calibration set-up and data reduction are provided in Sec. S3.1 of the Supplement. Uncertainty sources with respective estimates are detailed in Sec. S3.2. The overall uncertainty in the mean f_v is estimated to be $\pm 19\%$.

2.3.2. OH-PLIF

OH radical in non-premixed flames can approximately indicate the location of the reaction zone. Therefore, OH distribution is imaged using the planar laser-induced fluorescence (PLIF) technique. To generate OH-LIF signal, the $Q_1(6)$ line of the $A - X(1, 0)$ transition is excited near 283 nm. The resulting fluorescence was collected around 310 nm. The $Q_1(6)$ transition was selected due to a lower sensitivity to temperature [36]. Experiments with this excitation wavelength were ensured by comparing the measured excitation/emission spectrum with that of the LIFBASE [37]. To generate a laser beam with a wavelength of 283 nm, the following approach is adopted. A Nd:YAG laser (Brilliant-B, Quantel) operating at 532 nm was used to pump a frequency-doubled dye laser (TDL90, Quantel) running with Rhodamine 590 dye. The laser delivered pulses at a 10 Hz rate. A wider light-sheet was formed using the same optics as of the LII. A central portion of this light-sheet, uniform within 40% of the peak intensity, was used. The selected portion of LS measured ~ 90 mm high and ~ 0.15 mm thick. The laser energy was 7 mJ/pulse that corresponds to an average fluence of 0.05 J/cm². At this fluence, typical SNR and detection limit measures about 8 and 1500 counts, respectively. A linear dependence of the OH-PLIF signal with laser energy was verified, and

the resulting OH fluence curve is provided in Fig. S8 in the Supplement. The
 265 PLIF signal is corrected for light-sheet nonuniformity. For this correction, the
 light-sheet profile was deduced by assuming a constant OH intensity along the
 length of a laminar diffusion flame. Note, the OH-PLIF signal is not intended
 to be quantitative; instead, it is used to identify the reaction zone location and
 topology.

270 An emICCD camera (PI-MAX4: 512 EMB, Princeton Instruments) equipped
 with a UV lens (105mm f/4.5, UV-Nikkor) was used to image the LIF signal.
 The camera acquired an image of an 89 mm square region with a magnification
 of 5.75 *pixels/mm*. A narrowband 310 nm (#10BPF10-310, Newport) filter was
 used, which largely mitigated the interference from PAH-LIF. The camera was
 275 gated to 30 ns relative to the laser pulse. The OH-PLIF images were acquired
 at a 10 Hz rate. The numbers of acquired frames were 1500 for $y < 150$ mm
 and 2000 for higher heights ($y > 150$ mm).

2.3.3. PAH-PLIF

PAH, as a soot-precursor, plays a crucial role in soot formation. Thus, the
 280 relative concentration and distribution of PAH are examined by acquiring the
 PAH-PLIF signal. To excite PAH, the same laser excitation system and wave-
 length (283 nm) as of OH was used. However, to avoid PAH-LIF saturation,
 the pulse energy was reduced to 2.5 mJ. The corresponding fluence was esti-
 mated to be 0.02 J/cm² for LS of 90 mm × 0.15 mm dimensions. Such a low
 285 fluence is necessary to reduce soot interference from LII. Similar fluence level
 (0.02 J/cm²) was used by Olofsson et al. [38] and Köhler et al. [39] to avoid LII
 interference. The PAH fluorescence was imaged on an ICCD camera (PI-MAX:
 512, Princeton Instruments) through a UV lens (105mm f/4.5, UV-Nikkor) that
 led to the magnification of 5.75 *pixels/mm* (with 89 mm FOV). A broadband
 290 filter of 377 nm wavelength with the FWHM bandwidth of 50 nm (#84109,
 Edmund Optics) was used, similar to [17]. The LIF imaging camera was gated
 to 50 ns relative to the laser pulse. The 283 nm excitation and 350 – 400 nm
 collection leads to the imaging of LIF signal primarily from two- to four-ring

PAH (including naphthalene), as interpreted from Refs. [35, 40]. The SNR of
 295 the PAH-LIF signal is typically around 15; however, the signal intensity de-
 creases sharply in the turbulent flame. Consequently, for $Re = 21500$, the SNR
 decreases to 4, with a detection limit of ~ 100 counts. The PAH-PLIF data was
 acquired at a 10 Hz rate. The number of acquired PAH-LIF images were 1000
 for $y < 150\text{ mm}$, and 2000 for $y > 150\text{ mm}$.

300 A mild non-linearity in LIF intensity is noted (see Fig. S9a) with laser en-
 ergy even at a fluence below 0.02 J/cm^2 . A possibility of the ICCD camera
 saturation was verified (and ruled out) by imaging the signal through a neutral
 density filter. The non-linearity was indeed found to be associated with the
 partial saturation of PAH-LIF. The deviation from linearity is approximately
 305 $\pm 7\%$. Nevertheless, a non-linear LS correction strategy is adapted, as detailed
 in Sec. S2.3. Such precautions enable a qualitative deduction of PAH concen-
 tration. However, note that besides the targeted species concentration, the LIF
 signal also depends on the local gas temperature (through Boltzmann fraction)
 and gas composition (due to LIF quenching). This information is not available
 310 in the present flames. Even if the temperature and gas composition are known,
 there are two additional issues specific to the PAH quantification. Firstly, the
 overlapping excitation and emission spectra of different classes (rings) of PAH
 [41] eliminate the possibility of isolated detection of a single class of PAH. Sec-
 ondly, the spectroscopic parameters for accounting collisional quenching are not
 315 yet well established. Despite these issues, PAH-LIF can be assumed to be semi-
 quantitative (on a relative basis) for the following reasons. PAH forms at a
 specific range of temperature and gas composition (mainly the fuel concentra-
 tion and its gradient). For a given fuel, across different Re , the PAH formation
 conditions (i.e., local temperature and gas composition) may not vary signifi-
 320 cantly. Thus, the temperature-quenching dependence of the PAH-LIF signal is
 assumed to be approximately identical across Re . This assumption enables a
 relative comparison of the PAH-LIF signal on a semi-quantitative basis. Note,
 the transported (i.e., not locally formed) PAH may not be subjected to such
 assumptions. Nevertheless, PAH survives only in a narrow region between fuel

325 and soot zones. Thus, the assumption of a constant temperature-quenching dependence of PAH-LIF is not expected to affect the findings (in Sec. 3.4) of this work.

3. Results and Discussion

3.1. Spatial correlation between OH, PAH, and Soot

330 Figure 4 shows the mean images of OH-PLIF, PAH-PLIF, and soot volume fraction at $Re = 2100$ unsteady laminar flame. Only a relatively steady region of the flame is presented. The unsteadiness is quantified using OH-LIF in the following manner. The flame radius (radial distance between the jet axis and the location of OH-layer centerline) at each y location is extracted for several
 335 realizations (1500 frames). The standard deviation (σ_r) of the flame radius is found to be ≈ 0.05 mm for $y < 60$ mm, whereas σ_r increases to 0.7 mm at $y = 120$ mm. As these σ_r values are comparable to the flame thickness, flame until $y = 120$ mm is assumed to be a quasi-steady. This assumption permits analysis of spatial correlations between reaction zone (marked by OH), soot
 340 precursor, and soot.

Apart from the OH-PLIF signal, an internal low-intensity annular structure is observed around the jet core in Fig. 4a. Recall that the OH excitation and detection wavelengths are 283 nm and 310 nm, respectively. Thus, a minor LIF contribution from two-ring PAH (i.e., smaller PAH) [35, 40] is expected. For
 345 convenience, we assign the term smaller PAH to benzene or two-ring PAH. The PAH signal in Fig. 4b is entirely contained within the inner edge of OH iso-contour (at 3500 counts). We also note similar observations in a simultaneously acquired OH/PAH-PLIF dataset (not shown) in the same flame. In Fig. 4b, PAH distribution at the flame base shows an annular structure. PAH inception
 350 occurs at $y \approx 8$ mm, and it grows rapidly with height. PAH structure in Fig. 4b is located radially outward that of the smaller PAH signal observed in Fig. 4a. The spectral detection window of 350 – 400 nm in PAH-LIF (Fig. 4b) favors imaging of two- to four-ring PAH [35, 40] to which we notionally assign the

term, relatively larger PAH. As expected, larger PAH forms radially outwards
355 of the smaller PAH.

The soot inception (in Fig. 4c) occurs downstream of the PAH at $y \approx 15 \text{ mm}$. Similar to PAH, soot concentration increases sharply with height. This increase is expected to occur mainly because of the soot growth [42] via H-abstraction/ C_2H_2 -addition (HACA) mechanism [43]. The annular soot structure is confined within the inner OH contour. In general, no overlap is noted
360 between soot and OH. This is not unexpected since OH is known to be the dominant oxidizer of soot [44]. As evidenced from Fig. 4, in the soot inception region, species exist in a following radial order from the jet axis: fuel, smaller PAH, relatively larger PAH, soot, and then OH (or reaction zone).

365 3.2. OH, PAH, and Soot fields at Re 21500

The instantaneous fields of OH, PAH, and soot concentration are shown in Fig. 5 for a turbulent flame at Re 21500. The corresponding mean fields are presented in Fig. 6. Such data at other Re is available in the Supplement. The mean fields are deduced from 1500 images (for $y < 150 \text{ mm}$ region) or 2000
370 images (for $y > 150 \text{ mm}$). Due to stringent laser-sheet uniformity requirement (to ensure plateau fluence regime) of the LII, soot concentration is not available at certain heights, unlike OH and PAH fields. With additional acquisitions, it would have been possible to get the soot concentration data for the remaining optically accessible regions.

Instantaneous OH-PLIF images were acquired at different heights (not simultaneously), and the composite image is presented in Fig. 5a. Such OH-PLIF images for other Re are included in the Supplement (Fig. S10). In general, the OH-LIF intensity does not change significantly with HAB and with Re as well. At the base, the flame is not appreciably wrinkled. Although the OH-
380 layer is continuous, isolated flame-islands occasionally appear at the flame base upstream of the bulk OH structure. This is possibly attributed to a three-dimensional flame structure and not necessarily to the local extinction. The large-scale flame wrinkling is observed well-downstream in a $y = 450 - 600 \text{ mm}$

region. Such wrinkling is not present in the laminar flame ($Re = 2100$ in Fig. S10). A mild flame wrinkling is noted at transitional Re (5000 – 7200, in Fig. S10).

The OH-layer at the base of the turbulent flame (Fig. 5a) is thicker than lower Re flames. Since the $Re = 21500$ flame is considerably lifted, the jet turbulence leads to considerable partial premixing in the upstream region, as evidenced from the measured mixing field (detailed in Sec. S1.3 of the Supplement). The partial premixing can create favorable conditions for the formation of an edge flame containing tribrachial structure [45]. From the measured velocity field (Sec. S1.2), we also note the flow divergence upstream of the flame base. Such flow divergence along with the partial premixing is an indication of the edge flame structure [46]. This structure could broaden the OH distribution owing to the merger/vicinity of the non-premixed and fuel-lean branches of the triple flame. Additionally, turbulent transport may also play a secondary role in OH broadening. The partial premixing can influence the soot formation as discussed subsequently in Sec. 3.5.

The mean OH-LIF signal in Fig. 6a decreases significantly with height, while instantaneous OH-LIF showed in Fig. 5a does not show such a substantial diminution. The mean signal is averaged unconditionally. Therefore, any intermittency (instants without OH presence) will decrease the mean signal. Thus, the unconditional mean in a fluctuating field implicitly represents the intermittency component along with the instantaneous signal intensity. Consequently, for model validation purposes, the unconditional mean can be used to compare the combined effect of intermittency and concentration (signal intensity). Apart from the drop in the intensity, the mean OH distribution also shows an increase in the flame-brush thickness with height owing to the increased radial fluctuations. The mean reaction zone is thicker (relative to lower Re cases included in Fig. S11) even at the flame-base. This is primarily due to the broadening of the instantaneous OH-layer owing to the edge flame structure and turbulent transport, as discussed earlier.

Figure 5b shows the instantaneous distribution of PAH. For better visual-

415 ization, images are averaged over 1000 laser shots for $y < 150 \text{ mm}$ and over
 2000 shots at higher heights. The resulting mean PAH image is shown in Fig.
 6b. Since the light-sheet profile correction is one-dimensional (only along the
 height), a two-dimensional artifact remains. This artifact is attributed to the
 use of a dichroic mirror in the collection path, which produces a vignetting
 420 effect.

The instantaneous PAH structure (Fig. 5b) exhibits a diffused appearance.
 High-intensity patches of PAH are observed throughout the field. The forma-
 tion of a key PAH (naphthalene) is known to be highly sensitive to the local
 scalar dissipation rate [47]. Naphthalene was observed to form preferentially in
 425 regions of lower scalar dissipation rate. In the present work, the chosen PAH
 excitation/detection scheme also captures naphthalene. Thus, the observed in-
 tense local patches could be attributed to the spatial fluctuations of the scalar
 dissipation rate associated with the turbulent mixing process.

At the base of the flame, the mean PAH-LIF intensity (Fig. 6b) increases
 430 sharply with height. PAH inception occurs $\sim 30 \text{ mm}$ downstream of the flame
 lift-off height. The annular PAH structure merges at a downstream distance.
 Subsequently, the PAH-LIF intensity along the axis remains reasonably constant
 over a certain distance. The axial PAH intensity peaks at a location where the
 flame radius (interpreted from Fig. 6a) measures maximum. The PAH signal
 435 decreases rapidly near the flame-tip region.

Figure 5c shows the composite image of instantaneous f_v . Unlike PAH, the
 soot structures are highly localized even in a downstream region ($y = 450 -$
 590 mm) of the turbulent flame. This is attributed to a high Schmidt number
 of soot particles, which leads to a low soot diffusivity [47]. At the downstream
 440 region, patches of intense soot are observed with low-intensity soot filaments
 throughout the field. A similar pattern of high-intensity patches is noted in the
 instantaneous PAH field (Fig. 5b). Overall, the soot sheet structure appears
 drastically different from the reaction zone distribution (see Fig. 5a). Since the
 soot precursor (PAH) concentration is highly sensitive to the scalar dissipation
 445 rate, the soot formation is affected mainly by the fuel concentration gradient

rather than the reaction zone topology.

Figure 6c shows the mean soot concentration. Soot forms downstream of the PAH region, which is accompanied by a continuous decrease in the PAH-LIF signal. This can be clearly observed with lower Re flames (mean PAH distribution in Fig. S14, and f_v in Fig. S19). This is consistent with the fact that PAH have been known to contribute to the soot inception and further to soot growth through condensation on soot particles [48]. In Fig. 6c, peak- f_v is observed along the flame axis near the flame-tip region. In the peak- f_v region, the mean PAH signal (Fig. 6b) is low, as most of the PAH have been involved in soot formation. Relative to instantaneous f_v , mean values are significantly lower. Note that the soot is highly intermittent in space and time. Consequently, the mean f_v is affected by the unconditional averaging in a highly intermittent field. Therefore, we subsequently deduce a conditional average that isolates the intermittency effect.

The unconditionally time-averaged peak- f_v in the present turbulent butane flame ($Re = 21500$) measures 0.07 ppm . To enable the comparison with ethylene (which is most studied) fuel, we also performed LII measurements in a lifted ethylene turbulent flame at a comparable jet-exit velocity ($U_j = 31.3 \text{ m/s}$, $Re = 8700$, $h_{lift} = 7.5 \text{ mm}$) relative to the butane flame ($U_j = 27.1 \text{ m/s}$, $h_{lift} = 53 \text{ mm}$). The velocity for ethylene case was slightly higher to ensure a lifted flame. In this ethylene flame, time-averaged peak- f_v is found to be 0.57 ppm . Thus, for a lifted turbulent flame at a given jet velocity, butane appears to produce about 1/8 times the f_v found in ethylene fueled flames, on a time-averaged basis. Note that besides fuel type and velocity, the difference in h_{lift} may influence soot concentration owing to oxidizer leakage in a fuel stream. Therefore, we compare the peak- f_v of the present ethylene flame with that of a lifted DLR ethylene flame ($U_j = 44 \text{ m/s}$, $Re = 10000$, $h_{lift} = 26 \text{ mm}$) [5]. Despite the difference in lift-off heights of DLR and present ethylene flame, peak- f_v is found to be nearly identical, i.e., 0.54 ppm in the DLR flame and 0.57 ppm in the present flame. The extent of upstream partial premixing owing to different h_{lift} does not appear to be prevalent at a peak- f_v region.

A possible reason for this behavior can be found in a LES study by Grader et al. [24]. The authors showed that mainly the soot formation and growth are affected by upstream partial premixing, while in the downstream regions, the soot oxidation is dominated by the non-premixed combustion regime.

3.3. Soot intermittency and conditional mean

To characterize soot intermittency, we deduce the soot presence probability similar to the past works [1–3, 11]. Soot probability is defined as 1 when the f_v is above a certain threshold and 0 otherwise. Recall, the detection limit of the LII signal is around 0.015 ppm. Nevertheless, similar to [3], a threshold of 0.03 ppm is chosen to discard any spurious noise safely. Each instant provides a binary map of the soot presence. A number of such instantaneous maps are averaged, and the resulting mean probability is shown in Fig. 7a for Re 21500 (maps for other Re are available in Sec. S9). Lower probability values in Fig. 7a explains an order of magnitude difference between the time-averaged (Fig. 6c) and instantaneous (Fig. 5c) soot concentrations.

To isolate the intermittency effect on the mean, we deduce a conditional average by considering samples only with the soot presence ($f_v > 0.03$ ppm). At least 200 conditional samples at a given location are ensured for averaging. The conditional mean f_v field is shown in Fig. 7b. Similar data for other Re is available in the Supplement (Sec. S10). In the inception regions, Soot is highly intermittent (low probability). This is likely due to higher scalar dissipation and strain rates near the jet-exit regions. Soot probability increases with height. The scalar dissipation rate in the downstream region is expected to be lower, owing to reduced flow velocity. Additionally, the soot concentration increases with downstream distance owing to the increased residence time. These two factors can increase soot probability in downstream regions.

Since the intermittency is isolated, the conditional mean f_v is higher than the unconditional one. There are two main differences relative to the unconditional mean: 1) The annular soot-containing region extends to a higher HAB than observed in the unconditional mean. 2) The axial/centerline peak- f_v is located

further downstream than that of the unconditional mean. A similar observation has been reported in [18]. Results in Fig. 7 imply that near the flame-tip region, instantaneous f_v is appreciable, but soot is more intermittent owing to
510 oxidation. Soot concentration in the present butane flame is compared with the ethylene flame as before, but on the conditional mean basis. The conditionally averaged peak- f_v in the turbulent butane flame (at $U_j = 27.1\text{m/s}$, $Re = 21500$) is 0.3 ppm , while in ethylene flame (at $U_j = 31.3\text{m/s}$, $Re = 8700$) it is 0.6 ppm . By accounting for soot intermittency, butane fuel produces $1/2$ times f_v found
515 in the ethylene flame. Recall, this factor is $1/8$ if the soot intermittency is unaccounted for.

3.4. Soot-PAH correlation

In the preceding sections, mainly the results of a $Re = 21500$ flame are discussed. For brevity, data for other flames are included in the supplement. This
520 data is used to examine the effect of Re variation on f_v . A peak- f_v parameter is used as a representative value due to its low sensitivity to the lift-off originated partial premixing, as explained subsequently. Recall, from Table 1, Re 2100 and 5000 flames are attached, while at higher Re , the flames are lifted. The conditionally averaged data is considered to avoid intermittency biases. The ex-
525 tracted axial (i.e., along the jet centerline) and global peak- f_v values are plotted in Fig. 8a as a function of Re . A piecewise polynomial is fitted to guide the eye. The global and axial peak- f_v values exhibit an identical trend with Re . The global peak- f_v can occur off-axis, either near the flame-tip or in the annular structure.

530 As Re increases, f_v decreases with a weakly exponential or possibly linear trend in the $Re = 5000 - 21500$ range. This f_v decrease with Re is primarily attributed to the increased scalar dissipation and flow strain rates. The discussion on this aspect is extended subsequently in Sec. 3.5, where the analysis is based on the instantaneous f_v data. In the inception region, besides the flow
535 strain, partial premixing also influences the soot formation. Due to differences in flame lift-off characteristics, the upstream local premixing levels inevitably

vary with Re . Note, the downstream peak- f_v region signifies the transition of soot growth and oxidation zones of the jet flame. As stated earlier (in Sec. 1), based on [24], the soot oxidation region of the flame is likely to be dominated
540 by the non-premixed mode of combustion. Thus, the peak- f_v value is expected to have a weaker sensitivity to upstream partial premixing.

The conditional mean maps are also deduced for PAH-PLIF (available in Sec. S6). The PAH presence threshold is set to 150 counts, while the detection limit is 100 counts. A higher threshold is used to avoid a possible influence
545 of noise. The axial and global peak PAH-LIF intensity values are extracted from the conditional mean. The axial and global peak intensities in Fig. 8b are almost identical, except for the laminar flame ($Re = 2100$). Recall that some of the regions are optically inaccessible. Thus, the actual axial peak may not have been well-captured. This issue of optical inaccessibility is of lesser concern in
550 other flames due to larger flame length and axially uniform PAH-LIF intensity over a considerable distance. Therefore, only the global peak PAH trend is discussed. Note, with the missing field, it is not possible to conclude whether the axial and global peaks could differ in $Re = 2100$ flame.

PAH-LIF intensity variation with Re is shown in Fig. 8b on the linear scale.
555 We also examined Fig. 8b on the log scale (not shown) to facilitate comparison with the DNS results reported in Refs. [47, 49], where the authors examined the sensitivity of naphthalene mass fraction to local scalar dissipation rate (which is expected to increase with Re). Overall, the trend is in qualitative agreement with the DNS results. This apparent consistency implies that the PAH-LIF
560 intensity trend could represent the PAH concentration behavior.

As Re increases, the PAH-LIF intensity drops sharply until $Re = 7200$, as noted from Fig. 8b. In the $Re = 7200 - 21500$ range, the PAH-LIF signal drops asymptotically at a lower rate. Although both the soot and PAH intensity drops with increasing Re , the rate of decrease of soot with PAH is different
565 for laminar and turbulent regimes. This is better visualized in Fig. 8c, where the conditional peak- f_v is plotted against the peak PAH-LIF signal for respective Re . Both the axial and global peak-based data show similar trends. In

the $Re = 2100 - 7200$ range, the rate of change in soot concentration with the PAH signal is constant. In the turbulent regime ($Re = 7200 - 21500$), a strong correlation between soot concentration and PAH intensity is observed. Besides PAH, soot in turbulent flames can be affected by an increased flow strain and reduced residence time. A wide range of flow scales (large characteristic scale to Kolmogorov scale) exists in turbulent flows owing to eddies. Since soot formation timescales are relatively longer ($> ms$) than that of PAH, shorter local residence timescales (due to small-scale eddies and turbulent fluctuations) in a turbulent flow may reduce the soot concentration, possibly by limiting the involvement of PAH to soot formation. To verify this, we estimate a spatial rate of PAH consumption by comparing the conditional mean PAH-LIF intensity at axial peak- f_v (centerline) location with that of a respective peak-PAH intensity along the flame axis. From this analysis, the rate of PAH consumption is noted to reduce with an increase of Re . As Re increases, global residence time decreases owing to a higher velocity. In a turbulent regime, besides global flow timescale, the local residence time may reduce substantially (compared to soot formation/growth timescales) owing to turbulent eddies. Thus, in turbulent flames, in addition to the PAH concentration, the residence time is likely to be a governing parameter. This is a possible explanation for the observed difference in the soot-PAH correlation between laminar and turbulent regimes.

3.5. PDF of soot concentration

The conditional mean revealed the global trends with Re . The local instantaneous f_v is also important. Since the flame length varies with Re , quantities at a fixed axial location are not comparable across different flames. Therefore, we perform the local analysis at an axial location where unconditional mean f_v peaks (denoted as $y-pk$).

The locally maximum f_v , within the radial domain of $r = -44$ to 45 mm and the axial location of $y-pk \pm 5$ mm, is extracted from each instant, without any threshold condition. Such peak- f_v samples over 2000 realizations are used to evaluate the probability density function (PDF). The resulting PDFs are

shown in Fig. 9, along with the respective analysis region (y) in the inset. f_v varies from 0 – 4 *ppm* in non-turbulent flames, and from 0 – 2 *ppm* in the
600 turbulent flame (Fig. 9d). A peak near 0 *ppm* indicates either a negligible soot concentration or the absence of soot due to intermittency.

To examine the effect of Re on soot concentration, the most probable (i.e., mode) f_v is obtained from PDF as indicated by a red circle. Figure 9e shows the variation of mode- f_v with Re , where the error-bar indicate an estimated
605 standard deviation (σ_{Gauss}). σ_{Gauss} is obtained by evaluating full width at half maximum (FWHM) of the PDFs. Next, FWHM is related to σ_{Gauss} by invoking the assumption of Gaussian distribution.

In Fig. 9e, as Re varies from 2100 to 5000, f_v increases, despite the increase in exit strain rate. To examine further, we also evaluate PDFs and mode- f_v at a
610 peak- f_v location occurring along the axis in the conditional mean ($y-pkC$) data. These PDFs and related data extraction procedure are provided in the Supplement (Sec. S11). Figure 9f shows mode- f_v trend with Re at $y-pkC$ location of the respective flame. The increase in f_v from $Re = 2100$ to 5000 is much milder than that of Fig. 9e. Nonetheless, in this Re range with increasing strain rate,
615 f_v does not decrease. Note, the $Re = 2100$ flame is buoyancy dominated, while the other flames are momentum dominated. This difference can influence the mixing process and residence time relative to the soot formation timescales [26]. This may be the reason for different f_v trend between $Re = 2100$ to 5000.

For non-laminar flames ($Re = 5000 - 21500$), f_v drops with Re in both Figs.
620 9e and 9f. As apparent from Fig. 9e, the f_v trend is closer to an exponential fit than a linear fit, though the difference is not significant. To confirm the type of fit function reliably, additional data points are needed. Nonetheless, an exponential trend has been reported with strain rate in laminar one-dimensional flames [50, 51]. The f_v trend in Fig. 9f resembles as of the conditional mean f_v
625 in Fig. 8a. In the $Re = 5000 - 21500$ range, the trend appears to be linear. An identical linear trend of f_v with exit strain rate is reported in ethylene-based turbulent jet flames [14]. Despite this agreement, data points at an additional Re are needed to establish the fit function with certainty.

An early explanation for the decrease in f_v with Re was provided by Kent
 and Bastin [26]. They argued that at a low flow rate (or Re), the soot reaction
 630 kinetics is faster than the air-fuel mixing (or diffusion) rate, and thus the process
 is mixing rate controlled. Conversely, at a high flow rate, the mixing rate exceeds
 the soot formation timescales, and therefore soot chemical kinetics becomes
 the limiting factor. Consequently, the soot concentration decreases with the
 635 increase in strain (or flow) rate. Bisetti et al. [47] provide further insights
 by demonstrating the high sensitivity of naphthalene (soot-precursor) to the
 scalar dissipation rate. Naphthalene concentration was shown to decrease in a
 region with a high dissipation rate. As expected, soot concentration was noted
 [47] to drop sharply with a reduction in naphthalene concentration. The scalar
 640 dissipation rate in the present flames is expected to increase with Re . Therefore,
 with an increase in Re (accompanied by a rise in strain and scalar dissipation
 rates), the soot concentration drops exponentially/linearly in Figs. 9e or 9f.
 Besides the exit strain rate, local mixture fraction also plays a key role since
 the soot concentration is governed by fuel pyrolysis reactions, which in turn is a
 645 function of the mixing field. In a lifted flame, partial premixing could suppress
 the soot formation. However, as discussed earlier, at the peak- f_v location,
 the impact of upstream premixing is expected to be low as interpreted from a
 numerical study [24]. Despite the varying level of upstream premixing (owing
 to different lift-off characteristics) in the present flames, the peak- f_v region is
 650 likely to be dominated by the non-premixed combustion regime. Nevertheless,
 the variation of the local scalar dissipation rate with Re may affect the soot
 locally. Further measurements and analyses are needed to understand the effect
 of partial premixing and scalar dissipation rate on f_v locally.

3.6. Intermittency in OH, PAH, and Soot

655 In Sec. 3.3, soot occurrence in a turbulent butane flame is shown to be
 highly intermittent. This soot intermittency is compared with the intermit-
 tency in soot-precursor (PAH) and reaction zone (OH) as a function of Re . An
 identical approach as of soot probability is used to deduce PAH and OH prob-

ability maps. For OH, the presence threshold is set to 3000 counts, which is
660 higher than the detection limit (1500 counts). This threshold is chosen based on
the intensity gradient of the OH-LIF and background signal. The binarized OH-
layer is assumed to mark the reaction zone region. The binarization threshold
for OH is kept constant across different flames since the instantaneous OH-LIF
signal does not change significantly with Re . In contrast, PAH-LIF signal in-
665 tensity varies widely with Re and also along the flame height. Thus, a dynamic
local threshold approach is used. For a given flame and axial location, the
threshold is defined as the 50% of the radial peak value noted in the conditional
mean data at a respective y location. This choice marks the region of PAH
prominence. In low signal regions (e.g., in $Re = 21500$ flame or near flame-tip),
670 conditional mean based threshold condition may fall below the detection limit
(~ 100 counts). In such a scenario, the minimum threshold of 150 counts is
imposed, which is identical to the value used for evaluating the condition mean
PAH field. The resulting PAH probability maps are provided in Supplement
(Sec. S7), along with further details of the rationale for threshold parameters.
675 Note, threshold choices will alter the probability values, but the spatial distri-
bution is not expected to differ qualitatively. Once the probability is evaluated,
the peak value along the jet axis is used as a representative value. The identical
method is used to extract the characteristic probabilities for OH and soot. This
approach accounts for varying flame lengths across different Re . Additionally,
680 for a given flame, the axial locations of peak probability for OH, PAH, and
Soot are allowed to vary (while r is restricted to flame axis/centerline). Thus,
differences in the respective species distributions (i.e., overall height) owing to
different formation-timescales are accounted for.

Figure 10 shows the variation of mean peak probability of OH, PAH, and
685 soot with Re . For soot, besides a fixed threshold, we also used a dynamic
local threshold with identical parameters (detailed in Sec. S9) as of PAH. As
observed in Fig. 10, no significant differences in soot probability trends are
noted between the dynamic (Soot-D) and fixed (Soot-F) threshold approaches.
This is a consequence of the identical order of magnitude of instantaneous f_v

690 across Re and lower diffusivity soot in space.

The OH presence probability does not change appreciably with Re . This suggests that the effect of turbulence on the reaction zone fluctuation is not significant in the present jet diffusion flames. The soot-precursor shows moderate sensitivity to Re . PAH probability increases in the $Re = 2100 - 5000$ range. 695 There is a possibility that the actual axial/centerline peak of PAH probability for $Re = 2100$ may not have been imaged, as discussed earlier. Recall that the PAH-LIF intensity in the $Re = 2100 - 5000$ range decreases sharply (Fig. 8b). As discussed earlier, $Re = 2100$ flame is buoyancy-dominated, while at higher Re flames are momentum-dominated. This may have an impact on the mixing 700 field and, consequently, on PAH behavior. Coherent PAH structures are noted in instantaneous images at $Re = 5000$ (Fig. S13b) due to flow instability associated with transitional Re . These structures enhance PAH transport towards the flame axis (centerline), and thus leading to a higher probability. With a further increase in Re from 5000 to 21500, the PAH presence probability appears 705 to decrease linearly. The probability approximately drops from 1 to 0.6. The intermittent nature of PAH at higher Re is attributed to fluctuating strain and scalar dissipation rates, which drastically affects PAH formation [47].

The soot presence probability trends follow the identical behavior as of PAH, although with lower probability (i.e., high intermittency). The overall soot probability trend appears quite close to that of the mode- f_v shown in Fig. 9f. In the 710 $Re = 2100 - 5000$ range, soot probability increases slightly. Similar to the PAH explanation, this increase in probability is either due to differences in mixing mechanism (buoyancy vs. momentum) or due to unresolved axial peak. For the $Re = 5000 - 21500$ range, the soot probability decreases similar to PAH 715 probability. However, the rate of decrease is sharper than the PAH probability. The increase in Re is likely accompanied by elevated strain and scalar dissipation rates, which result in a lower concentration of the soot-precursor (Fig. 8b) with a reduced probability that consequently is expected to decrease the soot probability. Relative to PAH, soot probability is consistently lower for several 720 reasons. Besides PAH, the soot formation also depends on two other key param-

eters, namely temperature and residence time. Fluctuations of these quantities in a turbulent flame can increase soot intermittency in both space and time. The chemical timescales of soot formation are longer than that of PAH, which can also contribute to higher intermittency due to lag [52] in response to change
725 in local conditions. Finally, soot is not as diffusive as PAH, and this can lead to lower probability due to high soot intermittency. To summarize, the reaction zone intermittency is least affected by turbulence, while PAH are moderately affected, whereas soot intermittency is greatly influenced.

3.7. Fractal dimension of soot filaments

730 Fractal dimensions can provide a quantitative description of the complexity of the soot sheet/filament field in terms of wrinkling and fragmentation. Such analysis has been applied in the past to investigate turbulent flows [53] and premixed flames [54, 55]. Fractal dimensions are generally reported for aggregated soot particles, for instance, in Ref. [56]. We apply the fractal method
735 for the first time to analyze soot filament fields (as in Fig. 5c) in turbulent non-premixed flames.

An overview of the fractal theory and background can be found in [53, 54]. LII data provides a planar slice of the three-dimensional soot structure. Thus, the fractal dimension of only a 2D field (D_2) is accessible. Nevertheless, the
740 characteristic fractal dimension of a surface (D_f) is approximated as $D_2 + 1$, following [53]. To calculate D_2 , a box-counting method [53] is used. The method involves overlaying the image with a grid of a given size (ϵ) and counting the number of boxes (N_b) needed to cover a given pattern entirely. The procedure is reiterated with a grid of successively larger box sizes (in a step of 2^n). The
745 slope, derived from the log-log plot of N_b vs. magnification ($1/\epsilon$), provides the fractal dimension.

Before applying the fractal analysis, it is necessary to identify the soot filaments. This is not a trivial task due to the complexity of soot sheets in turbulent flames. A local adaptive threshold approach is employed to binarize the soot
750 sheets. The details of image processing are available in Supplement (Sec. S12.1).

Once the soot sheets are identified, there are several analysis approaches. D_f could either be obtained for soot filament silhouette (blobs), borderline/outline, or skeleton [57]. We found that these three choices only weakly affect the D_f trends; however, the absolute values differ. Silhouette- and outline-based D_f values are sensitive to threshold choices, whereas skeleton-based D_f would be least sensitive. Thus, we use the skeleton of the soot sheets to evaluate the characteristic D_f . Note, D_f can be calculated either for an isolated soot filament or for an imaged sub-field containing several filaments. The former approach can provide the extent of filament roughness (i.e., wrinkling), while the latter will give the combined estimate of both the roughness and fragmentation. Since the soot sheets are not two-dimensional, D_f evaluated from isolated soot filaments could be biased. Therefore, we calculate D_f for the imaged soot sub-field to obtain both - the extent of wrinkling and fragmentation, similar to [53, 54, 58].

For reference, media files containing 20 sample frames of instantaneous f_v sub-fields (at different axial stations) are provided in the Supplementary Material for all the flames. Instantaneous D_f is calculated only for images in which soot is present (i.e., $f_v > 0.03 \text{ ppm}$). D_f values obtained over several frames are used to calculate the mean and standard deviation. The variation of mean D_f along the flame height is shown in Fig. 11 for different Re . The axial domain of D_f evaluation sub-field is marked by the horizontal bar, whereas the vertical bar indicates the standard deviation of D_f . The radial domain is kept constant ($r = -44$ to 45 mm) for all the cases. In principle, D_f is expected to be greater than 2. Lower D_f in Fig. 11 is due to the use of the skeleton of soot filaments. Additionally, the largest object-bounding box size (ϵ is varied in a step of power of 2) cannot be of the same size as of the object-bounded image size, which results in so-called over-empty boxes [59]. Nonetheless, in the peak- f_v region, D_f is appreciable greater than 2.

For a given Re , in the soot inception region D_f remains low. The peak- D_f region nearly coincides with the sub-field where unconditional mean peak- f_v is observed. D_f decreases in the downstream oxidation region. These observations indicate that the soot sheet wrinkling and fragmentation are highest between

soot growth and oxidation regions. In the soot inception regions, D_f unexpectedly appears to decrease with Re . Note, in the laminar flame, the soot sheet occupies a larger area (evident in a Media file), and thus, resulting in higher D_f . As Re increases, both - the soot concentration and filament size reduces, which leads to lower D_f .

Next, the fluctuation of soot field complexity in time is discussed by using the standard deviation of D_f (marked in Fig. 11). For reference, the mean flame length (from Table 1) is also indicated in Fig. 11, except for $Re = 21500$ case where flame-tip region was not imaged. The region between peak- D_f (that coincides with the mean peak- f_v region) and mean flame-tip is assumed to be the soot oxidation region. This assumption is made since the net reduction in f_v is attributed to the dominance of soot oxidation over soot growth. D_f fluctuates widely in the oxidation region, even in a laminar flame, likely due to the buoyancy effect. Additionally, significant values of D_f are noted, even beyond the mean flame-tip. Since simultaneous OH/LII data is unavailable, it remains unknown whether the soot structures in these regions have been partially oxidized (or leaked) through the reaction zone. The peak- f_v regions exhibit highest mean D_f values. These peak- D_f regions generally exhibit low temporal fluctuations of soot structure complexity, as noted from a relatively low standard deviation in Fig. 11.

To examine the global relationship between D_f and Re , peak- D_f parameter is used. Figure 12 shows the peak- D_f variation with Re . As indicated earlier, regions of mean peak- D_f and peak- f_v nearly coincide. Thus, peak- D_f and D_f evaluated in peak- f_v regions are almost identical. In the $Re = 2100 - 7200$ range, D_f grows sharply, which reflects an increased complexity of soot fields. In the turbulent region ($Re = 7200 - 21500$), D_f remains nearly constant. This indicates that in a high Re range though the soot concentration reduces with Re , overall soot sheet structure complexity remains largely unaffected. Such saturation of D_f with turbulence has also been reported for premixed flame-fronts [54, 58]. For a laminar premixed flame surface, a typical value of mean D_f is 2.1, while it increases to ~ 2.35 for turbulent ($u'/S_L = 20$) flames [54, 58].

This D_f range is higher than the present values (2.12 to 2.24) evaluated for soot-skeleton structures. Since in Refs. [54, 58], outline criteria is used we also
815 compare soot-outline based peak- D_f in our turbulent flame ($Re = 21500$), which measures 2.38, close to the D_f obtained for a turbulent premixed flame surface [54, 58]. Note that as observed in Sec. 3.2, the non-premixed flame surface (marked by OH) is only weakly convoluted relative to the soot filament structures. Overall, the fractal approach appears to be very promising to quantify
820 the soot structure topology in turbulent flames. Note, due to D_f sensitivity to evaluation methods, for quantitative comparison of D_f across different studies, a D_f deduction procedure should be specified in detail.

3.8. Soot sheet thickness

Soot sheet shape analysis is further extended by deducing the local thick-
825 ness of soot sheets (λ_S). The soot sheet scales may influence total soot yield. Additionally, soot oxidation efficacy may depend on λ_S . Thus, the knowledge of soot sheet thickness (as a function of Re) could provide insights into the effect of turbulence on soot formation and oxidation. Such length scale analysis has been reported by a few studies [1, 16, 60, 61]. Motivated by the above reasons,
830 λ_S analysis is pursued. However, identification of soot sheet boundary in turbulent flames is challenging owing to highly irregular shapes, merging of soot sheets, and branching of soot filaments. Such difficulties are well recognized in Refs. [16, 61]. Our data processing approach relies on the sequential protocol of image smoothing and binarization through the adaptive local threshold.
835 The binarization method is identical to the one implemented for fractal analysis (detailed in Sec. S12.1). The procedure to determine sheet thickness is described in Sec. S12.2. λ_S is obtained by deducing the soot filament centerline and boundary. A distance transform [62] is applied to the binarized f_v field to obtain the distance between a given pixel and the soot sheet boundary. Next,
840 the soot filament centerline is located by the skeletonization of the binarized image. Subsequently, the thickness is calculated as twice the distance between the soot filament centerline and boundary. This simplified approach provides

local thickness, λ_S , with reasonable robustness. Due to sensitivity to threshold and limitation of planar LII, the deduced λ_S is only a relative estimate of the true thickness. To obtain true λ_S , three-dimensionality needs to be accounted for either through tomographic or dual-plane imaging. Nonetheless, the present projected λ_S provides a useful estimate of the true thickness. Although the soot sheets in all the flames were analyzed, results for the laminar flame ($Re = 2100$) are not included since unusually large values of thickness and unclear trends owing to buoyancy-induced sheet merging (that results in soot clouds).

The local f_v is also extracted at the soot filament centerline (on the skeleton) to investigate the correlation between f_v and λ_S . The relation between area-averaged f_v and λ_S is examined. The available sub-fields are divided axially into 15 – 20 mm high regions. The radial domain is maintained at $r = -44$ to 45 mm. Instantaneous local λ_S and f_v values are averaged - first, within a given 15 – 20 mm high region (i.e., spatially) and then temporally over several frames (1000 – 2000). The deduced average values of f_v and λ_S are plotted in Fig. 13 for different Re . These trends appear to follow the power fit, as also demonstrated by Mahmoud et al. [16]. The authors compared the correlation between sheet thickness and f_v ; both averaged over a given soot sheet region. A global power fit function between sheet thickness and f_v was found, independent of Re [16]. However, the present observation in Fig. 13 indicates that the trend is global (power fit), but fit coefficients indeed depend on Re . Note, in [16], quantities (f_v and λ_S) are averaged over a single soot sheet rather than in a certain spatial region. It is unclear to what extent this difference in analysis protocol could affect the results and derived conclusions.

Note, the above semi-global analysis does not preserve local correlation. Therefore, we also analyze local correlations between f_v and λ_S by retaining pixel-to-pixel correspondence. Figure 14a shows the mean f_v conditioned on λ_S . To obtain this plot, the local f_v and λ_S pairs along the flame length are combined. Consequently, deduced analysis combinedly represents the behavior of soot inception, growth, and oxidation regions. Next, f_v within a given λ_S bins are averaged. In this manner, local correspondence between f_v and λ_S is

preserved, despite performing the bin-averaging. The trends in Fig. 14a are
875 drastically different from the semi-global analysis presented in Fig. 13. In Fig.
14a, for lower λ_S , f_v increases with sheet thickness, similar to the semi-global
trend noted in Fig. 13. However, $f_v|\lambda_S$ reaches a peak value at a certain sheet
thickness. The $f_v|\lambda_S$ curve is not symmetric about the peak. The statistical
analysis and peak $f_v|\lambda_S$ behavior is reported for the first time. Thus, a dedicated
880 study is needed to explain the reasons for the occurrence of peak- f_v at a preferred
soot sheet thickness.

To examine the effect of Re on $f_v|\lambda_S$, a peak (or mode) value is extracted
from Fig. 14a. To detect the peak, data points are fitted with exponential
pulses. Figure 14b shows the variation of mode- $f_v|\lambda_S$ with Re . f_v decreases
885 with Re in an identical manner as of other representations in Figs. 8a and 9f.
Thus, our characteristic choice of mode- $f_v|\lambda_S$ is representative of the physical
phenomena. Soot sheet thickness at which $f_v|\lambda_S$ peaks (denoted by $\lambda_{S,m}$) is
also plotted in Fig. 14b. Though trend appears to be linear with Re , there is
uncertainty due to limited data points, imaging resolution, and the choice of
890 the characteristic parameter ($\lambda_{S,m}$).

In turbulent flames, the effect of Re on λ_S is not straightforward. In lami-
nar one-dimensional flames, soot sheet thickness was observed to decrease with
strain rate [51]. A similar observation can be noted from Lee et al. [1] in the
soot inception regions of the turbulent jet flames where λ_S decreased with Re .
895 However, in the soot growth and oxidation regions, λ_S appears to increase with
 Re (interpreted from data in [1]). In the present analysis, since the f_v - λ_S pairs
along the entire flame height are combined, the soot inception, growth, and
oxidation regions are not considered independently. The characteristic sheet
thickness, $\lambda_{S,m}$ in Fig. 14b is observed to increase with Re , similar to the
900 data in [1] for soot growth and oxidation regions. Further analysis is needed to
gain a deeper understanding of the effect of Re on soot sheet thickness. The
present analysis is a preliminary step towards understanding f_v - λ_S relationship
in turbulent flames.

4. Conclusions

905 Soot formation is investigated in four non-premixed n -butane flames through laser-based measurements. Reynolds number (Re) was varied from 2100 to 21500, which covers laminar and turbulent regimes. Measured data include soot concentration (f_v), soot-precursor (PAH), reaction zone (OH), and boundary conditions. The effect of Re on soot and other quantities is examined. Spatial
910 and intensity correlations between soot and PAH are analyzed. Intermittency in soot, PAH, and OH structures is also investigated. Finally, soot filament topology is studied using fractal dimension and soot-sheet thickness. The key findings of this work are summarized below.

In a soot inception region, species exist in the following radial order: fuel,
915 smaller PAH, relatively larger PAH, soot, and OH. OH intensity does not change appreciably with Re and flame height, which suggests that the heat release rate is less affected by turbulence. In the turbulent flame (Re 21500), the thickness of the OH zone at the flame base is appreciably larger than low Re flames. This increase in OH-zone is likely associated with the edge flame which can form in
920 lifted jet flames owing to partial premixing.

Soot and PAH concentrations decrease with Re . In a momentum-dominated range of Re (5000 – 21500), both mean and most-probable f_v values decrease in a near-exponential manner. A decrease in f_v with Re is mainly due to reduced (global and local) residence time and possibly due to increased scalar
925 dissipation rate that in turn reduces PAH formation. In the $Re = 2100 - 7200$ range, the rate of decrease in soot concentration with PAH is nearly constant. In a turbulent regime ($Re = 7200 - 21500$), the soot decrease rate with PAH is sharper, possibly due to reduced local residence time owing to turbulent eddies. PAH appears to diffuse in space, whereas soot fields are highly localized due to
930 lower soot particle diffusivity. Soot layers are more convoluted than OH and PAH structures. Soot structures are highly intermittent. Soot intermittency is greatly influenced by Re , whereas PAH intermittency is mildly influenced while OH intermittency is the least affected by turbulence.

The fractal analysis requires careful image processing to identify soot sheets.

935 Soot-sheet skeleton-based characteristic fractal dimension (D_f) is used to quantify soot field complexity (in terms of wrinkling and fragmentation). Soot field complexity is lowest in the soot inception and oxidation regions, whereas it measures maximum at the soot growth/oxidation interface. D_f increases with Re until $Re = 7200$. Soot field complexity remains insensitive to Re in a turbulent

940 regime ($Re = 7200 - 21500$). The fractal approach is indeed a useful tool to analyze soot structure topology.

Finally, the soot-sheet thickness is obtained by developing a robust image processing approach. Correlation between sheet thickness and f_v is examined in semi-global and local manners. From a semi-global correlation, f_v is observed

945 to increase with thickness monotonically in a power-law manner. Coefficients of power-fit are found to be dependent on Re . The local correlation of f_v vs. sheet thickness indicated non-monotonic behavior, which to our knowledge, is reported for the first time. A dedicated study is needed to explore physical reasons for the non-monotonic trend.

950 Overall, this work examined various aspects of sooting jet flames through detailed analysis. Original contributions of this work are soot-PAH correlation, fractal analysis, and soot concentration/sheet thickness relationship. Additionally, soot measurements in a turbulent n -butane flame are performed for the first time. Physical insights and database derived from the present and companion

955 paper (Part 2) [32] can aid in the validation of turbulence and soot chemistry models focused on practical fuels.

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Table 1: Flame conditions. Air flow rate is kept constant at 5 (g/s).

<i>Sr.</i> <i>No.</i>	<i>Re</i> ($-$)	h_{lift} (mm)	σ_h (mm)	L_f (mm)	W_f (mm)	$\dot{m}_f$ (g/s)	U_j (m/s)	U_j/d (1/s)
1	2100	-	-	405	17	0.03	2.7	1125
2	5000	-	-	470	23	0.07	6.3	2625
3	7200	11	0.6	545	27	0.10	9.0	3750
4	21500	53	3.3	675	48	0.30	27.1	11300

Figure 1: Burner geometry (dimensions are in *mm*). Optically accessible regions are shaded and the corresponding dimensions are marked on the right.

Figure 2: Flame photographs at different exposures, $1/20$ s (left), $1/500$ s (middle), and $1/8000$ s (right): (a) Re 2100, (b) Re 5000, (c) Re 7200, and (d) Re 21500.

Figure 3: Wall temperature measured at different Re as marked in the legend.

Figure 4: Mean fields at Re 2100: (a) OH-PLIF, (b) PAH-PLIF, (c) Soot volume fraction. White curve represents an OH iso-contour.

Figure 5: Instantaneous fields of: (a) OH-PLIF, (b) PAH-PLIF, and (c) Soot concentration, at Re 21500.

Figure 6: Mean fields of: (a) OH-PLIF, (b) PAH-PLIF, and (c) Soot concentration, at Re 21500.

Figure 7: (a) Soot probability, (b) Conditionally averaged f_v , at Re 21500.

Figure 8: Axial and global peaks in: a) conditional mean f_v , b) conditional mean PAH, c) conditional peak- f_v and PAH as a function of Re .

Figure 9: PDF of local peak- f_v in the axial region where the unconditionally averaged centerline f_v peaks ($y\text{-pk}$): (a) Re 2100, (b) Re 5000, (c) Re 7200, and (d) Re 21500, (e) mode- f_v , and (f) mode- f_v in the axial region where the conditionally averaged centerline f_v peaks ($y\text{-pk}C$), corresponding PDFs are available in Fig. S23.

Figure 10: Peak probability of soot, OH, PAH with Re . The letter "F" and "D" signify evaluation with fixed and dynamic thresholds, respectively.

Figure 11: Evolution of mean characteristic fractal dimension along the flame length. Vertical bars indicate standard deviation as $\pm\sigma$, while horizontal bars mark the y range over which D_f is evaluated. The vertical dotted line marks the mean flame length.

Figure 12: Variation of peak characteristic fractal dimension with Re . Error bars indicate standard deviation as $\pm\sigma$.

Figure 13: Area- and time-averaged f_v variation with soot sheet thickness.

Figure 14: Soot concentration and sheet thickness correlation: a) f_v conditioned on sheet thickness, b) mode- f_v conditioned on λ_S and corresponding λ_S .

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