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Suppression of Parasitic Nonlinear Processes in Spontaneous Four-Wave Mixing

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We report an enhancement of over 10^4 in the signal-to-noise ratio characterizing the generation of identical photon pairs in a ring resonator system. Parasitic noise, associated with single pump spontaneous four-wave mixing, is essentially eliminated by employing a novel system design involving two resonators that are linearly uncoupled but nonlinearly coupled. This opens the way to a new class of integrated devices exploiting the unique properties of identical photon pairs in the same optical mode.

Nonlinear optics has been widely exploited to produce nonclassical states of the electromagnetic field. There has been a recent focus on the use of CMOS compatible materials, such as silicon and silicon nitride, which are characterized by a strong third-order optical response that can be further enhanced by the light confinement attainable in integrated microresonators [1]. With the fabrication quality and technological maturity achieved in the last decade, integrated devices based on these materials offer the promise of efficient generation of entangled photons [2–6], heralded single-photons [7, 8] and squeezed light [9, 10].

A key third-order nonlinear process is dual-pump spontaneous four-wave mixing (d-SFWM), in which pump lasers at ω_1 and ω_2 are used to generate photons at $\omega_T = (\omega_1 + \omega_2)/2$. This process can be used to generate single-mode squeezed light, a central resource in the development of continuous-variable quantum computing [11]. While conventional micrometric ring resonators have been used to enhance d-SFWM [12], their multimode nature inevitably also leads to the amplification of unwanted nonlinear phenomena, such as single-pump spontaneous four-wave mixing (s-SFWM). This is a problem: as shown in Fig. 1(a), if the two pumps are resonant with the microring, the generation of photon pairs within a target resonance (ω_T) through d-SFWM occurs along with two s-SFWM processes. Both of these parasitic s-SFWM processes lead to the generation of two photons, with one, and only one, of them in the mode at ω_T . This acts as a source of noise, leading to a degradation of the squeezed light [10].

To quantitatively characterize these nonlinear parasitic processes, in Fig. 1(b) we plot the photon generation rates (measured as described in the Supplemental Material) due to the d-SFWM and s-SFWM processes in an integrated silicon microring resonator (length 372 μm and quality factor around $6 \cdot 10^4$). As expected, the generation rate for the d-SFWM is unchanged as long as the product of the two pump powers is held fixed, while the generation rate of the s-SFWM processes scale quadratically with the appropriate pump powers [13]. The generation rates of the parasitic processes, given by the sum of the two s-SFWM rates, can even be one order of magnitude larger than the generation rate of the d-SFWM process, with a maximum signal-to-noise ratio (SNR) of only about 2 when the two pump powers are equal.

Strategies have been proposed to overcome this intrinsic limit. In one approach, the two pump lasers are slightly detuned from resonance, such that the s-SFWM rates are suppressed [10], but with a trade-off between SNR and generation rate. Alternatively, one can use systems composed of two or more linearly coupled resonators to engineer the spectral position of the resonant modes, with nonlinear phenomena selectively enhanced or suppressed [9, 14, 15]. While this can be very effective, the suppression of the parasitic processes is limited by the achievable resonant splitting of the coupled modes.

In 2019, Menotti *et al.* proposed a new strategy [16], in which two optical resonators are coupled solely through the nonlinear interaction. The system is characterized by two independent sets of resonances that can be tuned to selectively enhance or suppress different nonlinear phenomena. In Fig. 2(b) we represent a sketch of the realisation of d-SFWM in such a system. Two laser pumps are tuned to resonances of the first resonator, leading to the generation of photon-pairs within a target resonance of the second resonator. Yet s-SFWMs are expected to be suppressed, for the overall field enhancement

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FIG. 1. (a) Sketch of the s-SFWM and d-SFWM processes occurring in a single microring resonator when two laser pumps P_1 and P_2 are aligned to two resonances (ω_1 and ω_2). All the processes are resonant and exploit a significant intensity enhancement (I.E.). (b) Measurement of the pair generation rate in a single silicon microring resonator when the product of the powers of the two pumps is fixed. The blue triangles and the red circles show the s-SFWM processes pumped by the lasers at ω_1 and ω_2 , respectively. The black squares show the sum of the parasitic process rates, and the green stars show the d-SFWM generation rate. The measures are compared with the theoretical calculation (shown with the dotted blue line for the P_1 -pumped s-SFWM, the dashed red line for the P_2 -pumped s-SFWM, and the green line for d-SFWM.) See Supplemental Material for the experimental details, and Menotti *et al.* [16] for the theoretical calculations.

at $\omega_S = 2\omega_2 - \omega_T$ and $\omega_I = 2\omega_1 - \omega_T$ is strongly reduced by the absence of three resonances satisfying energy conservation. In this letter we experimentally demonstrate this scheme.

The device is presented in Fig.2(a): two silicon-on-insulator (SOI) racetrack resonators (waveguide cross-section $600 \times 220 \text{ nm}^2$) with different lengths $L_1 = 372 \text{ }\mu\text{m}$ and $L_2 = 366 \text{ }\mu\text{m}$, are located side-by-side forming a directional coupler (DC) of length $L_{DC} = 92 \text{ }\mu\text{m}$, chosen to minimise cross-transmission and achieve isolation of the two resonators. Thus one set of modes is associated with Resonator 1 (R_1), and another with Resonator 2 (R_2). During the fabrication process, a H_2 thermal annealing was used to smooth the sidewalls of silicon waveguides

[17]: this leads to the reduction of the propagation losses and, thus, to the realisation of resonators with high quality factors [18]. The optical characterization is shown in Fig. 2(c). The resulting two independent sets of resonances are clearly observed by injecting light from a tunable laser in the ports T_1 or T_2 and detecting the optical response at the ports T_6 and T_3 , respectively. The free spectral range (FSR) at 1550 nm is around 1.566 nm and 1.595 nm for R_1 and R_2 respectively. The loaded quality factors are around $6 \cdot 10^4$ and $3 \cdot 10^5$, with the difference due to the different number of waveguides coupled to the racetracks (two to R_1 , and one to R_2). The optical isolation is at least 20 dB over a 40-nm bandwidth, as observed from the transmission spectrum $T_1 \rightarrow T_3$.

FIG. 2. (a) Optical image of the device with two linearly uncoupled racetracks. A second image of the device without the electrical circuits has been superimposed to show the position of waveguides, which are covered by the metal. (b) Sketch of the s-SFWM and d-SFWM processes occurring in the device when two laser pumps are aligned to two resonances (ω_1 and ω_2). Single-pump processes which generate photons at ω_T are suppressed due to the weak field enhancement experienced at the spectral position where energy conservation is preserved. (c) Linear characterization of the device.

FIG. 3. Experimental set-up used to measure the coincidence rates. Pump light from two lasers, combined into the same fiber through a beam splitter BS_1 , is coupled to resonator R_1 , the resonances of which are tuned by changing the voltage applied to the heater. Photons generated through d-SFMW and s-SFWM are collected with a tapered fiber, and sorted by frequency using tunable fiber Bragg filters (TFB_1 - TFB_3) and circulators (C_1 - C_3). They are then detected using four superconductive single photon detectors (D_1 - D_4). The correlations between the detection times are recorded and analysed through time tagging electronics. The spectral alignment of the lasers with the device is checked with two power meters (PM_1 and PM_2), with an additional fiber Bragg filter (TFB_4) and circulator (C_4) used to separate the two beams. Bandpass filters BPF_1 and BPF_2 are used to eliminate amplified spontaneous emission from the output of the pump lasers, and BPF_3 - BPF_5 to filter out residual pump photons.

The two sets of resonances can be controlled independently by means of two electric heaters fabricated with a TiN layer on top of the silica cladding, and the electrical contact is realised with AlCu electric wires deposited on top of the chip.

Measurements of the nonlinear processes are realised with the experimental set-up presented in Fig.3. The light from two tunable lasers (Santec TSL710 and TSL510) is coupled using a collimator and lens to match the mode field diameter of the edge coupling tip on the chip, after two band-pass filters BPF_1 and BPF_2 (FWHM around 8 nm) have been used to filter out the amplified spontaneous emission from the lasers. The spectral position of the resonances of R_1 is controlled by using an external voltage source (Keithley 2400 Source Meter) and a multi-contact wedge. The generated photon pairs are collected by a tapered fiber coupled to the port T_3 of the device, and the fiber is connected to the circulator C_1 . A tunable fiber Bragg filter (TFB_1) is used in reflection [65 pm 3dB-bandwidth (BW) and 40 dB of extinction ratio (ER)] to route photons at frequencies around ω_T towards the detection system. Another band-pass filter (BPF_3) with more than 60 dB of ER filters out any residuals from the pump, and a fiber 50:50 beam splitter splits the photon flux towards the superconductive single-photon detectors D_1 and D_2 supplied by Photon Spot.

Photons at ω_T can be generated through s-SFWM only if another photon is generated to guarantee the conservation of energy. In particular, s-SFWM pumped by the laser at ω_1 (P_1 -SFMW) can generate a photon pair with one photon at ω_T and one at ω_I , such that $\omega_I = 2\omega_1 - \omega_T$. Similarly, s-SFWM associated with the laser at ω_2 (P_2 -SFMW) can generate one photon at ω_T and one photon at ω_S , where $\omega_S = 2\omega_2 - \omega_T$. To detect these photons, we use two tunable fiber Bragg filters (TFB_2 and TFB_3) and two band-pass filters (BPF_4 and BPF_5) to route photons at ω_I and ω_S towards superconductive single-photon detectors D_3 and D_4 , respectively. Finally, the alignment of the two laser pumps is checked during the whole experiment using two power meters (PM_1 and PM_2), a circulator (C_4), and an additional band-pass filter (TFB_4).

The total insertion losses from the lasers to the waveguide coupled with R_1 at the port T_1 are around -7.8 ± 0.1 dB for the light from both P_1 and P_2 . The losses from the waveguide coupled with R_1 at the port T_3 to D_1 and D_2 are around -10.7 ± 0.3 dB and -10.1 ± 0.3 dB, respectively, for the photons at ω_T ; the losses from T_3 to D_3 are -11.9 ± 0.3 dB for photons at ω_I , and -7.6 ± 0.3 dB from T_3 to D_4 for photons at ω_S . The efficiency of the detectors is -1.00 ± 0.05 dB.

We begin by verifying the capability of our structure to suppress s-SFWM. To do that, we measure the vari-

ation of the efficiency of an s-SFWM process by tuning the two sets of resonances, which leads to a modification of the nonlinear coupling of the modes. We start by adjusting the voltage applied to the heater of R_1 so that the frequency ω_2 of a resonance (vacuum wavelength $\lambda_2 = 1560.916$ nm) is in the middle of the frequencies of two resonances of R_2 (at vacuum wavelengths $\lambda_T = 1550.495$ nm and $\lambda_U = 1571.479$ nm). This configuration should guarantee a maximum efficiency of P₂-SFWM, since $\omega_U = \omega_S = 2\omega_2 - \omega_T$. Then, with laser P₁ turned off, we change the driving voltage of the heater of R_1 to shift its resonances, and we tune P₂ at each step to be on resonance with R_1 at each λ_2 by checking the transmission on the power meter PM₂. The tunable fiber Bragg filter TFB₁ is aligned to the resonance at ω_T at the beginning of the experiment, since thermal cross-talk leads to a tuning of the resonances of R_2 within the bandwidth of the filter. On the other hand, the filter TFB₂ is tuned to collect the photons generated at $\omega_S = 2\omega_2 - \omega_T$, which requires the adjustment of its spectral alignment during the whole experiment. In Fig.4 we show the attenuation of the single-pump SFWM process with respect to the detuning of the resonances involved, which is estimated from the driving voltage and the characterization of the heater (see Supplemental Material for details). In particular, that detuning is defined as $\Delta\omega_2 - (\Delta\omega_T - \Delta\omega_U)/2$. We find that the simulation and the data are in good agreement, and exhibit the expected behaviour.

FIG. 4. Plot showing the attenuation of s-SFWM as a function of the detuning of the resonances of the two resonators.

This result shows that by tuning the two sets of resonances one can manipulate the nonlinear coupling of the modes of the resonators, and, consequently, the generation of pairs due to the nonlinear processes occurring in the device. In particular, a detuning of around 65 pm (8.1 GHz, around 13 times the linewidth of the resonances of R_2) leads to a suppression of around three orders of magnitude with respect to perfect nonlinear coupling.

With the possibility of attenuating the parasitic processes demonstrated, we proceed to the dual-pump SFWM experiment. The laser pumps are aligned to two resonances of R_1 (vacuum wavelengths $\lambda_1 = 1540.374$ nm and $\lambda_2 = 1560.742$ nm), which are equally spaced in frequency about a resonance of R_2 at $\lambda_T = 1550.491$ nm. This configuration is associated with a detuning of the s-SFWM resonances of around -160 pm (-20 GHz), and the estimation of the resulting attenuation of the s-SFWM processes is around -37.3 dB. The quality factors of the resonances of R_1 are around $Q_1 = 6.7 \cdot 10^4$ and $Q_2 = 5.7 \cdot 10^4$, while the resonance of R_2 at λ_T has a much higher quality factor, $Q_T = 3.2 \cdot 10^5$. We align the tunable filter TFB₁ to λ_T , while TFB₂ and TFB₃ are tuned to route photons at $\lambda_I = 1530.388$ nm and $\lambda_S = 1571.129$ nm to D₃ and D₄, respectively. The analysis of the coincidences on the detectors allows for the recognition of the pairs generated through the different processes. In particular, the d-SFWM should give coincidence between the detection events at D₁ and D₂. Similarly, the single-pump processes should result in coincident detection: P₁-SFWM between the events at D₃ and D₁ (or D₃ and D₂), and P₂-SFWM between the events at D₄ and D₁ (or D₄ and D₂).

As discussed earlier [16], the efficiency of the d-SFWM process in our device is reduced from what could be achieved with a simple microring, since here the nonlinear interaction occurs only in the directional coupler region shared by the two rings. This decreases both the overlap integral of the fields ($1/4$) and the interaction length ($L_{DC} \approx \mathcal{L}/4$). This would be a limitation in the framework of squeezed-light sources, where high generation efficiency is required, but it could be overcome by working with ultra low-loss waveguides with high modal confinement in silicon nitride [19, 20]. In such a device one could also increase the pump power, since the two-photon absorption that affects silicon waveguides would not be present [21].

In Fig.5 we show the result of a coincidence experiment with the current device, where 0.95 ± 0.05 mW of optical power is coupled into the waveguide from each pump laser. The data are acquired for 20 minutes, and the histograms have a bin-width equal to 35 ps, which is comparable with the time jitter of the detectors. The red peak shows that photons arriving on D₁ and D₂ are emitted at the same time, since their arrival time is correlated: this clearly demonstrates they are emitted through d-SFWM, since any other process that can generate photons at λ_T cannot be characterized by this temporal correlation. We measure a coincidence rate equal to 164.2 ± 0.4 Hz, which

corresponds to an internal generation rate in the second resonator equal to 62 ± 6 kHz, and the CAR is 1190 ± 10 . The coincidence rate is estimated by integrating the peak within the whole window (and subtracting the noise), while the CAR is measured by taking into account the FWHM of the peak (16 bins of the histogram).

From the histograms in Fig.5 it is also possible to evaluate the photon pairs generated through s-SFWM, which lead to coincidence events between D_1 and D_2 with D_3 or D_4 . As can be seen, no peaks are clearly visible. In fact, the dark counts, the noise from the environment, and other parasitic processes occurring in the set-up (such as Raman emission from optical fibers) hide the signal given by time-correlated photons. This is due to the severe attenuation of the processes. Nevertheless, we can estimate a lower bound for the SNR by analysing the coincidences between D_1 and D_4 . We integrate the peak due to d-SFWM over its FWHM (16 bins), and we divide it by the noise, which is calculated as the average on the black histogram in Fig.5 multiplied by 16 bins. By taking into account the losses, we obtain a SNR equal to $(11.3 \pm 3.2) \cdot 10^3$. From the model, we should expect that the SNR is around $21 \cdot 10^3$, an improvement over that of a single ring system by over four orders of magnitude. Our experimental estimation is lower, since we are overestimating the noise due to s-SFWM.

These results demonstrate that the use of linearly un-

FIG. 5. Histograms representing the coincidences events detected. The red, black, and blue histograms represent, respectively, the coincidences due to d-SFWM (events on D_1 and D_2), P₂-SFWM (events on D_1 and D_4), and P₁-SFWM (events on D_1 and D_3). The width of each bin is 35 ps. The delay is calculated by taking into account the different optical lengths of the fibers from the device to the detectors.

coupled resonators allows for the effective control of the nonlinear interaction between optical modes, leading to the ability to enhance or suppress the generation of photon pairs through spontaneous four wave mixing. This kind of device will be a central component in strategies for the implementation of continuous-variable quantum computing. It will enable the possibility of realising sources of highly squeezed light, since the main sources of noise, due to single-pump spontaneous four wave mixing, can be effectively suppressed. In our experiment, we could confirm the improvement of the signal-to-noise ratio by over four orders of magnitude.

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