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► To cite this version:

David Labat, A. Mangin. TRANSFER FUNCTION APPROACH FOR ARTIFICIAL TRACER TEST INTERPRETATION IN KARSTIC SYSTEMS. *Journal of Hydrology*, 2015, 529 (3), pp.866-871. 10.1016/j.jhydrol.2015.09.011 . hal-03239237

HAL Id: hal-03239237

<https://hal.science/hal-03239237>

Submitted on 27 May 2021

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**TRANSFER FUNCTION APPROACH FOR ARTIFICIAL TRACER TEST
INTERPRETATION IN KARSTIC SYSTEMS**

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Revised form for Journal of Hydrology

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Abstract

A karstic formation consists in a three-dimensional hydrological system which involves horizontal and vertical, diphasic or saturated water transfers characterised by a large range of velocity. These subsurface flow processes correspond to various water pathways through fractured, fissured, and underground streams or conduits leading to a nonlinear global behaviour of the system.

An efficient way of investigating of a karstic system behaviour consists in the injection of artificial tracer tests at loss points and in careful analysis of the recovery tracer fluxes at one or several outlets of the systems. These injections are also an efficient way of providing hypotheses on characteristic time of contaminant transfer in these type of aquifers.

Here, we propose a Laplace-transform transfer function of the Residence Time Distribution function that allows to discriminate between a quick-flow advection-dominated component and a slow-flow advection-dispersion/ dominated component in the artificial tracer transfer in the system. We apply this transfer function on five high resolution sampling rate artificial tracer tests operated on the Baget system in the Pyrenees (France) in order to illustrate the advantages and limitations of this approach. We provide then an interpretation of the relationship between tracer test recovery shape and karstic system organisation between inlet and outlet site.

Keywords: artificial tracer tests, karstic system, transfer function,

Karstic systems as original hydrogeological formations

Karstic systems are calcareous formations (carbonate rocks) characterised by a fissured and cavernous geomorphology, with significant heterogeneities in water velocities present at different observation scales. Mainly under the action of acidified water infiltration, limestone is submitted to a dissolution process corresponding to a three-phase reaction involving water, gas, and calcite. This process called "karstification" generates a subterranean network of natural cavities and drifts, which become underground reservoirs and rivers, and a typical superficial landscape with dolines and lapiez. Therefore, the subterranean part of the karst is composed of two main parts.

The unsaturated permeable infiltration zone is composed of vertical fissures and natural sink holes that allows rapid and intense recharge and of a finer fissure system that allows diffusive diphasic (air/water) discharge. The saturated (flooded) karst constitutes the main storage of water of the karstic aquifer. This zone is characterized by the presence of two main water storage zones: a highly organized and hierarchized drainage network and the fractured/fissured media around the drainage network. Both zones contribute to the water storage in karstic systems but their strong heterogeneities in term of transmissivity lead to complex hydraulic relationships that explain for a large part the nonlinearity of the karst response. Then, the main peculiarity of karstic aquifers, compared to classical porous media, seems to be the dissociation in the saturated zone of transmissive and capacitive functions. The complexity of the karst systems lead to a number of rainfall-runoff approaches (Charlier et al., 2015, Duran et al., 2015, Hartmann et al., 2013, Jourde et al., 2013, Kong-A-Siou et al., 2014) that could include non linear models coupled to non-stationary analyses tools (Labat et al., 2000, 2001, 2002). We focus here on another systemic approach not based on rainfall impulsions as system entrance but based on artificial tracer injections. The tracer should have some properties such as the non absorbance in the system.

Residence Time Distribution estimation and interpretation

68 The concept of tracer test consists basically in an injection of tracer in an unknown system in
 69 order to analyse the transit time of the tracer i.e. the response of the system. In order to
 70 characterise the mixing conditions in the complex system, one should determine how long
 71 each volume element resides in the system. Basically, if you insert a tracer instantaneously
 72 in a system, the tracer fluid elements will leave the system at different times. These times are
 73 measured thanks to the tracer concentration variations at the outlet of the system or at a
 74 given point of a system. If a mass of tracer noted M is added to the system at time $t=0$, then
 75 the concentration at the outlet of the system will be function of time noted $c(t)$. After an
 76 infinite long time, because of mass conservation we have:

$$77 \quad M = \int_{t=0}^{t=\infty} c(t)Q(t)dt \quad (1)$$

78 Where $Q(t)$ is the spring flow function of time (m^3/s) and $c(t)$ is the concentration function of
 79 time measured at the outlet of the system (g/m^3). At this point, we already indicate that this
 80 assumption of mass conservation is rarely, if ever, met in field tracer experiments but for still
 81 debated reasons. That information can be sum up regarding the concept of Residence Time
 82 Distribution (RTD). The RTD here after noted $E(t)$ (s^{-1}) can be estimated as

$$83 \quad E(t) = \frac{c(t)Q(t)}{\int_{t=0}^{t=\infty} c(t)Q(t)dt} \quad \text{where} \quad \int_{t=0}^{t=\infty} E(t)dt = 1 \quad (2)$$

84 The main parameters that can be derived from the RTD function consists in the mean
 85 residence time noted θ defined by

$$86 \quad \theta = \int_{t=0}^{t=\infty} tE(t)dt \quad (3)$$

87 Dye tracer experiment constitute one the most effective way to quantify flow and mass
 88 transfer in karst aquifers and then infer some hypotheses on the structure of a karstic
 89 system. These tests consist in a rapid injection of a fluorescent dye at a supposed recharge
 90 point. These tests first allows to delineate the recharge area of these particular aquifers.

91 Then, the examination of the tracer breakthrough curve at one of several outlets of the
92 system is supposed to give relevant information about the degree of karstification and
93 connexion of the drainage network system and the presence of internal water reserves in the
94 capacitive areas or not (Massei et al, 2006, Geyer et al., 2007, Goldsheider, 2008). However,
95 one should keep in mind as stated by Maloszewski et al. (2002) that “artificial tracers are
96 usually injected into sinkholes and they usually supply information only on preferential flow
97 paths”.

98 A primary interpretation of the experimental RTD is based on the Advection Dispersion
99 equation that lead to a Log-Gaussian form but when dealing more specifically with karst
100 systems, this approach usually failed reproducing the tail observed on tracer injections in
101 hydrogeological systems. Currently two models are commonly used by the community:
102 QTRACER2 (Field and Pinsky, 2000, Field, 2002) and CXTFIT (Toride et al. 1995, Field and
103 Pinsky, 2000). The first model proposes an analytical solution of the classical advection-
104 dispersion equation and is mainly dedicated to conduit flows. Therefore, it does not allow in
105 general to reproduce the long tail of tracer concentration function of time that we can observe
106 in karst tracer tests for example. The CXTFIT program is based on a two region non
107 equilibrium transport model. However, these models suffer of two main limits: it does not lead
108 to a unique interpretation of the karst system and it is based on global parameters such as
109 velocity, dispersivity that should be constant in the karstic system. This point is really crucial.
110 On these models, for example, the dimensionless Peclet number is a crucial parameter. This
111 parameter is defined as a characteristic length of the flow multiplied by the mean velocity and
112 divided by the diffusivity. It also correspond to the product of the Reynolds number by the
113 Schmidt number. But is it reasonable to provide a Peclet number for a flow process in a karst
114 system on several kilometers distance? All these parameters will be characterized by a large
115 interval of variations and for example, it would be very difficult to provide a mean Reynolds
116 number for such flow process. We then propose to follow a new way of tracer test
117 interpretation methods.

118   **A new transfer function approach**

119   We propose a new paradigm in tracer breakthrough interpretation in karst system based on
120   chemical engineers expertise in control process experience (see Wolf, D., Resnick, W.,
121   1963, Levenspiel, 1975, Niemi, 1977, Villiermaux, 1982, Nauman E.B., Buffham BA, 1983,
122   Walas, 1991 for example) and first applied to porous media by Sardin et al. (1991). Chemical
123   reactors are a succession of ideally mixed or not reservoirs connected by a network of tubes.
124   In industrial process, the definition and the optimisation of the residence time in each step of
125   the process is crucial. In a similar way, we could consider that in a karst system the tracer
126   (and then mass transfer) follows water movement on a set of different reservoirs such as
127   fracture or fissure networks, annex systems, underground rivers or pipes. However, two main
128   limitations remain:

- 129   -   The stationarity of the flows,
- 130   -   The determination of the system and the uniqueness of the solution.

131   For example, Becker and Bellin (2013) proposed a transfer function approach of the Mobile-
132   Immobile model. Following Dreiss (1982), Mangin (1984) and Labat et al. (2000) among
133   others, we think that a transfer function approach similar to the rainfall/runoff transformation
134   could be applied to the issue of artificial tracer tests interpretation in karstic system. This
135   transfer function should give semi-quantitative information about the relative importance in
136   the tracer test response of a quick-flow component and a slow-flow transfer. The
137   quantification of these two pathways is very important for example in the dissemination of a
138   given contaminant since the predominance of rapid flow implies in general a very tiny
139   attenuation of the pollutant concentration (if there is no adsorption in the system) whereas
140   the predominance of the slow-flow implies in general a dispersion of the pollutant and then a
141   diminution of the peak of pollutant concentration at the outlet of the system. Therefore how
142   can we discriminate the two main components in the RDT function?

In a similar way as in surface hydrology, a classical form of the transfer function could be based on a successive cascade of tanks. However, this model fails here to simulate both the presence of a peak and of a long tail since this model implies either the presence of a peak of high amplitude but with no tail (small number of tanks) or the presence of a peak of small amplitude conjugated to a longer tail (large number of tanks).

The model of Becker and Bellin (2013), proposed a cascade of similar transfer functions derived from the mobile-immobile model. The results of simulation leads to set of parameters that are still difficult to interpret in term of physical processes even though if the number of reservoirs could be related to the Peclet number of the system and then to the “complexity” of the flow in the mobile part of the model. Moreover this model does not provide the ability to discriminate between quick and slow components but between a mobile and an immobile part of the fluid transfer. The quick component correspond roughly to flow processes in the drainage network and the highly transmissive fracture network whereas the slow component roughly corresponds to the delayed response in relationship with flow process in less transmissive fractured or fissured zone.

We choose to propose a model based on the coexistence of a rapid component and a slow component. We also choose to restrict the number of parameters for each component but to allow the presence of a cascade of similar components that lead to the presence of the exponents N_A and N_D .

Finally, by analogy with experimental models developed in Marsili-Libelli (1997), we propose to use 7 parameters transfer function in the Laplace domain that appear as a convenient compromise between the existence of two components and a limited number of parameters :

$$H(p) = \alpha \left[\frac{1}{(1 + A_1 p)(1 + A_2 p)} \right]^{N_A} + (1 - \alpha) \left[\frac{1}{(1 + D_1 p)(1 + D_2 p)^2} \right]^{N_D} \quad (4)$$

Where

- α is a coefficient of partition between rapid and slow component and is comprised between 0 and 1,
- A_1 and A_2 are the two parameters that control the advective component of the transfer function,
- D_1 and D_2 are the two parameters that control the slow component of the transfer function,
- N_a and N_d are the two exponents respectively of the advective and the slower part of the transfer function.

The first component based on a second-order transfer function correspond to a transport by rapid process whereas we choose to increase the order of the second transfer function in order to reproduce a slower component. We also choose not to propose a large number of parameters A_i and D_i but to propose that the systems can be connected in series which lead to a multiplication in Laplace domain leading to the N_a and N_d exponents. At this point, other choices could be made such as a parallel form of the components of the transfer function but it will lead to a rapid increase of the number of parameters.

The inverse Laplace transform cannot be operated analytically and then we choose to use the algorithm described by de Hoog et al. (1982) and implemented in MATLAB by Hollenbeck (1998). The next step consists in the optimisation procedure that allows the determination of the 7 parameters of the model. The optimisation minimisation criteria between the experimental and the simulated RTD is based on a classical Nash-Sutcliffe (Nash and Sutcliffe, 1970) coefficient:

$$Nash = 100 \left(1 - \frac{\sum (y_{mod}(i) - y_{mes}(i))^2}{\sum (y_{mes}(i) - \overline{y_{mes}(i)})^2} \right) \quad (5)$$

Where $y_{mod}(i)$ is the discretised time series simulated by the model and $y_{mes}(i)$ is the discretised experimental time series measured on the field. The optimisation procedure consists on the application of a genetic algorithm. Genetic algorithm is a searching procedure

based on the mechanics of natural selection and natural genetics. Genetic algorithm has known to be efficient and robust (Wang, 1991) and are based on an artificial survival of the fittest with genetic operators abstracted from nature. In this work a genetic algorithm developed by Dorsey and Mayer (1995) is introduced and applied to the calibration of the parameters of inverse Laplace transform of the $H(p)$ function. This approach has been applied to five tracer tests operated on a Pyrenean karst.

Results and discussion

We propose here to apply these functions to several tracer tests experiments over the Baget karstic watershed, part of the SNO Karst consortium. This basin located in the Pyrénées Mountains (Ariège, France) is characterised by a median altitude about 940 m and an area around 13 km². The specific runoff is 36 l/s/km² with a mean daily runoff about 0.45 m³/s (Labat et al., 2000). The injections and recovery site are located on the downstream part of the aquifer as depicted in Figure 1. In this zone, the system is characterised by the presence of loss and of temporary and permanent resurgences on a spatially restrained area of about 2 Km².

Five tracer tests based on fluoresceine injection were conducted during periods with no-rainfall influence in order to avoid any strong variability of the spring flow during the tracer test recovering. On the five tracer tests, the flush of the injected tracer was very rapid (less than one minute) and the tracer directly gets into the loss directly connected to river sinks and drains. By this way, we avoid non-instantaneous but mass-decaying injection at the inlet of the system, due for example to an insufficient flush of the injected tracer and/or to density effects (if the density of the injected solution is higher than that of the groundwater), which may delay the flow of the injected tracer solution into the system. Effectively, the "instantaneous" injection assumption, on which most currently used analytical solutions are based, may be not valid in real field tracer experiments.

The five tracer test characteristics (date, delay, spring flow variations, weight of tracers, and delay of recovery) are shown in Table 1. For each tracer, the spring flow and the

concentration function of time were measured with a high resolution sampling rate of 8 up to 15 minutes on the most critical part of the recovery. Then, the tracer recovery is sampled on a long time interval but at a lower sampling rate in order to provide a valuable survey of the tail of the RTD function. For the five tests, the tracer recovery rate was superior to 95%. The figures 2 to 6 depict the superposition of the experimental and simulated RTD function but also the representation for each tracer test of the advective and the ~~diffusive~~ slower part of the RTD function. For each simulations, the Nash coefficient was superior to 90%.

A comparison between the recovery simulations of the tracer tests 1, 2 and 3 (or 5) allows to identify in the system different levels of karstification. The tracer test 1 indicates the presence of a drain that allows a rapid advective component in the system response. This advective component corresponds roughly to the maximum at $t=4h$ highlighted in the global RTD. However, this advective component only corresponds to around 30% of the integral of the simulated RTD. That indicates that the slow part constitutes the main way of transfer in the aquifer between the injection and the recovery station. The tracer tests 2 and 3 indicates the concomitance between the advective and the slow components with a maximum around 1h before the beginning of the recovery and a shift of about 15 minutes. That indicates that the advective part is not predominant in the global RTD and indicates the presence of a less developed drainage system in this area but the presence of a fractured media around this drainage system. The slow component of tracer tests 2 and 3 respectively corresponds to 20% and 45% of the integral of the simulated RTD. Therefore, we may think that the fractured media plays a more important role in the water transfer in the inlet-outlet system corresponding to the tracer test 3.

Then, the recovery of tracer tests 3 and 5 allows to identify for a given inlet-outlet system (namely an injection at the P2 loss and a recovery at the Las Hountas spring) possible discrepancies between low (tracer test 5) and medium (tracer test 3) water levels. When the water levels increase, the advective component of tracer tests 3 and 5 respectively corresponds to 55% and 90% of the integral of the simulated RTD. On one hand, during low

water periods, the advective component is predominant since all the water flows by the drain and the hydraulic connexion with fractured media is very tiny. On the other hand, during the medium flow periods, the advective and slow components are concomitant since the hydraulic connexion between drainage system and fractured media is characterized by higher piezometric levels in the fractured media.

Finally, tracer tests 3 and 4 allows to identify differences in the system organisation since for a given injection point, we examine the tracer test recovery at two different outlets corresponding to two-ways water path is possible in the system. Here, an injection at the P2 loss is recovered both at the Las Hountas and Moulo de Jaur outlet. The advective component of tracer tests 3 and 4 respectively corresponds to 55% and 90% of the integral of the simulated RTD. Moreover, the maximum of the slow component is delayed in the tracer test 4 compared to tracer test 3. That indicates that the hydraulic connexion between P2 loss and Moulo de Jaur is characterised by a well organised drainage system whereas the hydraulic connexion between PS loss and Las Hountas is characterised by a drainage system connected to fractured media located in the vicinity of its outlet.

Conclusion

We propose here a new paradigm in the artificial tracer tests interpretation in karstic systems. Following Sardin et al (1991) and Becker and Bellin (2013), we think that a transfer function approach of the RTD function is a very promising way of research. We propose here a transfer function that allows the identification of an advective and a slow part in the water/contaminant transfer and we try to relate the shape of these two components to the degree of karstification of a well-known karstic system Le Baget. That allows to precise the spatial organisation of this system. The following step consists now in the determination of plausible correspondence between the parameters of the transfer functions and physical parameters. Therefore, we strongly encourage karstic community to apply this approach to other systems and to propose if necessary alternative transfer functions but keeping in mind the parsimonious principle.

273 Acknowledgment

274 This work benefits from INSU/CNRS CRITEX Program RBV-SOERE. The Baget watershed
275 is part of the French national observatory SO KARST (www.sokarst.org). We also thank the
276 three anonymous reviewers for improvements of the initial version.

277

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TABLE 1:

Description of the five artificial tracer tests operated on the Baget karstic system (Pyrenees, France) used in this study.

NAME	DATE	INJECTION	RECOVERING	WEIGHT (G)	MEAN SPRING FLOW (M ³ /S)	SAMPLING RATE (MIN)
TRACER TEST 1	12/10/1977	La Peyrère	Las Hountas	160	0.07	15
TRACER TEST 2	15/12/1977	Moulo de Jaur	Las Hountas	50	0.275	15
TRACER TEST 3	07/03/1978	P2 Loss	Las Hountas	750	0.650±0.05	8-15
TRACER TEST 4	07/03/1978	P2 Loss	Moulo de Jaur	750	0.355±0.01	8-15
TRACER TEST 5	03/05/1979	P2 Loss	Las Hountas	700	0.340±0.01	8-15

FIGURE 1:

Top: Localization of the Baget karstic system and description of the watershed. The inlet and outlet tracer injection/recovery are located in the upstream part of the basin (black rectangle).

Bottom: Zoom on the injection/recovery sites used in the five tracer tests of the study and localization of the gauge station

FIGURE 2:

Comparison between experimental (EXP) and simulated (MOD) RTD function and visualization of the advective (blue line) and slow (dark dashed line) component based on the equation 4 for the tracer test 1.

FIGURE 3:

Idem for tracer test 2.

FIGURE 4:

Idem for tracer test 3.

FIGURE 5:

Idem for tracer test 4.

FIGURE 6:

Idem for tracer test 5.