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# 1 Fracture processes imaging in concrete using nonlinear ultrasound

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11

## 12 Abstract

13 This paper shows the complementarity of two nonlinear ultrasonic imaging methods to characterize  
14 closed macro cracks in concrete. A time reversal mirror is used to locally probe and image the  
15 nonlinearity of a cracked region. Two nonlinear parameters are extracted to map the cracked region. The  
16 image obtained using the first parameter relates the harmonic generation due to the contact and frictional  
17 behaviors at the crack lips, correlated with vibro-thermography imaging of the same crack. The image  
18 obtained using the second parameter is based on the conditioning of the material induced by distributed  
19 micro cracks arising from the fracture process zone. These results show a great potential for  
20 characterization of fracture processes in concrete, with the possibility to uncouple the effects of the crack  
21 itself from surrounding distributed micro damage.

22 **Keywords:** Nonlinear ultrasound, Concrete, Cracks, Fracture process zone

## 23 Highlight:

- 24
- 25 • Nonlinear ultrasound can image and distinguish fracture processes in concrete
  - 26 • Nonlinear responses from the fracture process zone and the crack lips are separated
  - The results are correlated with vibro-thermography images

## 27 **1. Introduction**

28 In civil engineering, increasingly more stringent safety and maintenance requirements have called for  
29 more sophisticated detection and imaging NDT tools. This is particularly true in the nuclear-energy  
30 industry, in the context of license renewal and need for structural assessment. Ultrasonic assessment of  
31 concrete structures has been successfully achieved since 1990's with the possibility to image complex  
32 structures using tomographic approaches [1,2]. Ultrasonic crack-depth estimation in concrete is  
33 standardized [3], based on low-frequency (tens of kHz) wave propagation. However, the resolution is  
34 limited by the wavelength and only the opened portion of the crack can be detected. More refined  
35 methods based on the multiple scattering of higher-frequency waves [4] are more sensitive to the  
36 complex morphology of the crack, including partially opened cracks [5]. Nonlinear-ultrasonic-based  
37 methods have been proven efficient in detecting many types of damage and pathologies in concrete  
38 [6,7,8,9]. Nonlinear ultrasound has also been successfully employed to probe closed cracks [10,11] and  
39 exhibited a promising sensitivity. Even if the industrial civil engineering community reveals a growing  
40 interest for these methods, nonlinear ultrasonic inspection of concrete has been limited to laboratory  
41 studies.

42 So far, ultrasonic imaging of closed cracks remains a challenge. As for characterization, ultrasonic  
43 imaging can be achieved [12] but with a sensitivity limited to the large wavelength employed and to the  
44 opened portion of the crack. Again, higher frequencies fall in the multiple scattering regime into which  
45 standard methods do not apply. Recent research based on higher frequency diffuse waves showed the  
46 ability to image macro crack in laboratory samples [13] as well as real structures [14]. However, this  
47 approach only applies to image variations, i.e., crack propagation or crack opening due to external  
48 loadings, and only image the opened portions of the cracks.

49 The aim of this paper is to investigate the potential of methods based on nonlinear acoustics for closed-  
50 crack imaging. The imaging method employed here is based on time reversal, which focuses elastic  
51 energy at a prescribed location [15]. A study of the amplitude dependence of the elastic response allows  
52 then to locally probe the nonlinearity of the medium. Repeating this experiment over a regular grid  
53 spanning a region of interest on the surface of the concrete may provide a map of the nonlinearity. Such  
54 a method was already applied to probe distributed damage in concrete [16], as well as in other materials

55 such as metals [17]. This paper shows that contact phenomena at the crack lips are well imaged using a  
56 method based on harmonic generation. These physical phenomena are also validated using active vibro-  
57 thermography. The fracture process zone surrounding the main crack lips exhibits micro damage  
58 occurring during fracture formation [18]. This zone is also imaged using a time-delay method, similar  
59 to the one used in [16].

60

## 61 2. Materials and Methods

62 We study a notched rectangular prism of ordinary concrete with dimensions of  $10 \times 10 \times 60 \text{ cm}^3$ . The  
63 composition of the sample is provided in table.1.

64 Table.1. Concrete sample composition

CEM I 52.5 N PMES CP2 (Saint Vigor, FR)	340 kg/m <sup>3</sup>
Sand 0/4 (Bernières, FR)	739 kg/m <sup>3</sup>
Gravel 8/22 (Bernières, FR)	1072 kg/m <sup>3</sup>
Total water	184 kg/m <sup>3</sup>

65

66 A macro-crack departing from the notch was generated in the sample via a three-point bending test.  
67 Photographs of the sample and crack are shown in Figure 1(a,c) as well as the force versus vertical  
68 displacement curve recorded during the mechanical test (Fig.1b).

69 In the following, our ultrasonic measurements capitalize on a well-known property of elastic waves to  
70 focus a high level of elastic energy in time and space, namely a Time Reversal Mirror (TRM). A  
71 description of time reversal and its application to non-destructive testing was given by Anderson et al.  
72 [19]. The reciprocal TRM version employed in this study provides an opportunity to focus energy  
73 remotely from a set of source transducers. After the forward step has been conducted independently with  
74 each of these source transducers, they can be synchronized to emit simultaneously their TR signals and  
75 focus elastic wave energy at a point of interest, thus allowing relatively large strain amplitudes to be  
76 reached. The large strain amplitude is necessary for the study of nonlinearity while the localized  
77 excitation is necessary for imaging application, to probe the nonlinearity of the material locally (e.g.,  
78 near a crack).

79 The sample was instrumented with 10 piezoelectric disks, which were used as source transducers  
80 randomly glued on the six faces of the sample. The piezoelectric disks were made by APC International  
81 using material type 855 (Navy VI), had a diameter of 25.4 mm and thickness of 6.3mm. Devcon® 5  
82 Minute epoxy was used to bond the transducers to the concrete sample. The source transducers were  
83 individually driven with signals generated by 16-bit waveform-generator cards (National Instrument,  
84 PXI-5421) and amplified 50 times by power amplifiers (Tabor Electronics, Model 9400). The out-of-  
85 plane component of the particle velocity was measured on the surface of the sample using a laser Doppler  
86 vibrometer (Polytec OFV-303). The laser head was mounted on a moving stage capable of scanning the  
87 vibration field on a region of interest. The data measured by this instrument was digitized at a sampling  
88 rate of 10 MHz (National Instrument, PXI-4122) with a sensitivity of 5 mm/s/V. The linearity of the  
89 setup was checked on a plexiglass sample.

90 In this experiment, the band-limited impulse response between the sources and the receiver (focal point)  
91 are obtained using a combination of chirp signals and cross-correlations, to increase the signal-to-noise  
92 ratio in the frequency band of interest. The chirp signal used in the forward step had a frequency range  
93 of 50 kHz to 150 kHz, which encompasses the operating frequency of the piezoelectric source at 80  
94 kHz. The full TRM procedure used in this study is gathered in Figure 2. Figure 2a shows the ten forward  
95 signals (band-limited impulse responses) obtained independently for the ten source transducers by cross-  
96 correlation with the laser signal at the focal point. Once reversed in time, the summation of the ten  
97 sources give rises to a localized signal in time (Fig 2b) and space (Fig 2c). In Figure 2c, the white cross  
98 denotes the point in space where the ten signals in Figure 2a and the time reversed summation is  
99 recorded. Theoretically, the full-width half-maximum (FWHM) size of a focal spot is equal to a half  
100 wavelength at the center frequency of the pulse [20]. As shown in Figure 2c, the size of the measured  
101 focal spot is approximately 1 cm. Considering a center frequency of 100 kHz, we estimate the wave  
102 speed to be approximately 2000 m/s, which would correspond to the wave speed of surface waves in  
103 concrete [21]. In other words, the focal signal in this particular setup is mainly produced by surface  
104 waves. The *local* (at the focal spot) strain amplitude is approximated as the ratio between the out-of-  
105 plane particle velocity and the mean wave speed as in [16]. This estimation of the strain amplitude is  
106 essential for quantitative nonlinear studies [16,22].

107 TR-based imaging was performed around the crack and above the notch, within a square region of  $60 \times$   
108  $60 \text{ mm}^2$ . The scan grid consisted of 1600 points with a spatial resolution of 1.5 mm. At each scan point,  
109 the TR experiment was repeated at 10 amplitudes (before amplification): 5 negative amplitudes  $x_i^- = -$   
110  $1\text{V}, -0.8\text{V}, -0.6\text{V}, -0.4\text{V}, -0.2\text{V}$ , and 5 positive amplitudes  $x_i^+ = 0.2\text{V}, 0.4\text{V}, 0.6\text{V}, 0.8\text{V}, 1\text{V}$ . The phase  
111 shift in the amplitude sweep will be useful in the nonlinear analysis. The TR signals obtained at a point  
112 of focus on the scanning grid with the 10 source amplitudes are shown in Figure 2a. Two nonlinear  
113 parameters are extracted from this set of data: one that is representative of a diffuse damage of the  
114 sample [16] and one that is representative of clapping phenomena at the crack lips interface [7,17].

115

116 The first parameter is related to the time at which the maximum signal amplitude is achieved at the focal  
117 point, which we will refer to as focal time. The signals shown in Figure 3a-1 are used for this analysis.  
118 The dependence of the focal time on the vibration amplitude is related to nonclassical nonlinearity and  
119 will be described by a parameter  $\alpha$  [16]. The focal time at the lowest vibration amplitude of the  
120 experiment is used as a linear reference against which the focal times at the larger vibration amplitudes  
121 are compared to compute a time delay using cross correlation. The time delay experienced by the focal  
122 signal as a function of strain amplitude at this particular focal point is shown in Fig. 3a-2 for the 5  
123 positive source amplitudes (from 0.2V to 1V). The slope of the linear fit for this set of time delays is the  
124 parameter  $\alpha$  used in this analysis.

125

126 The second parameter is estimated using the pulse inversion harmonic processing [23]. In brief, when  
127 two waves of equal amplitude but opposite phase propagate in a nonlinear material at a frequency  $f_0$ , the  
128 linear component of the summed waves (spectral content at the fundamental frequency  $f_0$ ) should vanish  
129 while some of the nonlinear components (spectral content around the even harmonic frequencies, e.g.,  
130  $2f_0$ ) should be doubled. This technique has been amply used to enhance the signal to noise ratio of  
131 harmonic imaging in the medical field. The harmonic generation appears in the frequency band 150-  
132 250kHz, above the sources bandwidth (150kHz) and below the signal to noise ratio (250kHz), depicted  
133 with a blue background area in Figure 3b-1. The summed focused signal ( $x_i^+ + x_i^-$ ) are then filtered in  
134 this frequency band (150-250 kHz). The residual intensity is reported to the strain amplitude in Figure

135 3b-2. We observe a quadratic evolution of this parameter with the strain amplitude. The retained value  
136 for this nonlinear parameter is the quadratic term  $\beta$  of the fitted polynomial. The asymmetry of the  
137 focused signals is representative of a difference between pushing and pulling at the surface. It is expected  
138 to be sensitive to the crack interface through clapping phenomena [17].

139 The procedures are repeated for all 1600 points of the scanning grid to provide a map of the nonlinear  
140 parameters. The linear and quadratic regression are calculated only for the 5 available strain amplitudes.  
141 However, each point results from the combination of two independently ran signals. In addition, the  
142 spatial measurement density ( $1.5 \text{ mm}^2$ ) in view of the mean wavelength (1 cm) allows the spatial  
143 smoothing of the obtained images.

144

### 145 **3. Results and discussion**

146 The two images obtained using nonlinear ultrasound are displayed on Figure 4a and 4b respectively for  
147  $\alpha$  and  $\beta$  parameters.

148 Fig. 4a reveals several zones surrounding the crack with a higher  $\alpha$  parameter. It was shown in previous  
149 work [16] that this parameter was related to the amount of micro-cracking damage in concrete. The size  
150 of the micro-cracked region occurring before coalescence of connected microcracks is known to depend  
151 on the size of the aggregates [18]. Our concrete sample being made with 22 mm aggregates, the size of  
152 the fracture process zone is expected to scale about 2 cm apart from the crack [18,24]. This corresponds  
153 to the extent of the highest  $\alpha$  values shown in Fig 4b. This map of  $\alpha$  seems to be a reasonable  
154 representation of the fracture process zone [18,25,26].

155 In Figure 4b, the parameter  $\beta$  exhibits a relatively large dynamic range and is thus displayed in log scale  
156 for clarity. The highest  $\beta$  values are observed along the crack lips and do not overlap with the map of  
157 the  $\alpha$  parameter. We explain the results as follow: some parts of the cracks can be opened and closed by  
158 the push-pull induced by the ultrasonic focusing, generating the strong asymmetries in the signals, thus  
159 producing a strong residual energy. As a correlation step, a vibro-thermography experiment is carried  
160 out using the same sources at the same frequencies. One of the piezoelectric devices is driven at 400Vpp  
161 (maximal amplitude reachable by the amplifiers), at the frequency which produces the highest amplitude  
162 in the sample (80kHz). The images are recorded using a FLIR SC8200 IR camera. The image is obtained

163 using the protocol described by Remillieux et al. [27] to image cracks in metal. The image (Fig.4c)  
164 reveals high intensity spots occurring during wave propagation in the crack region. The apparent  
165 correlation of both images in Figures (4b,4c) suggests that both techniques are sensitive to the same  
166 physical features of the crack despite the wavelength of the source signal being much larger than those  
167 features.

168

#### 169 **4. Conclusion**

170 This paper demonstrates the ability of nonlinear ultrasonic methods to image macrocrack processes in  
171 concrete. The time reversal method employed here allows to image independently the fracture process  
172 zone and the crack lips using two physical parameters ( $\alpha$  and  $\beta$ ) respectively sensitive to the presence of  
173 diffused micro-damage and friction/clapping phenomena. The beta mapping is correlated with a vibro-  
174 thermography image. The alpha mapping reveals a micro-damaged zone corresponding to the size of  
175 already observed FPZ in samples with aggregate size of about 20mm.

176 In view of field applications, the method employed here presents the advantage that the location of the  
177 sources is not an issue and it does not affect the resolution which is driven by the scan span defined with  
178 the laser. However, the main limitation is the surface nature of the measurements even if the information  
179 is also related to the penetration depth of the focal still driven by the wavelength. Another limitation of  
180 the present experiment is the time needed to perform such a scan (about 80h) even if the spatial  
181 resolution could be reduced to meet more realistic industrial conditions. Nonetheless, the main  
182 conclusion concerns the ability of the two nonlinear ultrasonic parameters to image and characterize  
183 fracture processes in concrete. From a more practical standpoint, recent technological advances using  
184 ultrasonic phased arrays in concrete [28] could allow to image a macrocracks in the bulk of concrete  
185 using nonlinear phenomenon similarly as nonlinear imaging methods employed in metals [29] in the  
186 near future, once high amplitude waves will be available on such equipment.

187

#### 188 **Acknowledgments**

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190

191 **References**

192

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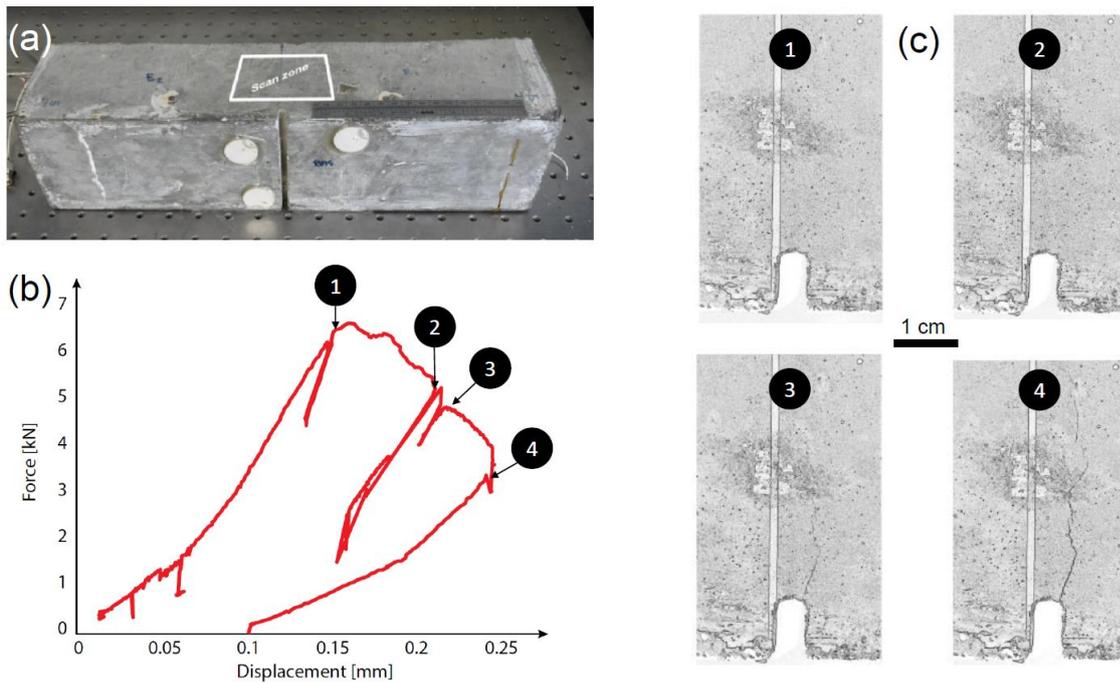
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258

259 Figure 1. (a) Image of the sample showing where the acoustic scan zone is located. (b)  
260 Force/displacement curved recorded during the mechanical test. 1 to 4 symbols represent the times when  
261 the notched region was photographed. Corresponding images are shown in (c).

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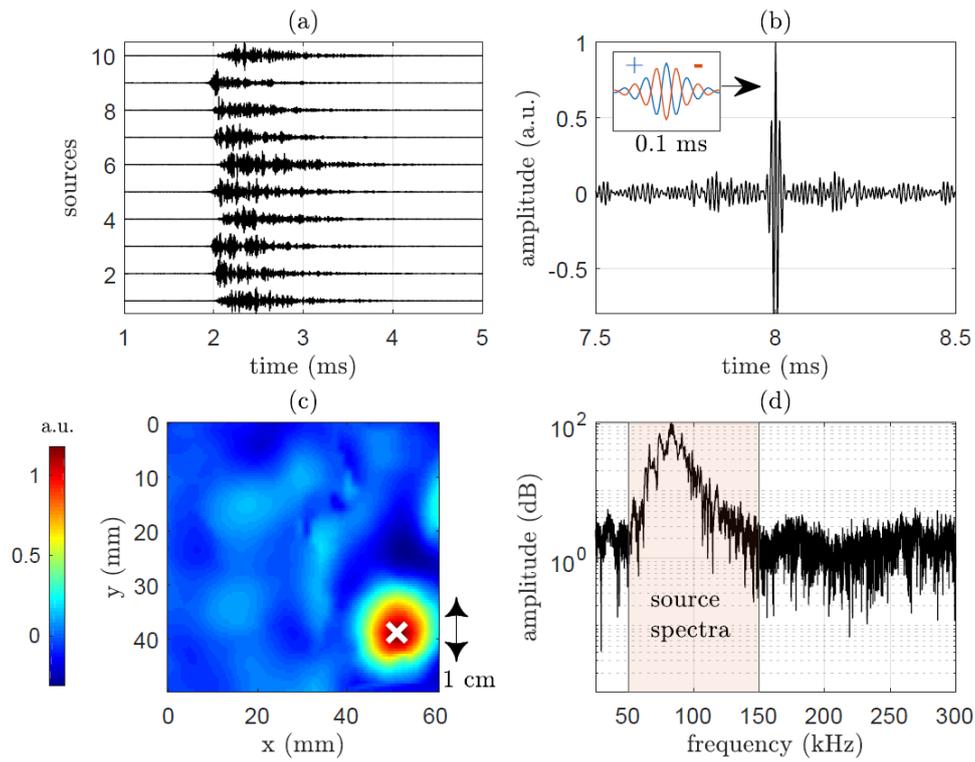
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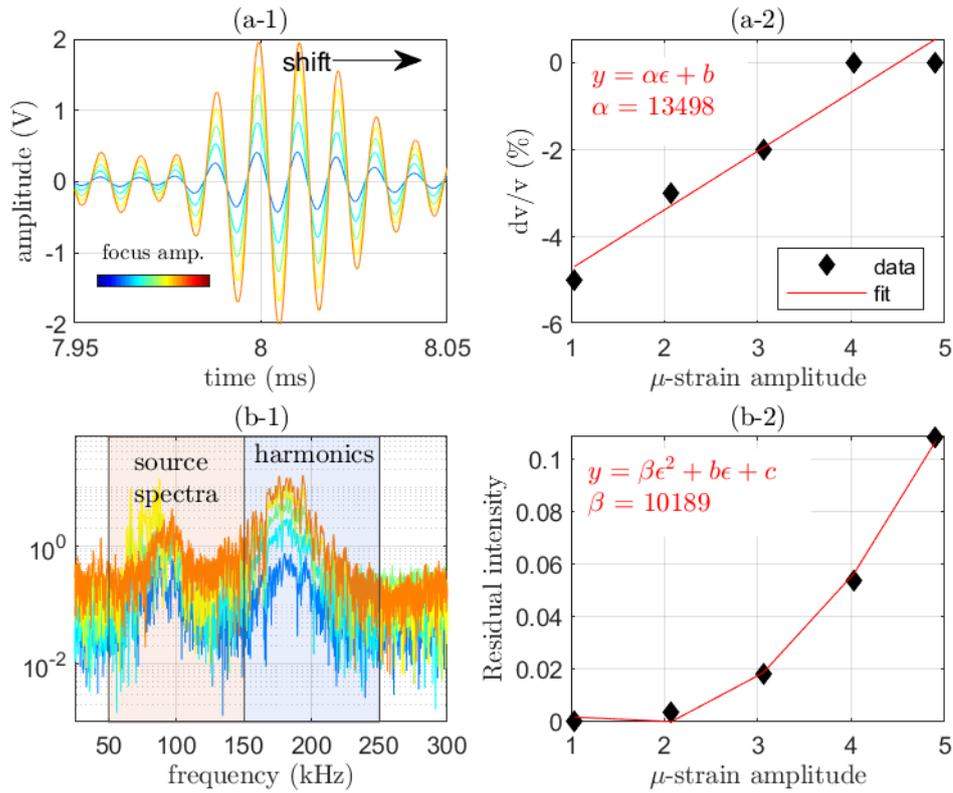
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271 Figure 2: Time reversal mirror principle. (a) Ten forward signals sent by the sources. (b) Focused signal  
 272 in time produced by rebroadcasting the time reversed version of the forward signals. (c) Focal spot in  
 273 space (white-cross is the point where TRM is applied) recorded at focal time. (d) Frequency content of  
 274 the focus signal. The input source spectra is highlighted by a red background area.

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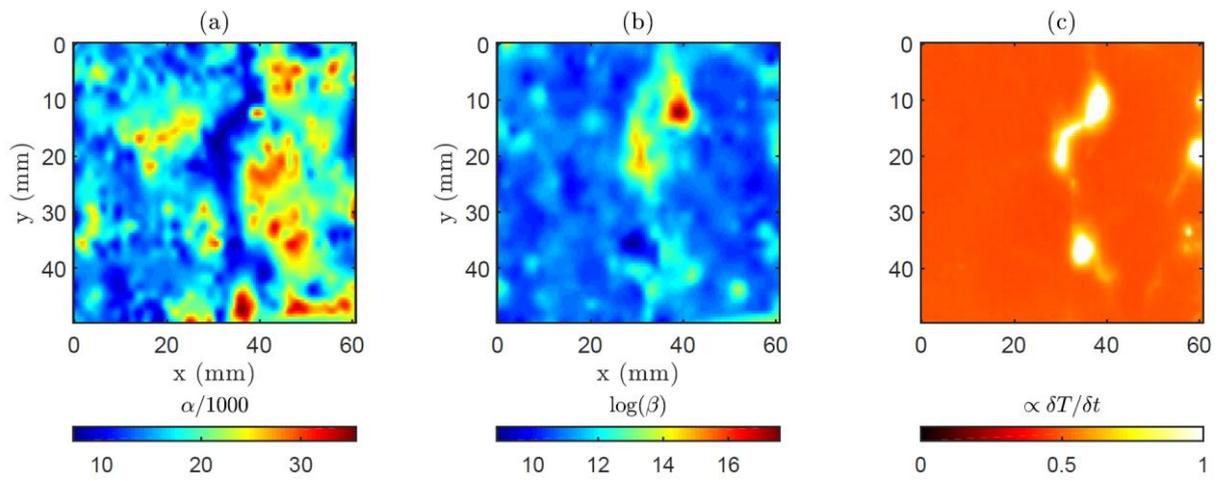
277 Figure 3: Representative results for the extraction of nonlinear parameters. (a)  $\alpha$  and (b)  $\beta$  are extracted  
 278 from the measured focused signal. (a-1) Five positive focused signals. (a-2) Time shift (or  $\Delta t/t_0$ ) at the  
 279 focal spot as a function of amplitude (black diamond) with a linear regression (red curve and equation).  
 280 The color code (blue to red) represents the 5 focused amplitudes. (b-1) Residual spectra for the  
 281 summation of the five positive and negative signals. The red background area is the linear frequency  
 282 band (that of the source signal) and the blue background area is the frequency width considered for the  
 283 harmonic generation measurement. (b-2) Residual intensity into the harmonic frequency band a function  
 284 of strain amplitude (black diamond) and quadratic regression (red curve and equation).

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291 Figure 4: Experimental images of the cracked region. (a) Nonlinear  $\alpha$  parameter. (b) Harmonic  
292 generation ( $\beta$  parameter). (c) Vibro-thermography image: first derivative of the temperature with respect  
293 to time (the reader can refer to [23] for more details).