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Tight Focusing Properties of Radially Polarized Doughnut Gaussian Beam through a Dielectric Interface

K. Prabakaran^{1*}, R. Loganathan¹, A. Kesavan¹, K.B. Rajesh², A. Mohamed Musthafa³, V. Aroulmoji⁴

¹Department of Physics, Mahendra Arts and Science College (Autonomous), Namakkal, Tamilnadu, India

²Department of Physics, Chikkanna Government Arts College, Trippur, Tamilnadu, India

³Department of General Studies (Physics Group), Jubail University College (Male Branch),

Royal Commission of Jubail, Kingdom of Saudi Arabia

⁴Center for Research and Development, Mahendra Engineering College, Namakkal District, Tamil Nadu, India

ABSTRACT: Tight focusing properties of an radially polarized doughnut Gaussian beam through a dielectric interface is theoretically investigated by vector diffraction theory. For the incident beam with topological charges (m), probe depth (d) and revive in the vicinity of focal plane, which results in the generation of many novel focal patterns. Such kind of focal structures may find applications in micro-particle trapping, manipulation, and material processing.

KEYWORDS: Radially polarized DG beam, Focal shift, Dielectric interface, Vector diffraction theory,

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1. INTRODUCTION

In recent years, cylindrically polarized beam have attracted great interests because of its interesting properties and potential applications [1-4]. For example, tight focusing of radially polarized light beams can create a very strong longitudinal electric field component in the focal region [1]. Moreover, in many practical applications, an objective is used to focus an incident light beam through an interface between different media of different refractive indices. For example, in the application of semiconductor inspection, light beams are focused from air onto silicon substrate. Torok et al [5] developed the theoretical method for studying the focusing of an electromagnetic wave through dielectric interfaces [6, 7]. More recently, a sub-wavelength light needle with a longer depth of focus (over 9.5λ) has been obtained using dual-beam focusing [8]. All these researches, the incident light beam is focused mainly in the vacuum. However, in some practical applications, the incident light beam is focused through an interface between different media by a high-NA lens. For example, in the case of optical trapping, a laser beam is focused through an interface between glass and water [9].

In recent times, many other kinds of beams, such as the Laguerre– Gaussian (LG) beam, the high order LG beam, the high order BG beam and the sinh-Gaussian beam, Multi gaussian beam, Hollow gaussian beam are discussed in depth [10-14]. Generally, their results have indicated that the form of the designed filters and their corresponding focusing performance are strongly influenced by the incident beam. Therefore, a new kind of radially polarized beam called doughnut Gaussian (DG) beam is introduced in a high NA focusing system. The defined DG beam is similar

to a hollow Gaussian beam. In 2010, a subwavelength focal spot was achieved by using a radially polarized narrow-width annular beam [15]. The DG beam, which is similar to the narrow-width annular beam, is falling to the category of the Gaussian beams [16]. Considering that the intensity is null at the center of the doughnut beam, the focusing field of a radially polarized DG incident beam through a high NA lens will exhibit high resolution. Meanwhile, other focusing patterns, such as a doughnut beam and the special polarized beam, were also investigated, based on the filtering technology [17-21]. In this Letter, we study the tight focusing of radially polarized doughnut gaussian beam passing through dielectric interface by vector diffraction theory. The principle of the optical focusing radially polarized DG beam is given and the simulation results are discussed in depth.

2. The principle of the optical focusing radially polarized DG beam

The scheme of the optical system is shown in Fig. 1. Assume the interface between two dielectric media of refractive indices $n_1 = 1$ and $n_2 = 3.55$, such as focusing in air onto silicon substrate in the application of semiconductor inspection. The geometric focus of the objective without the interface is located at the origin of the coordinate system. The distance between the interface and the geometric focus is d which is referred to as probe depth in Ref. [6]. For radially polarized beams, on the basis of vectorial Debye theory [2] the Cartesian components of the electric field vector in the focal region may be expressed as [22]

*Corresponding Author: prabakaran27mar@gmail.com

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$$E(r, \varphi, z) = \begin{bmatrix} E_x(r, \varphi, z) \\ E_y(r, \varphi, z) \\ E_z(r, \varphi, z) \end{bmatrix} = \frac{-iE_0}{\pi} \int_0^\alpha \int_0^{2\pi} \exp[-ik_0 \Phi(\theta_1, \theta_2)] \times \sin \theta_1 \sqrt{\cos \theta_1} A(\theta_1) \\ \times t_p [ik_2 z \cos \theta_2 + ik_1 \sin \theta_1 \cos(\varphi - \phi)] \begin{bmatrix} \cos \theta_2 \cos \varphi \\ \cos \theta_2 \sin \varphi \\ \sin \theta_2 \end{bmatrix} d\phi d\theta_1 \rightarrow (1)$$

Where $k_i = n_i k_0$ and $k_0 = 2\pi/\lambda$ is the wave number, $J_n(x)$ is the Bessel function of the first kind of order n , $\alpha = \arcsin(\text{NA})$ is the maximal angle determined by the NA of the objective; t_p

is the amplitude transmission coefficients for parallel polarization states, which is given by the Fresnel equations [23].

$$t_p = \frac{2 \sin \theta_1 \cos \theta_1}{\sin(\theta_1 + \theta_2) \cos(\theta_1 + \theta_2)} \rightarrow (2)$$

The function $\Phi(\theta_1, \theta_2)$ is given by

$$\Phi(\theta_1, \theta_2) = -d(n_1 \cos \theta_1 - n_2 \cos \theta_2) \rightarrow (3)$$

Representing the so-called aberration function caused by the mismatch of the refractive indices n_1 and n_2 . Here θ_1

and θ_2 are related by the well-known Snell law. The Eq. (1) could be simplified to

$$E(r, \psi, z) = \begin{bmatrix} E_x(r, \psi, z) \\ E_y(r, \psi, z) \\ E_z(r, \psi, z) \end{bmatrix} = -i^{n+1} E_0 \begin{bmatrix} i(I_{n+1} e^{i\psi} - I_{n-1} e^{-i\psi}) \\ I_{n+1} e^{i\psi} + I_{n-1} e^{-i\psi} \\ 2I_n \end{bmatrix} e^{im\psi} \rightarrow (4)$$

$$I_n(r, z) = \int_0^\alpha \exp[-ik_0 \Phi(\theta_1, \theta_2)] A(\theta_1) \sqrt{\cos \theta_1} \times \sin \theta_1 t_p \sin \theta_2 J_n(k_1 r \sin \theta_1) \times \exp(-ik_2 z \cos \theta_2) d\theta_1 \rightarrow (5)$$

$$I_{n\pm 1}(r, z) = \int_0^\alpha \exp[-ik_0 \Phi(\theta_1, \theta_2)] A(\theta_1) \sqrt{\cos \theta_1} \times \sin \theta_1 t_p \cos \theta_2 J_{n\pm 1}(k_1 r \sin \theta_1) \times \exp(-ik_2 z \cos \theta_2) d\theta_1 \rightarrow (6)$$

With similar simplification for the radially polarize doughnut gaussian beams can be written as

$$E(r, \psi, z) = \begin{bmatrix} E_x(r, \psi, z) \\ E_y(r, \psi, z) \\ E_z(r, \psi, z) \end{bmatrix} = i^{n+1} E_0 \begin{bmatrix} I'_{n+1} e^{i\psi} - I'_{n-1} e^{-i\psi} \\ -i(I'_{n+1} e^{i\psi} + I'_{n-1} e^{-i\psi}) \\ 0 \end{bmatrix} e^{im\psi} \rightarrow (7)$$

where

$$I'_{n\pm 1}(r, z) = \int_0^\alpha \exp[-ik_0 \Phi(\theta_1, \theta_2)] A(\theta_1) \sqrt{\cos \theta_1} \times \sin \theta_1 t_p \cos \theta_2 J_{n\pm 1}(k_1 r \sin \theta_1) \times \exp(-ik_2 z \cos \theta_2) d\theta_1 \rightarrow (8)$$

$A(\theta_1)$ describes the doughnut Gaussian beam, this function is given by [24,25]

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$$A(\theta_1) = \exp \left[- \left(\frac{\sin(\theta) - \theta_0}{w_0} \right)^2 \right] \rightarrow (9)$$

Where w_0 reflects the beam size at the beam waist of the Gaussian beam. θ_0 relates with the radius of the DG beam. θ is the variable of the function. Obviously, the shape of the defined doughnut Gaussian beam is determined by θ_0 and w_0 . To be more specific, the position of the maximum field intensity depends on θ_0 . For $\theta_0=0$ the beam governed by Eq. (9) is a conventional Gaussian beam. The width of the DG beam is determined by w_0 .

Fig.1.Schematic diagram of the optical system

3. RESULTS AND DISCUSSION

Without loss of generality and validity, it is proposed that the parameter chosen as $\lambda = 633$ nm. $NA=0.9$, $\theta_0=0.8$, and $w_0=0.125$. For all calculations in the length unit is normalized to λ and the energy density is normalized to unity. Figure 2 illustrates the evolution of three-dimensional light intensity distribution of high NA lens for the incident radially polarized doughnut Gaussian beam through dielectric interface.

Figure 2(a-c) shows the intensity distribution for topological charge $m=1$, probe depth $d=1\lambda$. It is observed from the figure due to the mismatch of refractive index across the interface, the on axial maximum intensity is not at the focus and it is shifted to 5λ and is shown in Fig. 2 (a & c). The calculated focal depth is 8λ . The FWHM of the generated focal spot is 0.44λ and is shown in Fig. 2(b). Moreover, it is observed from the figure that the longitudinal component is much smaller than the radial component. However, for $d=2\lambda$, it is noted from Fig. 2(d), that the presence of dielectric interface shifts the position of an axial maximum intensity to 10λ and the focal spot size is slightly reduced to 0.42λ , focal depth is improved to 11λ and is shown in Figs. 2(e) and 2(f).

Fig.2. (a) 3d intensity distribution for topological charge $m=1$ and $d=1\lambda$. (b) 2d intensity of the components E_x (red line), E_y (blue line) and E_{tot} (black line) at $z=5\lambda$. (c) On axial intensity at $r=0$. (d) 3d intensity distribution for topological charge $m=1$ and $d=2\lambda$. (e) 2d intensity of the components E_x (red line), E_y (blue line), and E_{tot} (black line) at $z=10\lambda$ for $d=2\lambda$. (f) On axial intensity at $r=0$.

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Fig.3. (a) 3d intensity distribution for topological charge $m=2$ and $d=1\lambda$. (b) 2d intensity of the components E_x (red line), E_y (blue line) and E_{tot} (black line) at $z=5\lambda$. (c) On axial intensity at $r=2\lambda$. (d) 3d intensity distribution for topological charge $m=2$ and $d=2\lambda$. (e) 2d intensity of the components E_x (red line), E_y (blue line), and E_{tot} (black line) at $z=10\lambda$ for $d=2\lambda$. (f) On axial intensity at $r=2\lambda$.

Such a dark channel may have many applications such as imaging the silicon integrated circuit. We also observed the focal properties of the radially polarized doughnut Gaussian beam with the probe depth $d=1\lambda$, topological charge $m=2$, the generated focal segment is a focal hole and shown in Fig. 3. It is observed from the figure the on axial maximum intensity is not at the focus and it is shifted to 5λ as shown in Fig. 3(a). The calculated focal depth is 8.4λ as shown in fig.3 (c). The FWHM of the generated focal hole size is 0.34λ as shown in Fig.3 (b). Moreover, it is observed from the figure the longitudinal component is much higher than the radial component. However, by setting $d=2\lambda$, we observed from the Fig.2.(e), increase in size of the probe depth further shifted the on axial maximum intensity to 10λ and focal hole size is slightly reduced to 0.32λ , focal depth is improved to 9.6λ as shown in Fig. 3(e), 3(f) respectively. We also observed that by altering the probe depth of the dielectric interface alters the focal shift position and focal depth of the generated focal segment. In optical trapping system, it is usually deemed that the forces exerted on the particle in light field consist of two kinds of forces, one is the optical gradient force, which play a crucial role in constructing optical trap and its intensity is proportional to the optical intensity gradient; the other kind of force is scattering force, which usually has complex forms because this kind of force is related to the properties of the trapped particles, and whose intensity is proportional to the optical intensity [26]. Therefore, tunable optical intensity distribution in focal region means that the controllable optical trap may occur [27]. The intensity distribution in focal region of the radially polarized DG beam can be altered considerably by beam parameter m and probe depth d , and many novel focal patterns can occur, which can be used to construct tunable optical traps.

4. CONCLUSION

In summary, we have derived the expressions for intensity distribution of tightly focused radially polarized doughnut gaussian beam passing through a dielectric interface have been investigated theoretically by the vector diffraction theory. It is observed that the presence of dielectric interface one can generate many novel focal patterns such as focal spot and focal hole suitable for micro particle trapping, manipulation and material processing. We also observed that by altering the probe depth of the dielectric interface alters the focal shift position and focal depth of the generated focal segment.

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