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Theoretical study of xenon adsorption in UO_2 nanoporous matrices

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Abstract

We present a theoretical study of xenon incorporation in UO_2 nanocavities, by means of Grand Canonical Monte Carlo calculations based on semi-empirical potentials. We first characterize the reconstruction of the matrix around an empty cavity which leads to a stoichiometry change from UO_2 to UO in this region. Then, we determine xenon adsorption isotherms which exhibit an abrupt transition from a dilute phase to a dense one and an increase in the density of the latter phase as a function of temperature. This last result is attributed to a vibrational entropy effect by means of a mean field analysis. Finally, the pressure calculation inside the bubble proves the limitations of the usual mesoscopic models based on gas state behaviour.

Keywords: UO_2 , xenon, adsorption, modeling, Monte Carlo, nanoporous

(Some figures may appear in colour only in the online journal)

1. Introduction

Porous materials have recently attracted interest in many areas including industry, chemical engineering and material science due to their potential for use in the separation and storage of gases [1–4] and for catalysis [5]. Thus, numerous experimental as well as theoretical studies have been performed on various systems combining different nanoporous matrices and different gases. In particular, much work concerning zeolite [6–8], carbon porous matrices [9] and gas adsorption isotherms in these systems. Beyond this applied interest, such studies are also important from a fundamental point of view to characterize the effects of confinement on phase transitions such as solid/liquid or order/disorder ones [10, 11].

In the nuclear field, porosities inside UO_2 fuel are very important since they contribute to limit fission gas release, in particular xenon, in the gap between the fuel matrix and the cladding and then to overpressurize the latter. However, the presence of gases inside the fuel matrix impacts all its thermomechanical properties and can also increase the cladding mechanical stress through additional fuel swelling. This last phenomenon is particularly important as a safety concern since it could lead to the cladding cracking. In order to describe the effect of intragranular nanobubbles on

the thermomechanical properties of UO_2 , micromechanical models have been developed [12, 13], which need to be fed by local pressure value *inside* and *outside* the bubbles. Usually, the pressure inside the bubbles is determined using either the perfect gas or the Van der Waals equations of state. Unfortunately, these expressions are totally unsuited to the temperature and pressure ranges encountered in nuclear fuel intragranular bubbles. Indeed, experimental results indicate that the xenon pressure order of magnitude is of a few GPa in these systems [14, 15]. That is the reason alternative equations of state have been proposed [16, 17], but without taking into account the Xe– UO_2 interactions at the gas-matrix interface, which implies neglecting the confinement effects even though they are known to be important [18, 19].

The aim of this work is to go beyond these limitations by means of atomistic simulations. Indeed, computer simulations have been considered as a new research tool for a better understanding of processes occurring at the atomic scale, as well as for processes that could not be observed directly by experimental means. Here, we will first characterize the empty cavity surface reconstruction before determining the xenon adsorption isotherms into the UO_2 matrix by Grand Canonical Monte Carlo (GCMC) calculations, with particular attention to the possible condensation of the gas phase. Then, we will

calculate the pressure inside the bubble, in order to check the limits of the traditional equations of state and possibly to feed higher scale modelings. Furthermore, we will propose a mean field approach analysis of the adsorption isotherms, which could be a useful tool to enable us to go from an atomistic to a macroscopic system description.

It is worth noting that not only the methodology adopted here, but also the objectives pursued and the physics explored, are fundamentally different from those described in the article by Jelea *et al* [19], which can be considered as a preliminary work with respect to the current one. Indeed, its purpose was to quantify the pressure generated by a given amount of xenon introduced into a cavity in an arbitrary manner with regard to both the quantity entered (estimated from experimental data) and its crystallographic nature. On the contrary, in the approach used here, we address the problem from the other end, since our primary goal is to determine the characteristics (density and structure in particular) of a physical incorporation of xenon corresponding to given experimental conditions (temperature, chemical potential). This physical filling, characterized by the isotherms calculated here, will be the essential result of our paper, concerning both the evolution observed from GCMC calculations and the physical identification of their driving forces through their mean field analysis. In this context, the change in pressure is one of the signatures of this behaviour, the point corresponding to the paper by Jelea *et al* being positioned in this general (and physical) trend.

2. Methods

2.1. UO_2 Matrix modeling

As previously described [20, 21], the system under study is a network of perfect UO_2 , generated by infinitely duplicating the elementary cell in the three space directions. The UO_2 elementary cell is of fluorite type and its lattice constant is $a = 0.547 \text{ nm}$ as determined experimentally at 296 K [22]. The porosities are introduced in the system as spherical cavities. These cavities are created inside cells by first eliminating all uranium and oxygen atoms contained in a sphere having a radius R . Then, the global stoichiometry of the system is preserved by removing excess uranium or oxygen atoms from the surface, in order to ensure the cell electroneutrality. To this aim, a criterion based on atom coordination is used, which requires determining a first neighbor distance threshold. This is achieved by the analysis of the Radial Distribution Function, which clearly separates a first coordination shell around 0.24 nm from the second one around 0.45 nm. This allows us to unambiguously fix the distance threshold to the value of 0.34 nm. Then, all the undercoordinated atoms (based on this threshold criterion) compared to the bulk reference are considered as surface atoms and are removed in priority.

In practice, we use as a starting point a perfect fluorite structure cell of 2592 atoms ($6 \times 6 \times 6$ supercells), corresponding to a volume of about 35 nm^3 . These supercells are large enough to allow the creation of nanopores with

diameters comparable to the experimental ones. We have checked that a larger ($6 \times 6 \times 12$) cell leads to the same results which confirms the absence of non-physical boundary effects. The cavity radius R is ranging from 0.4 to 1 nm which leads to a global porosity f (ratio between the number of cancelled atoms and the total number of atom in the perfect cell) ranging from 0.05 to 0.12.

However, the system so obtained is far from being equilibrated. Therefore, it must be relaxed by a suited thermodynamical procedure within an appropriate energetic model.

2.2. Energetic model

Ab initio methods are not suited to nanocavity modeling since it involves the study of several thousand atom systems. In addition, the physical properties of interest, such as mechanical or thermal properties, do not require a precise calculation of the electronic structure. Therefore semi-empirical potentials are well suited here.

2.2.1. UO interaction model. The system total energy E_{tot} can be written analytically as a function of the atomic positions, as a sum of an electrostatic term (E_{Coulomb}) and a two body interaction one (E_{inter}):

$$E_{\text{tot}} = E_{\text{Coulomb}} + E_{\text{inter}} \quad (1)$$

where E_{Coulomb} is given by:

$$E_{\text{Coulomb}} = \sum_i \sum_j \frac{q_i q_j}{4\pi\epsilon_0 r_{ij}} \quad (2)$$

with $q_0 = -1.2$ and $q_U = 2.4$ the particle charges and r_{ij} the interatomic distances. This term is taken into account by an usual Ewald summation.

Concerning the interaction term, there are a variety of UO_2 effective energetic models in the literature [23–26]. We choose here the Basak potential [27] which accounts for the interactions involved in UO_2 and correctly reproduces macroscopic quantities such as the elastic constants (see table 1, especially at high temperature and for structures far from the perfect cristal [22, 28]. In addition, this potential reproduces fairly well surface properties and in particular surface energies for main orientations [20].

This potential is grounded on Buckingham–Hill (in the case of U–U, O–O and partly U–O) and Morse (for the covalent part of the U–O term) interactions:

$$E_{\text{inter}} = E_{\text{Buck}} + E_{\text{Morse}} \quad (3)$$

The Buckingham–Hill component involves two terms : a short range repulsive part and an attractive Van der Waals term in $1/r^6$ for O–O:

$$E_{\text{Buck}}(r) = A \exp\left(-\frac{r}{\rho}\right) - \frac{C}{r^6} \quad (4)$$

The Morse component has the following analytical form :

$$E_{\text{Morse}}(r) = D[1 - \exp(\beta(r^* - r))]^2 - 1 \quad (5)$$

The different Basak potential parameters are given in table 2.

Table 1. Comparison of elastic properties calculated using Basak potential with experimental values: C_{ij} : elastic constants; K = Bulk modulus.

	Basak potential [27]	Experimental values [29]
C_{11} (Gpa)	408.1	389.3
C_{12} (Gpa)	61.2	118.7
C_{44} (Gpa)	59.5	59.7
K (Gpa)	176.9	204.0
Lattice parameters (Å)	5.454	5.47

Table 2. U–O Basak interaction parameters.

Parameters	O–O	U–U	U–O
A (eV)	1633.39	294.745	693.87
C (eV · Å ⁶)	3.950	—	—
ρ (Å)	0.327 022	0.327 022	0.327 022
D (eV)	—	—	0.57745
β (Å ⁻¹)	—	—	1.658
r^* (Å)	—	—	2.369

2.2.2. Xe–UO interaction model. Concerning the interactions involving xenon atoms, we use the ‘Buckingham–Hill’ analytical form (equation (4)). The corresponding parameters for the interaction between xenon and matrix atoms (XeU et XeO) are given by Grimes [25] and between two xenon atoms by Brearley [30]. For very short distances ($r < r_{\text{born}}$), the Van der Waals term induces numerical divergence. New parameters (A , r and C) are then adjusted on experimental data [19]. The whole set of parameters is given in table 3.

2.3. Monte Carlo thermostatic tools

Based on the energetic model previously described, we have separated our study in two successive steps: the first one is to relax the matrix cavity in absence of xenon and the second one is to fill the so-relaxed cavity by xenon atoms. In order to check the validity of our assumption not to relax the matrix under xenon incorporation, we have in a few cases added post-incorporation system relaxation studies. All the simulations are performed by Monte Carlo simulations, in canonical (NVT) ensemble for relaxation steps and in grand canonical (μ, V, T) ensemble for the incorporation study. The choice we made to perform calculation at fixed volume is motivated by the physical situation we want to simulate (UO₂ matrix constrained by a cladding).

In the canonical ensemble, the only proposed events between a configuration i with energy E_i and a configuration $i + 1$ with energy E_{i+1} are the atom displacements, which are accepted with the probability $P_{i,i+1}$:

$$P_{i,i+1} = e^{-\frac{(E_{i+1}-E_i)}{kT}} \quad (6)$$

with k the Boltzmann constant and T the temperature.

In the grand canonical ensemble two other types of events are proposed, the addition or the removal of one xenon atoms,

with the respective probabilities $P_{i,i+1}^{\text{add}}$ and $P_{i,i+1}^{\text{rem}}$ [31]:

$$P_{i,i+1}^{\text{add}} = \frac{V}{\Lambda^3(N_i + 1)} e^{-\beta[E_{i+1}-E_i+\mu]} \quad (7)$$

$$P_{i,i+1}^{\text{rem}} = \frac{\Lambda^3 N_i}{V} e^{-\beta[E_{i+1}-E_i-\mu]} \quad (8)$$

where N_i is the number of atoms in the configuration i , V the system volume, $\Lambda = \frac{h}{\sqrt{2\pi kTm}}$, the De Broglie wavelength, m the xenon atomic mass, h the Plank constant and μ the fixed chemical potential.

In practice, the type of event is chosen randomly, according to the following probability: 40% for moves, 30% for additions and 30% for removals. Finally, the displacement vector is randomly chosen too, in the distance range 0 to 5% of the equilibrium Xe–Xe distance.

The Grand Canonical Monte Carlo approach allows us to determine isothermal xenon incorporation curve, in which we plot the equilibrium xenon density (g cm⁻³) at a given temperature as a function of the chemical potential. The thermodynamical equilibrium is assumed to be reached when the statistical number of created particules equals that of the removed ones, which generally requires more than 3×10^8 proposed steps. Additional Canonical Monte Carlo steps are then achieved to average the physiscal quantities of interest (the number of particules N_{Xe} , the xenon pressure P , the system energy E ...). Typically, 10 000 configurations each 3000 steps are used, to avoid correlation between consecutive steps.

2.4. Pressure determination

The average pressure inside the xenon bubble is obtained through the following equation, which is well suited to the case of system described by pairwise interactions and periodic boundary conditions [32]:

$$\langle P_{\text{bulle}} \rangle = \left\langle \frac{N_{\text{Xe}} kT}{V_b} \right\rangle + \left\langle \frac{1}{3V_b} \left(\sum_i^{N_{\text{Xe}}} \sum_{j \neq i}^N \frac{1}{2} r_{ij} f_{ij} \right) \right\rangle \quad (9)$$

where N_{Xe} is the equilibrium number of xenon atoms, N the total number of atoms inside the simulation box, V_b the bubble volume (assumed spherical), r_{ij} the distance between atoms i and j and f_{ij} the interaction force between these atoms, calculated as derivative of potential energy with respect to r_{ij} . In this equation, the first term is the kinetical contribution (perfect gaz law term) and the second one accounts for the Xe–Xe and the Xe–matrix interactions.

2.5. Mean field approach

The limitation of the previous numerical simulation is that the driving forces for the observed phenomena are hidden and then that they are hardly directly exploitable for upper scale modeling tools. To overpass this difficulty, one can simplify the description of the system, in order to be able to use a mean field approach approximation [33]. To this aim, we first decide not to take into account explicitly the atomic relaxations by using a rigid lattice description and second, to reduce the interaction models to first neighbour pairwise (Ising-like) one. In this framework, the idea is to treat the xenon atom condensation as

Table 3. Xe-matrix and Xe–Xe interaction parameters.

Parameters	XeU	XeXe	XeO	XeU	XeXe	XeO
r (Å)	$r < 1.1$	$r < 1.5$	$r < 1.8$	$r > 1.1$	$r > 1.5$	$r > 1.8$
A (eV)	2915.33	1171.48	136.7	6139.16	4934.10	598.00
r (Å)	0.410	0.466	0.561	0.34	0.35	0.42
C (eV. Å ⁶)	0	0	0	71.84	297.47	108.38

Figure 1. Bubble surface stoichiometry before and after relaxation for different initial dispersion (from 1 to 8 bubbles) corresponding to the same value of the porosity.

a binary xenon-vacancy system phase diagram determination. By this way, we will be able to determine effective rigid pairwise interaction, which take into account the atomic relaxation even though projected on rigid lattice. More precisely, the Ising description of the energy system writes:

$$E_{\text{tot}} = \frac{1}{2} \sum_{n \neq m} V_{nm} p_n p_m \quad (10)$$

where p_n is the n site occupation factor, which takes the value 1 if the site is occupied by a xenon atom and 0 otherwise. We choosed here to limit the range of interactions to the Z first neighbours, in which case, $V_{nm} = V$ if n and m are first neighbours and $V_{nm} = 0$ otherwise. The free energy minimisation of the previous function with respect to concentration $c = \langle p_n \rangle$, within the mean field approximation, leads to the usual expression:

$$\frac{c}{1-c} = \exp\left(-\frac{\Delta F_{\text{vib}} - \mu}{kT}\right) \quad (11)$$

where we denote ΔF_{vib} the part of the adsorption free energy in which the configurational part has been extracted:

$$\Delta F_{\text{vib}} = cZV - T\Delta S_{\text{vib}} \quad (12)$$

This equation involves two terms, the first one, cZV , the interaction between impurities and ΔS_{vib} the variation of the purely vibrational entropic term with respect to concentration, i.e. related to the incorporation of one additional Xe atom into the system.

Through this formalism, the link between μ and c as a function of the temperature is obtained trough the Monte Carlo

approach, so that one can easily determine ΔS_{vib} and ZV from the slope of the variation of ΔF_{vib} as a function of c for different temperatures.

3. Results

3.1. Cavity surface reconstruction

The figure 1 illustrates the variation of the bubble surface stoichiometry before and after relaxation for different initial bubble dispersions corresponding to the same porosity. More precisely, we have increased the vacuum/matrix interface by sharing this total porosity in various bubble distributions (from 1 to 8) bubbles. As can be seen, the relaxation leads to an almost equiatomic UO composition whatever the dispersion. This means that a larger number of uranium atoms are considered as surface atoms. Moreover, as can be observed in figure 2, configuration analysis indicates that oxygen atoms have been *pushed far* from their initial positions in the bulk towards the surface. These displacements lead to oxygen vacancy creation around the bubble and therefore to an increased number of uranium surface atoms according to our criterion. This analysis is confirmed by radial distribution functions which show that the oxygen atoms are found more numerous at a distance of approximately 0.7 to 1.1 nm, i.e. in the surface vicinity. This confirms that the full surface relaxation requires accounting for oxygen atom mobility. This important surface relaxation is consistent with the characterisation of a surface layer presenting an effective thickness of 2.3 nm, as previously commented in [21].

This surface thickness implies that a precise determination of the volume of the cavity, which is required to calculate the

Figure 2. Periphery of the cavity before and after relaxation. Uranium atoms in blue and oxygen ones in red. The yellow arrows indicate the atom displacement under relaxation.

Figure 3. Evolution of the density of incorporated xenon atoms ρ , in g cm^{-3} units, as a function of the chemical potential for two extreme temperatures. For the sake of comparison, the horizontal line indicates the value ρ_{eq} of this density for a perfect compact xenon bulk phase built with the equilibrium value of the atomic radius at $T = 0 \text{ K}$, namely 0.2 nm [36].

pressure through equation (9), by assuming a perfect spherical shape with radius R is somewhat approximated. In order to get an idea of the margin of error on this evaluation, we have estimated the radius of different bubbles by averaging the distances between the centre of the cavity and the atoms belonging to the thick surface layer. The margin of error on the value of the radius found within this procedure is of about 3%, which means an uncertainty of about 10% in the volume determination.

3.2. Incorporation isotherm

As previously detailed, the physical bubble filling has been achieved within GCMC, for different chemical potentials and temperatures. The values of explored chemical potentials have been chosen in the range characteristic of the xenon state inside the fuel, namely $[-2 \text{ eV}; 10 \text{ eV}]$, taking into account the energy of a xenon atom inside the UO_2 matrix in interstitial ($\sim 20 \text{ eV}$) or vacancy ($\sim 5\text{--}10 \text{ eV}$) positions [19, 34, 35]. Under this condition, we have checked that xenon atoms only incorporate inside the cavity, as expected. The temperature range has been

chosen to be consistent with the in-pile conditions and extents from 300 K to 1200 K. Finally, the effect of the xenon-matrix interface is examined through different cavity radius studies between 0.4 and 1 nm. Having not identified any significant size effect in this range, we only present in the following the results obtained for the 1 nm bubble radius.

Figure 3 represents the corresponding incorporation isotherms (incorporated xenon density as a function of the chemical potential for two extreme temperatures). Both curves exhibit the same general behaviour with a first zero or almost zero part followed by a more or less abrupt jump to a new plateau for approximately $\mu_c \simeq -0.5 \text{ eV}$. This behaviour is characteristic of a phase transition from dilute to condensed system, as confirmed by the microstructures shown in the figure 4. Both the values of the critical chemical potential μ_c and that of the saturation density ρ_s at the plateau, depend on the temperature:

- The xenon saturation density ρ_s corresponds to about 8 g cm^{-3} , which is twice ρ_{eq} the density of a compact xenon phase with an atomic radius of 0.2 nm [36].

Figure 4. Microstructures observed for $\mu = -1.5$ eV and $\mu = 2$ eV at $T = 300$ K.

Figure 5. Radial distribution function for xenon for $\mu = 2$ eV and $T = 300$ K. The vertical lines stand for the first three neighbouring distances in an ideal bcc structure.

- The higher the temperature, the lower μ_c and the higher ρ_s . For example, ρ_s increases by about 10% between 300 K and 1200 K. Furthermore, this temperature increase smoothes the phase transition. This temperature dependence of ρ_s value is far from being intuitive and should be related to thermal fluctuations. This point will be investigated in more details in the following section.

In order to get a microstructural signature of the phase transition from dilute to condensed phase and in particular the crystallinity or not of the later, we have plotted the radial distribution function of the xenon system. This is illustrated for $\mu = 2$ eV and $T = 300$ K in figure 5 which allows to clearly identify a first neighbour shell at about 0.35 nm, consistent with Van der Waals radius of xenon atoms. The second neighbour shell around 0.4 nm suggests that xenon has crystallised on a bcc lattice rather than on a fcc one. This result is consistent with high pressure and temperature xenon structuration [37, 38].

3.3. Xenon bubble pressure

Let us recall that the stress undergone inside the bubble implies a counterpart in the UO_2 matrix which is a key element for nuclear safety. Therefore it is important to estimate as precisely as possible the pressure inside bubble. This point has motivated a lot of works, both experimentally [14, 15, 39, 40] and theoretically [17, 19, 28]. However, the results of these studies exhibit a large dispersion, the pressure values ranging between 1.6 GPa and 15 GPa at 700 K. Therefore, one can expect that the present atomic scale study will clarify these data.

The calculation of the average pressure in the bubble is performed using the equation (9). We present in figure 6 (left) the average pressure of the bubble as a function of the chemical potential μ for two extreme temperatures. The main trends are a significant pressure increase with chemical potential, and temperature, until very high pressure values (between 25 and 45 GPa). Taking into account the fact that the energy of

Figure 6. Total pressure (GPa) in the bubble for two extreme temperatures as a function of (left) xenon chemical potential and (right) incorporated xenon density.

incorporation of xenon in UO_2 is in the range [5 eV; 20 eV] depending on the incorporation site, the value of the pressure obtained in the present study (between 15 GPa and 50 GPa) shows that this quantity is greatly underestimated in the models based on gaseous equation of state, which are used currently. Increasing the temperature from 300 K to 1200 K enhances the pressure value of almost a factor two in the whole chemical potential range.

From the μ dependence of the xenon density (see figure 3) on one side and of pressure (see figure 6 left) on the other side, it is easy to extract the variation of the pressure as a function of the xenon density for the different temperatures. This is illustrated in figure 6 (right). The most striking feature is that, within this representation, the temperature effect seems to disappear.

Let us emphasize that one must be very careful to the explored thermodynamic system condition before deriving physical conclusion. Thus, following figure 6, a temperature increase at fixed chemical potential will impose a xenon density increase inside the bubble and therefore a pressure increase, contrary to what could be erroneously deduced from an analysis at fixed density. However, it should be kept in mind that some of these findings could be slightly modified by taking into account the relaxation of the matrix during filling. In fact, the assumption of keeping the matrix rigid during the incorporation process seems to have almost no impact on this result as checked by a post incorporation global system relaxation followed by a new incorporation process, which does not lead to any noticeable matrix reorganisation or ρ_s increase.

This absence of any significant modification of the cavity configuration can appear as somewhat contradictory with the observations made in the calculations performed by Jelea *et al* [19] for an *a priori* fixed number of Xe atoms, even though the pressure value found by these authors is consistent with the present work. In fact, the variance in the behaviours comes from the total difference in perspective already explained in the introduction. Indeed, we worked here with a fixed total cell volume (μ VT or NVT ensembles) and then verified that we do not get any change of the geometry of the cavity, whereas

Figure 7. Free energy variation as a function of the xenon concentration for $T = 300$ K (blue circles) and $T = 1200$ K (red squares).

in [19] the relaxation is performed in the NPT ensemble which is further from the physical situation and raises the problem of filling arbitrarily the cavity.

3.4. Mean field analysis

In order to analyze the previous results and to derive the driving forces of the isotherm behaviour, we have applied the mean field approach presented in section 2.5. The main difficulty here is the choice of the underlying rigid lattice, to be occupied by xenon atoms or vacancies, and therefore the xenon concentration definition. Here, the concentration c at a given μ is defined as the ratio between the average xenon density at this potential (derived from figure 3) and $\rho_s = 7.8 \text{ g cm}^{-3}$. Using this definition and the protocols described above, we have plotted in figure 7 the variation of ΔF_{vib} as a function of c for $T = 300$ K and $T = 1200$ K.

This figure raises the following comments:

- One can observe two different regimes as a function of c , below and above a critical concentration of $c = 0.37$.
- In the first regime, $\Delta F_{\text{vib}} \simeq 0$ independently of T and c .
- In the second regime the variation of ΔF_{vib} as a function of c for a given temperature is quasi linear, with a positive slope ZV , which is consistent with a constant value for a strongly repulsive effective pair interaction V , corresponding to an overstressed cristal lattice.
- The linear variation of ΔF_{vib} for the second regime for different temperatures are quasi parallel, which confirms the validity of a mean field description for this system. One can then extract a value for $ZV = 19\text{ eV}$ from the slope of these curves and $\Delta S_{\text{vib}} = 32k_b$ from the difference between the two curves.
- The constant value of ΔS_{vib} allows us to describe the vibrational entropy through the mean field approach : $S_{\text{vib}} = c\Delta S_{\text{vib}}$ which means that ΔS_{vib} is the *per atom* entropic effective term, independent of environment.

From this analysis it appears that the vibrational entropic term is responsible of the temperature effect on the adsorption isotherm previously described.

4. Conclusion

We have presented here a theoretical study of xenon incorporation in UO_2 nanocavities, by means of GCMC approaches based on semi-empirical potentials. The corresponding results allowed us to highlight a number of points. First, the nanostructuration of the cavity leads to a drastic change in stoichiometry at its surface. Then, xenon adsorption isotherms exhibit an abrupt transition from a dilute phase towards a dense one as a function of increasing chemical potential. The xenon density at saturation is found in good agreement with experimental values available in literature. In addition, one finds that the higher the temperature, the higher the density of xenon for a given chemical potential. In order to elucidate this behaviour, we have resorted to a mean field analysis of our system. The conclusion is that this temperature effect is related to the vibrational entropy. Complementary direct calculations of ΔS_{vib} should confirm this interpretation. This density increase with temperature leads to a pressure rise inside the bubble. Whatever the temperature, the corresponding pressure values are in agreement with most recent atomistic studies, but indicate that mesoscopic models based on gas state behaviour should be unsuited and then improved. In order to have a global physical view of the situation, the next step is now to investigate also, by similar approaches, the pressure inside the matrix. Some work is currently done in this direction.

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