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The Effect of Palladium and Platinum Doping on the Structure, Stability and Optical Properties of Germanium clusters: DFT study of PdGe_n and PtGe_n (n=1-20) clusters

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Abstract

Structural, electronic and optical properties of germanium clusters doped with palladium and platinum atoms MGe_n (M=Pd,Pt and n=1-20) are investigated in the framework of the density-functional theory. From n ≥ 10 or 11, the cage-like structures where the doping atom is totally encapsulated inside a Ge_n cage are favored. Relative stabilities of different MGe_n clusters have been analyzed from the average binding energies, second energy differences, HOMO–LUMO gap, and the vertical ionization potential and electronic affinity. Our results show that the clusters of MGe_n (M=Pd,Pt) with n = 10, 12, 16 and 18 exhibit relative high stability. Optical absorption spectra are predicted to be unable to discriminate the endohedral and exohedral structures.

1. Introduction

During the last decade, many efforts have been devoted to investigate the properties of pure or metal-doped germanium clusters due to their potential uses as assembled nanomaterials in the field of semiconductor materials and nanoelectronics. Recently, a number of experimental and theoretical studies have demonstrated that adding a metal atom in small germanium clusters could change dramatically their structural, electronic, magnetic and optical properties. [1-32] Particularly, in some cases the hybridization of orbitals and the pooling of valence electrons can stabilize germanium cages thanks to the encapsulation of the metal atom which absorbs the dangling bonds responsible of the instability of pure semiconductor clusters. [3-7]

Several transition metal (TM) atoms such as Cu, Ni, Sc, Ti and V were showed to stabilize the host structure when they are encapsulated by germanium clusters [4-6]. The doping with other metal atoms like Co, Fe, Mn, Ni, Ti, Zr, He, Al and Ru were also investigated [2,3,8-20]. All of these studies have provided important information on the physical and chemical properties of the TM doped germanium cagelike system together with their evolution as a function of size and composition. They show that the changes in properties of the host

germanium structures are strongly related to the nature of the guest metal atom. Generally, the stability of the structure is enhanced with the encapsulation of a transition metal atom. Tran et al. [21-23] have published several joint experimental and computational investigations of the stability and geometrical and electronic structures of very small neutral and anionic clusters of $VGe_n^{-/0}$ and $CoGe_n^{-/0}$, they especially showed that multiconfigurational post-Hartree methods reproduce well the experimental electron detachment energies. First principles calculations have been performed by Wang et al. to study the doping with Co, Ni, or W atom in a small germanium cage clusters [24-26]. While the encapsulation of a transition metal atom into germanium cage generally enhances the stabilities, the growth patterns depend on the doping metal atom. Chromium-doped germanium clusters were the subject of several studies [27-30], which showed that the magnetic behavior of the ground state structure is highly affected by the metal atom. Very recently, investigations on germanium cage clusters doped with V, Cu, Ag and Au atoms have highlighted a large stability of some clusters, such as VGe_{14} , $CuGe_{10,12,14}$, $AgGe_{12,14,15}$, $AuGe_{12,14,15}$, which is related to their quasi-spherical geometry and to their peculiar electronic structure in which the valence electrons of metal and Ge atoms are delocalized and exhibit a shell structure [31, 7]. Similar results were found for anionic gold-doped Ge [32].

Despite the relative abundance of investigations on the structural and electronic properties of small metal-doped germanium clusters, and to the best of our knowledge, systematic investigations of Palladium (Pd) and Platinum (Pt) doped germanium clusters have not been reported to date. It is questionable whether the doping with Pt and Pd, two elements belonging to the d-block beside noble metals on the periodic table, will lead to a somewhat metallic character where valence electrons occupy orbitals fully delocalized over the whole volume of the cluster, as previously reported for coinage metal doped Ge_n clusters [7], or conversely to chemical bonds and hybridization involving more localized orbitals as expected for open d-shell elements.

Here, we investigate the structural, electronic and optical properties of MGe_n ($M=Pd, Pt$ and $n=1-20$) clusters by performing density-functional theory (DFT) calculations. The theoretical method is detailed in section 2, while results and a discussion are presented in sections 3 and 4 respectively.

2. Computational methodology

We have used the spin polarized density functional theory (DFT) within the generalized gradient approximation (GGA) parameterized by Perdew, Burke and Ernzerhof (PBE) [33] implemented in the SIESTA simulation code [34]. The norm conserving Troullier-Martins pseudopotentials [35] was used for all species. The optimization of the structures was obtained by self-consistent solving of the Kohn–Sham equations with a convergence criterion of 10^{-4} a.u. on the energy and electron density. Using the conjugate gradient (CG) algorithm, the geometries were optimized without any symmetry constraints, and a large supercell of 40 Å side-length was used to avoid the interaction between neighboring clusters. Geometrical optimizations were considered as converged when the residual forces were smaller than 10^{-3} eV/Å. Double zeta basis set (DZ) was used for Ge while double zeta basis including polarization functions (DZP) were used for both Pd and Pt species. In the Brillouin zone sampling, only the gamma-point (Γ) was used for the k grid integration. The current calculation scheme performed on the Ge_2 dimer gives a bond length of 2.450 Å and a dissociation energy of 1.446 eV/atom, in good agreement with the experimental data of 2.44 Å [36] and ~ 1.35 eV [37] respectively.

A large number of possible initial structures have been relaxed for each size. Amongst them, some initial structures of Ge_{n+1} and metal-doped Ge_n clusters were taken from literature [7, 31 and references therein]. Also, the putative structures of MGe_n were obtained by local relaxation after the substitution of one Ge atom by M atom in several isomers of the original pure Ge_{n+1} cluster. The different initial positions of the Ge atom in the Ge_{n+1} clusters lead to different MGe_n isomers. But the search for the lowest isomer cannot include a global optimization procedure of the potential energy surface, and we cannot be sure that a more stable structure than those found in our calculations does not exist. Here, we only show the lowest-energy isomers for each cluster size. The spin on the metal is found to be quenched, as in the case of NiGe_n [5,25], and the spin state of all low-lying structures is found to be singlet. Triplet states are found to lie at more than 0.1 eV/atom above the lowest-energy singlet state.

Further analysis of the electronic properties and molecular orbitals have been performed with the software Gaussian09 [38] using PBE and the Gaussian-type basis sets cc-pvtz for Ge and LanL2DZ for Pd and Pt atoms. Optical absorption spectra are calculated in the framework of the Time-Dependent DFT (TDDFT) using the PBE functional and the range-separated hybrid functional ωB97x which includes an increasing amount of Hartree-Fock exchange at long-range (16% at short-range and 100% at long-range) [39]. ωB97x is became very popular as it is expected to give a more suitable description of excitations in the adiabatic linear-response approximation currently used in TDDFT calculations [40]. Post-processing operations were performed using the graphical interface Gabedit [41].

3. Results

3.1 Structural properties

The ground state isomers of PdGe_n and PtGe_n clusters are showed in Figures 1 and 2 respectively. More low-energy isomers are given in Figure S1 and S2 in Supplemental material. Some physical parameters such as symmetry group, binding energy E_b (eV/atom), HOMO-LUMO gaps (highest occupied–lowest unoccupied molecular orbital energy gap), vertical ionization potential (VIP) and electron affinity (VEA), and chemical hardness η are reported in Table 1 and 2 for PdGe_n and PtGe_n clusters respectively. Data for others isomers can be found in Supplemental informations (Tables S1 and S2). For smaller size, the metal is located on a peripheral position at the surface. The endohedral structures where the metal is totally encapsulated inside a germanium cage appear at $n = 10$ and 11 when the dopant is Pd and Pt respectively. So, the transition process in which the M atom moves from the surface to interior of the germanium cage appears at relative small size. For comparison this transition from exohedral to endohedral structure is observed at $n = 12$ in the case of doping with Ag and Au [7].

Now we describe briefly the structures of the most stable isomers for each species. The PdGe and PtGe diatomics have a bond length of 2.349 and 2.364 Å respectively, which are shorter than the corresponding bond distance 2.450 Å in the pure Ge_2 dimer [31]. Also the binding energy of PdGe and PtGe calculated at 1.292 and 1.201 eV/atom are lower than the that of the Ge_2 dimer (1.446 eV). The lowest energy isomer of PdGe_2 and PtGe_2 have a triangular structure with C_{2v} symmetry. A linear structure was also considered for this size but it is found to lie at higher energy comparatively to the C_{2v} triangular structure. The calculated Ge-Ge and Ge-Pd bond lengths are 2.456 and 2.475 Å respectively for PdGe_2 and the calculated Ge-Ge and Ge-Pt bond lengths are 2.468 and 2.533 Å for PtGe_2 clusters. The binding energy of PdGe_2

and PtGe₂ clusters are 0.082 and 0.004 eV/atom larger than that of Ge₃ clusters [31]. In the case of PdGe₃ and PtGe₃, planar rhombus structure with C_{2v} symmetry is the most stable isomers. The best structure for PdGe₄ and PtGe₄ is a distorted Ge₄ rhombus with one capped M atom and belonging to the C_{2v} point group. For PdGe₅ and PtGe₅ clusters, a bicapped distorted Ge₄ rhombus with C_{2v} symmetry is obtained as the ground state structure. The metal M (M=Pd, Pt) atoms capping a pentagonal pyramid Ge₆ is the most stable structure for MGe₆. For n = 7, the lowest-energy isomer differs with the metal dopant since the Pd atom caps the pentagonal bipyramid of Ge₇, while two germanium atoms cap the distorted PtGe₅ bipyramid with C_s symmetry in the case of PtGe₇. For MGe₈ (M=Pd, Pt) clusters, three Ge atoms cap the MGe₅ (M=Pd, Pt) clusters in the lowest-energy isomer. By adding one Ge atom to cap one face on the most stable structure of MGe₈ clusters, we obtain the most stable structure for MGe₉ clusters. Pt atom caps a Ge₁₀ cluster in the best structure for PtGe₁₀ clusters.

Starting from n = 10 for PdGe_n and from n = 11 for PtGe_n clusters, all of the lowest-energy isomers exhibit a cage-like structure with the metal atom completely encapsulated, and highly coordinated at the center of the Ge_n cage. A high symmetry D_{4d} structure where Pd located at the center is coordinated with all atoms of the germanium cage is obtained for the best isomer of PdGe₁₀. For n=11, the structures obtained for Pd- and Pt-doped Ge₁₁ are somewhat similar but differ by the symmetry (C_{5v} for PbGe₁₁, and C_s for PtGe₁₁). Pt- and Pd-Ge₁₂ belong to the S₄ symmetry point group. A spherical-like structure with a centered Pd atom is observed for PdGe₁₃, while in the case of PtGe₁₃, a Ge atom caps one face of the best isomer of PtGe₁₂. For larger sizes n, the growth pattern is somewhat similar for both metals while the lowest-energy isomers differ. For n = 14, 15 and 16, the most stable structure for MGe_n clusters is generally formed by one, two or three Ge atoms capping a spherical-like cage of MGe_n where the M atom occupies the center of the Ge_n cage. Adding one Ge atom at the surface of MGe₁₄ (resp. MGe₁₅) leads to the most stable structures of MGe₁₅ (resp. MGe₁₆). PdGe_{15,16} and PtGe_{15,16} have the larger binding energy among all size considered here. From n = 17 - 20, a distorted endohedral structure is observed for the lowest-energy isomer. The metal is encapsulated inside a germanium cage on which additional Ge atoms are attached at the surface.

3.2 Energetics and electronic properties

The binding energy is a good parameter for the study and the evaluation of the stability of small clusters. The average binding energy per atom is defined as:

$$E_b(MGe_n) = (n E(Ge) + E(M) - E(MGe_n))/(n+1), \quad (1)$$

where E(Ge) and E(M) are the total energy of free Ge and M atoms respectively. E(MGe_n) is the total energy of the corresponding cluster. The size evolution of E_b for the most stable structures of PdGe_n and PtGe_n clusters is shown in Figure 3. The binding energy of their corresponding pure germanium clusters [31] is plotted in the same figure for comparison. For all species, the value of E_b increases with increasing size, which means that clusters gain in the stability during the growth process. For n ≤ 6, the doping does not systematically increase the binding energy in comparison with the corresponding Ge_{n+1} cluster. In contrast, for n ≥ 7 the doping by the metal atom enhances considerably the stability of the host clusters. Thus, the doping M atom has no immediate effect on the stabilities of very small germanium clusters. This behavior can be related the structural properties of small MGe_n (n<7) clusters where the M-Ge bond lengths are much larger than Ge-Ge bond lengths as we can see from Tables 1 and 2. The highest values of E_b are obtained for n = 12-16, i.e. when the endohedral structures

appear. Relative high values of the binding energy are observed for $n = 12, 16$ and 18 which means that the corresponding MGe_n clusters exhibit high stability comparatively to their neighbors.

The second energy difference is one of important parameter in clusters physics which can be used to evaluate the relative stability of one cluster size comparatively to their neighboring size. It is defined by:

$$\Delta_2 E = E(MGe_{n+1}) + E(MGe_{n-1}) - 2 E(MGe_n) \quad (2)$$

where E is the total energy of the ground state cluster. Calculated second energy differences as a function of the size for the best isomers are shown in Figure 4. A pronounced maximum is found at $n=4, 7, 10, 12, 16$ and 18 . This indicates that these clusters have specific stabilities comparatively to their neighbors.

The HOMO–LUMO gap can give information about the stability of clusters and their chemical activity. In general, a large HOMO–LUMO gap implies a low chemical activity and a high chemical stability, while the latter decreases as the HOMO–LUMO gap decreases. The evolution of the calculated HOMO-LUMO gap of each species studied here is showed in Figure 5. In contrast to the roughly decreasing tendency of the evolution of HOMO-LUMO gaps for pure Ge_n clusters, an oscillating behavior is observed for Pd- and Pt- Ge_n clusters. As expected, the gap of very small metal-doped Ge_n is lower than that of the pure germanium clusters, but for $n \geq 10$ the presence of the metal generally increases the HOMO-LUMO gap. This somewhat surprising behavior is due to the encapsulation of the metal into the Ge structure which stabilizes the electronic structure by absorbing the dangling bonds. Values oscillate in the 0.5–2.0 eV range, but the evolution with cluster size shows a non-monotonic behavior. Pronounced values of HOMO-LUMO gaps are observed for $PdGe_{7,9,16,18}$ and $PtGe_{7,10,16,18}$ which indicates that theses clusters have probably a lower reactivity than their neighbors.

Other parameters that are generally calculated in order to gain an insight into the electronic structure are the vertical ionization potential (VIP) and electron affinity (VEA). They are defined with the following formulas:

$$\begin{aligned} VIP &= E(MGe_n^+) - E(MGe_n), \\ VEA &= E(MGe_n) - E(MGe_n^-), \end{aligned} \quad (3)$$

where $E(MGe_n^-)$ and $E(MGe_n^+)$ are the energy of the anionic and cationic MGe_n clusters calculated using the geometrical structure of the neutral cluster. The VIP can give information about the capacity of a cluster to lose a valence electron. Values are in the 6.2-7.6 eV range. The evolution of VIPs for the ground state structure in each species are shown in Figure 6. We observe that VIPs show a decreasing evolution with an oscillating behavior as the cluster size increase. Local maxima are observed for $n = 5, 10, 12, 16, 18$. The variation of the VEAs as a function of the size is plotted in Figure 7. The values of all species increase from 0.6 to 2.6 eV with an oscillating behavior as the size increases. One can note the relative small value for doped Ge_{16} clusters. Both VIP and VEA are relatively little dependent on the nature of the doping metal.

Another parameter that can be used to give more information about the relative stability of molecules and small clusters is the chemical hardness defined through the principle of maximum hardness (PMH) of Pearson [42] as:

$$\eta = \text{VIP} - \text{VEA} \quad (4)$$

where VIP and VEA are the vertical ionization potential and electron affinity of the corresponding cluster. In general, a high value for η indicates a high stability of the corresponding clusters. The evolution of η with the cluster size n are plotted in Figure 8. A relative high value is observed for $\text{PdGe}_{5,7,16,18}$ and $\text{PtGe}_{7,10,16,18}$ suggesting that these clusters should be less reactive than their neighbors, which is in total agreement with the predictions from the HOMO-LUMO gap analysis.

4. Discussion

Our results highlight a transition from exohedral to endohedral structures of PdGe_n and PtGe_n occurring at $n = 10$ and 11 respectively. This structural modification strongly affects the electronic properties. The atomic charges on metal atoms have been estimated through a natural population analysis (NPA) [43]. When Pd is located on a surface site, its atomic charge is relatively low (between -0.5 and -0.1 a.u.), but when the M atom move to an endohedral position to be encapsulated inside the germanium, its charge strongly increases to about -1.6 a.u. or more (Table S3). Similarly, the atomic charge on Pt in PtGe_n goes from about -0.4 to about -1.7 a.u. for the exohedral and endohedral structures respectively. The additional electrons captured by the metal atom in cage-like structure are mainly associated to $5p$ or $6p$ electron configurations. The large atomic charge indicate that the metal interacts with several Ge atoms, thus playing a stabilizing role of the Ge_n cage.

The transition from exohedral to endohedral structure has been already observed at $n = 12$ in the case of AgGe_n and AuGe_n [7], at $n = 10$ for CuGe_n [6,7], VGe_n [3,31], WGe_n [26], NbGe_n and TaGe_n [44], and at $n = 9$ for NiGe_n [5,25]. The encapsulated transition metal eliminates the dangling bonds of germanium atoms. In the present work, the cage-like structures enhance the binding energy, in particular for $n = 12-16$.

Interestingly, PdGe_{16} and PtGe_{16} present a relatively high stability. They have the highest stability from both the binding energy (Figure 3) and the second-order energy difference (Figure 4). They also show a relatively high HOMO-LUMO gap (Figure 5), and a large chemical hardness (Figure 8). In Figure 9, we show the density of states (DOS) and the Kohn-Sham orbitals calculated at PBE/cc-pvtz level with the software Gaussian09 [38] in the case of PdGe_{16} . The 10 valence electrons of Pd, and the $3s$ and $3p$ valence electrons of Ge exhibit a shell structure associated to the somewhat spherical structure. We can easily distinguish the character of the orbitals, though there are some little deviations from a perfect sphere due to explicit location of atoms and the C_s symmetry instead of K_h (the symmetry of the atom). The 74 valence electrons of the cluster are organized with the following occupations: $1S^2 1P^6 1D^{10} 1F^{14} 2D^{10} 2S^2 2P^6 1G^{18} 1H^6$. The number of electrons does not fit with shell closings numbers, but the pooling of electrons and the organization in shell contributes to the high stability of the cluster. Similar results are found for PtGe_{16} .

In experiment, the geometrical structure is most often inaccessible, and the discrimination between endohedral and exohedral structures is generally highlighted by a

measurement of discriminant physical or chemical properties. For example, the expected relatively low reactivity of endohedral structures has been used to highlight the formation of metal-doped germanium or silicon cages [45]. Neukermans et al. [1] have used the mass spectroscopy and interpret the high abundance CuGe_{10} in terms of peculiarly stable dopant-encapsulated cage-like structures. More recently, several groups have used the photoelectron spectroscopy [2,3,23]. Here, we have calculated the UV-visible absorption spectra of both cage-like and surface-bound metal structures in order to discriminate endohedral and exohedral structures. Spectra are given in Figure S3 for PdGe_{16} and PdGe_{10} . Unfortunately, they are found to be only few dependent on the position of the metal atom, while the density of states is much higher in the case of surface-bound metal due to a lower symmetry of the structure. Spectra show a slowly increasing response in the visible and near UV domain, and a strong signal above 7 eV (above the ionization potential). This low dependency of the absorption spectra on the geometrical can be explained by the electronic arrangement which tends to favor the pooling of valence electrons and the organization in shells where electrons occupy orbitals fully delocalized over the whole volume of the cluster. The shells are clearly visible in the case of symmetric structures, like cage-like structures (Figure 9 for example), but are no easily identifiable in the case of geometries without any symmetry like exohedral structures. The pooling of electrons is likely to be somewhat independent of the details of the structure, and consequently the optical absorption as well.

5. Conclusion

In summary, a theoretical investigation of the structural, stabilities and electronic properties of palladium- and platinum-doped germanium clusters has been carried out using the DFT method. Results are compared with the properties of pure Ge_n clusters.

From $n \geq 10$ or 11, the cage-like structures where the doping atom (Pd or Pt) is totally encapsulated at the center of Ge_n cage are favored. The binding energy per atom, second-order difference of energies, HOMO-LUMO gaps, vertical ionization potential and electronic affinity and the chemical hardness have been studied as function of the cluster size. Our results show that measurements of optical absorption spectra are likely unable to discriminate the endohedral and exohedral structures.

The doping M atoms have no immediate effect on the stabilities of very small germanium clusters, but starting from $n = 8$ the doping M atom enhances considerably the stability of the host clusters. Our results highlight the relatively high stability of PdGe_n and PtGe_n clusters with specific sizes $n = 10, 12, 16$ and 18. Amongst, PdGe_{16} and PtGe_{16} are the most stable clusters. These clusters can be considered as a good candidate to be used as building blocks to make cluster assembled materials for eventual applications in the news nanotechnologies.

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Data availability

The raw/processed data required to reproduce these findings cannot be shared at this time due to technical or time limitations.

Table 1. Symmetry group, binding energy E_b (eV/atom), HOMO-LUMO gap ΔE (eV), vertical ionization potential VIP (eV), vertical electron affinity VEA (eV), chemical hardness η (eV) and average bond length a_{Ge-Ge} (Å) and a_{Pd-Ge} (Å) for PdGe_n clusters.

Size (n)	Sym.	E _b (eV/atom)	ΔE (eV)	VIP (eV)	VEA (eV)	η (eV)	a_{Ge-Ge} (Å)	a_{Pd-Ge} (Å)
PdGe	C _∞	1.292	0.597	6.599	0.693	5.906	/	2.349
PdGe ₂	C _{2v}	2.141	0.758	7.309	1.217	6.092	2.456	2.475
PdGe ₃	C _{2v}	2.530	1.331	7.338	0.999	6.340	2.420	2.574
PdGe ₄	C _{2v}	2.738	1.328	7.450	1.259	6.191	2.610	2.698
PdGe ₅	C _s	2.846	1.413	7.566	1.367	6.199	2.759	2.959
PdGe ₆	C _{5v}	2.924	1.007	7.458	2.027	5.431	2.737	2.824
PdGe ₇	C _s	2.992	1.400	7.248	1.605	5.643	2.800	2.535
PdGe ₈	C ₁	2.987	0.933	6.976	2.160	4.816	2.788	2.596
PdGe ₉	C ₁	3.041	1.401	6.964	1.842	5.122	2.784	2.586
PdGe ₁₀	D _{4d}	3.096	1.282	7.504	2.463	5.041	2.823	2.608
PdGe ₁₁	C _{5v}	3.126	1.054	6.958	2.158	4.800	2.766	2.716
PdGe ₁₂	S ₄	3.184	1.004	7.065	2.431	4.634	2.630	2.834
PdGe ₁₃	C ₁	3.171	0.959	6.739	2.236	4.503	2.727	2.880
PdGe ₁₄	C _s	3.172	0.766	6.679	2.461	4.218	2.659	2.925
PdGe ₁₅	C _s	3.196	1.142	6.638	2.092	4.546	2.739	2.801
PdGe ₁₆	C ₂	3.204	1.674	6.779	1.845	4.934	2.772	2.877
PdGe ₁₇	C ₁	3.162	1.141	6.590	2.248	4.343	2.787	2.933
PdGe ₁₈	C ₁	3.170	1.206	6.618	2.262	4.356	2.765	2.891
PdGe ₁₉	C _{3v}	3.142	1.008	6.415	2.305	4.110	2.703	2.917
PdGe ₂₀	C ₁	3.155	1.068	6.625	2.548	4.076	2.723	2.844

Table 2. Symmetry group, binding energy E_b (eV/atom), HOMO-LUMO gap ΔE (eV), vertical ionization potential VIP (eV), vertical electron affinity VEA (eV), chemical hardness η (eV) and average bond length a_{Ge-Ge} (Å) and a_{Pt-Ge} (Å) for PtGe_n clusters.

Size (n)	Sym.	Eb (eV/atom)	ΔE (eV)	VIP (eV)	VEA (eV)	η (eV)	a_{Ge-Ge} (Å)	a_{Pt-Ge} (Å)
PtGe	C _∞	1.201	1.635	6.826	0.624	6.202	/	2.364
PtGe ₂	C _{2v}	2.064	0.785	7.293	1.272	6.021	2.468	2.533
PtGe ₃	C _{2v}	2.477	1.329	7.308	1.011	6.297	2.427	2.629
PtGe ₄	C _{2v}	2.703	1.393	7.451	1.224	6.227	2.615	2.757
PtGe ₅	C _s	2.802	1.326	7.519	1.431	6.088	2.833	3.001
PtGe ₆	C _{5v}	2.902	1.049	7.440	1.982	5.458	2.741	2.740
PtGe ₇	C _s	2.9596	1.574	7.242	1.456	5.787	2.772	2.719
PtGe ₈	C ₁	2.9598	0.958	7.067	2.067	5.000	2.795	2.656
PtGe ₉	C ₁	3.014	1.395	7.046	1.795	5.252	2.769	2.648
PtGe ₁₀	C ₁	3.064	1.753	7.243	1.640	5.603	2.795	2.605
PtGe ₁₁	C _s	3.086	0.919	7.008	2.370	4.638	2.672	2.806
PtGe ₁₂	S ₄	3.169	0.9789	7.069	2.471	4.598	2.653	2.856
PtGe ₁₃	C _s	3.146	0.954	6.560	2.064	4.495	2.696	2.888
PtGe ₁₄	C ₁	3.176	0.857	6.519	2.247	4.272	2.664	2.947
PtGe ₁₅	C _s	3.189	1.179	6.615	2.037	4.578	2.751	2.892
PtGe ₁₆	C ₁	3.188	1.544	6.808	1.952	4.856	2.742	2.906
PtGe ₁₇	C ₁	3.151	1.145	6.571	2.235	4.337	2.800	2.956
PtGe ₁₈	C ₁	3.159	1.178	6.612	2.276	4.336	2.764	2.919
PtGe ₁₉	C ₁	3.134	0.543	6.240	2.638	3.602	2.816	2.917
PtGe ₂₀	C ₁	3.143	0.809	6.415	2.592	3.824	2.704	2.949

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Figure 1: Lowest-energy isomer for PdGe_n (n=1-20) clusters.

Figure 2. Lowest-energy isomer for PtGe_n (n=1-20) clusters.

Figure 3. Binding energy per atom (E_b) for the most stable isomer of MGe_n ($\text{M}=\text{Pd}$, Pt and $n=1-20$) clusters.

Figure 4. Second energy differences ($\Delta_2 E$) for the ground-state isomer of MGe_n ($M=Pd, Pt$ and $n=1-20$) clusters.

Figure 5. HOMO-LUMO gap (ΔE) for the ground-state isomer of MGe_n ($M=Pd, Pt$ and $n=1-20$) clusters.

Figure 7. Vertical electron affinities (VEA) for the ground-state isomer of MGe_n ($\text{M}=\text{Pd}, \text{Pt}$ and $n=1-20$) clusters.

Figure 8. Chemical hardness (η) for the ground-state isomer of MGe_n ($M=Pd$, Pt and $n=1-20$) clusters.

Figure 9. Density of states (DOS) of $PdGe_{16}$ for alpha spin electrons. For each band, the Kohn-Sham orbitals are plotted. The electronic structure shows a shell filling with the following sequence: $1S^2 1P^6 1D^{10} 1F^{14} 2D^{10} 2S^2 2P^6 1G^{18} 1H^6$.