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Channel Characterization for Optical Extra-WBAN Links Considering Local and Global User Mobility

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ABSTRACT

We investigate channel characterization for wireless body-area networks (WBANs) in medical applications using optical signal transmission. More specifically, we focus on uplink communication from a central coordinator node (CN), placed on the patient's body, to an access point (AP) in a typical hospital room, which is usually referred to as extra-WBAN link. Using a ray-tracing based approach, we quantify the main characteristics of the optical channel while considering the effects of body shadowing and mobility (accounting for body movements and user global mobility inside the room). Based on the presented results, we discuss the impact of the positions of the CN and the AP on the link parameters. We also evaluate the link performance based on the outage probability criterion, and further quantify the performance improvement achieved by using multiple APs in the room.

Keywords: Wireless body-area networks; optical wireless communications; optical channel characterization; user mobility.

1. INTRODUCTION

E-Health solutions are gaining increasing popularity in a number of application scenarios as efficient means for improving the quality of life and reducing health-care costs.¹ Typical examples include real-time monitoring of patients in health-care centers and tele-monitoring post-operative patients or elderly people at home. These can be realized through the use of medical wireless body-area networks (WBANs) for sending timely data from several medical sensors. These sensors are typically connected to a coordinator node (CN), placed on the patient's body. The collected data at the CN is then sent to a mobile device or to a fixed access-point (AP) through what is called an extra-WBAN link.

Whereas a number of solutions have been proposed so far based on the radio-frequency (RF) technology mostly in the unlicensed frequency bands, the considerations of electromagnetic interference, data security, and the possible impact of RF waves on the tissues makes optical wireless communications of particular interest within this context.^{2,3}

We focus in this paper on extra-WBAN *uplink* communication, i.e., from the CN to the AP, and consider the characterization of the wireless optical channel by estimating the channel impulse response (CIR). An important point here is to take into account user mobility, which can considerably affect the link availability and performance. In this sense, most previous works have been based on simplified models in order to reduce the computational complexity. For instance,^{4,5} considered channel characterization for optical extra-WBAN links using a Monte-Carlo ray-tracing based simulation tool called Rapsor. In,⁴ downlink extra-WBAN transmission was studied while neglecting local body movements and assuming that the Rx (CN) is at a distance of 29 cm from the body. Also, the effect of patient's body was neglected in.⁵ In,^{6,7} user mobility was taken into account based on random user positions and random orientations of the sources and the detectors, considering uniform distributions. In contrast to these works, which consider simplified models, our study is based on more accurate and more realistic models with an acceptable level of details, in particular, concerning the body 3D shape and user mobility. More specifically, we propose a dynamic model based on 3D animation of a walk cycle to model body movement and random trajectories based on a modified random waypoint (RWP) mobility model. From

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Figure 1. Illustration of the considered placements for (a) the APs and (b) the CNs.

the simulated CIRs, we study different link metrics including channel DC gain and delay spread. We also present a stability analysis of the channel using the auto-correlation function (ACF) and the channel coherence time criteria. Moreover, considering the simple on-off keying (OOK) modulation, we evaluate the link performance in terms of outage probability and investigate the benefit of using multiple APs in the room.

The remainder of the paper is organized as follows. Section 2 presents the main assumptions on the considered WBAN link and the methodology for simulations. Numerical results are then presented in Section 3 to study different optical link metrics. Afterwards, we evaluate the outage probability of the link in Section 4 and investigate the performance gain offered by using multiple APs. Section 5 concludes the paper.

2. ASSUMPTIONS AND SIMULATION APPROACH

2.1 General Assumptions

Consider an extra-WBAN link between a CN on the patient's body and an AP. We consider two different placements for the CN, i.e., on the shoulder (the Rx pointing upward) and on the waist (the Rx pointing horizontally ahead), as suggested in,⁸ see Fig.1(b). For the former case, the communication link would be less affected by body shadowing when the AP is placed on the ceiling. We consider an LED at the transmitter (Tx) side, i.e., at the CN, emitting on infrared wavelength of $\lambda_0 = 850$ nm with a bandwidth of $\Delta\lambda = 30$ nm. Without loss of generality, we consider a Lambertian pattern³ for the LED. Also, in order to ensure minimum beam blockage, we consider a Lambertian order of $m = 1$, corresponding to a semi-angle of 60° . For the sake of simplicity, we assume an empty room, i.e., without any furniture or equipment.

At the receiver (Rx) side, i.e., at the AP, we consider a simple PIN photo-detector of 1 cm^2 active area without any lens and with a large field-of-view (FOV) of 60° (semi-angle). Note that the assumption of such a relatively large active area is justified by the fact that relatively low data-rates, on the order of 1 Mbps at most, are required in medical WBANs.⁹ To investigate the practical interest of using more than one AP at the Rx, we also consider the case where several APs are used in order to minimize beam blockage probability. For this, multiple APs will be considered either on the ceiling or on the walls of the room. Then, the received signals are combined based on equal-gain combining (EGC) or selection combining (SC, i.e., taking the strongest signal) strategies.¹⁰ Figure 1 shows the top view of the room with the considered positions for the APs, and also illustrates the considered positions of the CN on the body. As it can be seen, AP1-AP5 are symmetrically placed on the ceiling and point downward. Also, AP6-AP9 are placed at half width and 2 m height and point straight toward the center of the room. Note that, by default, we consider the case of AP5 (i.e., a single AP at the center of the ceiling).

Table 1. Simulation parameters.

Tx (CN)	m	1
	λ_0	850 nm
	$\Delta\lambda$	30 nm
Rx (AP)	FOV	60°
	Active Area	1 cm^2
	$\mathcal{R}$	0.65 A/W
Room ¹²	Dimensions	$(5 \times 5 \times 3) \text{ m}^3$
	Walls Reflectivity	0.83 (Plaster)
	Floor Reflectivity	0.87 (Pinewood)
	Ceiling Reflectivity	0.83 (Plaster)
Body	Dimensions	$(1.7 \times 0.3 \times 0.2) \text{ m}^3$
	Reflectivity	0 (absorbing)

Denoting the CIR by $h(t)$, we will in particular study the channel DC gain H_0 and the root mean squared (RMS) delay spread τ , defined in the following.³

$$H_0 = \int h(t) dt, \quad \tau = \sqrt{\frac{\int_0^\infty (t - \varepsilon_0)^2 h^2(t) dt}{\int_0^\infty h^2(t) dt}}. \quad (1)$$

Here, ε_0 denotes the mean excess delay spread, given by:³

$$\varepsilon_0 = \frac{\int_0^\infty t h^2(t) dt}{\int_0^\infty h^2(t) dt}. \quad (2)$$

To characterize channel time variations, we consider the channel coherence time. This is approximated by the point where the ACF falls below a certain value, e.g., 0.5. We will denote this by T_c .

Moreover, in order to quantify the link performance, we consider the outage probability P_{out} , which is defined as the probability that the bit-error-rate (BER) for a given channel realization is higher than a pre-defined threshold BER_{th} . We assume negligible background noise effect at the Rx, which can be justified assuming the use of a narrow-band optical filter.

2.2 Simulations Methodology

To estimate the CIR, we use ray-tracing based Monte-Carlo simulations using Opticstudio software from Zemax.¹¹ We set the reflection properties of the different surfaces according to¹² and consider at least 3 order reflections for beam propagation. To design the 3D scene for the simulator, we use the Blender software. We then use a Python script to load a set of configurations describing the user movements and orientations for a set of consecutive snapshots of a walk scenario. Afterwards, the CIR for different user positions and body configurations are calculated using Opticstudio, which we then use to analyze different channel metrics.

To study the effect of user mobility, we take into account both the change in the position of the user inside the room and the movement of the body parts, i.e., the arms, legs, etc. Concerning the former, which we will refer to as *global* user mobility, we have simulated a walk trajectory based on a modified RWP model. In contrast to the RWP model according to which the user moves in a straight line from one point to another,¹³ here we consider the movements of the user along a curved path by interpolating the waypoints using a 3-order polynomial. This provides a more realistic trajectory by avoiding sharp rotations. To consider the movements of the body parts, that we will call *local* mobility, we use a sampled walk animation sequence. Table 1 summarizes the parameters we have used in our simulations.

Figure 2. H_0 variations for the cases of CN1 and CN2 in the single AP configuration for AP5 and AP8 positions (see Fig. 1).

3. CHANNEL CHARACTERIZATION, NUMERICAL RESULTS

3.1 Channel DC gain

One of the most important channel metrics is its DC gain that directly determines the signal-to-noise ratio (SNR) at the Rx.

3.1.1 Single AP Configurations

Consider first the case of a single AP. Figure 2 shows the evolution of H_0 (in dB) for AP5 and AP8 as the Rx, as well as for the two cases of CN1 and CN2 (see Fig. 1). The abscissa represents the simulation time, assuming a walk speed of 0.45 m/s.

We observe from these results that, reasonably, we have a larger H_0 on average for the case of CN1 (located on the shoulder), compared to CN2 (located on the waist). Interestingly, the average H_0 is more or less the same, regardless of the position of the AP: the mean H_0 corresponding to CN1 and CN2 cases is around -53 and -55 dB, respectively (for both AP5 and AP8). An important result is that we notice larger H_0 variations and longer mean time between fades (MTBFs) for CN1, compared to CN2. For instance, with AP5, the range of variations of H_0 are around 9.2 and 4.4 dB, for CN1 and CN2 cases, respectively. The corresponding standard deviation is about 3 dB for CN1, and it ranges between 1 to 2 dB for CN2.

Larger H_0 variations are observed for AP8, with the range of variations of H_0 about 12.8 and 7.3 dB, for CN1 and CN2 cases, respectively. These relatively larger variations can be explained by the fact that AP8 (placed on the wall) is more sensitive to body shadowing resulting from body rotations during the walk trajectory (compared with AP5).

3.1.2 Multiple AP Configurations

Consider now the case where four APs are used for signal reception. Two configurations are studied: where the APs are placed on the ceiling (i.e., AP1 to AP4) or on the walls (i.e., AP6 to AP9), see Fig. 1. Based on EGC

Figure 3. H_0 variations for the cases of CN1 and CN2 in the multiple-AP configurations using EGC and SC detection methods.

or SC combination methods, we have shown the variations of the channel DC gain in Fig. 3 for the cases of CN1 and CN2. As expected, using multiple APs allows an increase in the mean H_0 and a reduction of its standard deviation, compared to the single AP configuration. Obviously, compared with SC, the EGC method (which provides performance close to the optimal maximal-ratio combining¹⁰) provides an improved performance, i.e., a higher average and a lower standard deviation for H_0 .

Compared with single AP configurations, here we have an improvement of the mean H_0 of 5.8 to 6.2 dB with EGC, and around 2.2 to 2.8 dB with SC (for both cases of AP1-AP4 and AP6-AP9). Meanwhile, similar to the case of single AP, we notice a higher average channel gain (about 1.1 to 2.6 dB) and larger variations (about 1.4 to 3.6 dB) for the case of CN1. Also, larger variations and shorter MTBFs are observed for the APs on the walls, compared with the APs on the ceiling.

3.2 Channel RMS Delay Spread

Channel delay spread is the key factor for quantifying channel frequency selectivity and the need to channel equalization at the Rx.¹⁴ From the simulated CIRs, we have calculated the mean and the standard deviation of the RMS delay spread, denoted by $\bar{\tau}$ and σ_{τ} , respectively. Results are presented in Table 2 for single and multiple AP configurations and the cases of CN1 and CN2.

For the single AP configurations, $\bar{\tau}$ ranges between 5.2 to 10.2 ns, with σ_{τ} between 1.9 and 4.4 ns. For AP5, we notice a smaller $\bar{\tau}$ with CN1, whereas a smaller $\bar{\tau}$ is obtained for AP8 with CN2. Comparing the cases of CN1 and CN2, we generally notice shorter $\bar{\tau}$ for the former, and lower σ_{τ} for the latter. A shorter $\bar{\tau}$ can be explained by a less shadowing impact on the direct (LOS, line-of-sight) path, given the random orientations and positions of the Tx.

For the multiple AP configurations, we notice the same trend and the same range of $\bar{\tau}$ for the cases of CN1 and CN2 as for the single AP configurations. Nevertheless, with EGC detection, we have a quite smaller σ_{τ} , especially for APs on the ceiling, but it is the inverse for SC detection, which is again rational.

Table 2. Mean and standard deviation (in ns) of the RMS delay spread.

Configuration			CN1		CN2	
			$\bar{\tau}$	σ_{τ}	$\bar{\tau}$	σ_{τ}
Single AP	Ceiling AP5)		5.2	4.4	10.2	1.9
	Wall (AP8)		7.3	4.2	8.3	3.7
Multiple APs	Ceiling (AP1-AP4)	EGC	4.7	1.6	11.3	0.8
		SC	7.9	3.8	7.1	3.6
	Walls (AP6-AP9)	EGC	6.1	4.2	8.6	2.9
		SC	7.4	3.0	9.5	1.9

Table 3. Estimated channel coherence time T_c (in sec) corresponding to the 50 % of the ACF, based on the simulated user trajectory.

Configuration			CN1	CN2
Single AP	Ceiling		4.2	1.4
	Wall		2.3	2.0
Multiple AP	Ceiling	EGC	1.5	1.0
		SC	1.4	0.9
	Walls	EGC	1.5	1.0
		SC	1.6	1.0

Overall, from these results and assuming simple OOK modulation, we can conclude that the communication channel can be considered as effectively frequency non-selective for data-rates up to approximately 10 Mbps, regardless of the position of the Tx. When AP(s) is (are) positioned on the ceiling, this condition is verified even for higher data-rates.

3.3 Channel Coherence Time

Channel coherence time T_c is a useful metric for characterizing channel time variations. It determines, for instance, the MAC layer parameters for setting the frame length and the transmission of training sequences. As explained in Section 2, to approximate T_c , we consider the delay where the ACF falls by 50%. The corresponding values are presented in Table 3. We have also presented the ACF plots for the different AP configurations and the cases of CN1 and CN2 in Fig. 4. The interesting point is the substantial reduction of the coherence time for the multiple-AP configurations. In particular, a reduction of factor 3 is observed for the case of CN1 with respect to the AP5 configuration. This means that despite the benefit of spacial diversity in reducing channel fading, we have a degraded channel stability due to a higher dynamic for the ensemble of underlying channels.

Focusing on the ACF plots, we further notice a different trend for CN1 and CN2 cases, for AP5 and AP8 configurations. These results are consistent with those previously presented for H_0 in Subsection 3.1. For instance, for AP5 with CN1, the LOS link is occasionally shadowed by the head of the user during relatively long periods, thus a more spread ACF and a longer T_c . Conversely, the LOS between AP5 and CN2 is more frequently subject to shadowing by the arms, resulting in more variations of H_0 , thus a more compact ACF and a shorter T_c . Similar trends are observed for the multiple AP configurations (see the low values of ACF on the plots). Here, focusing on T_c , we notice close values for for CN1 and CN2, independently of the position of the APs (i.e., on the ceiling or on the walls). Also, the SC method gives a slightly longer T_c .

4. LINK PERFORMANCE ANALYSIS

After presenting the main channel characterization metrics, we provide here a preliminary analysis of the link performance for the case of user mobility. Given the random time-varying nature of the channel, a relevant performance metrics is the outage probability P_{out} , which is defined as the probability that the instantaneous link BER falls below a pre-defined threshold BER_{th} . In order not to resort to time consuming simulations with

Figure 4. Calculated ACF for the cases of (a) CN1 and (b) CN2 and different AP configuration based on the simulated user trajectory.

Figure 5. Histogram of H_0 for 520 channel realizations for the case of CN1 and AP5 and estimated PDF by KDE with Gaussian kernel.

Opticstudio, we propose here a statistical model for the channel DC gain. This is obtained based on the non-parametric kernel density estimation (KDE), applied to the obtained results for the simulated user trajectory (see the previous section).

Given a set of N realizations x_i of a random variable x with probability density function (PDF) $f_X(x)$, the KDE estimate of the PDF is given by:¹⁵

$$\hat{f}_X(x) = \frac{1}{N\delta} \sum_{i=1}^N \mathcal{K}\left(\frac{x - x_i}{\delta}\right), \quad (3)$$

where $\mathcal{K}$ is the kernel and δ is the smoothing parameter, also called *bandwidth*. For the sake of simplicity, we consider here the case of a Gaussian kernel. We have presented in Fig. 5 for the case of CN1 and AP5 the histogram of the simulated H_0 together with the fitted PDF based on KDE. The corresponding δ is 0.18, which is calculated from¹⁶ $\delta = 1.06 \hat{\sigma} N^{-1/5}$, where $\hat{\sigma}$ is the estimated standard variation of $\log(x)$ related to (3), and $N = 520$.

Using this statistical model, we have randomly generated 10^7 values for H_0 . Then, for each channel realization, we calculate the BER for an uncoded OOK-based link for a given data-rate R_b and transmit power P_t . Note that we consider intensity levels of 0 and P_t for Off and On OOK symbols, respectively. The BER is calculated

Figure 6. P_{out} versus the transmit power P_t for different data-rates R_b for the cases of (a) CN1 and AP5, and (b) CN1 and AP1-AP4 with EGC detection. Uncoded OOK modulation.

using the following equation.³

$$\text{BER} = Q(\sqrt{\text{SNR}}), \quad \text{with} \quad \text{SNR} = \frac{(\mathcal{R} H_0 P_t)^2}{\sigma_{\text{th}}^2}, \quad (4)$$

where we have assumed that the dominant noise at the Rx is the thermal noise with variance $\sigma_{\text{th}}^2 = 4KT_e B/R_L$ with K being the Boltzman constant, $T_e = 298\text{ K}$ the equivalent noise temperature, B the system bandwidth, and R_L the load resistance of the trans-impedance amplifier, set to 50Ω .¹⁷ Parameter B is mainly determined by the Rx low-pass filter and is typically approximated by $R_b/2$. Also, in (4), $\mathcal{R}$ stands for the photo-detector responsivity, which is set to 0.65 A/W , and $Q(x) = \frac{1}{\sqrt{2\pi}} \int_x^\infty \exp(-u^2/2) du$.

For P_{out} calculation, we consider $\text{BER}_{\text{th}} = 10^{-3}$. We have shown in Fig. 6 plots of P_{out} versus P_t for R_b ranging between 10 Kbps to 1 Mbps. We have considered two cases of the link between CN1 and AP5, Fig. 6(a), and the link between CN1 and AP1 to AP4 with EGC signal detection, Fig. 6(b). Let us first consider the case of the single AP. We notice a degradation of P_{out} with the increase in R_b . Indeed, with increased link data-rate, and consequently, increased Rx noise variance (remember that the noise variance is proportional to R_b), a higher BER is obtained for a given H_0 . Obviously, for increased P_t , a lower P_{out} is obtained.

Now let us consider the case of multiple APs. We see from Fig. 6(b) that a considerably lower transmit power is required for a target P_{out} , for a given data-rate. For instance, for $P_{\text{out}} = 10^{-3}$ and $R_b = 500\text{ Kbps}$, the required transmit power is around 5 and 37 mW for the cases of four-AP and single-AP, respectively. This elucidates the substantial improvement achieved in the link reliability offered by spatial diversity. In fact, by comparing these results with Fig. 6(a), we can clearly see the impact of channel gain variations due to user mobility on the link performance. Lastly, note that in Fig. 6(b) for $R_b = 10\text{ Kbps}$, P_{out} is very low even for $P_t = 1\text{ mW}$ (that is why the corresponding plot is not seen in the figure).

5. CONCLUSIONS

This paper considered channel characterization for an optical-based extra-WBAN uplink for medical applications. Considering the typical case of a patient in a hospital room, we proposed an accurate approach for simulating body local and global movements and calculated the CIR. Different channel metrics were quantified, giving insight into the practical design of such systems. In particular, we studied the impact of the position of the CN on the patient body, that could be related to the practical implementation or user comfort reasons. Also, we showed the substantial improvement achieved in the link reliability when using multiple APs at the Rx, which is due to a significant reduction of beam shadowing during user movements. Although the use of multiple

APs increases the implementation complexity of the network, it can be justified given the achieved performance improvement, in particular, regarding the substantial reduction of the required transmit power.

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