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A Molecular Dynamics Simulation Study of Three Polysulfones in Dry and Hydrated States

GRÉGORY MARQUE,¹ JACQUES VERDU,² VALÉRY PRUNIER,³ DAVID BROWN¹

¹LMOPS, UMR CNRS 5041, Université de Savoie, Bâtiment IUT, 73376 Le Bourget-du-Lac, France

²LIM, UMR CNRS 8006, ENSAM, 151 Boulevard de l'Hôpital, Paris 75013, France

³EDF R&D, Site des Renardières, Moret-sur-Loing 77818, France

ABSTRACT: Molecular dynamics (MD) simulations of three polysulfones (poly(ether sulfone) PESU, poly(phenylene sulfone) PPSU and polysulfone PSU) in dry and hydrated states were undertaken in order to study the specific interactions between water and glassy polymer matrices of the same structural family. Dry polysulfone models were generated using a hybrid pivot Monte Carlo-MD single-chain sampling technique and the resulting relaxed densities were found to be in close agreement with experimental data. Hydrated systems are found to reproduce quite well volumetric changes experimentally observed. The concentrations of sulfonic groups can explain qualitatively their different water solubilities. Water is preferentially hydrogen-bonded to two sites which either link two polymer sites, or one polymer site and another water, or two other waters. A detailed

analysis of these water bridges that are formed is presented. Only a small quantity of potential bridging sites are occupied for water contents near the experimental saturation. The free fractional volumes, the probe accessible volumes, the swelling of the polymers, the water-polymer interactions and the hydrogen bond lifetimes, are also presented for these polysulfones. Water-water interactions and water clusters are found to be more important in the more hydrophilic PESU in comparison to the less hydrophilic PSU.

KEYWORDS: bridges; clusters; hydrogen bonds; molecular dynamics; poly(ether sulfone); poly(phenylene sulfone); polysulfones; simulations; water

INTRODUCTION The influence of absorbed water on structural,^{1–21} physical,^{1,11,18,21–37} mechanical,^{3,14,18,21,32,38–43} and electrical properties^{37,44–48} of polymers has been extensively studied and the consequent effects this can have during plastic processing has been highlighted.⁴ Hydrolysis of polymers by water is also a well-known phenomenon.^{3,18,43,49–61} For all these reasons, water sorption has been studied for many years mainly using techniques such as sorption isotherms,^{24,50,62–76} density or swelling measurements,^{1,11,22–35,49,77} differential scanning calorimetry (DSC),^{12,78–81} infrared experiments,^{6,28,81–100} dielectric measurements^{24,98,101,102} or nuclear magnetic resonance (NMR).^{12,78,79,102–106} Other specific experimental techniques have also been applied. The results of such experiments have mainly been interpreted in terms of Langmuir or Henry sorption mechanisms and water cluster existence (for the sorption isotherms), hole filling mechanism or additivity of water and polymer volumes (for density measurements), presence of “free” water (for DSC), hydrogen bonds and water arrangement (for IR), and “free” water and water linked to the polymer (for dielectric measurements and NMR). Such measurements have also given rise to, and been

used to discredit, a number of theories that have been proposed to explain water sorption in polymers. A relationship between the water solubility and the free fractional volume (FFV) of a polymer has been rejected by Schult et al. in a study on several polymers of a same structural family.⁶³ A correlation between the free space and the water sorption¹⁰⁷ has been discarded.^{49,64,108–110} Water absorption has also been directly correlated to the molecular formula of the polymer through a molar additive function of terms due to the constitutive groups of the monomer.¹¹¹ Attempts have also been made to apply the classical thermodynamic approach of polymer-solvent miscibility.^{111,112} Nevertheless, no real explanations of the underlying mechanisms have been provided by the aforementioned theories.^{49,64,108,109} Some authors have proposed that water molecules are doubly hydrogen bonded with hydrophilic sites in nylon 6,⁶² poly(ether imide),⁷⁷ amine/epoxy network,⁴⁹ or polysulfones.^{64,108} Interpretations of infrared spectra of other polymers have also considered such “water bridges.”^{83,88,98} From the variations of the water dissolution enthalpies in poly(ether sulfone) (PESU), poly(phenylene sulfone) (PPSU), and

FIGURE 1 The chemical structures of poly(ether sulfone) (PESU), poly(phenylene sulfone) (PPSU), and polysulfone (PSU).

polysulfone (PSU; see structures in Fig. 1), Gaudichet et al. have proposed that all water molecules are always doubly hydrogen bonded to two hydrophilic sites on the polymer in which case water solubility should be directly linked to the pair distribution of these hydrophilic sites.^{64,108}

Molecular dynamics (MD) simulations are of particular interest to test such hypotheses concerning the structure at the molecular scale. Many MD studies of hydrated bulk polymers like PESU,¹¹³ PA,^{114–116} amide-based structures,^{117–120} PMMA,¹²¹ BPA-PC,¹²² PEI,¹²³ PVA,^{122,124–131} EVOH copolymers,¹³² PEO,¹³³ PEO-based polymer electrolytes,^{134,135} perfluorinated ionomers,^{136,137} poly(phenylene sulfones),¹³⁸ sulfonated polyimides,¹³⁹ PE,^{140–142} PDMS,^{141–144} PP,¹⁴⁵ epoxy resins,^{98,146–148} polystyrene and copolymers,¹⁴⁹ rubbers,¹⁵⁰ polyacrylates,¹⁵¹ polyesters,¹⁵² or biopolymers^{153–155} have now been reported in the literature. They put forward water-polymer and water-water interactions through hydrogen bonds. Water clusters have been observed in different polymers (PE, PP, PS, SBR, EVOH, PA 6-6, PMDA-ODA),^{115,132,140,141,145,149,150,156} using different water models, such as SPC/E,^{115,141,156} TIP4P,^{140,145} or models available in commercial codes,^{98,132,149} and cluster sizes can exceed 10 H₂O molecules.^{115,156} However, the same model of water has been found to form clusters in some hydrated polymer systems and not in others.^{149,150} In the same vein, for the same polymer matrix, Tamai et al.¹⁴¹ find water clusters whereas Fritz et al.¹⁴³ do not; a result the latter explain by the use of a different water potential. Nevertheless, water cluster existence indicates that water interactions in a polymer can not be limited to interactions with polymer sites.

Several simulations have shown that water molecules diffuse in the polymer by a jump mechanism.^{116,118,129,131,141,143,145,149} For some authors, it implies cooperative motions of the polymer matrix and of the H₂O molecules.^{118,126} The Einstein diffusion regime is not always attainable for hydrated polymers under simulations of several nanoseconds near ambient temperature due to the diffusion coefficient of water being too low.^{116,119,149,150} Few studies report the density variations of the models with the water content. Only an initial increase followed by a decrease of the density of PA 6-6 and an epoxy resin have

been reported,^{115,148} as well as a continuous decrease of the density for PMMA above its glass transition temperature.¹²¹

Very short-time simulations (<200 ps) on dense models of polysulfone oligomers (<12 monomers of PESU, PSU, or PPSU) have been carried out.^{157–161} These PSU models have been used to examine their mechanical,¹⁵⁸ thermal,^{158,159} and dynamic properties.^{157,159,160} Gas transport properties have also been studied in PSU,^{160,161} PESU and PPSU systems.¹⁶⁰ Few simulations have been carried out on long-chain polysulfone models.^{113,162–165} However, the method of growing the chains used by Ahn et al.,¹¹³ Hölck et al.,^{163,164} and Heuchel et al.¹⁶² is known to give a bias in the configurations because of the ever-increasing density.¹⁶⁶ Furthermore, these authors use a complicated series of heating-cooling and compression-decompression cycles to try and approach the experimental density of the polymers. Despite this procedure, the densities of their models are only within ~5%,¹¹³ and ~2.7% for PESU¹⁶² and ~3% for PSU.^{162–164} This may not only be linked to the parameters used but also to the generation procedure.¹⁶⁷

Here, we apply a simpler and more reliable amorphous sample generation procedure to three long-chain polysulfone models (PESU, PPSU, and PSU) and simulate these systems in dry and hydrated states. The interaction potential is presented in “Interaction Potential” section. In “Dry Polysulfones” section, the hybrid pivot Monte Carlo-Molecular Dynamics (PMC-MD) technique^{167–179} is validated for these polysulfones and used to generate bulk models. In “Hydrated Polysulfones” section, different hydrated systems with different water contents are simulated and analyzed in terms of swelling, energetic properties, specific interactions between polymer, and water, existence of “water bridges,” water clusters and water mobility as a function of the water content.

INTERACTION POTENTIAL

The force field for polysulfones is based on the same as that already described for various polyimides^{167,171,172,180} and used recently for PMDA-ODA.¹⁵⁶ Only the main features will be outlined here. All bonds are modeled as rigid constraints¹⁸¹ so as to eliminate all the very high-frequency bond stretching modes. This allows for the use of an integration time step, Δt , of 10^{-15} s and avoids problems with the equipartition of kinetic energy. Continuous analytical “bonded” potentials are used to describe the energies associated with angle-bending, torsional rotations around the dihedral angles, and out-of-plane distortions of planar sp^2 structures. “Nonbonded” pair potentials are applied to all atom pairs belonging to different molecules and also between those on the same molecule that are separated by more than two bonds. The Van der Waals interactions between atoms of types i and j are of the Lennard-Jones (LJ) 12-6 form. The Ewald summation method is used to calculate the electrostatic potential.^{182,183} Polysulfone parameters were mainly taken from TRIPOS 5.2 force field.¹⁸⁴ However, this force field does not contain some parameters associated to the sulfonic group. For this reason, parameters for the S—O bond, the C—S—C flexion angle, the C—C—S—C and

C—C—S—O torsion angles were taken from MM3.¹⁸⁵ Partial charges were obtained by doing *ab initio* calculations using the Gaussian computer program¹⁸⁶ at the B3LYP/6-31G** level on small fragments.¹⁷¹ The actual values have been reported elsewhere.¹⁸⁷

As for PMDA-ODA,¹⁵⁶ the water model chosen is the extended single point charge model, SPC/E,¹⁸⁸ and Lorentz–Berthelot combination rules¹⁸⁹ were used to obtain the Van der Waals parameters for the interactions between water and the polymer. The MD simulations were performed using the *gmq* program¹⁹⁰ either in its scalar or in its parallel form on the Linux servers of the LMOPS and the University of Savoie as well as on the EDF “Rendvous” cluster in France.

DRY POLYSULFONES

Hybrid Pivot PMC–MD Single-Chain Sampling

The starting configurations for the polysulfones have been generated by the hybrid PMC–MD method¹⁷⁵ which has already been validated for a large variety of polymer chains.¹⁶⁷ With this technique, the configurational phase-space of a single polymer chain is efficiently sampled by interspersing occasional pivot Monte Carlo (PMC) moves¹⁹¹ for rotatable torsions, whilst performing standard molecular dynamics. As the method is based on Flory’s hypothesis¹⁹² that polymer configurations in the pure melt are only governed by near-neighbor intramolecular interactions, only a certain number of specific near-neighbor intramolecular interactions are considered between atoms separated by no more than a fixed number of backbone bonds (n_{bonds}). Above the glass transition temperature (T_g), this procedure leads to chain configurations similar to those obtained by doing MD with the full potential in the bulk melt. The procedure to define and validate n_{bonds} is thus to compare the configurational and conformational properties of chains sampled by the PMC–MD method (“single-chain”) with those of a fully interacting dense system of the same chains decorrelated by MD only (“bulk melt”). However, to decorrelate the bulk melt chains within a timescale accessible to MD simulations, this test is carried out both at high temperature and on short oligomers. In general, it has been found that optimum value of n_{bonds} is independent of chain length so the extension to longer chains is straightforward.¹⁶⁷

To optimize n_{bonds} for the three types of polysulfone, “single-chain” test systems containing one 4-mer chain were simulated for 10,000 ps at 750 K with the PMC–MD method for a range of values of n_{bonds} . For the “bulk melt” simulations, boxes containing 27 such oligomers were first constructed. MD simulations were then carried out for 15,000 ps under NpT conditions at 750 K in which the isotropic pressure, p , was maintained at 1 bar by loose coupling, with a coupling constant of 5 ps,¹⁹³ and the temperature, T , was held constant by weak coupling to a heat bath with a coupling constant of 0.1 ps.¹⁹⁴ Optimum parameters for the Ewald sum^{195,196} were $\alpha = 0.27$, $K_{\text{max}} = 9$ and $R_c = 7.5$ Å for the PESU and PPSU systems, and $\alpha = 0.25$, $K_{\text{max}} = 9$ and $R_c = 9$ Å for PSU. The Van der Waals potentials were truncated at

FIGURE 2 Single-chain-sampled (circles) vs. bulk melt (line) probability densities for the C—C—O—C pivot torsion angle in 4-mer PESU chains using $n_{\text{bonds}} = 4$ at 750 K.

9 Å in all systems and standard long-range corrections to the energy and the pressure were applied.¹⁸⁹

The decorrelation of the chains from their initial configurations was monitored by calculating the normalized autocorrelation functions for the end-to-end vector, $\mathbf{R}_i$, of the individual chains as a function of time:

$$C_R(t) = \frac{\langle \mathbf{R}_i(0) \mathbf{R}_i(t) \rangle - \langle \mathbf{R}_i \rangle^2}{\langle \mathbf{R}_i^2 \rangle - \langle \mathbf{R}_i \rangle^2} \quad (1)$$

The results (not shown) demonstrate that 8 ns is sufficient to decorrelate the end-to-end vector of the chains in all systems. The 4-mer PESU chains decorrelate notably faster due to their shorter length.

In Figure 2, the distributions of the C—C—O—C pivot torsion angle, τ , for both single-chain and bulk-melt relaxed chains of PESU are shown. This torsion angle has been found to be the most sensitive to the n_{bonds} value. Single-chain distributions for PESU are in good agreement with the bulk melt ones for a value of $n_{\text{bonds}} = 4$. The same value also gives good results for PPSU and PSU. A value of $n_{\text{bonds}} = 4$ is also found to be appropriate in the case of the C—C—S—C and C—C—C—C torsional angles for all three polysulfones studied here. Similar good agreement (not shown) is also found for the distributions of the mean square end-to-end distances $\langle R^2 \rangle$ and mean-square radii of gyration $\langle S^2 \rangle$. The value of $n_{\text{bonds}} = 4$ was thus considered optimal for its subsequent use in PMC–MD calculations for longer chains and for generating starting configurations of PESU, PPSU, and PSU for the multichain MD simulations of the bulk amorphous phases.

To choose an appropriate length of chain to use in the bulk simulations, PMC–MD calculations on single chains of PESU, PPSU, and PSU of different sizes (expressed in number of monomers n_{monomers}) with $n_{\text{bonds}} = 4$ were carried out. These showed that the ratio $\langle R^2 \rangle / n_{\text{monomers}}$ becomes

TABLE 1 The Number of Chains in the System (n_{chains}), Number of Monomers Per Chain (n_{monomers}), Total Number of Atoms Per System (n_{atoms}), and Convergence Parameters for the Ewald Sum and Van der Waals Potential for the Three Polysulfone Systems

Polysulfone	n_{chains}	$n_{\text{monomers}}/\text{chain}$	n_{atoms}	α	K_{max}	$R_c/\text{\AA}$	$R_{\text{vdW}}/\text{\AA}$
PESU	20	100	48,100	0.19	11	11.5	11.5
PPSU	20	50	45,100	0.17	9	12.0	12.0
PSU	20	50	54,100	0.20	12	11.5	11.5

number-independent for n_{monomers} in excess of about 20; the plateau values being ~ 135 (or ~ 270 if we consider the PESU unit being 2 monomers long), ~ 320 and $\sim 265 \text{ \AA}^2$ for PESU, PPSU, and PSU, respectively. To have similar chain lengths for the polysulfones in the remaining studies, chains of 50 monomers were constructed for PPSU and PSU whereas chains of 100 monomers were used for PESU. Given the chemical structures (Fig. 1), this leads to all chains having the same number of cyclic rings. Moreover, experimental measurements of number molar mass (M_n) report $\overline{M}_n^{\text{PESU}} = 26,675 \text{ g mol}^{-1}$ and $\overline{M}_n^{\text{PSU}} = 20,810 \text{ g mol}^{-1}$,⁶⁴ values which can be used to obtain the average number of monomers per chain by calculating the degree of polymerization, DP_n ,

$$DP_n = \frac{\overline{M}_n}{M_0} \quad (2)$$

where M_0 is the molar mass of one monomer. This gives average experimental chain lengths of ~ 115 and ~ 47 monomers for PESU and PSU, respectively. Corresponding weight molar mass (M_w) have also been given equal to $70,421 \text{ g mol}^{-1}$ and $49,944 \text{ g mol}^{-1}$ in the same work.⁶⁴ Other experimental values of M_w have been reported to be $49,000 \text{ g mol}^{-1}$ and $39,000 \text{ g mol}^{-1}$ for PESU and PSU, respectively.¹⁹⁷ Thus the size of the chains in our simulations are comparable to those used experimentally.

Generation of Dense Polysulfone Models

In the laboratory, the synthesis of polysulfones is generally carried out by polycondensation of 4,4'-dichlorodiphenyl sulfone with the respective phenolic monomer, i.e., the dihydroxy diphenyl sulfone for the PESU, the biphenol for the PPSU and the bisphenol A for the PSU. To terminate the polymerization, methyl chloride can be added into the polymerizing mixture and the reaction involves the conversion of aryl oxide ends to their respective methyl ethers.¹⁹⁸ Thus, theoretically, chain ends should be 50% chlorine and 50% methoxy endgroups. A BASF correspondent advised us that in reality, the proportion of methoxy endgroups was $\sim 60\%$ – 70% . For practical reasons we choose to only model chains with one chlorine and one methoxy endgroup ($\text{Cl}-\{\text{monomer}\}_n-\text{OCH}_3$).

In a first step, polysulfone chains are generated by PMC-MD single-chain sampling at temperatures corresponding to melt conditions (550 K for PESU and PPSU, and 500 K for PSU), i.e., slightly above their experimental glass transition temperature ($\sim 497 \text{ K}$ for PESU^{15,63,199–207} and PPSU,^{201,204,208} and $\sim 459 \text{ K}$ for PSU.^{9,15,16,63,163,199,204–212} Then, in a second step, 20 uncorrelated chains are randomly reoriented

and distributed in a periodic cubic MD box at an initial density close to the experimental values which are $\sim 1.37 \pm 0.01 \text{ g cm}^{-3}$ for PESU,^{197,199,201,204,206,207} $\sim 1.291 \pm 0.001 \text{ g cm}^{-3}$ for PPSU,^{204,209} and $\sim 1.238 \pm 0.001 \text{ g cm}^{-3}$ for PSU.^{9,29,197,204,206,207,209–215} To avoid unphysical spearings and interlockings²¹⁶ during the introduction of excluded volume, a « phantom » atom is briefly placed at the centre of mass of each six-atom ring.¹⁷⁵ The «bonded potentials» are then switched on progressively during short MD simulations under constant volume and temperature conditions (NVT). Phantom atoms are then removed, and electrostatic interactions are switched on. Details of the three systems and the nonbonded parameters used in each are reported in Table 1.

Following the introduction of the excluded volume, the systems were then relaxed under NVT conditions at 550 K (for PESU and PPSU) or 500 K (for PSU) until thermal equilibrium was established. The bulk systems were then cooled to 300 K at a rate of -1 K ps^{-1} , relaxed for 100 ps at NVT, before being further relaxed at constant pressure (NPT) conditions. In these, latter NPT simulations the on-diagonal and off-diagonal components of the required pressure tensor $\mathbf{P}$ were set to 1 and 0 bar, respectively. Once the densities and energies stabilized, production runs were carried out over $\sim 5000 \text{ ps}$ at both 300 K and 373 K. Configurations were stored every 5 ps for postanalysis. Simulations were performed on the EDF «Rendvous» cluster with the parallel version, *ddgmg*, of the *gmg* program, on 27 CPUs. Parallel efficiency, i.e., the ratio of CPU time to wall time, was very high at 99.94%.

Validation of the Dry Polysulfone Models

Average pressures in the production simulations were all close to the target pressure at $1 \pm 1 \text{ bar}$. The corresponding average densities for the dry polysulfone systems at 300 and 373 K are given in Table 2.

In comparison, the averages of experimental densities found in the literature are $\sim 1370 \pm 10 \text{ kg m}^{-3}$ for PESU,^{197,199,201,204,206,207} $\sim 1291 \pm 1 \text{ kg m}^{-3}$ for PPSU,^{204,209} and $\sim 1238 \pm 1 \text{ kg m}^{-3}$ for PSU.^{9,29,197,204,206,207,209–215} Relative differences between model densities at 300 K (Table 2) and experimental densities are about 1.6% for PESU, 1.7% for PPSU and 0.7% for PSU, which is reasonably satisfactory if we compare with previous work which reported differences of $\sim 5\%$ and 2.7% for PESU models,^{113,162} and $\sim 3\%$ for PSU models.^{162–164} Use of hydrogens as end groups,¹¹³ or possibly other end groups (such information is not always given) could be one reason for these differences, as could the different chain lengths used: 60 PESU monomers for Ahn

TABLE 2 Relaxed Densities (ρ) Average Potential (pot), Polymer–Polymer (pol–pol), Polymer–Water (pol–wat), and Water–Water (wat–wat) Potential Energies for the Dry and the Hydrated PESU, PPSU, and PSU Models

System	(ρ) (kg m ⁻³)	$U_{\text{pot}}^{\text{inter}}$	$U_{\text{pol}}^{\text{intra}}$	$U_{\text{pol–pol}}^{\text{inter}}$	$U_{\text{pol–pol}}^{\text{inter } LJ}$	$U_{\text{pol–pol}}^{\text{inter Coul}}$	$U_{\text{pol–wat}}^{\text{total}}$	$U_{\text{pol–wat}}^{\text{LJ}}$	$U_{\text{pol–wat}}^{\text{Coul}}$	$U_{\text{wat–wat}}^{\text{total}}$	$U_{\text{wat–wat}}^{\text{LJ}}$	$U_{\text{wat–wat}}^{\text{Coul}}$
PESU 300 K	1391.9	−69.5	37.2	−69.5	−58.0	−11.5						
PESU 373 K	1376.7	−67.7	49.9	−67.7	−56.5	−11.2						
PESU 1:8	1384.4	−73.9	49.6	−66.9	−56.2	−10.7	−6.1	−0.6	−5.5	−0.9	0.28	−1.2
PESU 1:4	1388.8	−80.2	49.6	−66.3	−56.0	−10.4	−11.2	−1.2	−10.0	−2.7	0.74	−3.4
PESU 1:2	1397.3	−92.6	49.4	−65.1	−55.2	−9.9	−20.1	−2.6	−17.5	−7.4	2.03	−9.4
PPSU 300 K	1313.2	−123.8	3.7	−123.8	−112.3	−11.5						
PPSU 373 K	1295.8	−120.5	27.4	−120.5	−109.3	−11.2						
PPSU 1:8	1301.4	−126.6	27.6	−120.2	−109.2	−10.9	−5.6	−0.6	−5.0	−0.9	0.24	−1.1
PPSU 1:4	1304.9	−132.4	27.1	−119.6	−108.8	−10.8	−10.1	−1.3	−8.8	−2.7	0.74	−3.5
PPSU 1:2	1310.9	−144.1	26.8	−118.3	−108.1	−10.3	−18.8	−2.8	−16.0	−6.9	1.86	−8.8
PSU 300 K	1229.8	−124.5	−45.2	−124.5	−113.5	−11.0						
PSU 373 K	1203.5	−120.1	−17.3	−120.1	−109.1	−11.0						
PSU 1:8	1207.7	−125.9	−17.6	−119.6	−109.1	−10.6	−5.6	−0.6	−5.0	−0.7	0.20	−0.9
PSU sat	1208.0	−128.0	−17.8	−119.2	−108.8	−10.4	−7.5	−0.8	−6.7	−1.3	0.34	−1.6
PSU 1:4	1211.7	−131.8	−17.7	−119.1	−108.8	−10.2	−10.3	−1.3	−9.0	−2.4	0.65	−3.0
PSU 1:2	1216.4	−143.4	−17.7	−118.0	−108.3	−9.8	−19.3	−2.7	−16.6	−6.1	1.64	−7.7
Max. error	0.8	0.2	0.2	0.1	0.1	0.1	0.3	0.2	0.3	0.1	0.02	0.1

Total U^{total} , intramolecular U^{intra} , and intermolecular U^{inter} energies are reported along with the specified Van der Waals U^{LJ} and Coulombic U^{Coul} contributions in kJ mol⁻¹ of monomer.

The maximum errors on each column are given by the line “Max. error.”

et al.,¹¹³ 210 PESU monomers for Heuchel et al.,¹⁶² 94 PSU monomers for Hölck et al.,^{163,164} and 210 for Heuchel et al.¹⁶² The influence of the generation procedure can also be a factor.

By applying average experimental linear expansion coefficients ($\alpha_i^{T \rightarrow T_0}$), determined in the range of 300–373 K, to the average experimental densities of PESU, PPSU, and PSU, we can have a good approximation to their experimental densities at 373 K ($\rho_{\text{exp}}^{373\text{K}}$):

$$\rho^T = \rho^{T_0} [1 - 3\alpha_i^{T \rightarrow T_0} (T - T_0)] \quad (3)$$

where ρ^T and ρ^{T_0} are the polymer densities at the temperatures T and T_0 (in kg m⁻³) and $\alpha_i^{T \rightarrow T_0}$ is the linear expansion coefficient of the polymer between T and T_0 (in K⁻¹)

Between 300 and 373 K, average experimental linear expansion coefficients found in the literature are $\sim 5.3 \times 10^{-5}$ K⁻¹ for PESU,^{42,204} $\sim 5.5 \times 10^{-5}$ K⁻¹ for PPSU,²⁰⁴ $\sim 5.1 \times 10^{-5}$ K⁻¹ for PSU.²⁰⁴ We can thus estimate $\rho_{\text{exp}}^{\text{PESU}373\text{K}} \sim 1354$ kg m⁻³, $\rho_{\text{exp}}^{\text{PPSU}373\text{K}} \sim 1275$ kg m⁻³ and $\rho_{\text{exp}}^{\text{PSU}373\text{K}} \sim 1224$ kg m⁻³. These differ by $\sim 1.7\%$, $\sim 1.6\%$, and $\sim 1.7\%$, respectively, from our model densities of PESU, PPSU, and PSU at 373 K (Table 2).

The average total intermolecular potential energies ($\langle U_{\text{pot}}^{\text{inter}} \rangle$), also given in Table 2, are due mostly to Van der Waals interactions ($\sim 83\%$ for PESU and $\sim 90\%$ for PPSU and PSU). This trend has already been seen in polyimides.^{156,171,176} Hilde-

brand solubility parameters of the models $\delta_{\text{model}}^{300\text{K}}$ have also been calculated at 300 K by using the following equation:

$$\delta = \sqrt{\frac{\langle U_{\text{pot}}^{\text{inter}} \rangle}{V}} \quad (4)$$

We have found: $\delta_{\text{PESU model}}^{300\text{K}} = 20.4$ (J cm⁻³)^{1/2}, $\delta_{\text{PPSU model}}^{300\text{K}} = 20.1$ (J cm⁻³)^{1/2}, $\delta_{\text{PSU model}}^{300\text{K}} = 18.6$ (J cm⁻³)^{1/2}. Rigorously, Hildebrand solubility parameters can only be experimentally determined on vaporizable molecules, which is not the case of our polymers. However, experimental techniques based on the wave propagation velocity of ultrasonic sounds in polymers,²¹⁷ or on viscosity measurements have also been used,²¹⁸ even if authors themselves warn strongly about the accuracy of their data. Empirical techniques to evaluate Hildebrand solubility parameters¹¹¹ can also be used but are rarely satisfactory, and the discrepancy of their results on a same polymer has already been shown.²¹⁹ Thus, empirical and experimental values reported by a same author using different techniques are found to vary between 21.3 and 28 (J cm⁻³)^{1/2} for PESU,²¹⁷ and between 17.38 and 21.79 (J cm⁻³)^{1/2} for PSU.²¹⁸ Using the increments given by Mat-suura et al.,²²⁰ we can also evaluate $\delta_{\text{PESU}}^{300\text{K}} = 22.3$ (J cm⁻³)^{1/2}, $\delta_{\text{PPSU}}^{300\text{K}} = 21.6$ (J cm⁻³)^{1/2}, and $\delta_{\text{PSU}}^{300\text{K}} = 20.3$ (J cm⁻³)^{1/2}. If the different methods lead to different values of the solubility parameter for the same polymer, we can see that our models agree favorably well with the trend $\delta_{\text{PESU}} > \delta_{\text{PPSU}} > \delta_{\text{PSU}}$.

The fractional free volume, FFV, in the dry models can be empirically calculated using the following equation:

$$\text{FFV} = \frac{V - V_0}{V} \quad (5)$$

where V is the actual volume and V_0 is the zero point molar volume. V_0 was taken as being 1.3 times the Van der Waals volume V_w of the polysulfone monomer calculated by a group contribution method ($V_w^{\text{PESU}} = 111.9 \text{ cm}^3 \text{ mol}^{-1}$ of monomer; $V_w^{\text{PPSU}} = 203.5 \text{ cm}^3 \text{ mol}^{-1}$ of monomer; $V_w^{\text{PSU}} = 234.2 \text{ cm}^3 \text{ mol}^{-1}$ of monomer).^{111,221} We have so calculated FFV values for our models at 300 K: $\text{FFV}_{\text{model}}^{\text{PESU300K}} = 0.130$, $\text{FFV}_{\text{model}}^{\text{PPSU300K}} = 0.135$, $\text{FFV}_{\text{model}}^{\text{PSU300K}} = 0.156$. FFV values for polysulfones under study have been reported in the literature.^{9,15,16,63,200,201,209–212} Nevertheless, the values used for V_w are not always clearly stated. We can calculate the experimental FFV from the average densities previously shown by using the same V_w values than those used with our models. In this case, FFV is calculated by:

$$\text{FFV} = \frac{\frac{M}{\rho} - V_0}{\frac{M}{\rho}} \quad (6)$$

where M is the molar mass of one mole of monomer (in g mol^{-1} of monomer) and ρ is the average experimental density of the polymer (in g cm^{-3}). So, with $M_{\text{PESU}} = 232 \text{ g mol}^{-1}$ of monomer, $M_{\text{PPSU}} = 400 \text{ g mol}^{-1}$ of monomer, $M_{\text{PSU}} = 442 \text{ g mol}^{-1}$ of monomer, we obtain $\text{FFV}_{\text{exp}}^{\text{PESU300K}} \sim 0.141$, $\text{FFV}_{\text{exp}}^{\text{PPSU300K}} \sim 0.146$, $\text{FFV}_{\text{exp}}^{\text{PSU300K}} \sim 0.147$, which compare quite well with our model values.

As far as the structures of the polysulfones under study are concerned, the indiscriminate intermolecular radial distribution functions for the chains $g_{\text{inter}}(r)$ do not show any sign of crystallinity, which is in agreement with the well-known amorphous nature of polysulfones.^{42,163,202,204,209,222,223} Experimental studies of the structure of these polysulfones are available in the form of X-ray diffraction patterns, see for example Figure 1 of Khayet and Garcia-Payo²²⁴ for PESU and Figure 8 of Aitken et al.²⁰⁹ for PPSU and PSU (labeled BIPSF and PSF, respectively, in their figure). In an attempt to make comparisons with experimental data, pseudo X-ray powder diffractograms (Debye formula) were generated using the DISCUS program.²²⁵ Diffractograms were obtained from the coordinates of configurations separated by 100 ps over the last 1 ns of the production runs of the pure polysulfones at 300 K. The average diffractograms for each polysulfone are shown in Figure 3.

The X-ray wavelength used in the calculations was $\lambda = 1.54 \text{ \AA}$, corresponding to that of Cu K_α radiation used in the experiments. All three model polysulphones show a single broad peak centered in the region from $\sim 16^\circ$ to $\sim 18^\circ$ in broad agreement with experimental studies.^{209,224,226,227}

Figure 4 shows the average distributions of pivot torsion angles in the dry PESU, PPSU and PSU from the simulations at 300 K. The C—C—S—C pivot torsion angle has a bimodal distribution at $\pm 90^\circ$ and the C—C—C—C angle shows favored

FIGURE 3 Pseudo X-ray diffractograms for the three pure polysulfones at 300 K.

positions at $\pm 127^\circ$ and $\pm 44^\circ$, in agreement with previous simulation results.^{159,160} The distribution of C—C—O—C angles shows maxima at $\pm 138^\circ$ and $\pm 44^\circ$, which agrees with the results of Niemela et al.,¹⁶⁰ whereas Hamerton et al.¹⁵⁹ find a broader bimodal distribution at $\pm 90^\circ$, which is not incompatible with our more resolved distributions.

To characterize the actual void space in the models, we use a version of the widely encountered “phantom sphere” geometric technique.^{216,228–231} Full details can be found elsewhere¹⁹⁰ but in this technique the probe accessible volume (PAV) is obtained by trial insertions of a virtual probe of a given radius at random positions in the polymer configurations. Probe insertions are then labeled “accepted” or “rejected” according to whether the probe overlaps with any of the atoms in the system; atoms being considered as hard spheres for this purpose with the following radii: C = 1.70 $\text{\AA}$, O = 1.52 $\text{\AA}$, S = 1.80 $\text{\AA}$, H = 1.20 $\text{\AA}$. The PAV is then defined as the product of the total volume and the fraction of “accepted” insertions. As such, the PAV gives just that part of the volume accessible to the centers of the probes. It does not give the actual volume that the entire probe can access. The PAV is just a simple way to compare different model systems under the same conditions.

The probe radii leading to a PAV equal to the $\text{FFV}_{\text{exp}}^{\text{300K}}$ previously determined, is 0.34 $\text{\AA}$ for PESU and PPSU, and 0.37 $\text{\AA}$ for PSU, whereas it has been found equal to 0.4 $\text{\AA}$ by Heuchel et al. for PESU and PSU.¹⁶² We can explain these differences by the lower densities of their PESU and PSU systems, by the possible use of different reference values for the FFV, and also by the use of slightly inferior radii for atoms of the polymer. Nevertheless, to a first approximation, the values are in reasonable agreement.

The qualitative distribution of the PAV was obtained by analyzing the connectivity of the positions of accepted probe insertions. Effectively two accepted probes are considered to be “linked,” i.e., in the same hole, if the distance between their centers is less than some arbitrary distance. Hole sizes are then obtained from a standard cluster analysis of the interconnected centers. As already said, this analysis can not be interpreted in terms of actual volume accessible and can

FIGURE 4 Probability densities for the (a) C—C—O—C, (b) C—C—S—C, and (c) C—C—C—C pivot torsion angles in the dry systems of PESU, PPSU, and PSU at 300 K.

just be used to compare different models under same conditions. No attempt to compare with experimental²³² or simulation^{161,162} results concerning the average cavity size in polysulfones will thus be done. Using a probe radius of 1.6 Å, with a cutoff distance linking the probe centers of 0.5 Å, leads to a distribution of void volumes which can be compared between the systems. All subsequent analyses will be done with these parameters. Moreover, 1.6 Å corresponds to the Van der Waals

radius of a water molecule if we consider a spherical geometry. Figure 5 shows the distribution of the amount of PAV, normalized by the total volume (V_{total}), in the polymer matrices in holes of different sizes for the PESU, the PPSU and the PSU at 300 and 373 K. The distributions have been averaged over all configurations stored during the 5 ns production runs.

Figure 5 shows a monotonically decreasing amount of PAV is to be found in holes of increasing size. There is no sign of cavitation, i.e., large holes, for any of the polysulfones considered. Increasing temperature gives rise to a fairly homogeneous increase in the PAV as the densities drop with temperature. The PAV in PSU is more important than in PESU or PPSU, which is consistent with our model values of FFV. The areas, Ω , under the curves displayed in Figure 5 give the total proportion of the volume of the polymer which is accessible to the center of a spherical probe of radius 1.6 Å, that is to say, accessible to the center of a probe of the same volume than the Van der Waals volume of a water molecule. The average values found were: $\Omega_{\text{PESU}}^{300\text{K}} = 0.00093$, $\Omega_{\text{PPSU}}^{300\text{K}} = 0.00086$, $\Omega_{\text{PSU}}^{300\text{K}} = 0.00127$, $\Omega_{\text{PESU}}^{373\text{K}} = 0.00123$, $\Omega_{\text{PPSU}}^{373\text{K}} = 0.00137$, $\Omega_{\text{PSU}}^{373\text{K}} = 0.00202$, $\Omega_{\text{PMDA-ODA}}^{373\text{K}} = 0.006$. As water solubility in PESU is about 2 times higher than those in the PPSU and in the PSU, this is an indication that the volume “accessible” to a water molecule does not govern alone the water uptake. In comparison to the polysulfones the PAV in PMDA-ODA at the same temperature is considerably higher and larger holes are present. This is consistent with its capacity to absorb more water and, as we will see, explains differences in the water clustering behavior.

HYDRATED POLYSULFONES

Water Insertion

The procedure of water insertion is the same as has been explained in a previous article.¹⁵⁶ In brief, to avoid large

FIGURE 5 Distribution of the amount of probe accessible volume in holes of different sizes. Data are normalized by the total volume of the respective MD simulation boxes and averaged over all configurations of the dry PESU, PPSU, and PSU systems at 300 and 373 K. For comparison, we include the results obtained from our previous simulation of PMDA-ODA¹⁵⁶ using the same probe size and at 373 K also.

overlaps and spearing of aromatic rings, an equilibrated simulation box of SPC/E water ($\rho = 958 \text{ kg m}^{-3}$, $T = 373 \text{ K}$), of the same size than the preprepared dry polymer one, is superimposed over the dry polymer one and the water molecules to insert are chosen amongst those which overlap least with the polymer atoms. Only a small number of steps of energy minimization are then required to remove any slight overlaps. The hydrated systems were then simulated using MD under NPT conditions at 373 K and 1 bar for 5100 ps. As for PMDA-ODA,¹⁵⁶ an elevated temperature was required to provide sufficient mobility of the water molecules to consider the time of the simulation sufficient for the study of the structural properties of water in the polymer matrices. The Ewald sum parameters and Van der Waals potential truncation radii were the same than those used for the dry systems (see Table 1).

We point out that the initial configurations chosen for the insertion of water were those at the start of the production runs of the dry systems. In this way, the dry and hydrated production runs can be considered as being carried out parallel in time and thus any underlying differences due to the slow relaxation of the polymer matrices are minimized.

The actual choice for the amounts of water to insert was based on experimental results. The average water content at saturation, w_∞ is defined to be the weight percentage of water uptake by polymers exposed to an environment of 100% relative humidity (100% RH),

$$w_\infty = \frac{m_{\text{water}}}{m_{\text{dry polymer}}} \quad (7)$$

where m_{water} is the mass of water into the polymer and $m_{\text{dry polymer}}$ is the mass of the dry polymer. Experimentally determined values of w_∞ in the range from 20 to 50 °C, have been found to be 2 wt % for PESU,^{15,42,64,199,200,204,233} 1.1 wt % for PPSU,^{64,204} and 0.7 wt % for PSU.^{9,15,16,29,64,199,204,213,233} In addition, the hydrophilic behavior of the polysulfones is generally attributed to their sulfonic groups (SO_2).^{64,108} For this reason, we have chosen to simulate systems with different ratios of water molecules per sulfonic group ($n_{\text{H}_2\text{O}} : n_{\text{SO}_2}$) spanning the range up to and beyond experimental saturation. System names are defined from the polymer matrix and the $n_{\text{H}_2\text{O}} : n_{\text{SO}_2}$ ratio. In other words, the system "PESU 1:2" is a poly(ether sulfone) with a ratio $n_{\text{H}_2\text{O}} : n_{\text{SO}_2} = 1:2$. Details of systems simulated are given in Table 3.

Experimentally estimates of the heats of dissolution of water in polymers are often obtained by first measuring the equilibrium uptake of water at a range of temperatures. Fitting the data to an Arrhenius law then gives an activation energy which is considered to be approximately $\Delta H_{\text{mixing}} = \Delta H_s + \Delta H_v$ ^{51,77} where ΔH_{mixing} is the mixing enthalpy of liquid water in the polymer, ΔH_s is the heat of dissolution of water vapor in the polymer and ΔH_v is the heat of vaporization of liquid water. From the known values of the heat of

TABLE 3 The numbers of Water Molecules, Corresponding H_2O Weight Percentages (eq 7), and Total Number of Atoms in the Dry and Hydrated Systems

Polymer	System	$n_{\text{H}_2\text{O}}$	Wt % of H_2O	Number of Atoms
PESU	Dry	0	0	48,100
	PESU 1:8	250	0.97	48,850
	PESU 1:4	500	1.93	49,600
	PESU 1:2	1000	3.87	51,100
PPSU	Dry	0	0	45,100
	PPSU 1:8	125	0.56	45,475
	PPSU 1:4	250	1.12	45,850
	PPSU 1:2	500	2.24	46,600
PSU	Dry	0	0	54,100
	PSU 1:8	125	0.51	54,475
	PSU sat	172	0.70	54,616
	PSU 1:4	250	1.02	54,850
	PSU 1:2	500	2.03	55,600

vaporization of water, indirect estimates of ΔH_s can then be obtained. For the polysulfones under study the averages of such available experimental estimates are $\Delta H_s^{\text{PESU}} = -43 \pm 2 \text{ kJ mol}^{-1}$, $\Delta H_s^{\text{PPSU}} = -42 \pm 4 \text{ kJ mol}^{-1}$ and $\Delta H_s^{\text{PSU}} = -37 \pm 2 \text{ kJ mol}^{-1}$.^{64,108,187,217} These values suggest a weak temperature dependence of the water content at saturation, $w_\infty(T)$, due to the fact that the decrease of water solubility with temperature is almost entirely compensated by the increase of the saturated vapor pressure of water.^{64,108–110} Experimental measurements of the water content at saturation in these polysulfones at 373 K and 100% RH ($w_\infty^{373\text{K}}$) tend to confirm this hypothesis ($w_\infty^{\text{PESU}373\text{K}} = 2.0 \pm 0.1 \text{ wt \%}$,^{187,202,217} $w_\infty^{\text{PPSU}373\text{K}} \sim 1.2 \text{ wt \%}$,¹⁸⁷ $w_\infty^{\text{PSU}373\text{K}} = 0.9 \pm 0.1 \text{ wt \%}$ ^{187,217}).

Volumetric and Energetic Properties

Figure 6 shows the relative variations of the volumes $\Delta V/V_{\text{dry}} = (V_{\text{hydrated}} - V_{\text{dry}})/V_{\text{dry}}$ at 373 K as a function of the water content for all three polysulfone systems. Experimental data obtained at ambient temperatures are also given for comparison in spite of the difference in temperature. Our experimental data were obtained using films of Radel R 5000 CL301 (PPSU) of thickness $e = 100 \mu\text{m}$, films of Radel A-200 (PESU), and films of Udel P-1700 NT-11 (PSU), both with $e = 125 \mu\text{m}$, provided by Solvay Advanced Polymers. Samples of $\sim 9 \text{ cm}^2$ were exposed to different relative humidity controlled environments as obtained above various saturated salt solutions: $\text{MgCl}_2 \cdot 6\text{H}_2\text{O} \approx 33\% \text{ RH}$, $\text{Ca}(\text{NO}_3)_2 \cdot 4\text{H}_2\text{O} \approx 55\% \text{ RH}$, $\text{NaCl} \approx 76\% \text{ RH}$, and $\text{ZnSO}_4 \cdot 7\text{H}_2\text{O} \approx 90\% \text{ RH}$.^{234–236} Densities have been experimentally determined by flotation in heptane-carbon tetrachloride mixtures at 297 K with solvents of analytical grade just after the withdrawal of the equilibrated samples of their RH controlled environment to avoid water loss. Volume expansions are then obtained from the experimental density measurements using the following expression

FIGURE 6 Average relative variations, $\Delta V/V_{\text{dry}} = (V_{\text{hydrated}} - V_{\text{dry}})/V_{\text{dry}}$, of the simulated PESU, PPSU, and PSU systems plotted as a function of the water content at 373 K. Average experimental data obtained from density measurements and eq 8 at 297 K are reported with their standard errors. Experimental data taken from the literature are also displayed.^{29,30}

$$\frac{\Delta V}{V_{\text{dry}}} = (1 + w) \frac{\rho_{\text{dry}}}{\rho_{\text{wet}}} - 1 \quad (8)$$

where ρ_{dry} is the density of the dry polymer, ρ_{wet} is the density of the hydrated polymer and w is the weight water content ($w = m_{\text{water}}/m_{\text{dry polymer}}$). Three measurements have been made for each sample and each RH.

Other experimental values from the literature are also shown in Figure 6. They are obtained from linear expansion coefficients, β_l , of the thickness of polymer films as measured by ellipsometry.^{29,30} Rowe et al. showed for their films that expansions in the transverse directions are negligible.²⁹ Thus we can, to a first approximation, consider β_l as being equal to the volume expansion coefficient.

In Figure 6, it appears that our models reproduce quite well the swelling behavior of the tested polysulfones. For water contents below and above the experimental saturation values, we observe volume expansions in the models. A global linear regression of all the data points suggests that the expansion could be zero up to ~ 0.3 wt %. A comparison can be made here with our previously published results for a model PMDA-ODA system, which did not show any swelling below the much higher value of ~ 3 wt % of water.¹⁵⁶ We had interpreted this as being due to a hole filling mechanism of water molecules being preponderant at water contents inferior to ~ 3 wt %; a result consistent with the comparison shown for the probe accessible volumes in Figure 5. At the time the available experimental data for PMDA-ODA was rather inconclusive with volume swelling at high RH varying from as much as 2.5% down to negligible values.^{24,31,34,237} Since then we have carried out our own experimental tests on PMDA-ODA (using Kapton® film) in the same manner as

described above for the polysulfones. These new measurements show a fairly linear amount of swelling in PMDA-ODA up to $\sim 1.5\%$ at saturation (~ 2.5 wt % of water).¹⁸⁷ It is interesting to note also that the swelling in this family of polysulfones is very similar despite their different hydrophilicities.

From these volume expansions, we can calculate the partial molar volume of one water molecule (δV) as a function of the water content in these polysulfones by using:

$$\delta V = \frac{\Delta V}{n_{\text{H}_2\text{O}}} \quad (9)$$

Figure 7 shows the partial molar volumes of H_2O (δV) as a function of the water content in the hydrated PESU, PPSU, and PSU models.

We can see that the partial molar volume of the water in these polysulfones generally increases with water content. Near experimental saturation, δV in PESU and PSU is $\sim 12 \text{ \AA}^3$ and $\delta V \sim 8 \text{ \AA}^3$ in PPSU. As was the case for PMDA-ODA,¹⁵⁶ these values are well below the partial molar volume of liquid water ($\sim 30 \text{ \AA}^3$), and even below the Van der Waals volume of a water molecule ($\sim 17 \text{ \AA}^3$). This is in agreement with the usual observation that hydrated polymers are far from ideal solutions at low water content.^{11,25,26} Tests of the swelling data using various empirical models shows that one based on the assumption of constant capacity, i.e., the ratio of Van der Waals to total volume, but incorporating a term to account for the “volume contraction” provided by the hydrogen bonds of the H_2O Van der Waals volume, gives the best predictions to the observations.¹⁸⁷

The distributions of void volumes in the dry and hydrated PSU systems, calculated with the same probe radius ($1.6 \text{ \AA}$) and distance linking the probe centers ($0.5 \text{ \AA}$) as already used for the dry systems are displayed in Figure 8. The PAV can be calculated with or without taking into account the

FIGURE 7 Partial molar volumes (δV) of water molecules as a function of the water content in the hydrated PESU, PPSU, and PSU models at 373 K.

FIGURE 8 Distribution of the amount of probe accessible volume as a function of the hole size in the dry and the hydrated PSU 1:2 models at 373 K. Calculations have been made with and without taking into account the space occupied by water molecules. Data are averaged over all configurations.

penetrants. The first option gives an idea of which type of holes H_2O occupies, whereas the second one characterizes the influence of the water molecules on the polymer matrix. By comparing the distribution of the PAV in the dry polymer to the hydrated system called PSU 1:2 with option 2, i.e. without taking into account space occupied by H_2O (“1:2 water occurred” in Fig. 8), we can see that the H_2O increases the amount of probe accessible volume for the existing hole sizes ($<120 \text{ \AA}^3$) and creates larger holes in the polymer matrix ($>120 \text{ \AA}^3$). However, no cavitation is created by the presence of H_2O , even for water contents two times superior than experimental saturation. The comparison of the PAV distributions in PSU 1:2 with options 1 (“1:2 water taken into account” in Fig. 8) and 2 (“water occurred”) also show that water molecules occupy holes superior to $\sim 20 \text{ \AA}^3$. Although not shown, the same trends are also seen for PESU and PPSU.

The average polymer–water $U_{\text{pol-wat}}^{\text{total}}$ water–water $U_{\text{wat-wat}}^{\text{total}}$ total potential, polymer–polymer intermolecular, $U_{\text{pol-pol}}^{\text{inter}}$, and intramolecular $U_{\text{pol-pol}}^{\text{intra}}$ energies were extracted and are reported in Table 2. An appropriate choice of normalization for the energies is slightly complicated in these three polysulfones. We have chosen to give energies in kJ mol^{-1} of monomer which in effect corresponds to a normalization by the number of SO_2 groups. This has some advantages in terms of comparisons of the electrostatic energies but is less meaningful for the Van der Waals term as the PESU monomer is about half the size of those in PPSU and PSU. For the hydrated systems, a normalization based on the number of water molecules is more appropriate. These factors have to be kept in mind in the following comparisons. The intermolecular (“inter”) terms were further resolved into their Van der Waals (“LJ”) and Coulombic (“Coul”) contributions. The consequences of the volume swelling are visible as a decrease (in absolute value) of the polymer–polymer inter-

molecular interactions. The intramolecular term $U_{\text{pol}}^{\text{intra}}$ decreases slightly with the water content. Changes in temperature have greater effects on it. The variations of the $U_{\text{pol-pol}}^{\text{inter-LJ}}$ and the $U_{\text{pol-pol}}^{\text{inter-Coul}}$ are similar. On the contrary, the polymer–water and water–water interactions increase (in absolute value) when the ratio $n_{H_2O} : n_{SO_2}$, i.e., the water content, increases. This was expected as all the added H_2O can interact with the polymer and the other H_2O molecules, and so bring an additional contribution. This contribution is mainly due to the Coulombic terms. It can be observed that the Van der Waals contributions of the water–water interactions are always repulsive. Qualitatively the variations with water content of the polymer–polymer, polymer–water and water–water energies are comparable from one polysulfone to another. In addition, the polymer–water and water–water interaction energies are quantitatively very similar in these three polysulfones, when expressed in terms of the number of SO_2 groups. The slight differences that exist can be used to propose a tentative classification of these polymers as a function of the importance of the polymer–water $U_{\text{pol-wat}}^{\text{total}}$ and water–water $U_{\text{wat-wat}}^{\text{total}}$ interactions: PESU $>$ PSU $>$ PPSU for $U_{\text{pol-wat}}^{\text{total}}$ and PESU $>$ PPSU $>$ PSU for $U_{\text{wat-wat}}^{\text{total}}$. Comparisons of the total intermolecular potential energy ($U_{\text{pot}}^{\text{inter}}$ on Table 2) with that expected on the basis of simple additivity show that the decrease in $U_{\text{pot}}^{\text{inter}}$ is more rapid than the ideal case. It is consistent with the results for the volume variations which, as shown above, are far from additive. This is also consistent with the negative values of the mixing enthalpies reported in Table 4 and calculated according to eq 10:

$$\Delta H_{\text{mixing}} = \frac{(n_{\text{monomers}} H_{\text{hydrated polymer}} - n_{\text{monomers}} H_{\text{dry polymer}} - n_{H_2O} H_{\text{water}})}{n_{H_2O}} \quad (10)$$

where ΔH_{mixing} is the mixing enthalpy (in kJ mol^{-1} of H_2O), n_{monomers} is the number of polymer monomers in the simulation box, n_{H_2O} is the number of H_2O molecules in the hydrated system, $H_{\text{hydrated polymer}}$ is the enthalpy of the hydrated system (in kJ mol^{-1} of monomer), $H_{\text{dry polymer}}$ is the enthalpy of the dry polymer (in kJ mol^{-1} of monomer) and H_{water} is the enthalpy of the SPC/E liquid water at 373 K (approximately $-42.3 \text{ kJ mol}^{-1}$ of H_2O). The values given in Table 4 suggest that water sorption is enthalpically more favorable in the PESU than in the two other polysulfones. From the average experimentally determined ΔH_s values given above ($\Delta H_s^{\text{PESU}} = -43 \pm 2 \text{ kJ mol}^{-1}$, $\Delta H_s^{\text{PPSU}} = -42 \pm 4 \text{ kJ mol}^{-1}$ and $\Delta H_s^{\text{PSU}} = -37 \pm 2 \text{ kJ mol}^{-1}$), we can estimate $\Delta H_{\text{mixing}}^{\text{experimental}}$ at 373 K using $\Delta H_{\text{mixing}} = \Delta H_s + \Delta H_v$ and the enthalpy of vaporization of water, ΔH_v (373 K) = $40.657 \text{ kJ mol}^{-1}$.²³⁴ Of course, the $\Delta H_{\text{mixing}}^{\text{experimental}}$ determined here can only be a rough approximation to the values at 373 K as the experiments have been carried out at lower temperatures. However, the values obtained: $\Delta H_{\text{mixing}}^{\text{PESU experimental}} \sim -2 \text{ kJ mol}^{-1}$, $\Delta H_{\text{mixing}}^{\text{PPSU experimental}} \sim -1 \text{ kJ mol}^{-1}$ and $\Delta H_{\text{mixing}}^{\text{PSU experimental}} \sim 4 \text{ kJ mol}^{-1}$, are somewhat less negative than is obtained by the models; although water sorption in PESU is again

TABLE 4 Mixing Enthalpies Calculated from Equation 10 in the PESU, PPSU, and PSU Systems with Different $n_{\text{H}_2\text{O}} : n_{\text{SO}_2}$ Ratios at 373 K

Ratio $n_{\text{H}_2\text{O}} : n_{\text{SO}_2}$	$\Delta H_{\text{mixing}}^{\text{PESU}}$ (kJ mol ⁻¹ of H ₂ O)	$\Delta H_{\text{mixing}}^{\text{PPSU}}$ (kJ mol ⁻¹ of H ₂ O)	$\Delta H_{\text{mixing}}^{\text{PSU}}$ (kJ mol ⁻¹ of H ₂ O)
1:8	-10 ± 1	-6 ± 3	-8 ± 3
~1:6			-7 ± 3
1:4	-8.9 ± 0.5	-7 ± 2	-6 ± 2
1:2	-8.6 ± 0.3	-6.3 ± 0.7	-5 ± 1

enthalpically more favorable than in PPSU and PSU. This result could perhaps be indicative of an overestimation of the water-polymer interaction in the models but the differences are probably too small to make any definite conclusions about this.

Figure 9 again reports the polymer-water and water-water total potential energies but this time expressed in kJ mol⁻¹ of H₂O, so as to try to better assess the behavior with increasing water content. The polymer-water potential energies reflect the finding above concerning the enthalpy that water clearly has a stronger affinity to PESU than to PSU or PPSU. It is also clear that the water-polymer energy is not independent of the water content. There is a general tendency for this contribution to diminish, in absolute terms, whilst a compensatory increase, in absolute terms, occurs in the water-water term.

Specific Interactions

Favorable interactions between different types of atoms have been identified by examining the corresponding intermolecular radial distribution functions, $g_{\text{inter}}(r)$, and certain are shown in Figure 10. As expected, water hydrogens, H_{wat} , have strong specific interactions with the sulfonic oxygens,

FIGURE 9 Polymer-water $U_{\text{pol-wat}}^{\text{total}}$ and water-water $U_{\text{wat-wat}}^{\text{total}}$ total potential energies in kJ mol⁻¹ of H₂O in the PESU, PPSU, and PSU systems at 373 K, as a function of their ratio $n_{\text{H}_2\text{O}} : n_{\text{SO}_2}$.

FIGURE 10 Intermolecular radial distribution functions $g_{\text{inter}}(r)$ between the water molecules (water oxygen O_{wat} or water hydrogen H_{wat}) and different sites of the polymer or of the neighbouring H₂O in the PESU 1:2 system at 373 K. The scale on the right axis is only for the $\text{H}_{\text{wat}}-\text{O}_{\text{wat}}$ rdf.

O_{sulf} , and the oxygens of neighboring H₂O, and, to a lesser extent, with the ether oxygens, O_{eth} . On $g_{\text{inter}}(r)$ distributions, this is characterized by a peak between ~ 1.4 and ~ 2.4 Å, which corresponds to the lower and the upper hydrogen bond distances between a hydrogen and an oxygen.^{238,239} Indirect peaks resulting from these interactions on distributions such as water oxygen O_{wat} and O_{sulf} , or sulfur S and H_{wat} are also present but at larger distances as can be seen in Figure 10 for the PESU 1:2 system. Thus, as seen in other atomistic simulations,^{115,116,118-120,124,127,130,132,133,136,138,146-148,151,156,180} the study of $g_{\text{inter}}(r)$ suggests the existence of hydrogen bonds between the water molecules and the hydrophilic sites. Hydrophilic sites identified in the polysulfones under study are O_{sulf} , O_{eth} , and O_{wat} .

As for PMDA-ODA,¹⁵⁶ hydrogen bonds have been characterized using a simple geometrical criteria. Based on the first minimum in the $g_{\text{inter}}(r)$ for $\text{H}_{\text{wat}}-\text{O}_{\text{wat}}$ and $\text{H}_{\text{wat}}-\text{O}_{\text{sulf}}$, and also on the experimentally-quoted limits of the hydrogen bonds,²³⁹ a hydrogen bond is defined each time a H_{wat} is less than 2.4 Å from a hydrophilic site ($d_{\text{H}\cdots\text{O}} \leq 2.4$ Å). Our experience with PMDA-ODA is that the $\text{O}\cdots\text{H}_{\text{wat}}-\text{O}_{\text{wat}}$ angle is not a discriminating parameter, which is also confirmed for these polysulfones; probability density distributions of the cosine of the $\text{O}\cdots\text{H}_{\text{wat}}-\text{O}_{\text{wat}}$ angle (not shown) show a single Gaussian peak centered at 180°.

The static and dynamic analysis of the hydrogen bonds (H-bonds) gives much information. To present this in a clear way, this study will be divided into two parts: "From the acceptor point of view" which is centered on the behavior of the acceptor sites of H-bonds, and "From the donor point of view" which concerns the way the H₂O molecules are hydrogen bonded.

From the H-Bond Acceptor Point of View

Figure 11 shows the ratio $n_{\text{O}_x\text{H-bonded}} : n_{\text{H}_2\text{O}}$ between the number of H-bonded acceptors (O_{sulf} , O_{eth} , and O_{wat}) and the

FIGURE 11 The ratio $n_{O_x \text{H-bonded}} : n_{H_2O}$ between the number of H-bonded acceptors (O_{sulf} , O_{eth} , and O_{wat}) and the number of water molecules plotted as a function of the ratio $n_{H_2O} : n_{SO_2}$ in the PESU, PPSU, and PSU hydrated systems at 373 K.

number of H_2O in the hydrated models of PESU, PPSU and PSU as a function of the water content, expressed as the ratio $n_{H_2O} : n_{SO_2}$. It is clear that significantly more O_{sulf} are hydrogen bonded with H_2O molecules than the other hydrophilic site in the polysulfones, O_{eth} . This confirms experimental studies which consider the O_{sulf} as the main reason for the hydrophilicity of these polymers.^{64,108} The values of $n_{O_x \text{H-bonded}} : n_{H_2O}$ superior to 1 arise due to water molecules forming two hydrogen bonds with two different acceptor sites. This phenomenon of “water bridging” will be discussed in the next section. It is also interesting to note from Figure 11 that although the proportion of O_{eth} sites H-bonded to water remains constant with increasing water content, that of the O_{sulf} decreases. The behavior of the H-bonding to O_{eth} sites suggests that it is driven simply by the water concentration; results proportional to water concentration are also obtained for the number of close encounters between atoms on the polymer chain and water molecules where no H-bonding is possible. The decrease in the proportion of O_{sulf} sites H-bonded to water is, however, concomitant with an increase in the proportion of water molecules H-bonded to others, i.e., clustering; at the lowest water content about a 1/4 of water molecules are H-bonded to others whereas at the higher contents this increases to about 1/2. This behavior reflects the findings, described above, for the behavior of the polymer–water and water–water interaction energies with water content and suggests that it is the interactions with the O_{sulf} groups which are responsible for the nonlinearity.

Some care should be taken interpreting Figure 11 because for water contents near experimental saturation, i.e., $n_{H_2O} : n_{SO_2} \approx 1:4$ for PESU and PPSU, and $n_{H_2O} : n_{SO_2} \approx 1:6$ for PSU, the ratio $n_{O_x \text{H-bonded}} : n_{H_2O}$ is about 1.2, 0.9 and 1.1 for PESU, PPSU, and PSU, respectively, which does not mean that almost all O_{sulf} are hydrogen bonded to one H_2O . In fact,

for these water contents, only $\sim 15\%$ of the O_{sulf} in PESU, $\sim 12\%$ in PPSU and $\sim 10\%$ in PSU are hydrogen bonded with a H_2O . In other words, at experimental saturation, more than 85% of the more hydrophilic sites of the polysulfones are still available. It has been suggested that this behavior could be simply due to the fact that some sites are inaccessible.¹¹⁵ We will return later to the accessibility of the hydrophilic sites.

As we have seen, at water contents near the experimental water saturation, $\sim 15\%$ of the O_{sulf} in the PESU, $\sim 12\%$ in the PPSU and $\sim 10\%$ of the O_{sulf} in the PSU models are hydrogen bonded with H_2O molecules at any particular instant in time. However, Table 5, which reports the percentages of different acceptors hydrogen bonded at least one time with a H_2O during the simulations, shows that these values are well below the percentages of the acceptor sites visited during the simulations. We can also add that, the values reported in the Table 5 are not the maximum values of sites potentially accessible since we do not observe a plateau in the timescale of the simulation. In other words, it is certain that 59.4% of the O_{sulf} are visited during the simulation of the PESU 1:4 system, and thus a minimum of 59.4% of O_{sulf} are accessible. However, without doing much longer simulations we do not have access to the total percentage of O_{sulf} accessible in this system. Of course, it could be argued that local fluctuations lead to only a subset of these sites being accessible at any one instant in time; demonstrating that this is or isn't the case might be feasible using simulation, *e.g.* by a judicious choice of initial configurations for the water molecules, but this has not been attempted as yet. We are certain though that interpreting the low ratio of water to polymer hydrophilic sites at experimental saturation by the permanent inaccessibility of a large fraction of the sites is incorrect.

Many water oxygens form at least one hydrogen bond during the simulation with another water molecule. The accessibility of these sites is largely related to H_2O mobility and this will be discussed later.

The dynamics of the H-bonds have also been analyzed. In our previous article on PMDA-ODA,¹⁵⁶ we had studied the

TABLE 5 Percentages of O_{sulf} , O_{eth} , and O_{wat} Which Form at Least One Hydrogen Bond with a Water Molecule Over a Period of 4000 ps at 373 K

System	% O_{sulf}	% O_{eth}	% O_{wat}
PESU 1:8	40.5	25.5	85.6
PESU 1:4	59.4	40.3	94.0
PESU 1:2	73.6	55.4	98.1
PPSU 1:8	35.2	20.1	80.8
PPSU 1:4	45.1	27.1	93.2
PPSU 1:2	60.7	39.9	95.8
PSU 1:8	39.3	20.4	75.2
PSU sat	43.1	21.8	81.4
PSU 1:4	48.4	27.1	92.0
PSU 1:2	66.5	42.8	94.8

continuous lifetime and looked at a correlation function analysis to take into account the global lifetime of the same H-bond in case it was alternately broken and reformed. In fact, the continuous lifetime analysis considers that such an H-bond is a different one after each break. Thus, it seems that it is more judicious to characterize the H-bond lifetimes by using a correlation function analysis, as has already been used in the past.^{240,241} Details of this analysis have already been given¹⁵⁶ so only the main steps will be explained here.

A function is defined for each pair ij of possible H-bond donors and acceptors, which just takes the values 1 and 0 according to whether an H-bond exists between them. In our case, this is simply based on their distance apart at time t , $r_{ij}(t)$, in the following way:

$$H\{r_{ij}(t)\} = 1 \text{ if } r_{ij}(t) \leq d_{H...O} \quad (11)$$

$$H\{r_{ij}(t)\} = 0 \text{ if } r_{ij}(t) > d_{H...O} \quad (12)$$

The autocorrelation function $R(t) = \langle H\{r_{ij}(0)\}H\{r_{ij}(t)\} \rangle$ then gives a description of the decay of the H-bond. In practice, we obtain this characteristic time for each type of H-bond from the normalized form of $R(t)$, which we refer to as $C(t)$.¹³⁰ The normalization is straightforward for these types of functions that only take values of 1 and 0 as $R(0) = \langle H\{r_{ij}(0)\}H\{r_{ij}(0)\} \rangle = \langle H\{r_{ij}(0)\} \rangle$:

$$C(t) = \frac{R(t) - \langle H\{r_{ij}(0)\} \rangle^2}{\langle H^2\{r_{ij}(0)\} \rangle - \langle H\{r_{ij}(0)\} \rangle^2} = \frac{R(t) - \langle H\{r_{ij}(0)\} \rangle^2}{\langle H\{r_{ij}(0)\} \rangle - \langle H\{r_{ij}(0)\} \rangle^2} = \frac{R(t) - R^2(0)}{R(0) - R^2(0)} \quad (13)$$

The normalized $C(t)$ thus gives the probability of an H-bond still existing between two atoms at some later time, given that it did exist at the time origin. As it could have been broken and reformed several times in the intervening time, it does not give the same information as the continuous lifetime analysis.

The resulting $C(t)$ all showed a similar behavior than that found for PMDA-ODA,¹⁵⁶ i.e., a highly nonexponential relaxation at short times and a slow exponential decay at long times. The combination of both these quite different behaviors had been found to be well fitted by using a weighted sum of a single exponential and a stretched exponential.¹⁵⁶ so the same expression was also used here:

$$C(t) = \lambda \exp\left(-\frac{t}{\gamma}\right) + (1 - \lambda) \exp\left(-\left(\frac{t}{\alpha}\right)^\beta\right) \quad (14)$$

The corresponding relaxation times, τ , could then be obtained from the best-fit values of the λ , γ , α , and β parameters and the analytical integration of eq 14:

$$\tau = \int_0^\infty C(t)dt = \int_0^\infty \lambda \exp\left(-\frac{t}{\gamma}\right) + (1 - \lambda) \exp\left(-\left(\frac{t}{\alpha}\right)^\beta\right) dt = \lambda\gamma + (1 - \lambda) \frac{\alpha}{\beta} \Gamma\left(\frac{1}{\beta}\right) \quad (15)$$

FIGURE 12 H-bond correlation times, as evaluated from eq 15, plotted for the hydrophilic sites O_{sulf} , O_{eth} , and O_{wat} in the PESU, PPSU, and PSU systems as a function of the $n_{\text{H}_2\text{O}} : n_{\text{SO}_2}$ ratio.

where the gamma function, $\Gamma(x)$, was estimated to high precision using a standard numerical technique.²⁴²

The values of τ obtained for H-bonds with the three types of acceptor sites on the polysulfone systems are displayed in Figure 12 as a function of the ratio $n_{\text{H}_2\text{O}} : n_{\text{SO}_2}$, i.e., the water content. In PMDA-ODA, the main hydrophilic sites were the carbonyl oxygens O_{carb} .¹⁵⁶ In polysulfones, a similar structure is encountered with main hydrophilic site O_{sulf} and with less interactive O_{eth} . The trend, $\tau_{O_{\text{carb}}} > \tau_{O_{\text{wat}}} \sim \tau_{O_{\text{eth}}}$, observed in PMDA-ODA is similar to that found here with $\tau_{O_{\text{sulf}}} > \tau_{O_{\text{wat}}} \sim \tau_{O_{\text{eth}}}$. Here also $\tau_{O_{\text{eth}}}$ is almost constant whereas $\tau_{O_{\text{sulf}}}$ and $\tau_{O_{\text{wat}}}$ decrease when the water content increases, which is in agreement with findings from MD simulations of PVA hydrogels and PEO solutions.^{130,133} No general trend of τ with the type of the polysulfone can be distinguished. However, it is clear that, for all types, the correlation lifetimes of the H-bonds are about twice as long in these polysulfones than in PMDA-ODA.¹⁵⁶ We can note here that the averages of experimentally determined diffusion coefficients of water in PMDA-ODA, PESU and PSU between 23 and 50 °C are $\sim 0.27 \times 10^{-8} \text{ cm}^2 \text{ s}^{-1}$,^{75,105,243-248} $\sim 8 \times 10^{-8} \text{ cm}^2 \text{ s}^{-1}$,^{64,199,200,249} and $\sim 9 \times 10^{-8} \text{ cm}^2 \text{ s}^{-1}$, respectively.^{9,16,29,64,199,213} This would suggest that the H-bond lifetime is not the critical parameter for defining water diffusion if the models reproduced the same tendencies for the diffusion coefficients. Unfortunately, as will be discussed later, a simulation time scale of 5 ns is insufficient to obtain diffusion coefficients of water in these dense polymer models. However, the observations do agree with Kucukpinar et al., who found that water diffusion was not really affected by the values of the water-polymer interactions in a model of hydrated NBR, and so deduced that these interactions do not govern the water diffusion.¹⁵⁰

From the H-Bond Donor Point of View

The average number of O_{sulf} , O_{eth} , and O_{wat} visited by one H_2O during a period of 4000 ps have been calculated from

FIGURE 13 Percentages of H_2O molecules which form one (1 H-bond) or two (2 H-bonds) hydrogen bonds through their hydrogens in the PESU, PPSU, and PSU systems with different $n_{H_2O} : n_{SO_2}$ ratios at 373 K. Water molecules not forming any H-bonds and those forming more than 2 H-bonds are not reported on this graph but represent $\sim 6\%$ of the total.

the production runs. From these averages, it is clear that at the same $n_{H_2O} : n_{SO_2}$ ratio the H_2O molecules visit more polymer sites in the PESU than in the PPSU and the PSU. This is particular the case as far as the O_{sulf} are concerned, e.g., 17.1 ± 0.5 , 12.1 ± 0.1 , and 12.7 ± 0.2 , for PESU, PPSU, and PSU respectively for a $n_{H_2O} : n_{SO_2}$ ratio of 1:8. This is consistent with Table 5 where we have seen that more acceptor sites on the polymer are visited in the PESU. However, it has to be remembered that there are twice as many sulfonic groups in the PESU system so their concentration is higher than PSU and PPSU. This would then suggest that water in fact is less mobile in PESU as the difference in the number of O_{sulf} groups visited for a given $n_{H_2O} : n_{SO_2}$ compared to PSU and PPSU is less than a factor of two. As will be seen later, this is what is found when the trajectories are analyzed.

Although it appears that for water contents up to the experimental saturation the number of O_{wat} visited in 4000 ps is small, ~ 5 to 8, and comparable to that of the O_{eth} , it again has to be taken into account that the water concentrations are lower compared to the other acceptor sites. The fact that the number of sites visited is roughly comparable results from the mobility of the H_2O molecules.

Figure 13 reports the percentages of water molecules forming 1 or 2 H-bonds through their hydrogens at the same time. Although there are “free” water molecules, i.e., not at all H-bonded, and even some H-bonded to more than 2 sites, the sum of these rarer kinds does not exceed 6%. We can see in Figure 13 that a majority of water molecules form two H-bonds and that there is only a small dependence of the percentages on the water content. This low dependence is in contrast to the behavior of the water-polymer and water-water interaction energies and suggests that subtle changes occur in the H-bonding pattern and this is discussed

in the next section concerning the water bridging. The actual percentages of water molecules with 2 H-bonds are very similar in PSU and PPSU, but are $\sim 15\%$ higher in PESU. This may be explained to a large extent by the higher concentrations of sulfonic groups in the PESU system compared to PSU and PPSU at the same ratio of $n_{H_2O} : n_{SO_2}$. Although this implies a higher concentration of water too in PESU, Figure 11 suggests this is not a big factor.

Water Bridging

As can be seen in Figure 13, $\sim 70\%$ in the PESU and $\sim 55\%$ in the PPSU and the PSU of the H_2O form two hydrogen bonds at the same time. The hypothesis of the existence of such H_2O molecules in polymers has already been made by experimentalists,^{62,64,83,88,98,108} and seen in simulations of hydrated polymers.¹¹⁵ In particular Gaudichet et al. have made the hypothesis that “water is always doubly bonded to polar groups by hydrogen bonds.”^{64,108} However, they only took into account O_{sulf} atoms as interaction sites, neglecting the O_{eth} and O_{wat} which have been shown in the present study to be important as well.

As shown in Table 6, the total number of bridges increases with the water content but the proportion of H_2O forming a bridge stays approximately constant in each polymer system. The more numerous water bridges at low water content link two polymer sites (P-W-P). Then, if the number of these kind of bridges increases with water content, the bridges linking one polymer site and one H_2O (P-W-W) gradually become as frequent. Few bridges are formed between two water molecules (W-W-W) at low water content but their proportion increases to slightly more than 10% at the highest concentration. This suggests that few water clusters exist at low concentrations but their number and size should increase with water concentration. A more extended study of the water clusters is done in the next section.

This gradual change in the bridging pattern with water concentration, most notably in the percentages of P-W-P and P-W-W bridges, is clearly the mechanism underlying the concomitant changes seen in the water-polymer and water-water contributions to the potential energy (Fig. 9). It is thus very likely that it also plays a key role in determining water solubility. Qualitatively, if the environment experienced by a water molecule resembles more and more that in pure water then the incentive to dissolve in the polymer must in some way diminish.

The less hydrophilic behavior of the O_{eth} is demonstrated by the low number of water bridges which imply O_{eth} . We also find some “cyclic bridges,” where both hydrogens from the same water molecule form a loop with only one acceptor, but this involves at the most, in all the simulations under study, 1% of the bridges for the O_{sulf} and less than 0.1% for the O_{eth} and O_{wat} sites. However, intramolecular bridges represent $\sim 7\%$ of the bridges in the PESU models, $\sim 5\%$ in the PPSU models, and $\sim 9\%$ in the PSU models. Minimum distances for O_{sulf} - O_{sulf} and O_{sulf} - O_{eth} oxygens of a same monomer are ~ 2.5 Å and ~ 6.6 Å, respectively, in the PESU, PPSU or

TABLE 6 Numbers and Percentages of the Different Types of Water Bridges Between Two Hydrophilic Sites

Systems	O _{sulf} -W-O _{sulf}	O _{sulf} -W-O _{eth}	O _{eth} -W-O _{eth}	P-W-P	O _{sulf} -W-O _{wat}	O _{eth} -W-O _{wat}	P-W-W	W-W-W	%H ₂ O
PESU 1:8	114 (59)	15 (8)	0 (0)	129 (67)	52 (27)	5 (3)	57 (30)	6 (3)	72
PESU 1:4	181 (48)	27 (7)	1 (0)	209 (55)	138 (36)	13 (3)	151 (40)	21 (6)	71
PESU 1:2	281 (36)	49 (6)	2 (0)	331 (42)	321 (41)	42 (5)	363 (46)	88 (11)	73
PPSU 1:8	37 (51)	10 (14)	0 (0)	47 (65)	20 (28)	3 (4)	23 (32)	2 (3)	55
PPSU 1:4	55 (37)	19 (13)	1 (1)	75 (50)	51 (34)	10 (7)	62 (41)	13 (9)	57
PPSU 1:2	97 (31)	31 (10)	2 (1)	130 (42)	115 (37)	26 (8)	141 (46)	37 (12)	59
PSU 1:8	40 (59)	10 (15)	1 (1)	50 (74)	14 (21)	2 (3)	16 (24)	2 (3)	53
PSU sat	55 (56)	12 (12)	0 (0)	67 (68)	24 (24)	4 (4)	28 (28)	4 (4)	56
PSU 1:4	61 (44)	17 (12)	1 (1)	79 (56)	44 (31)	8 (6)	52 (37)	9 (6)	54
PSU 1:2	106 (36)	34 (12)	1 (0)	141 (48)	101 (35)	19 (7)	120 (41)	31 (11)	56

P refers to a polymer site and W to a water site. The bridges have been analyzed over 5000 ps at 373 K both as a function of water content and as a function of the H-bond acceptor sites being O_{sulf}, O_{eth}, or O_{wat}. Results for each specific bridge type and each water content include the average number of bridges in the simulation cell and its total percentage with respect to the number of bridges in the systems (in parentheses) Columns "P-W-P," "P-W-W," and "W-W-W" are the sums of the water bridges formed between two polymer sites, one polymer site and another H₂O, and two H₂O respectively. The average percentage of water molecules acting as bridges is also displayed in the column "%H₂O."

PSU models. If we consider H-bond angles of 180° and lower and upper limit distances H_{wat}-O_{sulf} or H_{wat}-O_{eth} of 1.4 and 2.4 Å, the boundary distances between two hydrophilic sites so that a H₂O could form a bridge between them are 3.9 and 5.6 Å. Under these strict conditions, we would not have any "water bridges" between two acceptor sites of a same monomer and the intramolecular contribution would thus be due to the close approach of different parts of the same chain. However, to characterize the actual distances between water-bridged acceptor sites, each bridge has been examined and the distance, d , separating the two acceptor sites has been calculated. This distance has then been used to calculate the contribution, $g(d)$, to the corresponding radial distribution function for the pairs of hydrophilic sites actually engaged in water bridges. If we look at Figure 14, which reports this radial distribution function for the different types of bridges, we can see that the upper and lower bounds of d in our simulations are in fact $d_l = 2.4 \pm 0.1$ Å and $d_u = 6.0 \pm 0.1$ Å. This means that, within our purely distance defined definition of an H-bond, intramolecular bridges between two O_{sulf} of a same sulfonic group can exist. In fact, they represent $\sim 0.9 \pm 0.2\%$ of the bridges in the PESU and PSU models, and $\sim 1.9 \pm 0.4\%$ of the bridges in the PPSU models. They are characterized by a small peak at ~ 2.5 Å in the O_{sulf}-W-O_{sulf} distribution shown in Figure 14. We also observe a peak at ~ 2.7 Å in the O_{wat}-W-O_{wat} distribution. This peak results from configurations where the hydrogen atoms of one water molecule form H-bonds with oxygens in two other water molecules which themselves are already H-bonded. These two particular peaks are also visible on the PPSU and PSU hydrated models.

From the total radial distribution functions, $g(r)$, for the two types of atoms involved in bridges, it is also possible to calculate the number density of pairs of hydrophilic sites (n_{pairs}^{IJ}) which fall within the upper and lower bounds for d previously found:

$$n_{\text{pairs}}^{IJ} = \frac{1}{V(1 + \delta_{IJ})} \left(\frac{4\pi N_I N_J}{V} \int_{r=d_l}^{r=d_u} r^2 g(r) dr \right) \quad (16)$$

Where N_I and N_J are the numbers of atoms of types I and J, respectively, in the simulation box of volume V . The term $\delta_{IJ} = 1$, if $I = J$, or 0, if $I \neq J$, takes into account the double counting in the case of like types. In effect, n_{pairs}^{IJ} is an upper limit for the average number of "bridges" that could potentially exist at any one instant. In reality, some pairs can lie within the range of d required but not be able to be bridged by a water molecule due to other atoms occupying the space between them. At this stage, we make no attempt to assess

FIGURE 14 The contributions, $g(d)$, to the radial distribution functions of H-bond acceptor sites, which are involved in water bridges. $g(d)$ is reported for the different types of bridges in the PESU 1:2 system analyzed over 5000 ps at 373 K.

TABLE 7 Characteristics of Hydrophilic Sites

System (Number of H ₂ O nm ⁻³)	Number Density	O _{sulf} -W-O _{sulf}	O _{sulf} -W-O _{eth}	O _{eth} -W-O _{eth}	O _{sulf} -W-O _{wat}	O _{eth} -W-O _{wat}	O _{wat} -W-O _{wat}
PESU 1:4 (0.88 H ₂ O nm ⁻³)	n_{pairs}^H	21.7	20.9	4.7	6.4	2.7	1.0
	$n_{\text{intra pairs}}^H$	5.2	2.1	0.4			
	n_{visited}^H	7.5	2.6	0.3	10.5	2.7	2.7
	n_{formed}^H	0.32	0.05	0.002	0.24	0.02	0.04
PPSU 1:4 (0.48 H ₂ O nm ⁻³)	n_{pairs}^H	6.9	12.0	5.7	2.3	1.6	0.6
	$n_{\text{intra pairs}}^H$	2.2	0.8	0.4			
	n_{visited}^H	2.4	1.4	0.3	3.9	1.8	1.5
	n_{formed}^H	0.11	0.04	0.002	0.10	0.02	0.03
PSU 1:4 (0.41 H ₂ O nm ⁻³)	n_{pairs}^H	5.1	8.3	4.1	1.8	1.0	0.4
	$n_{\text{intra pairs}}^H$	1.9	0.8	0.4			
	n_{visited}^H	2.1	1.1	0.2	3.1	1.1	1.1
	n_{formed}^H	0.10	0.03	0.002	0.07	0.01	0.01

The numbers of pairs of hydrophilic sites (n_{pairs}^H) per nm³ potentially able to form a bridge, average numbers of bridges formed per configuration per nm³ (n_{formed}^H), and the cumulative numbers of different bridges visited by H₂O molecules in 4 ns of simulations per nm³ (n_{visited}^H) in the PESU 1:4, PPSU 1:4 and PSU 1:4 models. The intramolecular contribution $n_{\text{intra pairs}}^H$ to n_{pairs}^H is also displayed.

the importance of this possibility. In any case, it is highly likely that the formation of a bridge involves some local rearrangement of the atoms in proximity.

Values of n_{pairs}^H are displayed in Table 7 for the PESU 1:4, PPSU 1:4 and PSU 1:4 models. The values for the other hydrated and dry systems are very similar with just a slight trend of decreasing numbers of potential bridges with increasing water content. This would be consistent with the observed volume swelling and thus does not show any evidence of water promoting the number of potential bridging sites. Also shown in Table 7 are the average number of bridges actually formed per configuration per nm³ in our simulations (n_{formed}^H) and the cumulative number of different bridges visited by H₂O molecules in 4 ns of simulations per nm³ (n_{visited}^H). It can be seen that the PESU model has more “potential bridges” (n_{pairs}^H) than PPSU which in turn has more “potential bridges” than PSU. This trend is in agreement with the concentration of the total number of polymer hydrophilic sites (O_{sulf} plus O_{eth}) of the different models: ~10.7, ~7.8, and ~6.5 polymer hydrophilic sites/nm³ in the dry PESU, PPSU, and PSU, respectively. This trend is also consistent with that of the experimental equilibrium water uptakes at saturation of these polymers. If we consider just the sulfonic oxygens then their concentrations are: ~7.2, ~3.9, and ~3.2 per nm³, for the dry PESU, PPSU, and PSU, respectively.

As stated above, it is not certain that all these potential bridges are really accessible due to the neglect of steric hindrance in the calculation. However, the number of distinct bridges, i.e., between two specific acceptor atoms, actually visited increases inexorably during the simulation (curves not shown) suggesting that steric hindrance is not an insurmountable problem. It is, though, not possible to define an upper limit to the number of distinct accessible bridges without extending the length of the simulations considerably.

Concerning the equilibrium uptake of water at saturation, the PESU 1:4 and PPSU 1:4 models are those considered as the more representative of the experimental water saturation, whereas the PSU 1:4 model has more water than at saturation. In any case, the number of bridges actually formed at any one instant in our models is very much lower than the cumulative number of distinct bridges visited during the simulation, and we speculate from this that it is, thus, certainly lower than the number of accessible bridges. Previously we had shown that water uptake at saturation can not be explained simply by the number of accessible hydrophilic sites. Here we propose that it can not be explained either by the number of accessible bridging sites.

It can also be noted that the number of “potential intramolecular bridges” $n_{\text{intra pairs}}^H$ is already higher than the number of bridges formed n_{formed}^H . It is also perhaps necessary to explain why the number of visited W-W-W and P-W-W bridges can be superior to the number of potential bridges. Here, we compare a dynamic analysis (cumulative number of distinct bridges visited) with a static one (potential bridges). As the water molecules are relatively mobile, many “new” potential bridges are formed as the water molecules diffuse with time and some will be visited. Ultimately this leads to the average (static) number of “potential bridges,” n_{pairs}^H , being inferior to the cumulative number of distinct ones visited, n_{visited}^H .

Water Clusters

Experimentally, a common way to assess the degree of clustering of water molecules in polymer matrices is to plot curves of the volume fraction of water vs. water activity, as prescribed by the Zimm and Lundberg “cluster function” analysis.²⁵⁰ In this approach, the linearity in these sorption isotherms is interpreted as being due to the homogeneous dissolution of the water molecules in the polymer, whereas

nonlinearity is thought to be related to the clustering of water molecules.

No consensus exists concerning the shapes of the sorption isotherms of the polysulfones in the literature. As far as PESU is concerned, sorption isotherms are found to be totally linear,^{64,108} whereas others propose a concavity at low activities^{199,200} and an upward curvature at high activities.²⁰⁰ It is also reported that the low activity domain is not adequately resolved to talk about a concavity.^{203,249} For PSU, several authors find also linear curves,^{29,64,108,199,233} whereas other find a concavity at low activities with an upward curvature at high activities.¹⁶ To the best of our knowledge, PPSU sorption isotherms have only been published by Gaudichet et al. who find it to be linear, as in the case of PESU and PSU.^{64,108} A comparable discordance concerning the shapes of the sorption isotherms had previously been found for PMDA-ODA.¹⁵⁶ In fact, in most of the cases, it appears that similar shapes of sorption isotherms can be interpreted differently depending on the author. Some remarks of authors put forward difficulties of interpretations.^{203,233,249} Furthermore, we can not neglect the effect of the use of slightly different materials and equipment from one experiment to another.

Schult et al. have used the Zimm and Lundberg cluster function analysis on their PESU and PSU sorption isotherms.⁶³ They interpret its variations by the presence of water clusters in the PSU for activities superior than 0.5. However, they interpret a similar plot of the cluster function in PESU in terms of plastification of the polymer instead of presence of water clusters. For them, the presence of water clusters should induce a decrease in the rate of water diffusion which is not observed in PESU. According to them, it means that no water clusters exist in this polymer.⁶³ Yet, dielectric measurements on hydrated PESU, have been interpreted in terms of the presence of water clusters.²⁵¹

Water clusters have been analyzed in the model hydrated polysulfone systems using the same method than previously described in the case of PMDA-ODA.¹⁵⁶ We define water clusters through the aforementioned hydrogen bond criterion ($d_{H...O} \leq 2.4$ Å). A water molecule is considered to belong to the same cluster if it is hydrogen bonded to any other member of the cluster. The cluster size is then obtained from a standard analysis of the interconnected water molecules. We emphasize that this does not necessarily mean that each water molecule in a cluster has an H-bond with all other members of the cluster. This definition also means that water molecules in the cluster can also be H-bonded to the polymer. Probability density distribution functions for cluster sizes have been obtained from the production simulations. These distribution functions are shown in a form where they have been weighted by the cluster size in Figure 15 so as to give the amount of water involved in clusters of different sizes. For comparison with the relaxed systems, we have also calculated average “as inserted” distributions by repeating the initial water introduction step five times, with five different water configurations, on each dry polysulfone starting configuration.

FIGURE 15 The average amount of water found in clusters of a given size in the PESU 1:8, the PPSU 1:8, and the PSU 1:8 systems at 373 K. The averaged MD relaxed results are compared with those for the as inserted water molecules (see text for details).

First of all, we can see that, in the MD relaxed systems, there are few large water clusters at the relatively low water content, $n_{H_2O}:n_{SO_2} = 1:8$, reported in Figure 15 and 50%–60% of all water is isolated having no H-bonds with other water molecules. The amount of water involved in clusters of 7 or more molecules are negligible. This suggests that water clusters are much less favorably formed in polysulfones than in PMDA-ODA.¹⁵⁶ However, as already found in MD simulations of hydrated polymers, clusters can be larger than two or three water molecules.^{115,117,124,130,132,136,137,140,145} If we compare the average distribution of the amount of water in clusters for the “MD relaxed” systems with the “as-inserted” distributions, we can see that about 90% of the “as inserted” waters molecules are isolated from all others with clusters of four or more molecules extremely rare. This is in complete contrast to our previous results for PMDA-ODA where less than 30% of the “as inserted” water was isolated and clusters of 10 were initially present.¹⁵⁶ This confirms the results of the comparisons of the distributions of probe accessible volumes already shown in Figure 5 where the PMDA-ODA model displays a significantly larger quantity of PAV and a wider distribution of hole sizes than the polysulfone models.

The amount of water not involved in clusters, “isolated water,” is given as a function of the water content in Table 8. There is a clear decrease in the proportion of isolated water with increasing water content, as might be expected. This is consistent with the results shown for the potential energies, or the specific interactions. It is also interesting to note that about 1/12 of the H₂O added to the PESU 1:4 are isolated, $\sim 1/6$ of the H₂O added to the PPSU 1:4, and $\sim 1/5$ of the H₂O added to the PSU sat. In other words, even for higher water contents than the experimental saturation, added H₂O can be isolated. This means that, in the range of water

TABLE 8 Percentage of “Isolated” Water Molecules, That is, Water Molecules Not Involved in Any Clusters, in the Hydrated Polysulfone Models as a Function of Their Water Contents

Ratio $n_{\text{H}_2\text{O}} : n_{\text{SO}_2}$	% Isolated Water in PESU	% Isolated Water in PPSU	% Isolated Water in PSU
1:8	50.1	52.4	59.5
~1:6			53.0
1:4	33.1	34.9	39.8
1:2	20.9	25.4	30.6

contents studied, the polysulfone models are unlikely to be “saturated” in isolated H_2O .

The comparison of the polysulfone models at the same $n_{\text{H}_2\text{O}} : n_{\text{SO}_2}$ ratio (Table 8), gives the impression that more water molecules are involved in clusters in the order PESU > PPSU > PSU. However, if we instead make the comparison at the same water concentrations this has the effect of collapsing the results for PPSU and PSU on to the same curve (not shown) whereas the PESU has now less water involved in clusters than PPSU and PSU at water concentrations which can be compared.

The average mean square radii of gyration of the water clusters $\langle S_{\text{clust}}^2 \rangle$ are displayed as a function of cluster size in Figure 16 for polysulfones with $n_{\text{H}_2\text{O}} : n_{\text{SO}_2} = 1:2$ and for PMDA-ODA.¹⁵⁶ Results for $\langle S_{\text{clust}}^2 \rangle$ are very similar at different water contents. Only the results for the higher water contents are thus shown in Figure 16. We can see that for a given cluster size, $\langle S_{\text{clust}}^2 \rangle$ values are almost the same from one polymer to another. Discrepancies visible for large cluster sizes should mainly be related to the poor statistics available for these cluster sizes in polysulfones. It suggests that the shapes of water clusters should be similar in all these polymers. We had previously related the linear increase of $\langle S_{\text{clust}}^2 \rangle$ with the cluster size N as being due to more open geometries rather than globular ones; the latter following the relationship:

$$\langle S_{\text{clust}}^2 \rangle \approx \frac{3}{5} \left(\frac{3Nm}{4\pi\rho} \right)^{\frac{2}{3}} \quad (17)$$

with N the number of H_2O molecules in the cluster and m the mass of a water molecule. Equation 17 is applicable in the limit that globular clusters have a uniform density given by that of bulk liquid water (958.05 kg m^{-3} at 373 K). Figure 16 also displays $\langle S_{\text{clust}}^2 \rangle$ calculated by this way (“Globular”) and thus put forward the nonspherical geometries of the water clusters. This kind of geometry has already been observed in other simulation studies.^{98,115,136,137} Nevertheless, no simple or recurrent forms of clusters can be visually identified in the simulation movies. It appears that H_2O molecules involved in a cluster can stay in their clusters, leave it and come back later, or leave it definitively under the time-scale of the simulations. However, the water clusters persist during all the simulation, despite the changes in the constitutive members, without showing any evidence of displace-

ment. This has also been observed in other simulation studies.^{140,141,150}

Short Time Water Mobility

Our MD simulations being of relatively short duration, ~ 5 ns, with respect to real experiments, it is clear that only the very short time mobility of water molecules can be studied. All phenomena which occur on longer time scales are obviously beyond the range of this approach. With this in mind, the mean square displacements (MSD) for each type of atom in the dry and hydrated polysulfone systems have been calculated from the time-dependent positions, previously saved in coordinate trajectory files, in the following manner

$$\text{MSD} = \left\langle (\mathbf{r}(t) - \mathbf{r}(t_0))^2 \right\rangle \quad (18)$$

where $\mathbf{r}$ is the position vector of an atom, and the average is performed over all possible time origins t_0 . For the polymer atoms the MSDs are extremely small and in no case exceed $3 \text{ \AA}^2$ in 4000 ps. The curves obtained for water oxygens in the PESU 1:4, PPSU 1:2 and PSU 1:2 systems are shown on a log-log scale in Figure 17. For comparison the curve obtained for the PMDA-ODA system at 1.4 wt % water is also shown. All four of these systems are at similar water concentrations ($\sim 0.8 \text{ H}_2\text{O}/\text{nm}^3$). The MSDs of the water oxygens over 4000 ps in the hydrated polysulfone systems show that during this time the average root mean square displacements of the H_2O in the different models are comprised between ~ 10 and $\sim 14 \text{ \AA}$. A comparison with the dotted line of slope 1 shows clearly that this time scale is insufficient to reach the Einstein diffusive regime of water in these polymers at 373 K; the slopes being more in the region of 0.6–0.7. Up to a time interval of ~ 1000 ps water mobilities can be ranked in the four systems in the ascending order: PESU < PPSU < PSU < PMDA-ODA. At times beyond 1000 ps the curves for PESU

FIGURE 16 The mean square radii of gyration for the water clusters, $\langle S_{\text{clust}}^2 \rangle$, as a function of cluster size. Results are displayed for the polysulfones systems with $n_{\text{H}_2\text{O}} : n_{\text{SO}_2} = 1:2$, for a PMDA-ODA system,¹⁵⁶ and for the theoretical values for globular clusters based on the expression given in eq 17.

FIGURE 17 Mean square displacements (MSD) averaged over all time origins for water oxygens in the PESU 1:4, PPSU 1:2, and PSU 1:2 systems. For comparison, the curve obtained for the PMDA-ODA system at 1.4 wt % water is also shown.¹⁵⁶ All four of these systems are at similar water concentrations.

and PPSU become intermingled so predictions of the order in the limiting diffusion coefficients from short time data are hazardous. The higher MSDs in the case of PMDA-ODA are again consistent with the higher PAV and cluster size distribution which confer, at least at short times, greater mobility.

To study in more detail the mechanisms by which the water molecules move, simulation movies, created with VMD²⁵² from configurations stored at 5 ps intervals, were first studied. These showed that occasional jumps of H₂O molecules occurred within the time of two consecutive frames. As the disparity of jump durations and lengths make it difficult to make a quantitative study, free of arbitrary parameters to define what a jump is, it was decided instead to extract the self part of the Van Hove correlation function, $G_S(r, t)$. This function gives the probability density that an atom moves a distance r in a time interval t . The $G_S(r, t)$ functions of the sulfonic oxygens, the ether oxygens and the water oxygens in the PESU 1:2 system have been reported in Figure 18 for time intervals of 5 and 100 ps. As might be expected from the MSDs, the O_{sulf} and O_{eth} distributions just show a single peak at around 1 Å which only slightly broadens and diminishes in height between 5 and 100 ps. The distribution for water oxygens shows a quite different behavior with a first peak centered at slightly more than 1 Å and a substantial tail off towards higher r values. It is also evident that a lower second peak is formed at a distance of ~ 3 Å. This feature is evident also in the other systems and in the case of PMDA-ODA also. It persists in the case of polysulfones for at least 1000 ps. It is a clear signature of a hopping mechanism existing between neighboring binding sites which we presume to be on the polymer.

To characterize further these hops, the population of water molecules has been determined which move, in a time interval of 5 ps, a distance superior to a critical threshold, r_0 ,

defined from the maximum distance that a hydrophilic site on the polymer can move in the same time. The reasoning being that a water molecule hydrogen bonded to a site on the polymer can not move a distance $r > r_0$ without there being a high probability of breaking the H-bond. From the O_{sulf} and O_{eth} $G_S(r, t)$ functions at 5 ps, we have chosen an upper limit distance of $r_0 = 2.5$ Å. Percentages of H₂O moving a distance superior to r_0 are thus calculated from $\int_{r=r_0}^{+\infty} G_S(r, t) dr$ and are reported in Table 9. It appears that the percentages of water molecules moving a distance superior to 2.5 Å in 5 ps is comprised between ~ 13 and $\sim 22\%$ depending on the system considered. We have previously seen (see Fig. 17) that water molecules were more mobile in the order $\text{PSU} > \text{PPSU} > \text{PESU}$ at shorter times, which is corroborated here by the higher percentages of H₂O moving more than 2.5 Å in 5 ps in the PSU models in comparison with the other polysulfone models. We have also seen from the number of O_{sulf} , O_{eth} , and O_{wat} sites visited by one H₂O in a period of 4000 ps that, taking into account the higher concentration of hydrophilic sites, water moves less in PESU. Part of the explanation for this result could be that the O_{sulf} sites act as a trap for the water molecules; as the significantly longer H-bond decorrelation times of the O_{sulf} atoms demonstrate. Then the higher concentration of O_{sulf} , particularly in PESU where more water is to be found in bridging sites, leads to a higher probability of encountering another O_{sulf} and, thus, shorter displacements when a jump does occur. Further detailed analyses would be required to confirm, or infirm, this hypothesis, but it is almost certain that the influence of the other water molecules cannot be neglected.

CONCLUSIONS

Atomistic simulations of three long-chain amorphous polysulfone models (PESU, PPSU, and PSU) have been carried out in dry and hydrated states with water contents lower and higher than their respective experimental saturations. These dense models, each one containing more than 48,000 atoms,

FIGURE 18 The self parts of the Van Hove functions, $G_S(r, t)$, evaluated at time intervals of 5 and 100 ps for sulfonic oxygens, O_{sulf} , ether oxygens, O_{eth} , and water oxygens, O_{wat} , in the system PESU 1:2.

TABLE 9 Probabilities That a Water Molecule Moves a Distance Superior to 2.5 Å in 5 ps in the PESU, the PPSU, and the PSU Models at 373 K

System	Probability (%)	System	Probability (%)	System	Probability (%)
PESU 1:8	14.9	PPSU 1:8	19.5	PSU 1:8	21.5
				PSU sat	21.8
PESU 1:4	14.7	PPSU 1:4	19.8	PSU 1:4	21.5
PESU 1:2	13.2	PPSU 1:2	17.5	PSU 1:2	20.8

with chain lengths similar than those experimentally used, have been generated by the hybrid pivot Monte Carlo-Molecular Dynamics technique, which has been validated for $n_{\text{bonds}} = 4$. The dry bulk models prepared in this way relax, without any persuasion, to densities reasonably close to experimental values; at 300 K, the relative differences between the experimental densities and the model densities are $\sim 1.6\%$ for the PESU, $\sim 1.7\%$ for the PPSU, and 0.7% for the PSU.

Hydrated systems have been simulated for 5 ns at 373 K to obtain sufficient displacements of water molecules (~ 10 – 14 Å in 4 ns) for a reasonably representative sampling of different environments. All three model polysulfone systems swell to a very similar degree with the addition of water. The swelling is essentially linear above ~ 0.3 wt % water with a slope consistent with that from experimental studies. This is a quite different behavior to that found in PMDA-ODA where swelling only occurred above ~ 3 wt % water. This result correlates with the findings for the probe accessible volume which is significantly higher in PMDA-ODA thus leading to an initial hole-filling mechanism that is practically absent in the polysulfones. Further analysis of the probe accessible volume shows that water increases the size of the holes and creates some others in the polysulfone matrices without creating any cavitation. Water is also found to occupy these holes.

The swelling also leads to a decrease (in absolute values) of the intermolecular polymer-polymer energies. The polymer-water and water-water interactions are preponderant in giving negative values of the mixing enthalpies in the different systems. Although the sum of the water-polymer and water-water energies is proportional to water content the individual contributions are not. There is a general tendency for the water-polymer contribution to diminish in importance whilst a compensatory increase occurs in the water-water term. This results from a gradual change in the P-W-P and P-W-W bridging patterns with water concentration.

A study of the preferential sites of interactions indicates that the water molecules form hydrogen bonds with oxygens of the sulfonic groups (O_{sulf}), ether oxygens (O_{eth}), and also with other water molecules (O_{wat}). H-bonds with O_{sulf} are stronger and persist longer. About 70% of the H_2O in the PESU, and 55% in the PPSU and PSU are hydrogen bonded to two hydrophilic sites at the same time, and so form bridges between these sites. These bridges are mainly formed between two polymer sites (P-W-P) and between one polymer site and one other H_2O (P-W-W). A detailed analysis of these bridges showed that the minimum and maximum distances which can separate two hydrophilic sites spanned by a water bridge are

2.4 and 6 Å, respectively. With these limits we have been able to determine, from the corresponding radial distribution functions, the average numbers of pairs of hydrophilic sites which could potentially form bridging sites. These numbers are considerably higher than the actual number of bridges formed in each configuration of our simulations. Although the calculation does not take into account bridges that are unlikely to form due to steric hindrance, the cumulative number of distinct different bridges actually formed during the course of the simulations is considerably in excess of the instantaneous number of bridges formed, even at water contents close to experimental saturation. It thus seems unlikely that the equilibrium water uptake at saturation can be explained in a simple way by the number of accessible bridging sites.

Water clusters of a fairly limited size ($<7 H_2O$) have been found in the different hydrated polysulfone systems. This is in stark contrast to the PMDA-ODA hydrated models previously simulated which displayed a larger range of cluster sizes. This result again correlates with the findings for the probe accessible volumes. At comparable water concentrations, the tendency to form clusters is less marked in PESU whereas PPSU and PSU behave similarly. The clusters have a similar morphology in each polysulfone and their structure is more open than that of a dense droplet.

The H_2O molecules diffuse in part by a hopping mechanism in the polymer matrix. The populations of water oxygens which move more than 2.5 Å in 5 ps, i.e., hop, is higher in the order $PSU > PPSU > PESU$. This is also coherent with the mean square displacements of the H_2O molecules in the three polymer matrices at times less than 1000 ps. The 4 ns time scale of the simulations is too short to obtain the limiting Einstein regime diffusion coefficients.

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