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Bond-slip law and short tie behavior without main cracks

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ABSTRACT

The aim of this paper is to study the reinforced concrete short tie-rods behavior using the adhesion-slip curve shape between steel and concrete adopted by the European Concrete Committee. We are interested here in short tie-rods without main cracks for which we calculate and measure the maximum mobilization state of steel-concrete adhesion, and beyond the decrease mode of this bond. For this, tests of short tie-rods, with different high adhesion rebar diameters have been carried out. To characterize the first phase of the adhesion-slip behavior law (τ - g), pull out tests have been carried out with the same concrete, the same reinforcement and the same cross-section such as the tie-rod tests, with a proposed method to estimate the adhesion peak and the corresponding slip. For this adhesion peak value, slightly underestimated by the conventional curve of the European Concrete Committee, a new expression is suggested. A numerical model with theoretical relations of the behavior of such tie-rods is proposed. The comparison of this model with the obtained test curves of the short tie-rods shows a suitable approach. Also, we deduce that the steel (coated with concrete) fictitious module slope is even higher than the percentage of reinforcement is low. These results may help to understand the tie-rods behavior generally, in the phase of cracks stabilization, during which the tie-rod is composed of short tie-rods without main cracks.

1. Introduction

During dimensioning reinforced concrete structural elements (Reinforcement and stress testing), the contribution of tensioned concrete is totally neglected, which is sufficient in this case. However, for practical reasons, consideration should be given to:

- The estimation of the crack openings in the service limit state (SLS).
- The calculation of the mean rigidity of the tie rod to correctly evaluate the deformations at the SLS and even at the ultimate limit state (ULS) during the redistribution of forces in the hyperstatic structures (Effects of second order in shape stability and the response in alternating stresses).

Numerous studies have been carried out to evaluate the contribution of tensed concrete between cracks. Two types of approach are considered:

- The distribution hypothesis of the adhesion along the tie-rod, without involving the sliding [1].
- Using the equilibrium of forces and the compatibility of deformations from experimental relationships, such as the model of the European Concrete Committee [2], between the local stress of steel/concrete adhesion and the corresponding slip, to lead at the resolution of differential equations [3–5].

To express the solution of the problem, two types of formulation are distinguished:

- Mean fictitious behavioral laws of taut concrete, taking into account the addition of the reinforcement and concrete contributions to the cross section of the ‘tie rod’ [6–9].
- Fictitious behavioral laws of tensile steel (concrete-coated steel), implicitly taking into account tensed concrete in the form of a corrective term (Relative elongation deviation $\Delta\varepsilon$, between bare steel and concrete-coated steel for the same tensile force) [10–12].

Many studies have been carried out on the concrete steel connection, with series of experimental tests [13–16], mostly, the study of the geometry influence of the ribs on the resistance and rigidity [14] and the effects of passive and active confinement on the maximum stress of the bond [15]. Other studies propose models of local adhesion-slip relationships [13,17,18]. Several authors have investigated the behavior and estimation of crack openings [19–21] in the tie rods, and especially during the phase of stabilization of these cracks. During this last phase, the tie rod is composed of several ‘short tie rods’. The study of these latter makes it possible to understand how the forces redistribution is effected and the evolution of widths of crack openings because limited to the limit state of service by the different regulations around the world evolve [22].

The contribution of concrete, through experimental relations, is expressed here by fictitious behavior laws of steel in tension for short ties without major cracks.

To do this, pull out tests with different reinforcement diameters of high adhesion have been carried out to characterize the first phase of the law of stress-slip behavior ($\tau - g$) between steel and concrete. Short ties specimens were made with the same concrete, the same cross-section with varying the steel rebar’s diameter.

The adhesion-slip curve is obtained through pull-out tests [18,23–25] in order to characterize the curvilinear curve.

Tests on short ties, whose lengths are chosen so that no major cracks appear, will help us to better understand the mode of variation of the mobilization of steel/concrete adhesion and to propose behavior laws of steel in tension for such elements.

The behavior of short ties without major cracks also makes it possible to understand the response of tie rods in general [26]. In this work, the short ties without cracks highlight according to the loading and characteristics of the two materials the moment when a maximum mobilization of the adhesion is obtained. From this moment, it is interesting to see how this adhesion between steel and concrete decreases. This last observation makes it possible to understand the decrease of the contribution of the concrete after the stabilization of the cracks in a tie rod.

2. Curves ($\tau - g$) between steel and concrete adopted by the European Concrete Committee

The European Concrete Committee [2] adopted the stress-sliding relations 1, 2, 3 and 4 between steel and concrete. These curves (Figure 1) are derived from standardized steel bar coated with concrete pull out tests.

$$\tau = \tau_1 \left(\frac{g}{g_1} \right)^\alpha \quad \text{if } 0 \leq g \leq g_1 \quad (1)$$

$$\tau = \tau_1 \quad \text{if } g_1 \leq g \leq g_2 \quad (2)$$

$$\tau = -\frac{\tau_1 - \tau_r}{g_3 - g_2} g + \frac{\tau_1 g_3 - \tau_r g_2}{g_3 - g_2} \quad \text{if } g_2 \leq g \leq g_3 \quad (3)$$

$$\tau = \tau_r \quad \text{if } g \geq g_3 \quad (4)$$

The value of α is between 0.25 and 0.40 depending on the confinement of the concrete. The adhesion peak τ_1 is taken as:

$$\tau_1 = a \sqrt{f_{ck}} \quad (5)$$

With $a = 2.5$ for a confined concrete, otherwise $a = 2$

The normal compressive stress limit of the concrete f_{ck} is expressed in MPa. The value of the residual stress τ_r is taken equal to $0.20\tau_1$.

If the modeled curve (Figure 1) of the different phases seems rather representative, the intervals of variation of the different slips (g_1, g_2 and g_3) are closer to those given by Eligehausen [27].

These results (curves until adhesion depletion) are possible only if the percentage of steel in the concrete is very low, generally lower than the minimum ratio allowed by the various regulations around the world. For common cases [5,28], only the first curve (Figure 1) (relation 1) is effective.

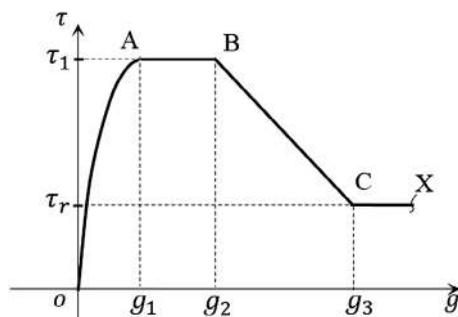


Figure 1. $\tau - g$ Curves adopted by the CEB.

3. Variation mode of stresses-deformations of short tie rods ($\sigma_s - \varepsilon_t$)

An analytical method is developed in this paper in order to study the short ties behavior based on the experimental results.

A short tie with a length ($l_t = 2L$), a section $A_t(a \times a)$ constant along the tie and a centered rebar section A_s , is considered and subjected to a variable tensile load N_t (Figure 2).

The normal stress $\sigma_c(x)$ in the concrete (with a Young Modulus E_c) is considered uniformly distributed and the normal stress in steel $\sigma_s(x)$ (with a modulus of elasticity E_s) remains lower to elastic stress of steel σ_e .

Figure 3 shows the normal stress-relative strain diagram ($\sigma - \varepsilon$) of the tie rod where ε_t represents the relative elongation of the tie rod and $\Delta\varepsilon_s$ the difference with the bare steel under the same normal stress $\sigma_{sn} = N_t/A_s$.

The rebar is embedded in the concrete and the origin of the abscissa is considered at the point O (Figure 4(a) and (b)). It is clear that, after the application of the load N_t , which is relatively small, the adhesion stress increases until it reaches a maximum, then decreases to zero at the abscissa l_1 , called introductory length, (Figure 4(c)). We suppose that the maximum of τ is located at the ends of the tie rod, Figure 4(d).

The normal stress in steel rebar and the relative elongation corresponding to the ends of the tie are denoted respectively σ_{sn} and ε_{sn} . The normal stress in steel is variable along $l_1, \sigma_{s1}(\varepsilon_{s1})$, and constant along $L - l_1, \sigma_{s2}(\varepsilon_{s2})$, Figure 4(e). Respectively, we have for concrete along $l_1, \sigma_{c1}(\varepsilon_{c1})$ and for $L - l_1, \sigma_{c2}(\varepsilon_{c2})$.

Here the concrete length is not long enough so that the mobilization of the adhesion allows to create a crack, (relation 6).

$$\int_L \tau(x).p.dx < A_c.f_{ctm} \quad (6)$$

With: f_{ctm} : Resistance (average) to effective tensile strength of the concrete; A_c : Net section of concrete subjected to tension ($A_c = A_t - A_s$).

3.1. Variation of the relative elongation of steel over the length l_1 of the tie rod

With (p) the useful perimeter of the steel section and $n = E_s/E_c$, the variations of the relative elongations of steel and concrete along the length l_1 are written respectively:

$$\varepsilon_{s1}(x) = \varepsilon_{sn} - \frac{p}{A_s.E_s} \int_0^x \tau(\xi).d\xi \quad \varepsilon_{c1}(x) = \frac{p}{A_s.E_s} \cdot \frac{n.p}{(1-\rho)} \int_0^x \tau(\xi).d\xi$$

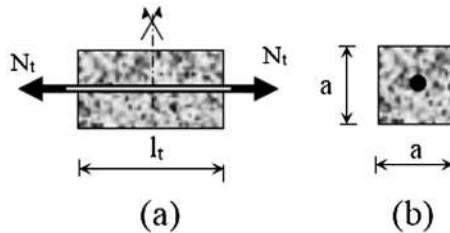


Figure 2. Short tie-rod, (a) View full length, (b) Straight section.

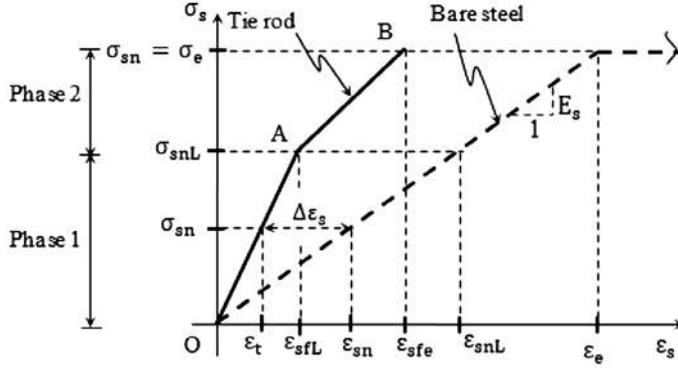


Figure 3. Diagram type $\sigma - \varepsilon$ of the short tie.

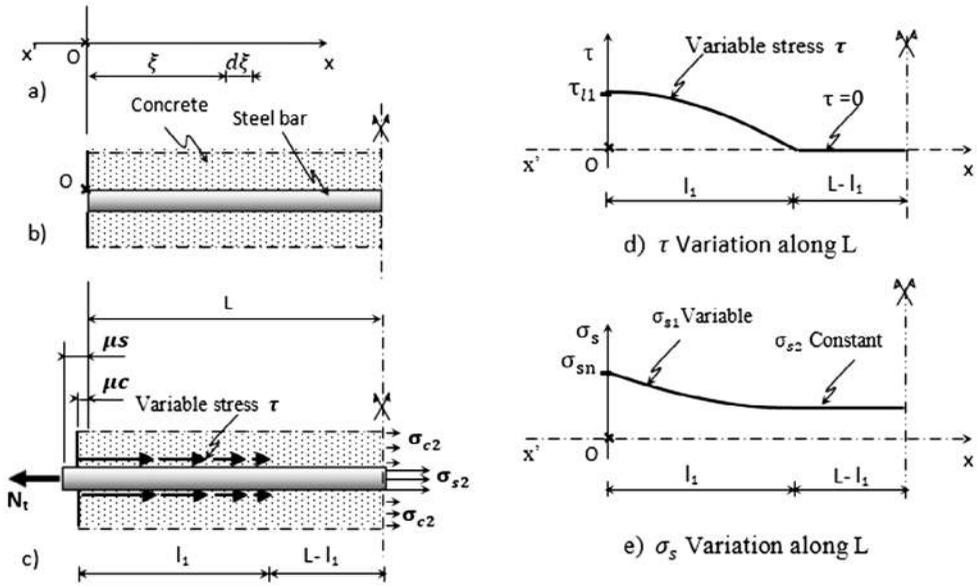


Figure 4. Slipping between steel and concrete and stresses generated under N_t in the tie.

For the two intervals of length l_1 on either side of the tie rod expressing the equilibrium of strength and the expression of the slip g between the elongations of steel u_s and concrete u_c , $g(x) = u_c(x) - u_s(x)$. We can write:

$$\frac{dg}{dx} = \frac{du_c}{dx} - \frac{du_s}{dx} = \varepsilon_c(x) - \varepsilon_s(x) \quad \Rightarrow \quad \frac{d^2g}{dx^2} = \frac{d\varepsilon_c}{dx} - \frac{d\varepsilon_s}{dx}$$

And the differential equation 7 can be obtained:

$$\frac{d^2g(x)}{dx^2} - \frac{p}{A_s \cdot E_s \cdot \bar{\rho}} \tau(x) = 0 \quad \text{Where} \quad \bar{\rho} = \frac{1}{1 + \frac{n \cdot \rho}{(1-\rho)}}, \quad \rho = \frac{A_s}{A_t} \quad (7)$$

The relation 8 represents the solution of the differential equation [3,4,12], and the variation of the bond stress τ can be deduced

$$g(x) = \theta^{1/(1-\alpha)} [l_1 - x]^{2/(1-\alpha)} \quad (8)$$

$$\text{where } \theta = \frac{\beta_1^2(1-\alpha)^2}{2(1+\alpha)}, \quad \beta_1 = \sqrt{\frac{k_1 \cdot p}{A_s \cdot E_s \cdot \bar{\rho}}}, \quad k_1 = \frac{\tau_1}{g_1^\alpha}$$

The variation of the adhesion along l_1 and its maximum at the extremities τ_{l_1} for $x = 0$ are written by expressions 9 and 10.

$$\tau(x) = k_1 \theta^{\alpha/(1-\alpha)} [l_1 - x]^{2\alpha/(1-\alpha)} \quad (9)$$

$$\tau_{l_1} = k_1 \theta^{\alpha/(1-\alpha)} l_1^{2\alpha/(1-\alpha)} \quad (10)$$

Thus, the normal stress exerted at the ends of the tie-rod (nude steel), replaced by its longitudinal relative deformation $\varepsilon_{sn} \left(\frac{dg}{dx_{x=0}} = \varepsilon_{sn} \right)$ can be written as:

$$\varepsilon_{sn} = \frac{2}{(1-\alpha)} \cdot \theta^{1/(1-\alpha)} l_1^{(1+\alpha)/(1-\alpha)} \quad (11)$$

The variation of the longitudinal relative deformation ε_{s1} of the steel along the length l_1 is deduced and after simplification we obtain the expression 12:

$$\begin{aligned} \varepsilon_{s1}(x) &= \varepsilon_{sn} - \frac{P}{A_s \cdot E_s} \int_0^x \tau(\xi) \cdot d\xi = \varepsilon_{sn} - \frac{P}{A_s \cdot E_s} \int_0^x k_1 \theta^{\alpha/(1-\alpha)} [l_1 - \xi]^{2\alpha/(1-\alpha)} \cdot d\xi \\ \varepsilon_{s1}(x) &= \left[1 - \bar{\rho} + \bar{\rho} \left(1 - \frac{x}{l_1} \right)^{(1+\alpha)/(1-\alpha)} \right] \varepsilon_{sn} \quad \text{for } 0 < x \leq l_1 \end{aligned} \quad (12)$$

3.2. Variation of the relative elongation of the steel over the length $(L - l_1)$ of the tie rod

At the distance x , comprised in the interval $[l_1; L]$ the behavior of the tie-rod is homogeneous, concrete and steel resist together to balance the stress N_t . There is compatibility in the deformations ($\varepsilon_{c2} = \varepsilon_{s2}$) and the sliding between the reinforcement and the concrete is equal to zero ($u_s = u_c$). We may write, in any straight section of this interval of the tie-rod:

$$N_t = \sigma_{c2} (A_t - A_s) + \sigma_{s2} \cdot A_s = \sigma_{c2} (A_t - A_s) + n \cdot \sigma_{c2} \cdot A_s$$

$$\frac{N_t}{A_s} = \sigma_{sn} = E_s \cdot \varepsilon_{sn} = E_c \cdot \varepsilon_{c2} \left(n + \frac{1-\rho}{\rho} \right) = E_c \cdot \varepsilon_{s2} \left(n + \frac{1-\rho}{\rho} \right) = E_s \cdot \varepsilon_{s2} \left(1 + \frac{1-\rho}{n \cdot \rho} \right)$$

$$\frac{N_t}{A_s} = E_s \cdot \epsilon_{sn} = \frac{E_s}{(1 - \bar{\rho})} \epsilon_{s2}$$

This gives the relation 13 which represents the constant relative elongation of the steel over the length $(L - l_1)$.

$$\epsilon_{s2} = (1 - \bar{\rho}) \cdot \epsilon_{sn} \quad \text{for } (L - l_1) \quad (13)$$

3.3. Proposition of a behavior law of short tie-rods ($\sigma - \epsilon$)

With theoretical results above and observations made by several authors on the slip between steel and concrete at the beginning of loading, we propose here laws of behavior $\sigma - \epsilon$ of the short tie rods.

This is in agreement with the study conducted by Giuriani [29] who showed that the sliding is effective for the spline bars only after a certain pulling force, and thus the $\tau - g$ curve does not pass through the origin of the abscissa g .

Eligehausen & al [27] reported that the slope of the curve is relatively high at the beginning. By increasing the pulling force of the bar, the ribs of the steel rebar abut on the concrete and begin to crush it. At this moment, the first cracks appear and the slip at this stage is relatively small (point A in Figure 5). The partial shearing of concrete rods results in a reduction in the slope between point A and B. The point C represents the moment when the maximum adhesion stress is obtained if the confinement is sufficient. Then the residual stress decreases due to the friction along the sheared concrete zone in the descending branch.

For our study, with relations 12, 13 and Figures 3 and 4, assuming a linear variation of $\sigma - \epsilon$ curve of short tie, the diagrams slopes (minimum and maximum) can be deduced for phase 1. With relation 12, when $l_1 = L$, we obtain the minimum slope:

$$\begin{cases} \epsilon_{s1} = \epsilon_{sn} & \text{if } x = 0 \\ \epsilon_{s1} = (1 - \bar{\rho})\epsilon_{sn} & \text{if } x = l_1 \end{cases}$$

As a first approximation, we can take the average: $\epsilon_{s1} = \left(1 - \frac{\bar{\rho}}{2}\right)\epsilon_{sn}$ and the minimal slope represented by the fictitious module is deduced: $\frac{E_s}{1 - \bar{\rho}}$

With relation 13, when l_1 tends to 0, we obtain the maximum slope either: $\frac{E_s}{1 - \bar{\rho}}$

So for the first phase, the dummy module E_{f1} is equal, relation 14

$$E_{f1} = \frac{E_s}{\psi_1} \quad \text{with } (1 - \bar{\rho}) < \psi_1 < \left(1 - \frac{\bar{\rho}}{2}\right) \quad (14)$$

For phase 2, after maximum mobilization of the adhesion between steel and concrete, this bond deteriorates and only a residual adhesion remains, in this case it is possible to take as fictitious module E_{f2} , relation 15

$$E_{f2} = \frac{E_s}{\psi_2} \quad \text{with } 0,8 < \psi_2 < 0,9 \quad (15)$$

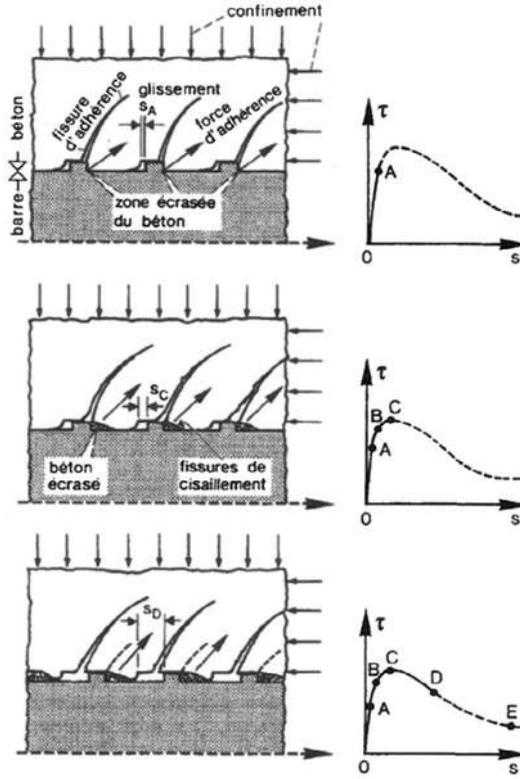


Figure 5. Adhesion mechanism and diagram from the full bond-sliding relationship according to Elgehausen et al. [27].

The ψ_1 and ψ_2 values are less than unity and will be estimated after carrying out the experimental tests.

The curve $\sigma - \varepsilon$ limit points of the short tie rods are A and B Figure 3.

At point A, at maximum mobilization of adhesion ($l_1 = L$), Figure 4(e) and using relation 11, the relative elongation of bare steel is written, expression 16.

$$\varepsilon_{snL} = \frac{2}{1-\alpha} \cdot \theta^{1/(1-\alpha)} L^{(1+\alpha)/(1-\alpha)} \quad (16)$$

We have also: $\sigma_{snL} = E_s \varepsilon_{snL}$

In our study, the normal stress in steel is limited to σ_e (also ε_e) corresponding to the fictional relative elongation of steel ε_{sfe} represented by point B, Figure 3 and determined by relation 17.

$$\varepsilon_{sfe} = \frac{\sigma_e - \sigma_{snL}}{E_{f2}} + \varepsilon_{sfL} \quad \text{with} \quad \varepsilon_{sfL} = \frac{\sigma_{snL}}{E_{f1}} \quad (17)$$

In summary, for the short tie-rods, at the elastic limit of concrete, the relation 18 represents the fictitious diagram $\sigma - \varepsilon$ of the steel:

$$\begin{cases} \sigma = E_{f1} \cdot \varepsilon & \text{if } 0 \leq \varepsilon \leq \varepsilon_{sfL} \\ \sigma = E_{f2} \cdot (\varepsilon - \varepsilon_{sfL}) + \sigma_{snL} & \text{if } \varepsilon_{sfL} \leq \varepsilon \leq \varepsilon_{sfe} \end{cases} \quad (18)$$

4. Materials

4.1. Concrete

The particle size analysis was carried out according to the French standard NF P 18-560 (Table 1), with a maximum diameter, $D_{\max} = 12.5$ mm for gravel and a fineness module for sand, $MF = 2.03$. A single formulation of an ordinary concrete has been used for all series of tests. The composition of the concrete for one cubic meter determined by Faury's method is given in Table 2. The use of large aggregates (15/25) was avoided considering the relatively small dimensions of specimens.

Prismatic ($15 \times 15 \times 15$) cm³ and cylindrical 11 cm \times 22.5 cm specimens have been prepared for compression and tensile tests respectively. The results of the various properties of the concrete are given in Table 3.

4.2. Steel

The used rebars for the pull out and the tie rods tests are steels with high rib adhesion (Figure 6). Tensile tests on nude bars of 18 cm long have been carried out. A yield stress of $\sigma_e = 530$ MPa and a longitudinal elastic modulus of $E_s = 200$ GPa have been calculated for the used diameters $\emptyset = 8, 12$ and 14 mm.

Note here that the adhesion between steel and concrete depends on the characteristics of the ribs.

The works, of Rehm [30], Sorez & Hölzenbein [31] as well as Martin & Noakowski [32] showed the geometric importance of the ribs of rebars in the steel-concrete adhesion.

The Studies carried out by Caetano & al [33] and Handika & al [26] showed the influence of the ribs in considering the height h_1 , the spacing e_1 , the angle of the ribs α_1 (45 to 50°) and the angle of inclination of the ribs α_2 (45 to 50°) (Figure 7).

The geometrical characteristics of the ribs of the reinforcement used for our tests are shown in Table 4.

5. Pull out tests

Pull-out tests are carried out with the machine shown in Figure 8. They are conducted on the same bars used for the tie rods.

5.1. Geometry of specimens and procedure (Figures 8 and 9)

Prismatic specimens with a cross section of 100 mm \times 100 mm and a length of 15ϕ where ϕ is the rebar diameter were used (Figure 9(a)). Reinforced concrete pull out specimens were

Table 1. Particle size analysis according to the French standard NF P18-560.

Sieve diameter (mm)	25	20	16	12.5	10	8	6.3	5	4	3.15	2.5	2	1.6	1.25
Sieve module	45	44	43	42	41	40	39	38	37	36	35	34	33	32
Gravel passing cumulative%	100	100	99.28	77.28	32.94	8.94	4.281	2.906	2.156	1.563	0.969	0.500	0.250	0.156
Sand passing cumulative %	100	100	100	100	100	100	100	99.30	99.20	98.81	97.61	95.12	92.44	90.15
Sieve diameter (mm)	1.0	0.8	0.63	0.5	0.4	0.315	0.25	0.2	0.16	0.125	0.1	0.08	0.016	-
Sieve module	31	30	29	28	27	26	25	24	23	22	21	20	19	-
Gravel passing cumulative%	0.063	0.063	0.063	0.063	0.063	0.063	0.063	0.063	-	-	-	-	-	-
Sand passing cumulative %	85.17	84.28	78.71	69.15	52.24	28.87	14.73	7.761	5.174	3.682	2.886	2.587	2.289	-

Table 2. Concrete constituents.

Sand 0/3	629 kg/m ³	26.4%
Rolled gravel 3/15	1148 kg/m ³	48.3%
Cement CEM 32.5 R	400 kg/m ³	16.8%
Water	202 kg/m ³	8.50%
Total	2379 kg/m ³	100%

Table 3. Concrete properties.

Compressive strength at 28 days (f_{c28})	33.7 MPa
Average tensile strength at 28 days ($f_{ctm,28}$)	2.60 MPa
Modulus of elasticity of concrete E_c	35.5 GPa
Cement/Water ratio (C/E)	1.98
Abrams cone subsidence	60 mm



Figure 6. High adhesion steel used.

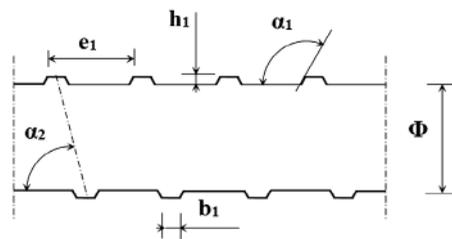


Figure 7. Geometric characteristics of the ribs taken into account by Caetano and al [33].

Table 4. Characteristic values and geometry of the ribs.

\emptyset (mm)	h_1 (mm)	b_1 (mm)	e_1 (mm)	A_s (mm ²)
8	0.7	0.9	5.3	50.3
12	1	1.2	7.2	1.13
14	1.1	1.4	8.4	1.154



Figure 8. Specimen used and device.

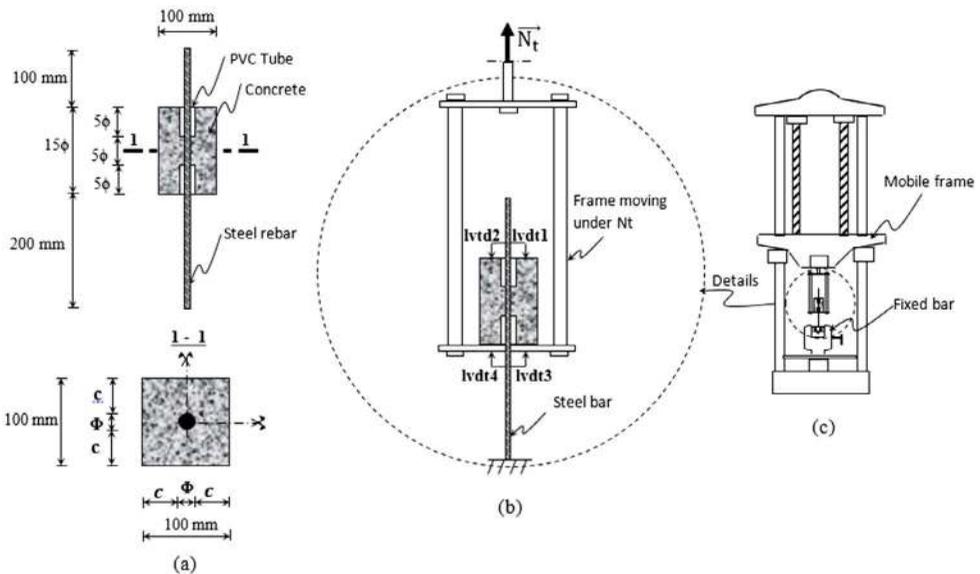


Figure 9. Specimen and device for the pull-out test, (a) Specimen geometry, (b) Concrete moving frame, (c) Concrete moving frame.

designed with a length varying in function of rebar's diameter ϕ . Reinforcing steel rods were placed prior to casting of concrete with a protective layer on the bottom and upper side of embedded steel over a length of 5ϕ using a PVC hose covering as shown in Figure 9(a) in order to avoid inaccurate stresses in the specimens and friction in the sample. Rebars are embedded into a 15ϕ concrete cube and the bond length of the steel bar and concrete was equal to 5ϕ .

As the section of specimens is kept constant, similar to that of RC tensile tests, the percentage of steel is varied $\rho = A_s/A_t$ where A_s and A_t represent respectively the section of the steel and the section of the specimen.

The pulling out and the withdrawal of the reinforcing element from concrete are performed in the axial tensile mode using a testing machine with a special metal framework. The sample was placed in a holder with a stopper fixed at the lower clamp of the testing machine while the free top part of the rod was fixed by the testing machine (Figure 9(b, c)). The sample was loaded by pulling out the rod at a constant velocity in the vertical direction. The loading force and displacement of the mobile clamp were continuously monitored. In addition, two LVDT sensors were placed in order to measure the slip between the rod and concrete on the bottom and the upper side of the sample in order to study any perturbations as flexion.

5.2. Experimental pull out results

Pull out tests were realized on reinforced concrete specimens with high adherence rebars HA8, HA12 and HA14 (Three specimens for each type), and thus different percentage of steel 0.50, 1.13 and 1.54% respectively.

The bond stress slip relationships ($\tau - g$) are presented in Figure 10 for rebars with different diameters. Tests with the HA14 rebars have broken out and are not shown here.

5.3. Characteristic values of the adhesion slip law ($\tau - g$)

Based on the bond stress slip curves obtained in Figure 10 and numerical results, the characteristics of the $\tau - g$ law can be deduced.

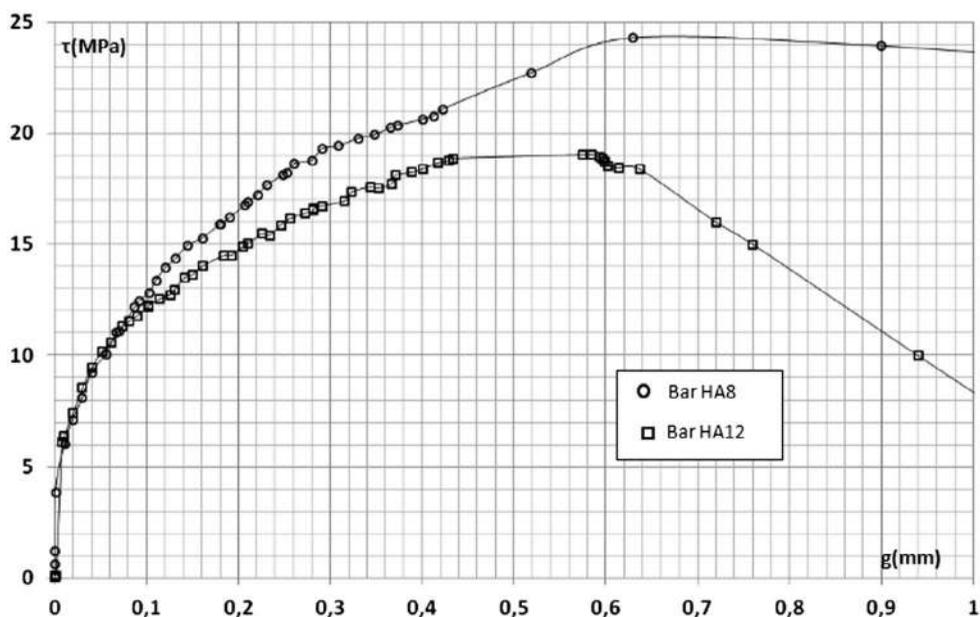


Figure 10. Stress –slip curves.

Eligehausen & al [27] law, adopted by the European Concrete Committee [2] is used for the first phase, with the tests values, we can write the expression 19.

$$\tau = \tau_{1\max} \left(\frac{g}{g_{1\max}} \right)^\alpha \quad (19)$$

The value of the confinement c for the tie-rods used here is given by the relation 20:

$$c = 50 - \emptyset/2 \quad \emptyset \text{ and } c \text{ in mm} \quad (20)$$

The value of $\tau_{1\max}$ is deduced directly from the maximal load obtained with the various pull out tests (Table 5) and the first part of the curvilinear curve at the beginning of loading.

Knowing two states of loading $j(g_j; \tau_j)$ and $k(g_k; \tau_k)$ with the loading level at k superior to that of j and $\tau_k > \tau_j$:

$$\begin{cases} \tau_j = \tau_{1\max} \left(\frac{g_j}{g_{1\max}} \right)^\alpha & (a) \\ \tau_k = \tau_{1\max} \left(\frac{g_k}{g_{1\max}} \right)^\alpha & (b) \end{cases}$$

Considering the ratio of (b) to (a), expression 21 can be deduced

$$\alpha = \frac{\log\left(\tau_k/\tau_j\right)}{\log\left(g_k/g_j\right)} = \log\left(\tau_k/\tau_j\right) - \log\left(g_k/g_j\right) \quad (21)$$

When α is determined, and for the state at the beginning of loading ($g; \tau$), $g_{1\max}$ can be deduced by the relation 22:

$$g_{1\max} = g \cdot \left(\frac{\tau_{1\max}}{\tau} \right)^{1/\alpha} \quad (22)$$

In our case, α was considered equal to 0.33, the others results are given in Table 5.

Note: The European Concrete Committee [2] uses here two coefficients α and a to express the same parameter: the confinement of the concrete. To keep only one, knowing that for $\alpha = 0.25$ and $\alpha = 0.40$ corresponding $a = 2$ and $a = 2.5$ respectively, the relation 5 can be written:

$$\tau_1 = \left(\frac{10}{3}\alpha + \frac{7}{6} \right) \sqrt{f_{ck}} \quad (23)$$

Table 5. Characteristic values of the $\tau - g$ law deduced from the pull out curves.

Diameter of the rebar \emptyset (mm)	HA8	HA12
Percentage of steel (A_s/A_t = Steel section/Tie-rods section)	0.503%	1.13%
Maximum pull-out load of the bar (kN), $F_{a,\max}$	24.4	43.0
Normal stress in the rebar (MPa)	485	381
Maximum adhesion stress $\tau_{1\max}$ (MPa)	24	19
Estimated Value of α	0.33	0.33
Estimation of the maximum slip value, $g_{1\max}$ (mm)	0.34	0.24

Based on the experimental tests, the conventional curve adopted by the European Concrete Committee [2], underestimated the value of τ_1 . Therefore, the relation 24 is proposed:

$$\tau_1 = (4.\alpha + 1) \sqrt{f_{ck}} \quad (24)$$

6. Tests on short tie-rods without main cracks

6.1. Specimens dimensions and preparation

The section of the tie-rods is the same as those of the pull out tests, Figures 9(a). Figure 11 presents a sketch of the short ties, where rebars are placed in the center with a total length of 480 mm. Rebars are embedded into a length of $l_t = 190$ mm chosen so that no principal cracking can appear during tensile tests. At both end of the RC ties, PVC tubes of 30 mm, are placed in order to avoid inaccurate stresses in the specimens and friction and splitting in the sample. Three specimens were prepared for each type of tie rod (THA8, THA12 and THA14).

6.2. Operating mode on the tie-rods

After casting, specimens were covered with a thin sheet of plastic to prevent water loss and were maintained in a climatic chamber at a temperature of 20 °C and a relative humidity

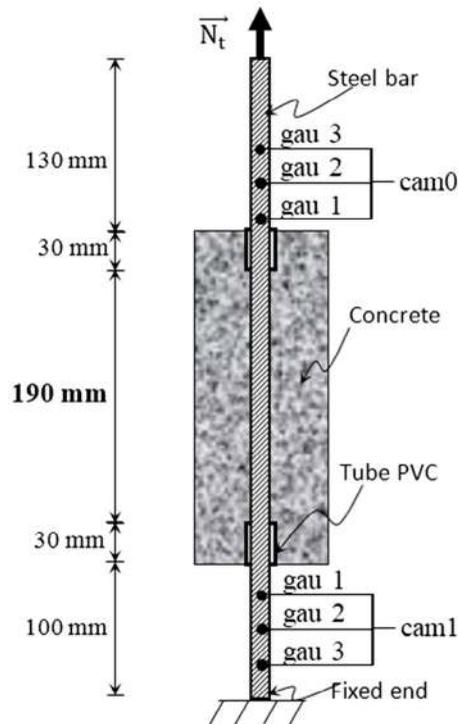


Figure 11. Tie-rods in tension.

(RH) of 95%. Twenty four hours after casting, specimens were stripped off from the molds and kept for curing in lime water, under a temperature condition of 20 °C for 28 days.

After 28 days, tensile tests on reinforced concrete ties are carried out with a hydraulic machine with a capacity of 200 kN.

The lower free part of the rods was fixed while the other free part was subjected to a tensile load N_t with a constant displacement kinetic of 1 mm/min (Figure 11).

Two cameras (cam 0 and cam 1), were also used in order to measure the displacement of both free parts of the rebar (gau 1, gau 2 and gau 3) (Figure 11). The obtained informations allow us to plot the stress strain diagram ($\sigma - \varepsilon$) of each short tie.

6.3. Experimental results and analyzes

The contribution of concrete is studied (in function of the adhesion) in a tie rod by measuring the difference between:

$$\Delta\varepsilon = \varepsilon_{sn} - \varepsilon_t \quad (25)$$

where ε_{sn} and $\varepsilon_t = \Delta l_t / l_t$ represent, at the same instant, the relative elongations respectively of the steel assumed to be nude and the tie rod under the force N_t .

We present in Figure 12, the $\sigma - \varepsilon$ curves of tie-rods with diameters equal to HA8 (THA8) and HA12 (THA12).

The relation 25 provides an overview of the variation of adhesion between steel and concrete. The plotting of the curve $\Delta\varepsilon$ as a function of loading (represented here in Figure 13 by the stress in the steel) shows:

- For THA8 ($\Delta\varepsilon 8$), the ‘mobilized’ adhesion in the tie rod increases linearly up to the force $N_t = 16$ kN, or a normal stress in the steel rebar of $\sigma_{sn} = 319$ MPa. The relative deformation of the tie rod is then $\varepsilon_t = 8.5 \cdot 10^{-5}$, which corresponds to $\Delta\varepsilon 8 = 1.51 \cdot 10^{-3}$. From this level of loading, the slope decreases considerably (Figures 12 and 13). The modulus of elasticity of the tie rod is slightly greater than that of the steel rebar.
- For THA12 ($\Delta\varepsilon 12$), the adhesion mobilized between the steel and the concrete in the tie rod increases linearly up to the load $N_t = 15.7$ kN, which corresponds to a normal stress in the steel rebar $\sigma_{sn} = 139$ MPa. At this moment, the relative deformation of the tie rod is equal to $\varepsilon_t = 3.84 \cdot 10^{-4}$, which corresponds to $\Delta\varepsilon 12 = 3.12 \cdot 10^{-4}$. A reduction in the adhesion between the steel and the concrete is then observed (Figures 12 and 13) and the modulus of elasticity of the tie rod is close to that of the steel. With the plasticization of the steel ($\sigma_{sn} = 450$ MPa), the deterioration of the adhesion appears.

6.4. Deductions of ψ_1 and ψ_2 values of the proposed laws

At the beginning of loading, phase 1, the experimental curves (Figure 12) are approximated by taking the expression 26 as the value of the coefficient ψ_1 . The other parameters ($1 - \alpha$) and γ take into account, respectively, the confinement and the coating.

$$\psi_1 = \frac{1 - \bar{\rho}}{\gamma \cdot (1 - \alpha)} \quad \text{with} \quad \begin{cases} \gamma = 1 & \text{if } c \geq 5.\emptyset \quad (\text{or } \rho < 1\%) \\ \gamma = \left(\frac{\emptyset}{c}\right)^{(1+\alpha)} & \text{if } c < 5.\emptyset \quad (\text{or } \rho \geq 1\%) \end{cases} \quad (26)$$

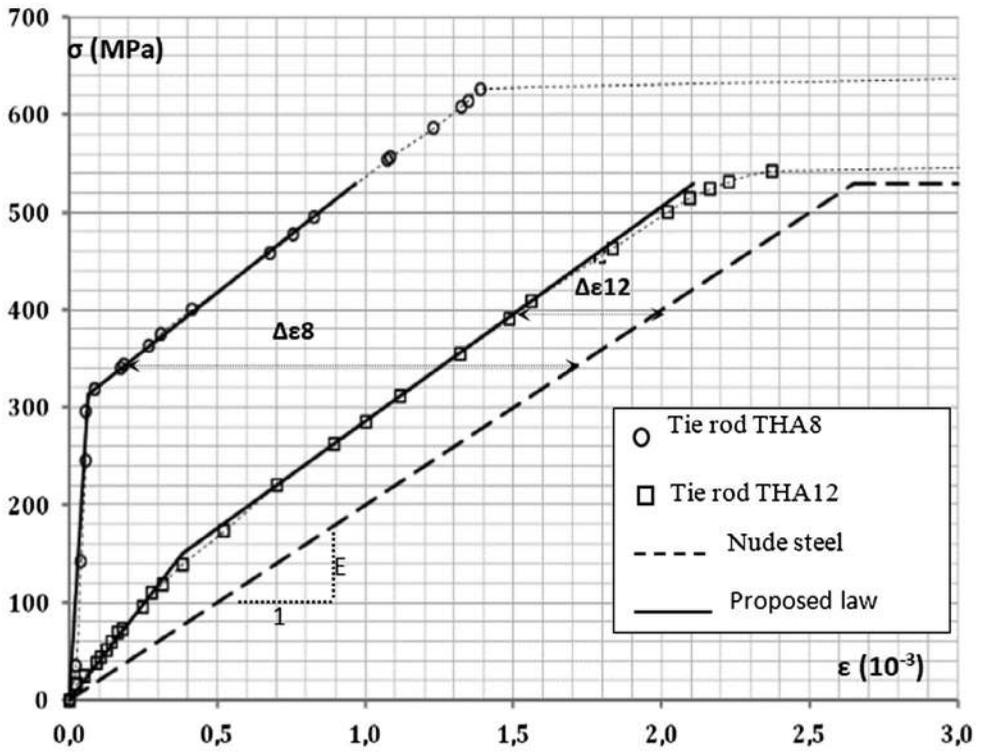


Figure 12. Diagrams $\sigma - \epsilon_t$ of tie-rods THA8 and THA12.

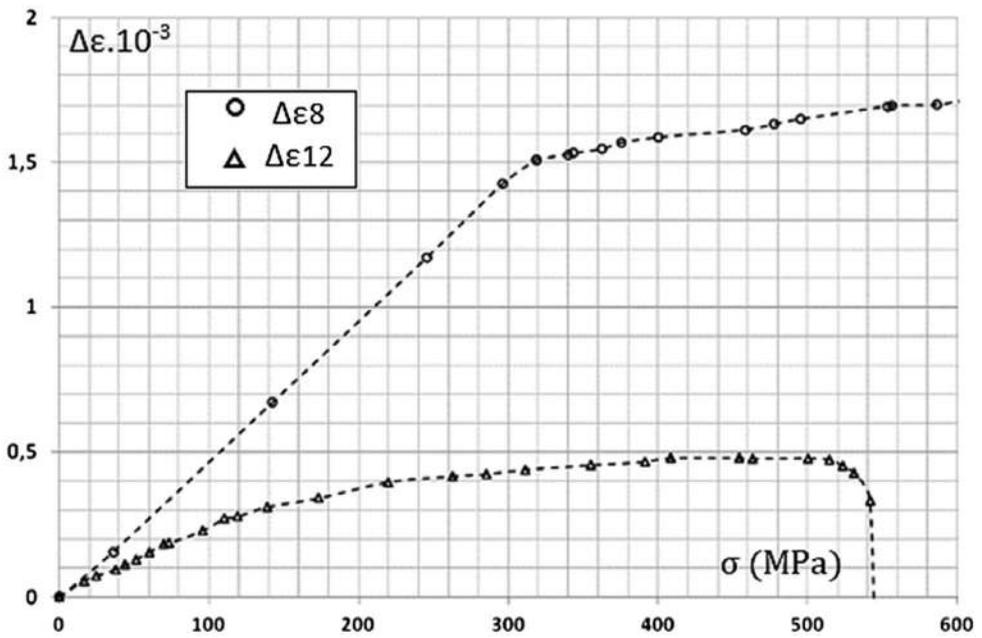


Figure 13. Diagrams $\Delta\epsilon_t - \sigma$ of tie-rods THA8 and THA12.

Table 6. Fictitious steel laws for short tie-rods without major cracks THA8.

RC concrete Short ties with HA8 rebar (THA8) without principal cracking				
E_{r1} (MPa)	σ_{snL} (MPa)	ε_{snL} (10^{-5})	E_{r2} (MPa)	ε_{sfe} (10^{-4})
$4.842 \cdot 10^6$	313.5	6.470	$2.4 \cdot 10^5$	9.679
$\begin{cases} \sigma = 4.842 \cdot 10^6 \cdot \varepsilon & \text{if } 0 \leq \varepsilon \leq 6.470 \cdot 10^{-5} \\ \sigma = 2.4 \cdot 10^5 \cdot \varepsilon + 297.7 & \text{if } 6.470 \cdot 10^{-5} \leq \varepsilon \leq 9.679 \cdot 10^{-4} \end{cases}$				

Table 7. Fictitious steel laws for short tie-rods without major cracks THA12.

RC concrete Short ties with HA12 rebar (THA12) without principal cracking				
E_{r1} (MPa)	σ_{snL} (MPa)	ε_{snL} (10^{-4})	E_{r2} (MPa)	ε_{sfe} (10^{-3})
$3.932 \cdot 10^5$	150.9	3.840	$2.2 \cdot 10^5$	2.107
$\begin{cases} \sigma = 3.932 \cdot 10^5 \cdot \varepsilon & \text{if } 0 \leq \varepsilon \leq 3.840 \cdot 10^{-4} \\ \sigma = 2.2 \cdot 10^5 \cdot \varepsilon + 66.52 & \text{if } 3.840 \cdot 10^{-4} \leq \varepsilon \leq 2.107 \cdot 10^{-3} \end{cases}$				

As a first approximation for the second phase, after maximum mobilization of the adhesion and its degradation we can take for the coefficient ψ_2 , relation 27:

$$\begin{cases} \psi_2 = 0,9 & \text{if } c \geq 5.\emptyset \quad (\text{or } \rho < 1\%) \\ \psi_2 = 0,8 & \text{if } c < 5.\emptyset \quad (\text{or } \rho \geq 1\%) \end{cases} \quad (27)$$

For the examples treated, THA8 and THA12, with the data of Tables 3 and 5 and the relationships 14 to 18, 26 and 27, the equations in Tables 6 and 7 are obtained.

The representation of these theoretical curves in continuous line is illustrated, Figure 12.

7. Conclusions

- In the estimation of the adhesion peak τ_1 , of the $\tau - g$ law proposed by the European Concrete Committee, the coefficient 'a' can be replaced by its equivalent as a function of α so as to keep the same confinement parameter (see Relation 24).
- The raw (unconventional) characteristic values of the $\tau - g$ law of the first curvilinear curve proposed by the European Concrete Committee can be estimated in the pull out tests at the beginning of the curve by the relations proposed here (Relations 21 and 22).
- For the pull out tests, under the same conditions, the order of magnitude of the maximum peak of adhesion does not depend on the percentage of steel because the adherent side surface of the bar to the concrete is all the greater as the perimeter is.
- The length of the tie-rods here does not allow an adhesion mobilization capable of creating a crack. The introduction length must not exceed half that of the tie-rod.
- The fictitious module slope of steel is higher the lower the percentage of steel. After a certain level of loading (maximum mobilization of the adhesion), the slope decreases and approaches that of the bare steel (10 to 20%). At the approach of the elastic normal stress, this slope declines, this is partly explained by the Poisson effect.

- The proposed laws, here, of simple analytic expressions, for short tie-rods without main cracks, suitably approach the test curves. However, other contributions are needed to improve this approach.
- It is clear that each steel-concrete mixture must include, after the granulometric analysis and the concrete formulation, a specific ‘pull-out’ study to be able to deduce the tie rods behavior.
- The results obtained in this study will serve to better understand the behavior of tie-rods in general (Fictitious diagram of steel and concrete, spacing of cracks, crack openings, ...). Indeed, during this last phase, the tie rod is composed of ‘short tie rods without main cracks’ object of this study.

Nomenclature

σ_e	Normal stress yield strength
ϵ_s	Relative elongation
E_s	Longitudinal elastic modulus of steel
E_c	Longitudinal elastic modulus of concrete
E_{f1}	Fictitious longitudinal elastic modulus of steel (phase 1)
E_{f2}	Fictitious longitudinal elastic modulus of steel (phase 2)
f_c^{ck}	Normal compressive stress limit of concrete
f_{ctm}	Resistance (average) to effective tensile strength of concrete
τ	Adhesion stress between steel and concrete
g	Slipping between steel and concrete
α	Concrete containment coefficient
φ	Diameter of steel bars
N_t	Tensile load on the tie rod
$\sigma_s = \sigma_s(x)$	Normal stress of concrete-coated steel at a distance x from the end of the tie rod
$\epsilon_s = \epsilon_s(x)$	Relative elongation of concrete-coated steel at a distance x from the end of the tie rod
$\sigma_c = \sigma_c(x)$	Normal stress of the concrete at a distance x from the end of the tie
$\epsilon_c = \epsilon_c(x)$	Relative elongation of the concrete at a distance x from the end of the tie
$\sigma_{sn} (= N_t/A_s)$	Normal stress in the bare steel at the ends of the tie rod ($x = 0$)
$\epsilon_{sn} (= \sigma_{sn}/E_s)$	Relative elongation of the steel at the ends of the tie rod ($x = 0$)
$\sigma_{s1}, \epsilon_{s1}$	Normal stress and corresponding relative elongation in bare steel, along the tie rod on the interval $[0; l_1]$
$\sigma_{s2}, \epsilon_{s2}$	Normal stress and corresponding relative elongation in bare steel, along the tie rod on the interval $[l_1; L]$
$\sigma_{c1}, \epsilon_{c1}$	Normal stress and corresponding relative elongation in concrete, along the tie rod on the interval $[0; l_1]$
$\sigma_{c2}, \epsilon_{c2}$	Normal stress and corresponding relative elongation in concrete, along the tie rod on the interval $[l_1; L]$
ϵ_t	Relative elongation of the tie rod ($= \Delta l_t / l_t$)
ϵ_{sf}	Fictitious elongation of steel
$\Delta \epsilon (= \epsilon_{sn} - \epsilon_t)$	Relative elongation gap between bare steel and tie rod under load N_t
$l_t (= 2L)$	Length of tie rod
A_t	Straight section of tie rod
A_s	Steel section in the tie rod
A_c	Net section of concrete subjected to tension ($= A_t - A_s$)
ρ	Percentage of steel ($= A_s/A_t$)
l_1	Length of introduction
ρ	Useful perimeter of steel (here bar perimeter)
u_s	Elongation of steel
u_c	Elongation of concrete
LVDT	Linear Variable Differential Transformer

Disclosure statement

No potential conflict of interest was reported by the authors.

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