Mapping lithological boundaries in mines with array seismology and in-situ Acoustic Emission monitoring

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26 **Summary**

27 Knowledge of the position of lithological boundaries is key information for a realistic interpretation of
28 geological settings. Especially in the mining environment, the exact knowledge of geometrical
29 boundaries and characteristics of rock structures has a great impact for both economic decisions and
30 safety awareness. For this purpose, we investigate the P-coda of high frequency acoustic emission events
31 (picoseismicity) and test the application of array seismology techniques, usually used to study the Earth's
32 deep interior, on a much smaller scale in a mining environment. In total 52 events were used, all of them
33 recorded in the Asse II salt mine in Lower Saxony (Germany) using a network of 16 piezoelectric sensors.
34 Many of these events show a pulse-like arrival in the late P-coda, suggesting the presence of a well-
35 defined structure which scatters seismic energy. To explore the directional information of the signals in
36 the seismograms we use the sliding-window slowness-backazimuth analysis, performed on the waveform
37 envelope of the entire recording. Strong direct P-wave arrivals are clearly visible with observed slowness
38 and backazimuth as expected for a homogenous medium. This implies straight ray paths from event to
39 sensors indicating that the medium between the events and the sensors is homogeneous for wavelengths
40 larger than about 60 cm. In the late P-coda we observe out-of-plane arrivals from South-East and,
41 assuming single P-to-P scattering, we find that the scatterers responsible for these observations are
42 clustered in space defining a sharp reflector corresponding to a known lithological boundary located at
43 the southern flank of the salt dome. In agreement with the established geological model we observe no
44 other dominant reflections in the analyzed waveforms that would indicate previously unknown
45 lithological boundaries. This study shows that array seismology can be applied to acoustic emissions in
46 mines to gain more information on structures and heterogeneities located in the vicinity of the monitored
47 rock volume. In micro-acoustically monitored mines, this technique could be a valuable addition to
48 increase hazard awareness and mining efficiency at little or no extra costs.

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Keywords: Time series analysis; Body waves; Coda waves; Wave propagation; Wave scattering and diffraction

73 **1 Introduction**

74 In underground exploration the monitoring and analysis of seismic events are common tools for risk and
75 hazard assessment, as underground operations induce low-magnitude seismicity and sometimes trigger
76 rockbursts that could harm miners and damage the mine ([Hasegawa et al. 1989](#); [Potvin, 2009](#)). Since the
77 beginning of last century seismic networks are used to study seismic events in mines ([Gane et al., 1946](#);
78 [McGarr, 1971a,b](#); [Spottiswoode, 1989](#); [Gibowicz and Kijko, 1994](#); [Collins et al., 2002](#); [Plenkers et al.,](#)
79 [2010](#)). Microseismic and sometimes in-situ Acoustic Emission (AE) monitoring networks are operated
80 in mines worldwide and provide large amounts of data (see [Manthei and Plenkers, 2018 for a review](#)).
81 Until today the analysis is often limited to the estimation of the location, the magnitude and in some cases
82 the faulting mechanism of the seismic events. Analysis of the coda wave field are rare, although the
83 event's waveforms are accessible in modern monitoring networks and coda wave analysis can provide
84 important additional information on structures and scattering properties of the propagation medium (see
85 [Sato & Fehler 2008](#); [Sato, Fehler and Maeda, 2012](#) for a review of coda waves analysis).
86 Of great importance in underground excavation is the in-depth knowledge of the internal structures of
87 the rock as this information is an important factor in the hazard assessment (e.g. [Milev and Spottiswoode,](#)
88 [2002](#)) since it influences our view of the stability of mine structures and directly reflects the production
89 rate. Investigation of mine structure is also crucial in the safety assessment of underground repositories
90 for radioactive nuclear waste. Some methods to study the rock's internal structure already exist, e.g.,
91 drilling combined with bore-core analysis, georadar, or seismic profiling. However, data gained by
92 passive seismic monitoring systems are only exploited in rare cases for such purposes (e.g., [Olivier et al.](#)
93 [2015a,b](#)).
94 Gaining information on internal rock structures using already existing waveforms of seismic monitoring
95 arrays is a cost-effective approach that has the potential to provide additional information on the existence
96 and location of geological boundaries, discontinuities, or cavities. Moreover, energy of underground

97 seismic events often travels through a rock volume that may be out of reach for other methods or not
98 suitable for drilling e.g., due to rock integrity requirements.

99 To exploit seismic arrivals other than simply using first onsets in recorded waveforms, here we apply
100 array seismological techniques. This approach is generally used to gain information on structures in the
101 entire Earth from crust and lithosphere to the Earth's inner core and has provided valuable information
102 on Earth structures (e.g., [Gu, 2010](#)). With the array techniques, we are able to extract coherent and
103 incoherent signals hidden by noise through stacking, and those techniques also provide directional
104 information of seismic arrivals ([Douglas, 2002](#); [Gibbons, 2014](#); [Husebye and Ruud, 1989](#); [Rost and](#)
105 [Thomas, 2002](#); [Ringdal et al., 1975](#); [Schweitzer et al., 2012](#)). One method is the frequency-wavenumber
106 (fk) analysis ([Capon, 1973](#)) that helps to detect waves arriving from out-of-plane directions that can
107 provide information on structures that do not lie on the direct wave path.

108 To our knowledge, these methods have not yet been applied to mine-scale investigations and
109 picoseismicity, even though, despite the different scales and magnitudes, it is well documented that
110 waveforms of picoseismicity events are well suited for extended waveforms analysis; e.g., source
111 parameter analysis ([Dahm et al., 1999](#); [Kwiatek et al., 2011](#)). We test the application of these techniques
112 to high-frequency AE picoseismicity that occurs in a frequency range from 1 kHz up to 200 kHz ([Manthei](#)
113 [and Plenkers, 2018](#)) on a data set recorded by a sensor network in a salt mine.

114 We chose the Asse II salt mine in Lower Saxony where seismic events recorded by in-situ AE monitoring
115 are reported ([Philipp et al. 2015](#)). By analyzing and interpreting these waveforms, we address the
116 following questions: Can seismic array methods be successfully applied to investigate AEs on mine-
117 scale applications? Is the upper salt dome homogeneous or is there an indication for additional geological
118 structures, presently unknown? Can we exclude the existence of cavities or large open fractures in the
119 upper salt dome? Can we detect and confirm the location of known structures e.g., the southern flank of
120 the salt dome using array seismological techniques?

121

122 **2 Dataset, observations, method and data processing**

123 We analyze single component waveforms from 52 events recorded at a network of 16 piezoelectric
124 sensors, deployed above the A3 (western) chamber of the Asse II mine ([Figure 1](#)) in Germany. The events
125 define a narrow cluster located in the upper part of the salt dome ([Figure 1](#)), with hypocentral distances
126 ranging from 120 to 150 meters. The sensors were installed vertically in upward 1 to 3 m deep boreholes,
127 drilled in the A3 chamber roof ([Philipp et al., 2015](#)), giving a 3D geometry to the network, with sensor
128 locations following the convex roof shape ([Figure 1](#)). The network has dimensions of about 37 m x 31
129 m x 5 m (X x Y x Z, see inset in [Fig. 1](#)). The piezoelectric sensors with a sampling rate of 1 MHz allow
130 the recording of very high frequency waves within a broad range from 1 kHz to 100 kHz. To reduce the
131 amount of stored data, the sensors were equipped with a trigger system for the detection and the
132 recordings of events. The recording time for each trigger is 32.768 ms ([Manthei and Plenkers, 2018](#)),
133 allowing the recording of the P-wave and S-wave onsets, necessary for locating the events. A more
134 detailed description of the events and sensors is found in [Phillip et al. \(2015\)](#).

135 A typical example of the waveforms of the event cluster used in this study is shown in [Figure 2](#). This
136 event occurred at a hypocentral distance of 122 m and shows clear direct P- and S-wave arrivals. The
137 direct P-wave arrival is followed by additional energy packets (pulses) suggesting scattering or reflection
138 of seismic energy somewhere in the propagation medium. Local reverberations close to the sensors can
139 be excluded as possible cause for those observations, since the additional phase appears at all sensors
140 indicating a more coherent structure. The additional signal also shows no clear move-out, when compared
141 to the direct P-wave arrival, suggesting that it likely traveled out of plane and may have been scattered
142 at a structure in the surrounding medium.

143 Scattering of seismic energy has been extensively used to characterize and probe heterogeneities at
144 different scales, using both stochastic and deterministic approaches (see [Sato, Fehler and Maeda, 2012](#)
145 [for a review](#)). Here we assume single scattering for this additional arrival since multiple-scattering
146 processes would scatter the seismic energy continuously in a diffusive manner, therefore generating a
147 smooth decay rate of the coda amplitude. Our observation of individual pulse-like signals, however,
148 suggests the presence of one or more well-defined reflectors or scattering bodies, which can be located
149 in a deterministic way provided that the direction of the incoming scattered wave-front can be measured.
150 Due to the intrinsic frequency dependency of scattering phenomena ([Sato, Fehler and Maeda, 2012](#)), we
151 applied different filters before the beamforming process, in order to search for the frequency band which
152 best enhances the amplitude of the scattered wavefield in the P-coda. In most cases, a butterworth
153 bandpass filter of 3 to 8 kHz best reduced the high frequency reverberations while at the same time
154 increased the amplitude of the additional arrival. A typical spectrogram of the analyzed recordings is
155 shown in [Figure S1](#) of the Supporting Information where we find the dominant frequency of the signal
156 in the band between 3 and 8 kHz.

157 Seismic array techniques allow to measure the direction of the incoming seismic energy at a seismic
158 network. A comprehensive description of array methods is found in [Rost and Thomas \(2002\)](#) and
159 [Schweitzer et al. \(2012\)](#). Array methods are based on shifting and stacking of waveforms with the aim to
160 increase the signal to noise ratio of coherent and incoherent seismic phases, and identify the direction of
161 arrivals ([Douglas, 2002](#); [Gibbons, 2014](#); [Husebye and Ruud, 1989](#); [Ringdal et al., 1975](#); [Rost and](#)
162 [Thomas, 2002](#)).

163 The technique most often used for stacking seismic data is beamforming, which is based on the delay
164 and sum method (e.g., [Rost and Thomas, 2002](#); [Schweitzer et al., 2012](#)). This method applies time shifts
165 (τ_j) to the traces depending on the slowness vector ($\mathbf{s}$) of the incoming planar wave front and on the
166 relative distance ($\mathbf{r}_j$) of the sensors with respect to the geometrical center of the array:

$$\tau_j = \mathbf{r}_j \cdot \mathbf{s} \quad (1)$$

167 for the j^{th} -sensor. Expanding the previous equation, we obtain:

$$\tau_j = \frac{-x_j \cdot \sin \Phi - y_j \cdot \cos \Phi}{v_{app}} + \frac{z_j \cdot \cos i}{v_c} \quad (2)$$

168 where the relative distance of the j^{th} -sensor (with respect to the array center) is now expressed in terms
 169 of Cartesian coordinates (x_j, y_j, z_j) projected in the direction of wave front propagation along the
 170 backazimuth Φ (Figure 3a). V_{app} is the apparent velocity of the approaching wave front which is related
 171 to the horizontal slowness (Figure 3b). The last term in the equation accounts for additional travel time
 172 shifts due to the 3D geometry of the network (Schweitzer et al., 2012), where z_j is the elevation of the
 173 j^{th} -sensor (the position in depth) and v_c is the velocity of the medium where sensors are located. In our
 174 case the velocity of both P- and S-waves is precisely known by ultrasonic transmission measurements
 175 performed on-site, using an ultrasonic signal in the same frequency range as the AE events and recorded
 176 on the sensors of the network. The ultrasonic transmitter was installed inside a borehole. The measured
 177 velocity for P- and S-waves are: $v_P = 4570$ m/s and $v_S = 2597$ m/s (Philipp et al. 2015). Using the
 178 measured v_P and a depth difference of up to 5 m between sensors results in a (vertical) delay time τ of
 179 about 1 ms. This is a significant and relevant additional time shift to take into account in the stacking
 180 procedure. In contrast, in global array seismology where the elevation of the station is often much smaller
 181 than epicentral distances, these time shifts can often be neglected, however, even there static corrections
 182 due to strong topography are important in some cases (e.g., Bokermann, 1995; Jacobeit et al., 2013).
 183 An approximation used in most array methods is that the wave front approaching the array is planar. This
 184 approximation works well at the large distances typical for global seismology but it might not hold for
 185 the short hypocentral distances considered in this study. Given the geometrical configuration of the array
 186 and its large aperture (~ 35 m), compared to hypocentral distances (120 – 150 m), we only consider the

10 innermost sensor locations closest to the geometrical center. This sub-network has an aperture (~ 20 m), which is six times smaller than the minimum hypocentral distance (120 m), validating the approximation of planar wave-front (Almendros et al., 1999). Relative distances of the sensors with respect to the geometrical center for this sub-network are shown in Figure 3c. This smaller configuration also improves the focusing of the arrivals at the remaining sensors. Due to the size of the source ruptures on the dm- to mm-scale in the considered frequency range (Kwiatek et al., 2011; Philipp et al., 2015), near-field effects on the wave-front geometry are largely negligible.

In general, the capability of the arrays in enhancing the seismic signals depends on the interstation distance (i.e., the geometry of the network) compared with the wavelengths of the signals of interest (Douglas, 2002; Gibbons, 2014; Rost and Thomas, 2002), although the variation of signal shape across the array (i.e., its intrinsic incoherency) might still result in a reduction of stacked signal amplitude (Douglas, 2002) especially for high frequencies (Ringdal et al., 1975). In our particular case, considering the dominant high frequencies (3-8kHz) of the signal, the expected wavelength of the plane wave is about 0.6-1.50 m for $v_p=4570$ m/s. In conventional phase-based beamforming, the stacking of coherent signals with this wavelength would then require an interstation distance of the same order, which is significantly smaller than the actual average distance of the order of a few meters between the used sensors (Figure 3). Moreover, the stacked beam might be affected by the poor signal correlation between the sensors (Husebye and Ruud, 1989). This problem in classical array processing arises when high frequency signals are recorded at large aperture arrays, and due to waveform dissimilarity between the sensors leads to beam degradation (Gibbons, 2014). However, to exploit high frequency energy, Ringdal et al. (1975) showed that these issues can be overcome by replacing the signals with their envelopes which leads to the so-called incoherent (envelope-based) beamforming (Douglas, 2002; Gibbons, 2014; Husebye and Ruud, 1989; Ringdal et al., 1975). Therefore, using the Hilbert transform we compute the envelope of the filtered signals (Kanasewich, 1981), which offers more insight on amplitude information of the

211 seismic trace and enhances the correlation among signals, rather than looking at the complexity of the
 212 waveforms which also depends on the phase contained in the high frequency signal itself (Farnbach,
 213 1975). In Figure S2 of the Supporting Information we show the comparison between conventional
 214 (phase-based) coherent linear beamforming and incoherent (envelope-based) beamforming, where we
 215 find higher amplitudes of the stacked signal when using the envelope of the individual waveforms. Phase-
 216 independent envelope-based stacking has also been used at global scale to detected scattering and
 217 heterogeneities in the mantle and the core (e.g. Bentham et al., 2017; Peng et al., 2008; Shearer ad Earle,
 218 2004) As shown in Figure 2 and Figure S2, the envelopes of the signals consist of several wave-packet
 219 arrivals with a time length of about 1 ms, which is more coherent across our large aperture array with 4-
 220 5 meters of interstation distances. However, the use of waveform envelopes might lower the resolution
 221 and the resulting ability of the array to locate the origin of signals in the propagation medium.
 222 For the beamforming procedure (following Rost and Thomas, 2001; Schweitzer et al., 2012) the stacking
 223 is performed on the shifted envelope of the traces w_j recorded at the sub-array, as shown in Figure S2 of
 224 Supporting Information, based on the following equation:

$$b(t) = \left[\frac{1}{M} \sum_{j=1}^M \sqrt[n]{w_j(t + \tau_j(s, \phi))} \right]^n \quad (3)$$

225 where M is the number of sensors. The n-root of the single traces reduces the difference in amplitudes,
 226 allowing coherent phases with small amplitudes to have a bigger influence on the stacked trace compared
 227 with the linear stacking ($n = 1$), and applying the power of n to the beam restores the amplitude
 228 differences, reducing incoherent noise after stacking. The search for out-of-plane signals is implemented
 229 using the slowness-backazimuth analysis, where a grid search is carried out by computing the energy of
 230 the beams for different slowness-backazimuth values.

231

232

233 3 Results

234 We apply the slowness-backazimuth analysis to the array recordings of the 52 events. To explore the
235 directionality of different energy packets arriving at the network, the analysis is carried out using a sliding
236 time-window with a duration of 4 ms. This window is moved along the entire recording with steps of
237 half the size of the window (i.e., 2 ms). Due to the reduced length of ~ 32 ms for all available recording,
238 we restrict our analysis to the P-coda, since the S-coda is sometimes abruptly interrupted by the end of
239 the recording.

240 We present the results of the slowness-backazimuth analysis as energy contour plots on polar diagrams,
241 where the direction of the energy arriving at the network can be picked (Figure 4). We clearly identify
242 the direct P-wave for all 52 events. As shown in Figure 4a,c, the direct P-wave arrival reaches the network
243 from the north-east, with the expected theoretical values of slowness and backazimuth. The theoretical
244 values were computed from the known position of the events and the array center, and the ray parameter
245 formula for a homogeneous propagation medium (Udias, 1999) with $v_p = 4570$ m/s. For the 52 events
246 analyzed, the average discrepancy between observed and theoretical slowness values for the direct P-
247 wave is of the order of 0.0073 s/km which corresponds to about 2 degrees of difference in incidence
248 angle between observed and theoretical direct P-wave, while the average residual in backazimuth is of
249 the order of 3 degrees. These small residuals lie within the average standard deviation σ , which is
250 representing the uncertainties in measuring the observed slowness ($\sigma=0.0075$ s/km) and backazimuth
251 ($\sigma=4^\circ$) values of the direct P-waves. To measure these uncertainties and estimate standard deviation, we
252 consider all points that have a variation of up to 10% in beam power with respect to the maximum (white
253 contour line in the polar plot of Figure 4c) as performed also by Schumacher et al. (2018).

254 The observations of the P-wave arrivals and the match between observed and theoretical slowness values
255 suggests the presence of a homogeneous medium between sources and receivers, at least at the short
256 wavelength signals (~ 60 cm) we used in our analysis. No other arrivals that deviate from the source to

257 receiver trajectory appear in the time window centered around the P-wave, implying that the early P-
258 coda (1 - 3 ms after the main P-wave arrival) mainly consists of direct energy radiated from the source
259 region.

260 In many cases the main P- and S-phases are immediately followed after a few milliseconds by a second
261 peak (Figure 2). Considering the distance (1 - 3 m) between the sensors and the underlying roof of the
262 A3 chamber and $v_p = 4570$ m/s and $v_s = 2597$ m/s, these second peaks are most likely reflections from
263 the top of the chamber, which acts as a total reflector since the chamber is hollow. Indeed, calculation of
264 the two-way-travel time (TWT) yields roughly 0.4 - 1.3 ms for the P-wave reflections and 0.8 - 2.3 ms
265 for the S-wave reflections for a vertical reflection. These near receiver reflections have roughly the same
266 slowness as the direct P-waves, but they arrive at the network from below. Due to the convex shape of
267 the chamber roof, defocusing of this reflected energy is expected to broaden the reflected P-wave peak
268 in the slowness backazimuth plots, as observed in the relevant time window in Figure 4c. In addition, the
269 use of the envelope in the stacking procedure might cause lower resolution of the slowness and
270 backazimuth values of the detected signals and consequently produce broader peaks. Despite this, the
271 aforementioned small uncertainties in the estimation of both observed slowness and backazimuth suggest
272 a very good capability of the envelope-based stacking method in detecting the travelling direction of the
273 waves.

274 In the later P-coda, we consistently observe secondary arrivals with propagation directions mainly from
275 the south-east (Figure 4c, middle) and observed backazimuth values ranging from 94° to 200° measured
276 from North. 17 out of 52 events show these late arrivals in the P-coda. These out-of-plane reflections
277 suggest a strong impedance contrast able to reflect/scatter the seismic energy within a wide range of
278 incidence angles. The location of the events showing out-of-plane signals can be found throughout the
279 event cluster, suggesting that these observations do not depend on event location i.e., it is not a local
280 effect.

281 On average these additional arrivals have a similar lapse time of about $6 (\pm 0.5)$ ms after the P-wave and
282 their energy is about half (0.5 ± 0.16) of that of the main P-wave arrivals. Moreover, the additional signals
283 are also characterized by a single energy peak in the energy contour plot (Figure 4c), therefore suggesting
284 that a reflector is responsible for these out of plane observations, rather than multiple-scattered energy,
285 which would appear as a series of peaks in the polar plots and a longer delay of the coda waves (Sato,
286 Fehler and Maeda, 2012). The small variance in the measured directionality (slowness and backazimuth)
287 and travel time suggests a common source region for the scattered wavefield. No other dominant arrivals
288 are visible in the contour plots of the slowness-backazimuth space at other times (Figure 4), implying
289 that the medium in the vicinity of the monitored rock volume is simple with no other scatterers/reflectors
290 influencing the data in our filtered frequency range.

291 To locate the position of scatterers/reflector responsible for the observed out-of-plane signals, we use the
292 measured slowness, backazimuth and relative travel time with respect to the direct P-wave. Particularly
293 the slowness and the backazimuth constrain the travelling direction of the out-of-plane arrival while the
294 travel time constrains the position of the scattering body along the ray-path direction (Figure 5). This
295 approach has been used in global seismology for the detection and location of heterogeneities in the Earth
296 mantle that cause scattering and/or reflection of seismic waves (e.g. Kaneshima, 2009, 2016; Kaneshima
297 & Helffrich, 2003; Rost et al., 2008; Schumacher & Thomas, 2016; Schumacher et al., 2018; Weber and
298 Wicks, 1996; Weber et al., 2015; Wicks and Weber, 1996; Wright, 1972; Wright & Muirhead, 1969).

299 We run a grid-search procedure aimed at finding the location of the scattering points which best fit the
300 observed travel times, given the observed slowness and backazimuth values (Figure 5). In our back-
301 tracing algorithm we assume that both primary and scattered waves travel in a homogeneous medium
302 which is supported by the undisturbed direct P-waves travel paths in the rock volume between the sources
303 and the receivers, for the entire azimuthal coverage available in our data. As stated before, we assume
304 that the observed out of plane signals are due to single P-to-P scattering. P-to-S scattering would have

larger travel times, unless the scatterers are located very close to the network but we can exclude this case due to the observed straight ray-paths of the direct P-waves (Figure 4c). Due to the smaller value of the S-wave velocity compared with the P-wave velocity, hence a different move-out, P-to-S scattered waves would also have larger slowness values than those observed for our out-of-plane waves (Figure 4c). We also exclude the possibility of S-to-P scattering because the observed travel times can only be matched by near source scattering, which we can exclude due to the large backazimuth deviations of the out-of-plane waves that are inconsistent with source-side scattering.

Carrying out the search for the reflector locations we find that, as expected by the small variance of the measured values of slowness, backazimuth and travel times, the reflection locations are very close to each other, defining a narrow cluster (Figure 6). As stated above and following Schumacher et al. (2018), we evaluate the uncertainties in estimating the scatter position by considering all points within the area of 90% of the maximum beam power, as shown by the white contour line in the slowness-backazimuth polar plots of Figure 4c and calculate the standard deviation of the maximum slowness and backazimuth values, which yields the angular error on the scatter position. The errors in travel time (i.e., the width of the peak) of the out-of-plane signals were picked as shown for one example in Figure 4c. On average, the travel time uncertainties are of the order of 1 ms, which roughly corresponds to a location uncertainty of about 4-5 meters. By using the back-tracing algorithm, the uncertainties in slowness, backazimuth and travel time were then translated into scattering volumes, that yield ellipses of a few meters which we project on the geological map and section of Figure 6.

The cluster of the back-projected reflection points delineates a south-west dipping steep ($\sim 70^\circ$ from horizontal) reflector located at a distance of about 70 m south-east of the network above the A3 chamber (yellow ellipses in Figure 6). It has a depth extension of about 80 m and is about 60 m long, with a strike direction about WNW/ESE. There are also 4 scatter locations which are further away from the cluster

328 (green ellipses in [Figure 6](#)). However, their origin is not clear as they do not coincide with any known
329 boundary in the geological section.

330

331 **4 Discussion**

332 By using seismic array analysis, originally developed for nuclear test monitoring and to address global
333 seismological problems (e.g. [Douglas, 2002](#); [Husebye and Ruud, 1989](#); [Rost and Thomas, 2002](#)), we
334 were able to locate the origin of the out-of-plane arrivals in the late P-coda of our in-situ acoustic emission
335 observations from 52 events recorded by a network of sensors deployed at the Asse II mine. To our
336 knowledge, the use of array analysis has never been tested on AE in-situ recordings at the small scale of
337 the mines with hypocentral distances on the order of about 100 m. While the principle of the waveform
338 stacking remains the same, there are some significant differences in the processing scheme that we
339 developed, compared with the application of array analysis at global seismological scale: 1) Due to
340 smaller source dimension (mm to dm scale) and because the high frequencies are damped more quickly,
341 in typical AE monitoring the hypocentral distances are usually within a radius of less than 200 m; 2)
342 Given the typical dimension of the network of a few tens of meters (see [Manthei and Plenkers, 2018](#) for
343 a review of AE monitoring), the approximation of a planar wavefront, that is used for most array methods,
344 might not hold. As a rough guideline, the curvature of the wavefront has an impact on the delay time
345 estimation when the source-receiver distance is smaller than about 4-5 times the array aperture
346 ([Almendros et al., 1999](#)). By excluding the outermost sensors of our network, we restrict the dimension
347 of the used sub-array to be approximately one-fifth of the minimum hypocentral distance in our dataset;
348 3) The 3D geometry of the network had to be considered in the calculation of the delay time as given by
349 equation (2), including the vertical distances between the sensors, while in global seismology the
350 elevation of the stations is often negligible compared to their horizontal relative position of stations. Note
351 also that, in contrast to standard seismological problems, in this experiment the events occur at shallower

352 depths than the receivers with the seismic energy arriving at the array from the top rather than from
353 below; 4) Given the very high frequency content of the AE (of the order of kHz) and due to the large
354 aperture of the array with sparse set of inter-sensor distances, incoherent (envelope-based) beamforming
355 is used to increase the correlation between signals recorded across the used sub-network, in contrast to
356 global seismology where the lower frequencies and the appropriate aperture array (compared also to
357 epicentral distances) allow the use of the classic (phase-based) array analysis.

358 Our observations of direct P-waves travel times agree with travel times calculated from straight ray-paths
359 from the sources to the receivers, therefore serve also as an independent constraint and validation of the
360 event locations provided by [Philipp et al., \(2015\)](#). Since we use seismic array methods and in particular
361 the slowness-backazimuth analysis, we constrain the directional information of the seismic energy
362 arriving at the network. [Figure 4](#) shows that the observed backazimuth and slowness matches the
363 theoretical values for a homogeneous medium ($v_p = 4570$ m/s) computed for each event location from
364 [Philipp et al. \(2015\)](#). If the medium between source and receiver was heterogeneous, the measured
365 slowness and backazimuth would differ from the theoretical values, because the travel path would be
366 bent. Secondly, in a homogeneous medium the backazimuth depends only on the horizontal (that is
367 geographical) position of the source with respect to the sensors and the slowness is related to the move-
368 out of the P-wave at the sensors (i.e., the incidence angle for a given v_p), which constrains the direction
369 of the source with respect to the sensors in the three-dimensional space. Then, knowing the differential
370 travel time between the first arrivals of the P- and S- wave from [Philipp et al. \(2015\)](#), allows an
371 independent estimation of source location compared with the inversion used by [Philipp et al., \(2015\)](#).

372 Using the observations of straight paths of the direct P-waves we conclude that the rock volume
373 between events and receivers in the upper salt volume does not contain structures, such as geological
374 heterogeneities or damage zones that are larger than 60 cm. Structures smaller than 60 cm that might be
375 present are not visible in this analysis and cannot be excluded, although we also filtered the data with

376 different frequency bands compared to the one used in the main analysis (3-8 kHz) and find that the
377 direct P-wave still travels relatively undisturbed through the medium. This suggests that there are likely
378 no additional impedance contrasts within the rock body sampled by the direct P-wave, which is in
379 agreement with the geological model of the salt structure (Figure 6). Confirming a homogeneous and
380 undisturbed rock volume in this particular area is an additional valuable information for the mine
381 operator, as it may provide indications on the integrity of rock above the mine's structure, in this case
382 the two chambers.

383 To verify the robustness of our assumption that the out of plane arrivals are due to P-to-P
384 reflection/scattering, rather than S-to-P or P-to-S conversion phenomena, we carried out the analysis for
385 the latter two cases. We find that it is not possible to fit the travel times using S-to-P reflections, since
386 they show a minimum residual between observed and computed travel times of about 10 ms (Figure S3),
387 much larger than the average travel time difference between the observed out-of-plane wave and the
388 direct P-wave. In contrast, using the P-to-P reflections we have residual travel time of about 0.01 ms.

389 To test the case of P-to-S reflections, we re-run the slowness-backazimuth analysis using $v_c = v_s$ in
390 equation (2) to account for the different move-out of the S waves. Using v_s we find that the S-wave direct
391 energy is focused better while the direct P wave defocusses. By back-tracing the out-of-plane arrivals as
392 potential P-to-S reflections we find that P-to-S reflection points would be located in a tight cluster directly
393 above the sensors with subvertical incidence to the array, as shown in Figure S4 of the Supporting
394 Information. This region is well sampled by the direct waves (Figure S4) and, as previously
395 demonstrated, P-waves travel undisturbed with straight ray-paths from sources to receivers which led us
396 to the conclusion that the rock volume above the sensor appears to be homogeneous (Figure 6). Since the
397 takeoff angles and azimuths of P waves and P-to-S scattered waves near the sensors are very similar
398 (Figure S5), a heterogeneous medium should affect both wave types and we can therefore exclude strong
399 heterogeneity near the sensor array above the A3 chamber. In contrast, the P-to-P reflections leave the

400 source region in a different direction compared with the P-wave (Figure S5), with larger take-off angles
401 and a range of azimuths, allowing the sampling of a larger rock volume outside the source and receiver
402 region. In addition, vertically installed piezoelectric sensors have a minimum sensitivity to vertically
403 travelling S waves, while it is maximum for horizontally travelling S waves. Since P-to-S scattered waves
404 would have a small incidence angle (see above) hence arrive almost vertically, we would not be able to
405 detect them as high-energy arrivals as those that we find in our dataset. Finally, the comparison with the
406 geological section and map (Figure S4) shows that the P-S reflection point locations do not coincide with
407 any known major geological discontinuity or structure within the *Rock salt (z3)* of the *Leine Zechstein*
408 sequence. We therefore believe that P-to-P reflections are a robust and valid explanation for the observed
409 out of plane arrivals.

410 It is unfortunate that the length of the recordings is limited in time by the event triggering which does not
411 allow us to use and analyze the S-coda as an independent proof of the imaged reflector as shown by
412 Weber and Wicks, (1996) and Weber et al. (2015) for the detections of heterogeneities at the larger scale
413 of the Earth's mantle. S-to-S reflections would arrive at travel time of at least 35 ms, while our recording
414 last 32.768 ms.

415 The frequency band (3-8 kHz) used in our analysis places some constraint on the gradient of the
416 impedance contrast across the reflector that is responsible for the observed P-to-P out-of-plane signals.
417 Considering a $v_P = 4570$ m/s and the highest frequency content of the signal, the impedance contrast
418 must vary within a wavelength of about 60 cm i.e., a sharp reflector. This agrees well with the geological
419 cross section and map of Figure 6, which show that the reflection points are located closely to an abrupt
420 lithological boundary at the southern flank of the salt dome.

421 The position of our calculated reflection points match the position of the southern flank of the salt dome
422 at depth between approximately -180 and -260 m (below mean sea level, m.s.l.), and define the
423 orientation (WNW-ESE) and dipping ($\sim 70^\circ$ from horizontal) of the contact between the salt dome and

424 the host rock, as shown by the yellow ellipses in [Figure 6](#). This part of the salt dome is characterized by
 425 the presence of thin, steep, subparallel layers marking the boundary of the main salt body, where the
 426 Permian *Rock salt* dome from the *Leine* (z3) and *Aller* (z4) *Zechstein* sequence is in contact with the
 427 lower Triassic *Röt anhydrite* of the *Buntsandstein* formation. The green ellipses in [Figure 6](#) represent
 428 scatterers whose location is far from the main cluster of reflection points (yellow ellipses in [Figure 6](#))
 429 and away from any lithological boundary in the geological section. However, the geological map shows
 430 that these location points might relate to a minor lithological contrast in the salt dome, where the
 431 *Anhydrite and salt layers* (z3) formation bends and extends over the *Rock salt* of the *Leine* sequence (z3)
 432 (see map in [Fig. 6](#)).

433 Based on the geological information reported in [Figure 6](#), the topography of the detected reflector is not
 434 expected to be rough. This allows us to calculate reflection coefficients assuming a flat discontinuity in
 435 order to compare them with measured P-to-P/P amplitude ratios. In computing the measured amplitude
 436 ratios we assume that the direct P-wave amplitude represents an estimate of the amplitude of the incident
 437 wave at the reflector. However, differences in take-off angle and azimuth at the source between the
 438 observed direct P-wave and the P-to-P reflection ([Figure S5](#)) might affect the P-to-P/P amplitude ratio.
 439 Despite this, we measure linear ($n=1$ in equation (3)) beam amplitude ratios of the P-to-P reflections and
 440 the direct P-waves and we compare them with the P-to-P reflection coefficient computed for an
 441 impedance contrast using the v_P , v_S , and density values for the lithologies across the salt dome edge
 442 (*Rock salt* and *Buntsandstein*), as provided by the Asse II mine operators and as found in [Karp et al.](#)
 443 [\(2011\)](#). We show the result of this comparison in [Figure S6](#) of the Supporting Information. For
 444 completeness we also computed theoretical P-to-S reflection coefficient values, although, as shown
 445 above, we can exclude this possibility based on travel times. Overall the P-to-P reflection coefficient
 446 agrees well with the observed amplitude ratios with discrepancies most likely due to source directivity.

447 It is possible that our out-of-plane waves result from a change in the rheology of the rocks involved,
448 since the location of the reflector agrees with the presence of a narrow branch of seismic activity along
449 the southern flank of the salt dome, at the depth and location where we find our reflections (Philipp et
450 al., 2015). In particular, cluster C1 of seismic activity, as reported in Philipp et al. (2015), is confined to
451 the edge of the salt rock and does not extend into the host rock. In this study, we do not attempt to
452 discriminate between different causes for the observed reflections based on amplitude, since amplitudes
453 of seismic waves depend on many factors, such as source directivity, radiation pattern, and anisotropy
454 which leads to magnification or reduction of the reflection coefficients in certain travelling directions
455 (e.g., Pisconti, et al., 2019). Source directivity and radiation pattern might also be a cause for the lack of
456 clear out of plane signals in several events of our dataset, which leaves us with only 17 out of 52 events
457 that show the additional arrival. Furthermore, the true amplitude of the waveforms are difficult to
458 estimate because the instrument response of piezoelectric AE sensors is partially unknown. Accurate
459 waveform modelling would be required to distinguish between these causes, which is beyond the scope
460 of this study but might be of interest in future studies.

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463 **5 Conclusions**

464 In this work we test the application of seismic array methods on in-situ AE recording from the Asse II
465 salt mine in Lower Saxony (Germany). We use recordings of 52 events from a network of 16 piezoelectric
466 sensors deployed above one of the chamber at Asse II. Hypocentral distances range from 120 to 150 m.
467 Applying a technique developed for monitoring the nuclear test ban treaty and for global seismology to
468 in-mine AE recordings requires some adjustments and complementary processing. To enhance the
469 correlation between the signals in the stacking procedure used in the application of array analysis: (1) we
470 compute the envelope of the bandpass-filtered data (3 – 8 kHz), which gives more emphasis to the

471 amplitude of the signal itself rather than its phase; (2) we reduced the size of the network (~ 20 m) to be
472 at least one fifth of the smaller hypocentral distances, which allows us to perform the stacking based on
473 a planar wave-front approximation; (3) we need to take into account that sensors are located at different
474 depth levels.

475 By applying the slowness-backazimuth analysis we found that all 52 events show direct P-wave arrivals
476 that consistently appear with the expected slowness and backazimuth values for a homogeneous medium,
477 indicating straight ray-paths between source and receivers. This confirms both homogeneity of the
478 sampled rock volume (at wavelength of ~ 60 cm) between sources and receivers and agrees with the
479 geological maps, and event locations as shown by [Philipp et al. \(2015\)](#).

480 We also find high amplitude pulse-like additional arrivals in the late P-coda of our AE recordings in 17
481 out of 52 events. Using seismic array methods we confirm these arrivals to be out-of-plane reflections
482 travelling to the network from the south-east. Assuming P-to-P single scattering and using the measured
483 backazimuth, slowness and travel time we back-project the data and find a narrow cluster of reflection
484 points delineating a SW dipping ($\sim 70^\circ$ from horizontal) steep reflector extending for about 80 meters
485 (from about -180 to -260 m below m.s.l.) in depth and 60 m in length. When compared with the available
486 geological information, this reflector matches a known lithological boundary, which has a strike direction
487 WNW/ESE and pertains to the transition from the Permian main salt body (*Rock salt* from the *Leine* (z3)
488 and *Aller* (z4) *Zechstein stratigraphic sequence*) to the lower Triassic *Röt anhydrite* of the *Buntsandstein*
489 formation. The reflector provides an estimation of the position and inclination of the southern flank of
490 the salt dome at a distance of about 70 m from the network.

491 This study proves that array seismology works at the small scale of mines and can be a valuable additional
492 technique to detect geological heterogeneities and structures underground. To our knowledge this is the
493 first application of array seismology techniques to mines and we find that this additional information
494 could potentially support efforts to reduce hazard risks and might lead to more efficient mining operations

495 and monitoring of underground nuclear waste repository mines. Large amounts of data are often collected
496 in standard routines underground (microseismic monitoring / in-situ AE monitoring) in the framework
497 of structural health monitoring and are available without deploying more instruments. These existing
498 data are able to provide significantly more information on a bigger rock volume, than currently exploited
499 in mine monitoring for hazard and risk purposes using both indirect and direct methods (i.e. drillings).
500 The analysis routine proposed in this work can be further tested and applied to other AE signals in
501 different mines setting, provided that the size of network is at least one fifth of the hypocentral distances.
502 The automatization of such technique and its application to large datasets including also the S-coda
503 analysis by increasing the recording's triggered time length, might provide an innovative and detailed
504 passive 3D image of the mine structure in future work.

505

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Figure 1. Map and geological section of the Asse II upper salt dome with events (red circles) and sensor locations (black triangles) used in this study. The geological cross section shows the main lithological formation with the upper part of the salt dome consisting of the Permian *Zechstein* evaporitic cycle (z2-z7) and the early Triassic *Buntsandstein* (map: BGE, Asse II mine, operational state after mining plans from April 1999, last updated on 22nd of February 2016; section: BGE, Asse II mine, operational state after mining plans from January 2012, last updated on 28th March 2012). The inset on the bottom left shows the detailed 3D locations of the piezoelectric sensors (black triangles) placed in boreholes (blue lines) on the roof of the A3 chamber of the Asse II mine, whose shape is represented by the gray lines. Depth are in meters below mean sea level (m.s.l.).

Figure 2. (a) example of single channel AE waveform recording from channel (trace) 12 of the network. (b) Record section (distance versus time) of a typical in-situ acoustic emission array recording of a small event that occurred in the upper salt dome of the Asse II mine. As in (a), waveforms were filtered using a bandpass filter of 3 – 8 kHz. Positive and negative amplitude lobes of waveforms are filled using yellow and black colors, respectively, while the envelopes are shown as blue lines. Both direct P- and S-waves clearly show their different move-out at the 16 sensors, as marked by the solid red lines. The red box with a question mark indicates additional pulse-like arrivals in the late P-coda.

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770 **Figure 3.** (a) Network configuration, as seen from above looking down into the Earth, and relative position of the
771 sensors with respect to the geometrical center of the array. x_{15} and y_{15} mark the distance from the center of the
772 array to sensor 15. A planar wave-front crossing the receivers with backazimuth Φ from North is indicated by
773 dashed lines. (b) Side view of sensor locations projected onto the sagittal plane containing the incident ray and
774 crossing the array with apparent velocity $v_{app} = v_c / \sin i$, where i is the incidence angle and v_c is the propagation
775 velocity of the medium. (c) Euclidean distance (r_j) between sensors and array center showing the sensors (in blue)
776 used in the analysis, within a distance range of maximum 15 meters, and the excluded sensors (in red)
777 clustered far away from the network center.

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Figure 4. (a) source (red circles) to receiver (triangles) configurations and ray trajectory (black line) for the event shown in Figure 2. (b) Record section of the waveform envelopes for this event. The envelopes considered in the analysis are shown in blue, while the discarded envelopes are shown in red (see text and Figure 3). Grey areas denote three selected time windows used for analysis. (c) Polar plots of slowness backazimuth contours for the beam power for the three time windows shown in (b) indicating the incoming direction of the energy as function of backazimuth (baz) and slowness (u) at the A3 network (displayed as reference at the center of each polar plot). The slowness (or the incidence angle at the array, inc) is increasing along the radial direction, while the backazimuth is represented as angle clockwise from North. The beam power is normalized to the power of the direct P-wave energy. Window 1 shows a strong direct P-wave arrival with slowness and backazimuth in the direction of the source. Window 2 shows a dominant out of plane secondary arrival with energy maximum coming from the south-east and traveling with a difference of 80° to the direct P-wave (shown by the solid black circle). This window encompasses the secondary arrival shown in the single recordings (b) and Figure 2. Window 3 shows no strong energy arrivals in the late P-coda. The white contour line in the polar plots of time windows 1 and 2 indicates the 0.9 isoline of the maximum for each arrival in the normalized beam power, from which we computed the uncertainties in slowness and backazimuth. Below each polar plot, the relevant beams are shown as computed using the slowness and backazimuth values of the energy maximum. Shown is also the uncertainty on the travel time estimation (dt) for the out of plane arrival of window 2.

Figure 5. 3D schematic illustration of the back-tracing algorithm used to find scatter locations. The red star indicates the event, the yellow circle indicates the scatter location and the black triangles represent the network. The ray path direction at the receiver is drawn given the measured backazimuth (baz) from North and incidence angle inc (from zenith).

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Figure 6. Geological map at a depth of 200 m below m.s.l. (left) and section (right) of the upper part of the salt dome (map: BGE, Asse II mine, operational state after mining plans from April 1999, last updated on 22nd of February 2016; section: BGE, Asse II mine, operational state after mining plans from January 2012, last updated on 28th March 2012). Location of the events (red circles), sensors (black triangles) and scattering volumes (yellow and green ellipses) are also indicated. The four green ellipses refer to scatterers located far from the lithological boundary that mark the southern flank of the salt dome. The ellipses represent the scattering volumes as computed from the uncertainties of slowness, backazimuth and travel time (see text for more information). The straight grey lines show the direct P-wave raypaths from the events to the array center, while the white segmented lines indicate the incident and reflected raypaths of the out-of-plane observations.

Supporting Information for

Mapping lithological boundaries in mines with array seismology and in-situ Acoustic Emission monitoring

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Figures S1 to S6

Introduction

The supporting information includes additional explanatory figures that are complementary to the research reported in the main document. In particular: Figure S1 shows a spectrogram displaying the dominant very high frequency nature of a typical AE recordings analyzed in this work; Figure S2 shows delay and sum (beamforming) processing on both the original filtered waveforms and their envelopes, justifying the use of incoherent (envelope based) stacking in our analysis; Figure S3 shows residual travel times (between observational and theoretical out of plane arrivals) obtained when interpreting the observed out of plane arrivals as S-to-P reflections and Figure S4 illustrates the locations of potential P-to-S reflections clustered in the homogeneous medium directly above the sensors, which is also sampled by the undisturbed direct P-waves; Figure S5 shows take-off and azimuth angles at the source for P, P-to-P and P-to-S rays and Figure S6 illustrates P-to-P (and P-to-S) theoretical reflection coefficients computed using the expected impedance contrast across the lithological boundary at the southeastern edge of the main salt body, that we sample with our observed out of plane arrivals, whose amplitude ratio with the direct P wave is also shown.

Figure S1. Spectrogram of the recording shown on top (trace 12 from Figure 2 of main document) highlighting the dominant frequency of the signals within the band 3 to 8 kHz (white dashed lines) used in the analysis of the waveform in this study.

Figure S2. Aligned and filtered (bandpass 3-8kHz) traces (black) and their envelopes (blue), for the event shown in Figure 2 of the main document. Alignment is done using the slowness and back-azimuth of the direct P-wave. The top trace represents the linear beam based on the stacking of the original signals (black trace) and their envelopes (blue trace), the latter showing a higher amplitude.

Figure S5. Lower hemisphere Schmidt projection displaying take-off and azimuth angles of direct P (red) P-to-P (yellow and green) and P-to-S (cyan) rays leaving the sources. The black cross at the center indicates the vertical radial direction (nadir) looking down into the Earth. Solid points indicate lower hemisphere directions, while the only green cross located to the SW indicates a ray leaving in the upper hemisphere direction.

Figure S6. Reflection coefficient for P-P (solid blue line) and P-S (dashed magenta line) computed for the impedance contrast between the *Rock Salt* ($v_P=4570$ m/s, $v_S=2597$ m/s, $\text{density}=2090$ km/m³) and the *Bundsandstein* ($v_P=5030$ m/s, $v_S=2900$ m/s, $\text{density}=2820$ kg/m³). Velocities and densities were provided by the Asse II mine operators and can be found in [Karp et al., \(2011\)](#). v_S for the *Bundsandstein* formation was estimated using the Poisson's solid approximation. The observed P-to-P/P amplitude ratios are color coded by their difference in take-off angle at the source, showing that possible discrepancies with theoretical values might be due to source geometry. Only reflection points located closely to the salt dome edge of Figure 6 are shown. Reflection coefficients were computed using the Zoeppritz CREWES Matlab Toolbox ([Margrave and Lamoureux, 2019](#)).