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HAL Id: hal-02388362
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Submitted on 1 Dec 2019

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Electron Transfer at the Metal Oxide/Electrolyte Interface: A Simple Methodology for Quantitative Kinetics Evaluation

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ABSTRACT: While quantitative models exist for measuring rate constants for electron exchange at the surface of semiconductors to or from redox couples in solution, their use is very limited for studying transition metal oxide electrodes. Taking advantage of the possibility of tuning the doping level of WO₃ by thermal treatment, we measured the rate constants for electron injection from soluble probes in the so-called reverse mode. Hence, we could demonstrate that intermediate states located below the conduction band take part to the oxidation process and that the rate constant is bimolecular with a first order dependence on the concentration of redox probes and the concentration of intermediate states. A kinetics model was thereby developed to describe this reverse mode and a zone diagram established which can then be used to quickly assess rate constants for interfacial electron transfer on the surface of transition metal oxides semiconductors that are critical for applications such as solar energy conversion.

Introduction

The ever-growing demand for clean and sustainable energies urges us to expand the use of renewable energies and to develop new energy storage and conversion devices. The last decades have thus seen the emergence of new classes of materials which led to the development of technologies such as Li-ion batteries, solar cells, fuel cells, photo-electrolyzers, among others. One class of materials has been critical for the development of these technologies, namely the transition metal oxides (TMO), and numerous efforts are still paid at further improving their physical and chemical properties. Along these efforts to design better materials, the realization that mastering the electrochemical interfaces became always more prominent.¹ Yet, controlling the charge transfer at the solid/solution interface becomes increasingly important for all these applications. Indeed, it is critical to prevent side reactions occurring at high potential on the surface of positive electrodes for Li-ion batteries² or to enhance dye-sensitive solar cells³–⁵ or photo-electrolyzers⁶–⁹ properties for instance by proper interface engineering. Therefore, only controlling this interface will allow for developing the next generation of energy storage and conversion devices.

Despite recognizing the importance of such fundamental understanding, relatively limited kinetic information has been obtained on transition metal oxides electrodes. Hence, a strategy commonly adopted consists in using soluble redox molecules from which qualitative observations about electron transfer are often made to evaluate the quality and the doping density of such electrodes.¹⁰–¹¹ However, quantitative models derived from the field of semiconductors physics exist, but their use is very limited in experimental studies¹⁵–¹⁷. This can be, in part, explained by the relative difficulty to accurately control physical parameters of TMO electrodes such as thickness and porosity, the surface termination and the
presence of surface states and the doping level, among others, to ensure sufficient reproducibility for the kinetics measurements. Theories on electron transfer mechanism at the interface between a semiconductor (SC) electrode (Figure 1a) and an electrolyte (Figure 1b) have been extensively studied. A simple description of the accepted model proposed by Marcus, Hush, Gerisher, Memming and others is presented in Figure 1c for n-type SC. Several cases were previously described in the literature that we briefly summarized below. For further details, readers can refer to previous reviews on this topic.

In the left side of Figure 1c is depicted a n-doped semiconductor at its flat band potential ($E_{fb}$) in contact with two redox probes of different standard potentials ($E_{redox}^0$ and $E_{redox}^0$, with $E_{redox}^0 < E_{fb} < E_{redox}^0$). For these two probes, electron exchange with the semiconductor electrode is supposed to occur through the conduction band (CB) as the valence band (VB) is too far in energy. For a redox couple with a standard potential negative to the conduction band edge, when the applied potential equals $E_{redox}^0$, the semiconductor is accumulating electrons at its surface in a so-called space charge layer. Under these conditions, whether a positive or negative bias is applied (compared to $E_{redox}^0$), the SC is maintained in an accumulation mode. Thus, a large density of states is available for electron transfer from the reduced form “Red” of the redox couple (filled states in the Gerischer model) to the semiconductor CB, and inversely from the CB to the oxidized form “Ox” (empty states) of the redox couple. Therefore, the SC behaves like a metallic electrode and the resulting cyclic voltammetry (CV) curve exhibits a typical reversible wave.

When the applied potential equals the standard potential of a redox couple located in the bandgap ($E_{redox}^0$, $E_{redox}^0$ and $E_{redox}^0$) in Figure 1c, the SC is in a depletion mode. The density of majority charge carrier (electrons in the case of a n-doped SC) in the space charge layer is lower than in the bulk. Under application of a negative bias, the band bending is lowered but the SC is still in a depletion regime and the density of electrons at the surface is very low. Therefore, in the so-called forward mode, i.e. injection of electron from the n-type SC to Ox, little cathodic current is expected. A large negative bias is then required to reach the flat band potential and suppress the potential barrier due to bend bending. Once this sufficiently negative bias is applied, a significant electron density at the SC surface is restored leading to an increase of the redox probe reduction current. A least studied case is the so-called reverse mode. When a positive bias is further applied, the depletion is strengthened and the band bending is increased. There are no states available in the SC at the Red energy distribution level, and a high potential barrier
prevents electron transfer from the probe to the CB. While this last case was previously described in the literature, very few is known concerning its kinetics which we intend to investigate in this work.\cite{36,39}

Rather than developing a new physical model, our aim is to provide a simple methodology so to quantitatively assess the electron transfer rate at the oxide/electrolyte interface in this reverse mode. In that respect, we revisited the approach consisting in using soluble molecular redox probes to investigate the electrochemical behavior of n-type semiconductors in a reverse bias mode (anodic polarization) taking WO$_3$, vastly studied as photocatalyst or for its electrochromic behavior, as a model oxide. Doing so, we could demonstrate the bimolecular nature of the rate constant characterizing this mode. Furthermore, we could provide evidence that this behavior is nested in the presence of so-called "intermediate states", i.e. energy levels created just below the conduction band of n-type SC and that can be thermalized. Then, using a kinetic model, we provide researchers from the broad field of energy a simple guide from which not only kinetics constants for electron transfer could be extracted, but also the quality of any transition metal oxides SC thin film could be rapidly and accurately assessed independently of the doping level.

Results

Energy levels diagram

Dense crystalline sol-gel WO$_3$ and TiO$_2$ films were synthesized on Fluorine-doped Tin Oxide (FTO) electrodes by a previously reported dip-coating technique (see Supporting Information, SI, for experimental details on the synthesis and characterization of the two oxides).\cite{35} The films were approximately 150 nm thick and presented a low degree of porosity (Figures S1 and S4 in SI). A series of porous WO$_3$ films were also prepared in order to investigate the effect of the porosity. Energy diagrams (Figure 2) reconstructed for WO$_3$ and TiO$_2$ from ultraviolet photoemission spectroscopy (UPS) and UV-vis measurements (see Figure S2 and S3 for UPS and UV-Vis results) are consistent with those previously reported in the literature for films deposited by wet techniques.\cite{35,36}

The two scales (energy and potential) of the diagram are correlated according to the equation:\cite{37}

$$E_{Energy/eV} = -4.7 - E_{Potential/V vs Ag/AgCl}$$

In the rest of the article, all energies are given using the potential scale, and potentials are reported in V vs Ag/AgCl.

In addition to the transition metal oxides band energies, the energy diagram in Figure 2a also includes the standard potential of five selected redox molecules, which will serve as probes to study the electron transfer with the semiconductor films. The chemical structure of the molecular redox probes and their standard potential in acetonitrile are reported in Figure 2b. These probes are all based on the same bis(cyclopentadienyl) motif and were selected because 1) they all demonstrate a reversible one-electron wave on metallic electrodes and 2) their standard potentials cover a wide potential window of more than 2 V.\cite{14,38} Hence, among the five selected redox probes, the two most negative (CoCp$_2$Me$_{10}$ and CoCp$_3$) have standard potentials within the conduction band of both WO$_3$ and TiO$_2$, while the three others lie in the band gap of the two oxides.

![Figure 2](image_url)  

Figure 2. (a) Band energy diagram of sol-gel WO$_3$ and TiO$_2$ films, compared to the 5 redox probes standard potential. (b) Molecular structure of the 5 selected redox probes with their standard potential in acetonitrile in V vs. Ag/AgCl.

Electrochemical measurements

The CV responses for the five molecular redox probes were studied on WO$_3$ and TiO$_2$ coated electrodes and compared to the responses measured with glasy carbon (GC) and non-coated FTO electrodes (Figure 3 and Figure S5; additional experimental details in SI). As expected, the five redox probes showed a perfectly reversible one-electron signal on GC and FTO. A similar response was observed with porous WO$_3$ films, indicating a rapid diffusion of the molecular redox probes through the pores of the films to the underlying FTO electrodes. On the contrary, the responses on dense metal oxide semiconductor electrodes were noticeably different, suggesting that diffusion phenomena can be neglected and that electrodes can be seen as flat and non-porous surfaces of WO$_3$ or TiO$_2$. For both WO$_3$ and TiO$_2$ electrodes, the two most negative redox probes with a standard potential in the TMO conduction bands (CoCp$_2$Me$_{10}$ and CoCp$_3$) demonstrate an almost perfectly reversible signal with apparent standard potentials similar to the ones measured on GC.
Only a slight increase of the peak separation ($\Delta E_p = E_{p,a} - E_{p,c}$) could be observed (Table S1 in SI). Unlike the behavior observed for CoCp$_2$Me$_{10}$ and CoCp$_2$, the electrochemical responses for the most positive redox probes (Fc, FcAc) on WO$_3$ and TiO$_2$ were dramatically different from the ones on GC. Indeed, a large drop of the current intensity was observed on the two TMO electrodes. The shapes of the CV were also far from the typical reversible – diffusion limited wave, and were noticeably different between WO$_3$ and TiO$_2$.

![Figure 3](image-url)

Figure 3. (a) Cyclic voltammetry of solutions of CH$_3$CN + 0.1 M n-Bu$_4$NPF$_6$ at 0.1 V/s under 1 atm. Ar on GC, WO$_3$ and TiO$_2$ working electrodes in absence (grey dotted lines) and in presence (colored plain lines) of the 5 redox probes at 1mM. (b) Anodic ($E_a$) and cathodic ($E_c$) onset potentials of the 5 redox probes as function of the working electrode material. Onset potentials are measured at the foot of the anodic and cathodic waves.

On WO$_3$, a clear anodic plateau could be distinguished, with a current decreasing with increasing standard potential for the redox probes. These anodic plateaus were accompanied by a cathodic peak on the reverse scan. Moreover, the onset potentials for these plateaus were similar to the onset potential of the anodic peak measured on GC, and the peak separation was found to moderately increase in comparison to GC (Figure 3b and Table S1 in SI).

On TiO$_2$, the positive redox probes (FcMe$_{10}$, Fc and FcAc) present a poorly defined anodic wave of relatively low current density in comparison to the diffusion limited reversible wave. The anodic onset potentials of these waves are significantly more positive than on GC or on WO$_3$. On the reverse scan, one or two cathodic peaks could be observed, once again, at more negative potentials than on GC, leading to a very large separation between the anodic and the cathodic features. Hence, for the three most positive probes, the cathodic peaks were lying at about the same potential (~0.3V), independently on their standard redox potential. This effect is similar to the so-called leveling effect previously discussed by Bard et al. for TiO$_2$.$^{13,14}$ This leveling of the redox potential is therefore attributed to the presence of trap states in the band gap of TiO$_2$ that mediate the electron transfer from the SC to the redox molecule, and vice versa. The absence of leveling effect for WO$_3$ strongly suggests the absence of trap states in the band gap mediating the charge transfer, and the existence of a different electron transfer mechanism.

The results reported in Figure 3 match well with the model of electron transfer developed by Gerischer.$^{20,22,25,39}$ The redox couples with standard potential above the lower edge of the conduction band (CoCp$_2$Me$_{10}$ and CoCp$_2$) show a reversible signal, while the exchange current is significantly reduced or almost suppressed for redox probes with standard potential in the band gap (FcMe$_{10}$, Fc and FcAc). We therefore decided to investigate in depth the origin for the low current anodic plateau observed for Fc and FcAc on WO$_3$ at a reverse bias mode.

In Figure 4a is shown a typical CV for Fc at $v = 0.1$ V.s$^{-1}$ and a concentration of 1 mM. The CV curve exhibits the characteristic anodic plateau accompanied by a cathodic peak on the reverse scan. We first demonstrate that the anodic plateau is scan rate independent from 50 to 1000 mV.s$^{-1}$, at a fixed Fc concentration of 1 mM (Figure 4b-c).

In contrast, the current for the anodic plateau varies linearly with the Fc concentration from 1 to 25 mM (Figure 4d-e). Hence, the rate for electron transfer from the probe to the SC shows a first order dependence on the concentration of the probe below a critical concentration. Over this critical concentration of about 25 mM, the correlation between the redox probe concentration and the plateau current deviates from linearity. As further discussed later on, this saturation effect was previously described and interpreted as a limitation related to the amount of available empty “intermediate states” in the SC mediating the electron transfer between the redox probe and the SC conduction band.$^{31}$
Electrochemical doping

Inspired by this result, we then explored the effect of increasing the density of these “intermediate states” for WO₃ under reductive potential. The shift of the cathodic inversion potential toward increasingly negative potential is supposed to partially reduce WO₃ and to create “intermediate states” below the CB. Because of the close proximity of these “intermediate states” with the CB minima edge, these states can be thermally ionized and electrons injected into the CB. This process increases the doping density of the SC and simultaneously leaves empty surface states that enhance the electron uptake from reduced redox probes. Two different solutions were thus prepared, the first one containing CoCp₃, FeMe₆0 and Fc (Sol. A) and the second one containing CoCp₃, FeMe₆0 and FeAc (Sol. B). The CVs for these two solutions with a cathodic inversion potential progressively shifting from -1.25 V (red curve) to -1.95 V (blue curve) are given in Figure 5a,b. A standard one-electron reversible signal is observed for CoCp₃ regardless of the cathodic inversion potential, ensuring that no film degradation occurs during the reduction process. In contrast, the three other probes see their signal evolving from no current to an almost perfectly reversible wave. This process was found reversible, and the anodic current decreases when increasing back the cathodic inversion potential to its original value (Figure 5g). The evolution of the anodic peak current for the three probes (FeMe₆0, Fc and FeAc) with the cathodic inversion potential is plotted in Figure 5c. The onset cathodic inversion potential for which the probe oxidation current starts to increase (green, blue and purple arrows in Figure 5d) is around -1.55 V for FeMe₆0 in both solutions A and B, and around -1.70 V and -1.80 V for Fc and FeAc, respectively. The linear correlation found between the standard potentials of the redox probes and the onset cathodic inversion potentials (Figure 5d) suggests that the more positive the standard potential (the further from the CB), the highest the concentration of empty intermediate states is required to allow electron transfer.

Visually, no color change of the WO₃ electrodes was observed during the progressive shifting of the cathodic inversion potential towards negative values. Likewise, in situ spectroelectrochemical measurements monitoring
the UV-vis absorbance of the WO₃ electrode while the cathodic inversion potential was shifted from -1.35 to -2 V didn’t show significant changes of absorption in the visible range (Figure S1o). This tends to rule out the formation of bandgap states due to the bulk reduction of W⁵⁺ to W⁴⁺, giving a deep blue coloration to the oxide.⁴³-⁴⁴

**Chemical doping – bimolecular process**

Using an electrochemical approach, we have qualitatively established that variation of the majority charge carrier (electrons) concentration by application of increasingly negative potentials is associated with the formation of empty intermediate states just below the CB that enhance the rate of probe oxidation at the SC surface. We then adopted a chemical approach for quantitatively monitor the SC doping density and establish a general kinetic model for the electron transfer from the redox probe to the SC.

For that, several WO₃ films underwent thermal treatments under a reductive atmosphere (5% H₂ in Ar) at 350°C for 20 to 45 min, treatment frequently used to increase the doping density of transition metal oxides.⁴⁵-⁴⁹ First, the doping density for these films was determined from the slope of the linear part of the Mott-Schottky (MS) plots obtained from impedance spectroscopy (see SI for more details) and the flat band potential was then estimated from the intercept of the slope with the x-axis. The electrochemical behavior of these H₂-treated electrodes was then investigated with solutions containing Fe(CN)₆³⁻, Fe and Fe(CN)₆⁴⁻. The CV for Fe on six different films as well as the corresponding MS plots are reported in the Figure 6a,b and compared with the electrochemical response measured for a GC electrode. The anodic current response measured by CV was found to increase with decreasing slopes on the MS plots (Figure 6a,b). Since the slope of the MS plot is inversely proportional to the doping density, this observation indicates that an increasing doping density leads to increasing anodic currents, evolving from low current plateaus for low doping densities to almost perfectly reversible wave for sufficiently high doping densities. This evolution is fully consistent with our previous observations made during the electrochemical reduction of WO₃ films. When plotting the anodic plateau or peak current versus the doping density, a clear trend can be established (Figure 6c). Hence, for relatively low donor density, the CV anodic response measured for Fe exhibits a plateau behavior, whose current intensity increases linearly with the doping density (red “Plateau” area in Figure 6c and Figure 7a). In this case, the current is purely limited by the kinetics of the electron transfer between the redox probe and the oxide film.

Above a certain doping density, the anodic plateau turns into peak, whose intensity progressively tends toward the Nernstian diffusion limited one-electron wave obtained for GC (blue “Peak” area in Figure 6c). In this latter case, the current is no longer limited by the electron transfer rate, but by the diffusion of the redox probe from the bulk solution to the electrode surface. Similar correlation could then be established for Fe(CN)₆³⁻ and Fe(CN)₆⁴⁻ (Figure 7b,c), where, alike for Fe, a linear trend between the anodic plateau current and the doping density could be observed in both cases.

Therefore, we establish a first order dependence for the anodic current on a reverse bias mode for n-type SC with the doping density. Combined with the first order dependence with the concentration of redox probe previously established (Figure 4c), this first order dependence on the doping density indicates that the charge transfer rate constant from the probe to WO₃ is bimolecular.⁵⁷

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![Figure 6.](image-url) (a) Cyclic voltammetry of Fe in CH₃CN + 0.1 M n-Bu₄NPF₆ under 1 atm. Ar on working electrodes of GC (black) and WO₃ with various amount of doping (colored). (b) Mott-Schottky plot of the corresponding electrodes. MS measurements were performed in CH₃CN + 0.1 M n-Bu₄NPF₆ under 1 atm. Ar in absence of redox probe. (c) Variation of the anodic plateau current with the doping density of the metal oxide electrode. “P/PR” and “G/GR” refer to the zone denomination as explicated in the zone diagram in Figure 9.
d) Correlation between the apparent rate constant and the standard potential of the redox probes.

**Physical origin**

After demonstrating the bimolecular nature for the charge transfer rate constant in the reverse bias mode, the question then arises about the physical origin for such transfer. As already mentioned, we assume that doping the SC film leads to the formation of “intermediate empty states” below the conduction band and, hence, we propose that oxidation of the probe in the reverse bias mode results from electron transfer from the probe to these empty “intermediate states”. These states may be qualified as “intermediates” since electrons transiently reside in these states, before to be transferred to the conduction band and eventually to the underlying conductive electrode. Our proposition is indeed supported by the following observations:

i) the reverse (anodic) current is not diffusion limited, ii) the variation of the current with the probe concentration and the doping density follows a first order law and iii) the current saturates above a limiting probe concentration. The last observation indicates that above a limiting concentration, the electron transfer from the intermediate state to the conduction band becomes rate limiting. The existence of a rate-limiting “intermediate state” has been similarly proposed by Memming for the reduction of a redox probe which standard potential is within the band gap of a p-type SC (reverse current and reverse bias). It was found that reverse (cathodic for p-type SC) current was lower than what would be expected for a diffusion limited process, and that the current increases with the probe concentration up to a limiting concentration. Above this concentration, the electron transfer from the valence band to the intermediate states become the rate determining state: the current saturates and further addition of redox probe in solution doesn’t lead to any increase of the current.

Altogether, these features suggest that a similar mechanism is ongoing in our system and that intermediate states may govern the electron transfer process at the WO3/electrolyte interface.

Moreover, our model does not take into account the reorganization energy, $\lambda$. However, based on previous reports, $\lambda$ for Fc would be close to 0.7 eV in organic solvents. Hence, given that the CB minima is located at approximately -0.7V vs. Ag/AgCl, no overlap is expected between the conduction band of WO3 and the states distribution of redox probes with potential greater than ≈ 0 V vs. Ag/AgCl (Figure 1). This is experimentally confirmed when observing the potential independent plateau for Fc and FcAc, even for a large charge carrier concentration. Furthermore, the anodic current was found to decrease at fixed charge carrier density when increasing the standard potential of the redox probe (from Fc to FcAc, Figure 7). A narrowing of the space charge region at greater anodic potential allowing for electron tunneling can thus be ruled out to explain this oxidative behavior.

Furthermore, no significant changes were detected on both UV-vis spectra and SEM-FEG pictures between pristine WO3 electrodes and WO3 electrodes treated under H2 5% in Ar at 350°C for 30min (see Figure S3e and Figure S6 in SI). These observations are corroborated by XPS measurements (Figure S7) performed on a H2 treated electrode showing only a slight increase of W5+ concentration, indicating that the reductive treatment may generates a small amount of surface intermediate states (W5+ states), but is not affecting the bulk of the materials. These measurements are therefore consistent with the presence of intermediate states involved into the oxidative process and which concentration is dependent on the concentration of majority charge carriers. Eventually, this supports the view proposed by Memming and coworkers that these intermediate states can originate from the thermal activation of majority charge carriers from surface states located below the CB into the CB.

![Figure 7](image1.png)

**Figure 7.** Variation of the anodic plateau current of Fc (a), FcAc (b) and FcMes (c) with the doping density of the WO3 electrodes. (d) Correlation between the apparent rate constant and the standard potential of the redox probes.

![Figure 8](image2.png)

**Figure 8.** Energy diagram representing the electron transfer mechanism between a redox probe in solution and the semiconductor metal oxide electrode through intermediate states (IS).
**Kinetic model and quantitative analysis**

Based on the above discussion, the experimental finding can be rationalized with the kinetic scheme shown in Figure 8. The semiconductor oxide electrode is characterized by two energies: the conduction band energy $E^0_{CB}$ (all energies are given using the potential scale), and the energy of intermediate surface states, $E_S$, involved in the electron transfer between the solution redox probes (characterized by its standard potential $E^0_{redox}$) and the TMO electrode. Oxidation of the probe occurs through electron injection to the conduction band which electron population depends on the band edge energy, the applied potential $E$ and the intrinsic donor density $N_C$. This electron transfer is mediated by intermediate states located below the conduction band and which density $N_S$ is controlled by the level of doping. Thermalization of intermediate states with the CB is kinetically characterized by $k_{th}^{th}$ and $k_{f}^{th}$ rate constants, while interfacial electron transfer between the probe and intermediate states is described by $k_f^i$ and $k_b^i$ rate constants (Figure 8). Fast electron transport is assumed within the TMO as well as fast electron transfer at the TMO/underlying conductive electrode (FTO) interface. The system depends on four dimensionless parameters (see Annex S3 in SI), two thermodynamic parameters:

$$K_i = \exp\left[-F\left(E^0_{redox} - E_S\right)/RT\right]$$

$$K_{th} = \exp\left[-F\left(E_S - E^0_{CB}\right)/RT\right]$$

and two kinetic parameters:

$$A_{i/D} = \frac{N_C k_f^i}{D \frac{Fv}{RT}}$$

$$A_{th/i} = \frac{k_{th}^{th} N_C}{k_f^i C^0}$$

where $D$ is the probe diffusion coefficient and $C^0$ is the probe concentration in the bulk of the solution. The two thermodynamic parameters only depend on the energy levels of the redox probe, the conduction band minima and the intermediate states. The kinetic parameter $A_{i/D}$ describes the competition between the electron transfer from the redox probe to the intermediate states and the diffusion of the redox probe from the bulk to the electrode surface, while $A_{th/i}$ describes the competition between the electron transfer from the intermediate states to the CB (thermalization) and the first electron transfer from the probe to the intermediate states.

The present analysis assumes that the rate constants are independent from equilibrium constants. This strong assumption is justified *a posteriori* from the observation that the rate constants measured with three redox probes are only slightly dependent on the probes standard potentials (Figure 7d). However, the kinetic description can be easily refined by introducing a kinetic law binding rate constants to driving forces.

In the framework of cyclic voltammetry, the general current potential curve is then given by (see SI):

$$\psi = A_{i/D} A_{th/i} \left[\frac{1}{1 + I challenged \left[1 + \exp(-\xi)\right]} \right]$$

$$\left[1 + \frac{1}{K_i} I_{ch} \right] \left[1 + \frac{1}{K_{th}} I_{th} \right] \left[1 + \exp(-\xi)\right]$$

where the dimensionless current is $\psi = I / FSC^0 \sqrt{D \frac{Fv}{RT}}$, the dimensionless potential is $\xi = \frac{F}{RT} (E - E^0_{redox})$ and $I_{ch}$ is the convolution integral. From this general equation, three limiting cases are worth examining.

If the redox couple standard potential is in the conduction band, i.e. $K_i K_{th} = \exp\left[\frac{F}{RT} \left(E^0_{CB} - E^0\right)\right] > 1$, then the present kinetic model is not relevant because electron transfer is not mediated by an intermediate state since the TMO electrode then behaves as a metal. Nonetheless, this can be described as $A_{i/D} = \infty$, i.e. $1 - I_{ch} \left[1 + \exp(-\xi)\right] = 0$, hence leading to a Nernstian CV equation as observed experimentally (see Figure 3a).

The second case which is worth emphasizing corresponds to a redox couple which standard potential is in the bandgap ($K_i K_{th} < 1$) with a small concentration of redox probe so that $A_{th/i} = k_{th}^{th} N_C / k_f^i C^0 \rightarrow \infty$. Physically, this implies that the thermalization of the intermediate state with CB remains faster than the interfacial electron transfer between the redox probe and the intermediate states. In this case, the general equation simplifies in:

$$\psi = A_{i/D} \left[\frac{1}{1 + K_i \exp(-\xi)} \right]$$
A 2D zone diagram representing the various expected CV shapes as function of the two dimensionless parameters \( A_{i/D} \) and \( K_i \) can thus be drawn and is represented in Figure 9a (see SI for details on zone diagram construction as well as expressions and characteristics of the CVs in the various zones). For low doping density (\( A_{i/D} \to 0 \); P, PI and PR zones in Figure. 9), the forward CV trace takes the form of a S-shaped curve with a plateau current:

\[
i_{pl} = FSC^0 N_S k^i_f
\]

with \( S \) the surface area of the electrode.

For a given redox probe, variation of the scan rate corresponds to a horizontal displacement in the zone diagram. As the scan rate is large enough for the system to enter the P, PR or PI zones, this plateau current is obtained and further increase of the scan rate does not modify it, which explain the scan rate independence of the anodic plateau. The anodic current is then kinetically controlled by the bimolecular reaction between the redox probe and the intermediate states. For a given redox probe, increasing the density of intermediate states, i.e. doping, also corresponds to a horizontal displacement toward the right side in the zone diagram, with the forward CV trace changing from a plateau (zones P, PI and PR) to a peak shape (zones G, GR and R). The evolution of the CV shape as a function of \( A_{i/D} \) for two given values of \( K_i \) are shown in Figure 10a and can be compared to the CV shape evolution observed experimentally for increasing doping density (Figure 6a). Furthermore, another good correlation can be found between the model anodic plateau or peak current evolution in Figure 10b and the experimental one in Figure 6c.

![2D zone diagram](image)

**Figure 9.** 2D zone diagram representing the expected CV shapes as function of the dimensionless parameters \( A \) and \( K \). Expressions and characteristics of the CVs in the various zones are given in the SI. \( G \): general zone governed by both parameters \( A \) and \( K \). \( P \) and \( RI \): general plateau and general peak zones governed by one parameter \( A/K \). \( GR \) and \( GI \): one parameter zones with reversible and irreversible CVs governed by \( A \). \( R \): nernstian zero parameter zone, nernstian CV. \( I \): irreversible CV zero parameter zone. \( PI \): irreversible plateau CV, zero parameter zone. \( PR \): reversible plateau CV, zero parameter zone.

As long as the system remains in the PI, P or PR zones (i.e. \( A_{i/D} \to 0 \), Figure 9), a plateau current proportional to the doping density is obtained, corresponding to

\[
i_{pl} = FSC^0 N_S k^i_f
\]

For a given redox probe concentration \( c^0 \), \( k^i_f \) can thus be retrieved from the slope of the plot of the anodic plateau current as a function of the doping density \( N_S \) of the metal oxide electrode. Control of \( N_S \) is achieved experimentally through chemical doping via reductive thermal treatments and \( N_S \) is evaluated from the MS plot (Figure 6a). The different rates were therefore
extracted for the three probes (Figure 7). Noticeably, the charge transfer rate constant was found to increase following FeAc < Fe < FeMe. As expected, when increasing the standard potential for the redox probe, in other words when increasing the barrier height for the electron transfer to the oxide CB, the rate constant for electron transfer decreases. We note however that the experimental rate constants exhibit a shallow variation with the driving force. Rate constants of the order of $10^{-24}$ cm$^3$s$^{-1}$ are obtained for the three redox probes, which is several orders of magnitude lower than what was previously obtained for the reduction of viologen molecules at the n-type Si-CH$_2$OH interface$^{16}$ ($=10^{-7}$ cm$^3$s$^{-1}$). Hence, we could confirm in this study that the rate exchange for a process based on injection of majority carrier from the redox molecule into the semiconductor is by far slower than for the injection of majority charge carrier from the semiconductor to the redox molecule.

From the plateau current expression derived in the $A_{\text{th}} \rightarrow 0$ limit (PI, P or PR zones) when $A_{\text{th}} \rightarrow \infty$, i.e. when the thermalization of the intermediate state with CB is faster than the interfacial electron transfer with the redox probe, we can predict a linear variation of the plateau current with the probe concentration $C^0$. It is indeed the case at small probe concentration (Figure 4e). However, a deviation from this limiting behavior is actually observed experimentally as the probe concentration is increased. This corresponds to the $A_{\text{th}} \rightarrow \infty$ assumption not being valid anymore. We are thus led to the third limiting case which corresponds to a situation where $A_{\text{th}} \rightarrow 0$, so that the consumption of the probe at the electrode surface is negligible on the forward scan but without constraint on $A_{\text{th}}$. The S-shaped steady-state (scan rate independent) CV forward scan expression then simplifies into (see SI for details):

$$\varphi = \varphi' = \frac{i_{pl}}{FSk_f^0N_C^0} = \frac{\varphi_{pl}}{1 + \exp(-\xi)}$$

where the plateau current is:

$$\varphi_{pl} = \frac{i_{pl}}{FSk_f^0N_C^0} = \frac{A_{\text{th}}}{1 + A_{\text{th}}}$$

and the half-wave potential $E_{1/2}$ corresponds to $\xi_{1/2} = 0$, i.e.:

$$E_{1/2} = E_S + \frac{RT}{F} \ln \left( \frac{K_{th} + A_{\text{th}}}{1 + A_{\text{th}}} \right)$$

As the concentration of probe is increased (decrease of $A_{\text{th}}$) the plateau current varies from $\varphi_{pl} = 1$ ($A_{\text{th}} \rightarrow \infty$) to $\varphi_{pl} = \lambda$ ($A_{\text{th}} \rightarrow 0$). This leads to the variation of the plateau current from $i_{pl} = FSk_f^0N_C^0$, proportional to the probe concentration, to $i_{pl} = FSk_f^0N_C^0$, independent on the probe concentration. In the latter case, the system is no longer kinetically controlled by the bimolecular electron transfer between the probe and the intermediate state (with fast thermalization of electrons between the intermediate states and the CB) but it is controlled by the kinetics of electron transfer between the intermediate states and the CB. Consequently, the deviation of linearity of plateau current with probe concentration observed experimentally (see Figure 4c) is an indication of increasing interference of intermediate state/CB electron transfer kinetics. Adjustment of the experimental data (Figure 4e and Figure S1 in SI) leads to an evaluation of $k_f^0/k_f^thN_C \approx 6.1 \times 10^{-3}$ cm$^{-1}$mol$^{-1}$ for Fe. Taking $N_C \approx 10^{19}$ cm$^{-3}$ and $k_f^0 = 3.1 \times 10^{-24}$ cm$^4$s$^{-1}$, we obtain $k_f^th = 5.1 \times 10^{-9}$ cm$^4$s$^{-1}$mol. Interestingly, we note that the half-wave potential $E_{1/2}$ is almost insensitive to the variation of the probe concentration (Figure 4d) indicating that $K^{th} \approx 1$ and therefore $E_S \approx E_{CB}^0$ in line with the idea that the intermediate states are very close to the conduction band edge.

**Conclusion**

In this work, we re-investigated the electron exchange on the surface of n-type semiconductor transition metal oxide WO$_3$ under reverse bias (anodic polarization). Doing so, we could first demonstrate that, as opposed to a process governs by the presence of trap states such as found for TiO$_x$, the oxidation of molecular redox probes with standard potentials within the band gap of WO$_3$ is controlled by the presence of intermediate states close to the CB. Hence, the anodic current was found potential independent as well as independent on the scan rate. We could further demonstrate that the anodic current is not only dependent on the concentration of redox probe but also dependent on the majority charge carrier concentration as determined by Mott-Schottky analysis. This observation allows for extracting the bimolecular rate constants for the electron exchange. To do so, we took advantage of an intrinsic property of oxides films prepared by soft-chemistry and so-far considered as a barrier for getting kinetics information, namely the scattering of doping levels among different films, to extract kinetics information. Finally, using a simple kinetic scheme, we provide a guide that will allow for an easy determination of the rate for electron exchange on the surface of transition metal oxides SC for researchers from the broad field of materials for energy. Indeed, we believe that this work provides the fundamental background to quantitatively investigate transition metal oxides electrodes used in a variety of energy storage and conversion devices. Furthermore, this methodology can be extrapolated to the study of porous films commonly used in practical devices.
ASSOCIATED CONTENT

Supporting Information.
Full experimental details, characterization data and detailed kinetic model description. This material is available free of charge via the Internet at http://pubs.acs.org.

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The manuscript was written through contributions of all authors. All authors have given approval to the final version of the manuscript.

Notes
The authors declare no competing financial interest

ACKNOWLEDGMENT
I.A, C.L-R and A.G. would like to acknowledge RS2E for financial support. We thank Dr. Cedric Boissiere at LCMCP for ellipsometry measurements.

Imaging was performed on a SU-70 HitachiFEG-SEM, instruments facilitated by the IMPC (Institut des Matériaux de Paris Centre FR2482) financially supported by the C’Nano projects of the Region Ile-de-France.

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