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Dip-coating with a particulate suspension

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The coating of a plate withdrawn from a bath of a suspension of non-Brownian, monodisperse and neutrally buoyant spherical particles suspended in a Newtonian liquid has been studied. Using laser profilometry, particle tracking and local sample weighing we have quantified the thickness h and the particle content of the film for varied particle diameters d and volume fractions ($0.10 \leq \phi \leq 0.50$). Three coating regimes have been observed as the withdrawal velocity is increased: (i) no particle entrainment ($h \lesssim d$), (ii) a monolayer of particles ($h \sim d$), and (iii) a thick film ($h \gtrsim d$), where the suspension behaves as an effective viscous fluid following the Landau-Levich-Derjaguin law. We discuss the boundaries between these regimes, as well as the evolution of the liquid and solid content of the coating over the whole ranges of withdrawal capillary number and volume fractions.

Key Words: dip-coating, film, surface flow, particulate suspension

1. Introduction

Immersion in a liquid bath (dip-coating) is a simple and efficient coating process, which is widely used across e.g. food, health, textile or plastic industries (Schweizer & Kistler 1997; Weinstein & Ruschak 2004). In its simplest version, a plate withdrawn vertically from the bath with a constant velocity U entrains a uniform liquid film. For a Newtonian liquid with viscosity η_0 , density ρ and surface tension σ the film thickness h_0 depends on the capillary number $Ca = \eta_0 U / \sigma$ and length $\ell = \sqrt{\sigma / \rho g}$, where g is the gravity. Provided Ca and $\rho U h_0 / \eta_0$ are both smaller than 1, it follows

$$h_0 \simeq 0.95 \ell Ca^{2/3}, \quad (1.1)$$

as derived by Landau & Levich (1942); Derjaguin (1943) and validated experimentally since then (Morey 1940; van Rossum 1958; Groenveld 1970; Lee & Tallmadge 1974; Kizito *et al.* 1999; Snoeijer *et al.* 2008; Maleki *et al.* 2011).

For a particle-laden liquid, a supplementary length – the particle diameter d – is introduced and different rheology (Guazzelli & Pouliquen 2018) and surface conditions (Kralchevsky & Nagayama 1994) are expected. Motivated by film deposition and self-assembly of colloids for surface patterning, lithography or optical applications (Yu & Zhang 2013) much attention has been devoted to colloidal particles suspended in a volatile liquid, for which evaporation is often a dominant factor (Dimitrov & Nagayama 1996; Ghosh *et al.* 2007; Buchanan *et al.* 2007; Le Berre *et al.* 2009; Faustini *et al.* 2010; Jing *et al.* 2010; Brewer *et al.* 2011; Berteloot *et al.* 2013; Jung & Ahn 2013). However, much fewer studies have considered suspensions of larger particles ($\sim 100 \mu\text{m}$) or low volatility liquids (Kao & Hosoi 2012; Colosqui *et al.* 2013; Gans *et al.* 2019). In these cases the

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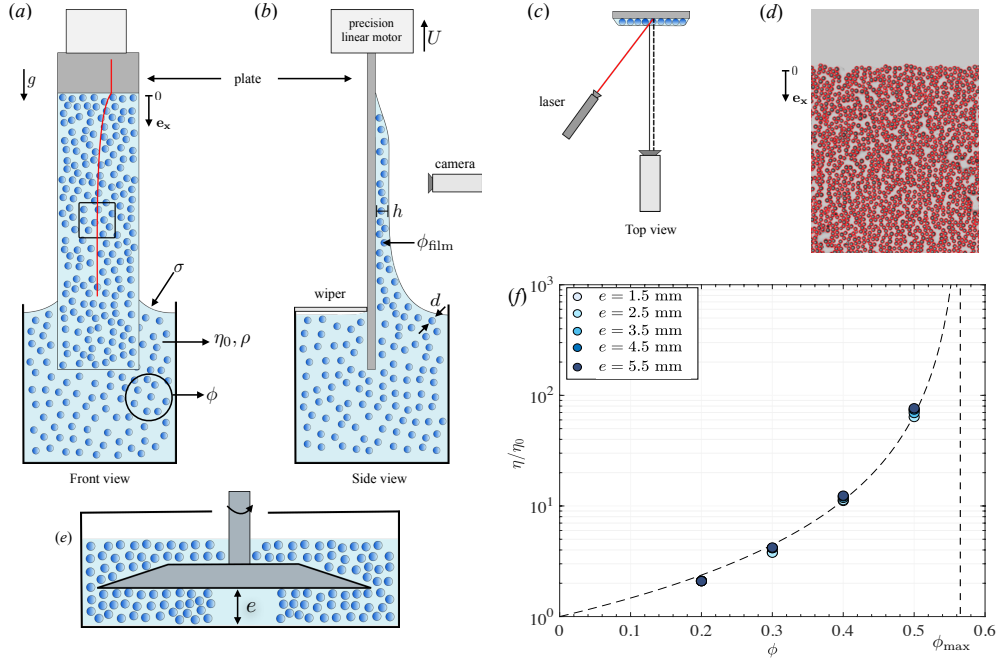


Figure 1: (a-c) Schematics of the experimental setup and laser profilometry measurement technique used for ‘thick’ films ($h \gtrsim d$). (d) Snapshot illustrating the particle tracking used to count the particles in ‘thin’ films ($h \sim d$). (e) Schematics of the large gap plate/plate shear cell used to measure the shear viscosity of the suspension. (f) Relative effective shear viscosity η/η_0 of the suspensions measured for different values of the cell gap e ($d = 145 \mu\text{m}$, $\eta_0 = 100 \text{ mPa.s}$). The dashed line indicates the correlation $\eta/\eta_0 = (1 - \phi/\phi_{\max})^{-2}$ (Guazzelli & Pouliquen 2018) with $\phi_{\max} \approx 0.57$.

thickness, particle content and structure of the coating remain to be characterized over the full range of withdrawal velocity and volume fraction.

We focus here on the case of a viscous flow for non-Brownian, mono-disperse and neutrally-buoyant spherical particles and experimentally study how the liquid and solid contents of the coating depends on U for different particle sizes ($80 \mu\text{m} \leq d \leq 550 \mu\text{m}$) and volume fractions ($0.10 \leq \phi \leq 0.50$). We present the experimental protocol in §2, discuss general observations, the different coating regimes and their boundaries in §3, and conclude in §4.

2. Experimental setup

The experimental setup is sketched in figure 1. It consists of a bath of a viscous suspension of solid and neutrally-buoyant particles, from which a plate is withdrawn vertically with a controlled velocity. The particles are spherical polystyrene particles (Dynoseeds TS, Microbeads) with a mean diameter $d = 80, 145$ or $550 \mu\text{m}$ and a low relative standard deviation in size ($\leq 8\%$) obtained by repeated sieving. The liquid is a water solution of PEGPG (3.9 kg/mol poly(ethylene glycol-ran-propylene glycol)-monobutyl-ether by Sigma-Aldrich) and 4 wt% zinc chloride, which matches the particle density ($\rho = 1050 \text{ kg/m}^3$) and wets the particles totally. Its viscosity η_0 is varied between 2 and 100 mPa.s by adjusting the PEGPG concentration (from 4 to 45.5 wt%), whereas

its surface tension σ varies only weakly between 38 and 47 mN/m. The particle volume fraction ϕ of the suspension is varied between 0.10 and 0.50. For all the experiments, the Reynolds number $\rho h U / \eta_0$ (based on (1.1)) remains lower than ~ 0.1 and the capillary number Ca is varied between 10^{-4} and 10^{-1} .

The suspension is prepared and homogenized by immersing the particles in small quantities and mixing thoroughly, but slowly to avoid air entrapment, before it is poured up to the top of the dipping container. The plate is a smooth glass plate having a width of 26 mm and a thickness of 1.2 mm, which is well wetted by the suspending liquid (the receding and advancing contact angles are $\approx 5^\circ$ and $\approx 35^\circ$, respectively, for all the liquids). Above the particle entrainment threshold we also use a PMMA plate, which allows a sampling of the coated film (see §3.4), without any observable difference on the coating. The plate is held and displaced vertically with a precision translation stage (M414.1PD, PI), while the bath remains in fixed position. It is slowly dipped in the suspension bath over a length of 50 mm and withdrawn with a constant vertical velocity U , which is varied between 0.03 and 13 mm/s. Before each dipping, the plate is cleaned and dried, and the suspension is re-homogenized by gentle stirring.

The coating of the plate is monitored from a front view with a digital camera and 60 mm macro-lens resulting in a spatial resolution down to $35 \mu\text{m}$. Depending on the opacity of the coating we measure either the average film thickness using a laser profilometry technique or the particle surface concentration from the tracking of each particle. Both techniques provide local and instantaneous measurements. This allows to characterize the coating in situ, without any edge effect or influence of the post-coating drainage. The first technique uses the transverse displacement of the intersection between an inclined laser sheet and the coating film surface (see figure 1(a-c)). It yields a measurement of the average coating thickness (independently from its solid content) with a precision of the order of the laser sheet thickness ($\simeq 35 \mu\text{m}$) or a fraction of the particle size and is mainly used for thick coatings. The second technique consists in detecting each particle entrained on the front side of the plate from shadowgraph pictures obtained with a cold back-lighting – the rear side of the plate is kept free of particles with the help of a wiper, see figures 1(b) and (d). It is available for coatings thinner than two particle diameters and only gives access to the solid content of the coating. To obtain information about both the liquid and solid content, these two techniques are complemented with sampling and weighing measurements of the coating, which will be detailed in §3.2 and 3.4.

Finally, the effective shear viscosity of each suspension is measured with a rotating rheometre (Anton Paar MCR 501) in a plate/plate device allowing a large cell gap $e \gg d$, which is varied between 1.5 and 5.5 mm (see figure 1(a) and details in Château & Lhuissier (2019)), at the same temperature (24°C) as the coating experiments. Figure 1(f) presents the measurements of the relative shear viscosity η/η_0 for the different particle volume fractions we have used. They are found to be independent of the gap e and consistent with values reported in the literature (Guazzelli & Pouliquen 2018).

3. Results

3.1. General observations

Figure 2(a) shows a typical coating film observed for a concentrated suspension ($\phi = 0.40$, $d = 145 \mu\text{m}$) and a velocity U much larger than the entrainment threshold. A typical film thickness profile obtained with the laser profilometry is shown in figure 2(b). The liquid/plate triple line is essentially pinned (at $x = 0$) and a slowly draining suspension film is entrained from the onset of the motion. As for a pure liquid with $Ca \ll 1$, the

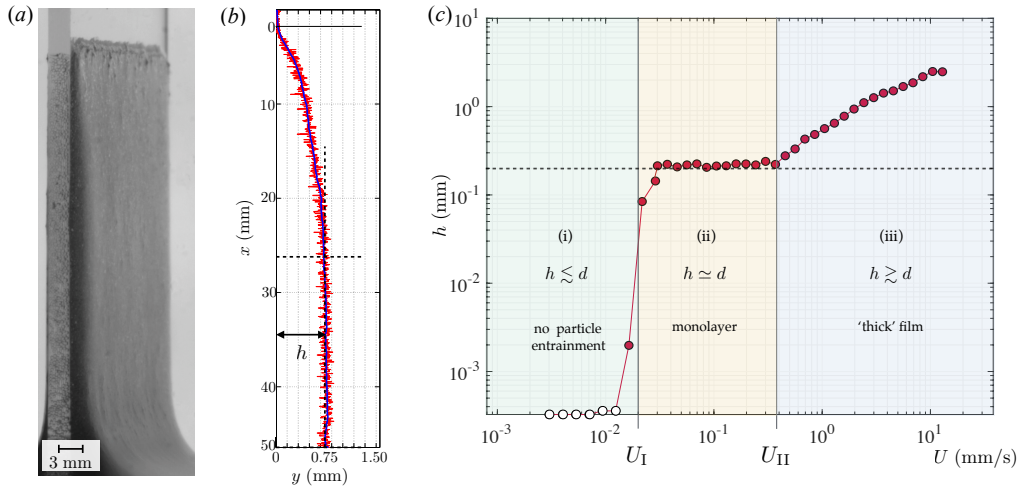


Figure 2: (a) Typical coating observed in the thick film regime ($d = 145 \mu\text{m}$, $\phi = 0.40$, $\eta_0 = 100 \text{ mPa s}$, $U = 6 \text{ mm/s}$). (b) Typical coating thickness profile measured from laser profilometry in the ‘thick’ film regime ($d = 145 \mu\text{m}$, $\phi = 0.40$, $\eta_0 = 100 \text{ mPa s}$, $U = 0.9 \text{ mm/s}$, the plate withdrawal length is 50 mm, and $x = 0$ labels the initial position of the triple line on the plate). The red and blue lines represent the raw and smoothed signals, respectively. The dashed lines delimit the thickness plateau over which the average steady state thickness h is measured. (c) Steady thickness versus withdrawal velocity (same suspension as in (b)) illustrating the three different coating regimes. From low to large velocities: (i) No particle entrainment regime ($h \lesssim d$), (ii) monolayer regime ($h \simeq d$), and (iii) thick film regime ($h \gtrsim d$). U_I and U_{II} denote the transition velocities between the regimes. The dashed line indicates $h = d$.

film is uniform at sufficient distance from the triple line. To characterize the coating we consider the steady state entrainment thickness of the film, h , which we measure by averaging the thickness over the plateau close to the suspension bath (see figure 2(b)). Figure 2(c) reports the evolution of h with the withdrawal velocity for the same suspension. From low to large velocities, it reveals three distinct coating regimes, as also reported very recently by Gans *et al.* (2019). (i) a ‘no particle entrainment’ regime, where the film is much thinner than d , (ii) a ‘monolayer’ regime, where the film thickness is of the order of the particle diameter ($h \simeq d$) and is essentially independent of U , (iii) a ‘thick film’ regime, where the film thickness is much larger than the particle size ($h \gtrsim d$) and increases with increasing U . These three regimes determine two boundary velocities U_I and U_{II} separating (i)/(ii) and (ii)/(iii), respectively.

3.2. Thick film regime (iii)

We consider first the thick film observed for large velocities. The inset of figure 3(a) presents the steady film thickness h as a function of the withdrawal velocity U for a particle volume fraction ranging from 0.20 to 0.50 and the same particles and liquid as in figure 2 ($d = 145 \mu\text{m}$ and $\eta_0 = 100 \text{ mPa s}$). The reproducibility of the coating is illustrated by the three series of measurements presented for $\phi = 0.40$. On the right hand side of the graph, where $h \gtrsim d$, the thickness h is found to increase with increasing U , as for a pure viscous liquid, but also with increasing ϕ . These two trends are consistent with the effective bulk rheology of a suspension, valid for large scale flows ($\gg d$) and

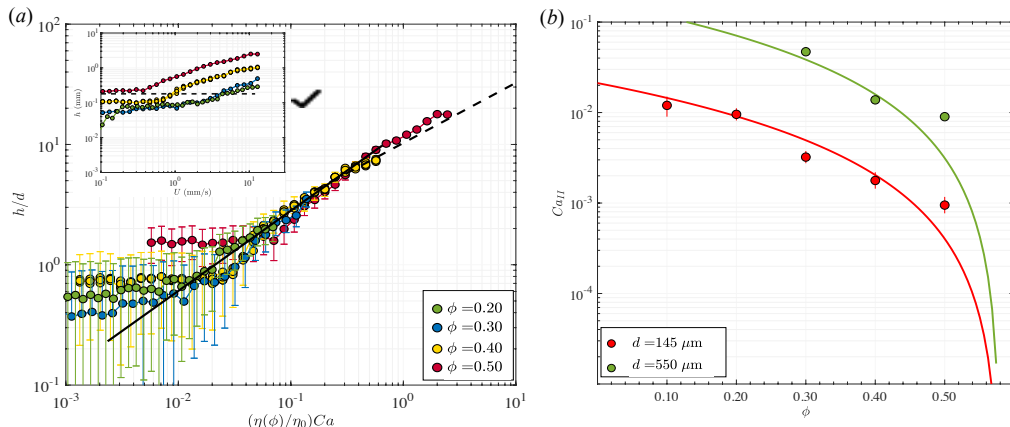


Figure 3: (a) Dimensionless thickness h/d versus effective capillary number $\eta(\phi)U/\sigma$ for different particle volume fractions ϕ . The error bar indicates the resolution of the laser profilometry (see §2). The solid line is (3.1). The dashed line is the Derjaguin asymptotic regime $h = 0.67 \ell(\eta(\phi)U/\sigma)^{1/2}$ expected for $\eta(\phi)U/\sigma \gg 1$ (Kizito *et al.* 1999). The inset shows the raw data and indicates the particle size $d = 145 \mu\text{m}$. The three series of measurements presented for $\phi = 0.40$ illustrate the coating reproducibility. (b) Transition capillary number between the thick film ($h \gtrsim d$) and the monolayer regime ($h \simeq d$) versus particle volume fraction for varied particle size. The solid lines represent (3.3).

low Reynolds numbers, in which the relative viscosity η/η_0 of the suspension increases with the particle volume fraction (Guazzelli & Pouliquen 2018). Therefore, it is natural to represent the thickness h as a function of the capillary number $\eta U/\sigma$ based on the effective shear viscosity η of each suspension, which is measured independently in the shear cell (see §2). In this representation, shown in figure 3(a), the experimental film thickness for the different volume fractions collapse and agree well with the Landau-Levich-Derjaguin (LLD) model

$$h \simeq 0.95 \ell \left(\frac{\eta(\phi)U}{\sigma} \right)^{2/3} = h_0 \left(\frac{\eta}{\eta_0} \right)^{2/3}, \quad (3.1)$$

over the thick film range, $h \gtrsim d$ and provided $(\eta/\eta_0)Ca$ remains smaller than 1 (as also reported by Gans *et al.* 2019). This suggests that, for the present case of fully wetted particles and for the range of particle volume fraction considered, the global surface stresses that limit the entrainment of the suspension are not very different from those expected from the surface tension of the pure suspending liquid. Finally, for $(\eta/\eta_0)Ca$ larger than 1, the effective behavior persists: the thickness agrees with the purely viscous regime $h \sim \sqrt{\eta U/\rho g} \sim \ell(\eta Ca/\eta_0)^{1/2}$ (Derjaguin 1943).

The above measurements concern the total quantity of suspension entrained and do not distinguish between the solid and liquid contents. To complete the characterization of the coating in the thick film regime, additional dip-coating experiments have been carried out to measure the particle volume fraction in the film. Five different withdrawal velocities have been considered for a fixed particle volume fraction of the bath, $\phi = 0.40$. The measurement procedure is as follows. Immediately after the plate has been fully withdrawn from the bath following the standard protocol, the whole of the suspension that has been entrained with the plate is weighed, rinsed, cleaned and dried thoroughly before being weighed a second time in order to measure the quantity of particles it

contains. The ratio of the latter to the former weights yields the average particle volume fraction in the coating, denoted ϕ_{film} . For the five effective capillary numbers ($5.1 \times 10^{-3} \leq \eta U / \sigma \leq 3.1 \times 10^{-2}$) we obtain $\phi_{\text{film}} = 0.398 \pm 0.003$, without significant variation with U . This shows that particle migration effects are negligible in the present case. The solid volume fraction of the coating is essentially the same as that of the bath:

$$\phi_{\text{film}} \simeq \phi, \quad (3.2)$$

which is consistent with the use of the effective viscosity of the bath in equation (3.1).

3.3. Transition from thick film to monolayer regimes (II)

The experimental data from figures 2 and 3 show that the LLD effective trend of the thick regime stops for small withdrawal velocities. The transition is rather sharp and occurs when the average film thickness plateaus at a value which is of the order of the particle diameter. Making use of the LLD effective law (3.1) and of the thickness $h \simeq d$ observed at the transition one can readily express the transition capillary number $Ca_{\text{II}} \equiv \eta_0 U_{\text{II}} / \sigma$ according to

$$Ca_{\text{II}} \simeq \frac{\eta_0}{\eta} \left(\frac{d}{0.95\ell} \right)^{3/2}, \quad (3.3)$$

and as also proposed by Gans *et al.* (2019).

The value of the transition velocity U_{II} can be extracted from the profilometry measurements. Figure 3(b) shows the experimental transition capillary number as a function of the particle volume fraction for a viscosity $\eta_0 = 100$ mPa s and two different particle sizes, $d = 145$ and 550 μm . Over the whole range of ϕ equation (3.3), which is represented by the solid lines, is in good agreement with the data.

3.4. Monolayer regime (ii)

Below U_{II} the profilometry measurements indicate that the average film thickness remains of the order of d over an extended range of velocities. This is consistent with direct observation revealing that the particles form a monolayer. In this regime, the particle surface concentration c_s becomes a relevant quantity to characterize the coating, which also has the advantage of being experimentally accessible with a great accuracy from single particle tracking (see e.g. figure 1(d)). Figure 4(a) presents the dependence of c_s upon U and ϕ in the steady state coating regime, as measured by averaging over a central zone of the plate of 20×30 mm^2 located 5 mm above the bath surface. We use the non-dimensional form $\tilde{c}_s \equiv \pi c_s d^2 / 6\phi \equiv h\phi_{\text{film}} / d\phi$, which is by definition equal to 1 for a film having a thickness h and the same particle volume fraction ϕ as the bath. For the smallest volume fraction, $\phi = 0.10$, the surface concentration decreases regularly with decreasing U below the transition velocity U_{II} . However, for larger volume fractions the dimensionless surface concentration \tilde{c}_s collapses on 1 (i.e. $h\phi_{\text{film}} / d\phi \simeq 1$) over a significant range of velocities, which further extends toward lower velocities for larger values of ϕ . This suggests that over this plateau $h \simeq d$ and $\phi_{\text{film}} \simeq \phi$. However, since other combinations of h and ϕ_{film} also yield $\tilde{c}_s = 1$ we have conducted additional measurements to determine unambiguously the solid and liquid contents of the coating. To this end, we have used a PMMA plate with a removable circular portion (with diameter 12 mm and removed when it is 35 mm above the bath surface), which allows to collect and weight a sample of the steady state coating and to determine its volume fraction ϕ_{film} from the comparison of its weight and the number of particles obtained from particle tracking. For a fixed bath volume fraction $\phi = 0.40$ and different withdrawal velocities (3.0 $\text{mm/s} \leq U \leq 10.5$ mm/s) we obtained $\phi_{\text{film}} = 0.389 \pm 0.003$ without significant

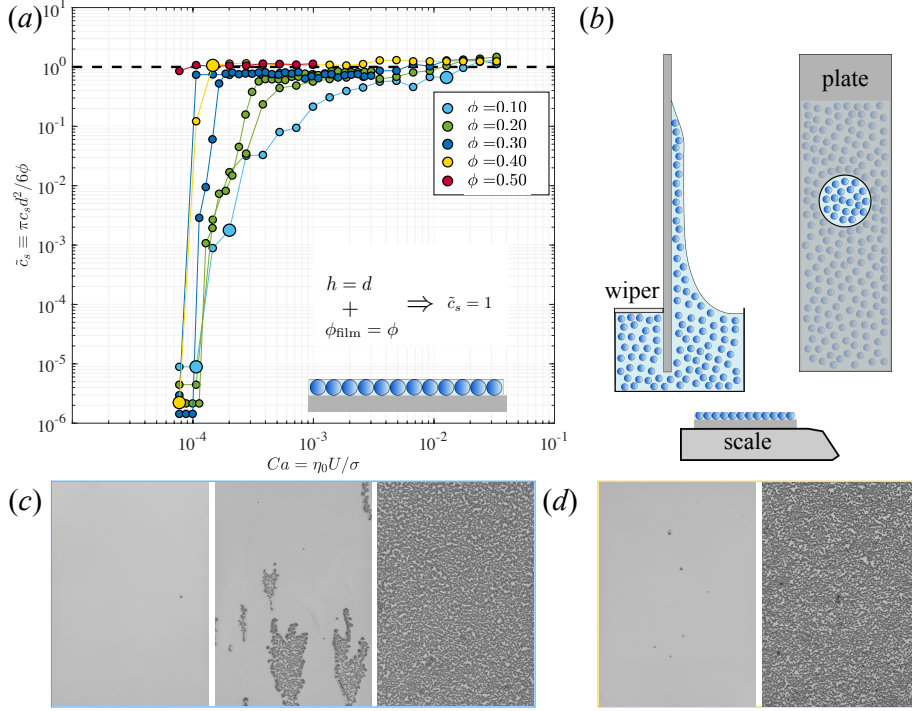


Figure 4: (a) Dimensionless particle surface concentration versus capillary number for ϕ ranging from 0.10 to 0.50 and $d = 145 \mu\text{m}$. The value $\tilde{c}_s \equiv \pi c_s d^2 / 6\phi \equiv h\phi_{\text{film}} / d\phi$ equals 1 for a monolayer with a flat liquid interface and the same particle volume fraction as in the bulk (as sketched in the inset). The two independent data series for $\phi = 0.20$ and 0.30 show the reproducibility of the transition. (b) Schematics of the sampling technique using a plate with a removable circular central part to measure the liquid content of the monolayer by weighing. (c-d) Typical coating structure observed across transition I for $\phi = 0.10$ (c) and $\phi = 0.40$ (d). The pictures correspond to the large symbols in (a), with withdrawal velocity increasing from left to right.

dependence on U , which means that the monolayer regime observed at large particles volume fractions is well characterized by

$$h \simeq d, \quad \text{and} \quad \phi_{\text{film}} \simeq \phi. \quad (3.4)$$

3.5. Transition from monolayer to no particle entrainment regimes (I)

Finally, we consider the transition from the monolayer regime to the no particle entrainment regime, labelled I, which represents the threshold for the steady entrainment of particles in the film. This transition shows in the measurements of figure 4(a) (for $d = 145 \mu\text{m}$ and various ϕ) as the dimensionless surface concentration drops from $\tilde{c}_s \simeq 1$ to $\tilde{c}_s \simeq 0$ with decreasing entrainment velocities. For large particle volume fractions the transition is sharp, whereas for low ϕ it is broad – extending over almost two decades for $\phi = 0.10$ – and shifted towards larger entrainment velocities. The typical structure of the coating across the transition is illustrated in figure 4(a-b) for a low ($\phi = 0.10$) and a large ($\phi = 0.40$) volume fraction. Close to the monolayer regime the coating is uniform for both diluted and concentrated suspensions. However, close to the lower end

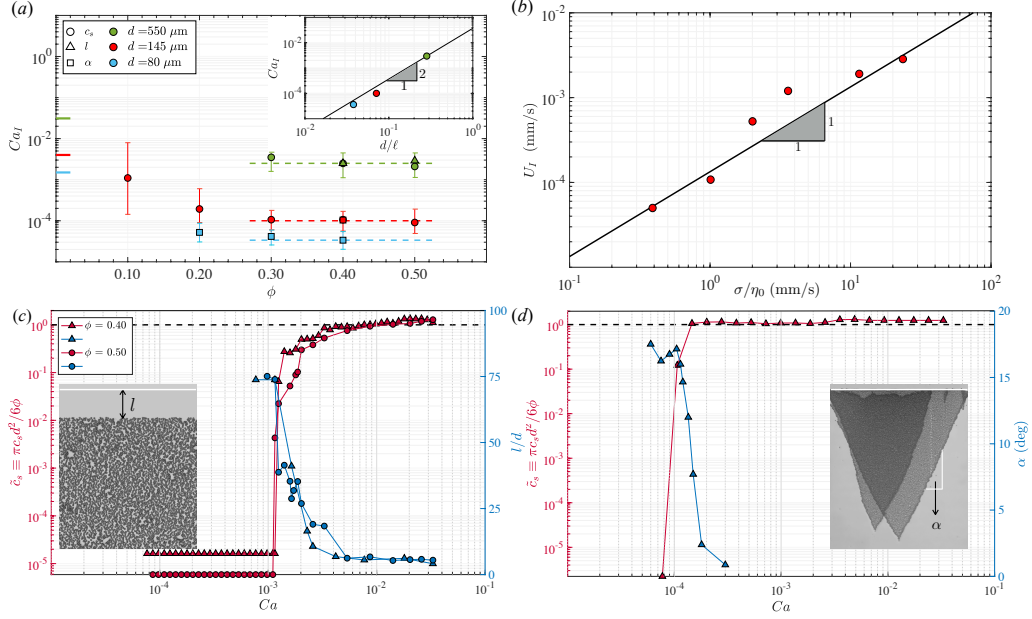


Figure 5: (a) Transition capillary number between the monolayer and no entrainment regimes versus ϕ for different particle sizes. The shape of the symbols indicates from which measurements (c_s , l or α) the transition capillary number is determined. The vertical bars represent the range over which \tilde{c}_s varies significantly ($10^{-6} \lesssim \tilde{c}_s \lesssim 1$), whereas the symbols indicate the geometrical mean of the range limits. The colored ticks at $\phi = 0$ indicate the entrainment threshold $Ca_I \approx (0.35d/\ell)^{3/2}$ derived by Colosqui *et al.* (2013) for isolated particles. The dashed lines indicate the plateau value of $Ca_{I, \phi \geq 0.30}$ observed for $\phi \geq 0.30$. Inset: $Ca_{I, \phi \geq 0.30}$ versus d/ℓ . The solid line shows $Ca_{I, \phi \geq 0.30} \sim (d/\ell)^2$. (b) Evolution of U_I with the suspending liquid viscosity for $d = 145 \mu\text{m}$ and $\phi = 0.40$. The solid line represents the capillary number $Ca_I \simeq 1.0 \times 10^{-4}$ reported in (a). (c) Co-evolution of the dimensionless surface concentration \tilde{c}_s and the particle-free length l (defined in the inset) with Ca for $d = 550 \mu\text{m}$ and $\phi = 0.40$ and 0.50 ($\eta_0 = 100 \text{ mPa s}$). (d) Co-evolution of \tilde{c}_s and the narrowing angle α (defined in the inset) with Ca for $d = 145 \mu\text{m}$ and $\phi = 0.40$ ($\eta_0 = 12 \text{ mPa s}$). The insets present typical pictures of the transients (each of the two triangular coatings in (d) is on a different side of the plate).

of the transition isolated clusters of particles form, which can be more easily observed for diluted suspensions because of the broadness of the transition. These evolutions are summarized in figure 5(a), which presents the capillary number $Ca_I \equiv \eta_0 U_I / \sigma$, around which the transition occurs, as a function of ϕ . As shown in figure 5(b) the raw transition velocity U_I varies as the inverse of the suspending liquid viscosity η_0 , which suggests that for a given particle size and volume fraction it is relevant to express the transition in terms of Ca_I . Experimentally, we define the latter as the geometrical mean of the ends of the range over which \tilde{c}_s varies significantly ($10^{-6} \lesssim \tilde{c}_s \lesssim 1$), whereas the vertical bars show the range itself (which is much broader than the typical variability in the measurements, see the repeated measurements in figure 4(a)). It is found to decrease with increasing ϕ below 0.30. These measurements at low ϕ are consistent with the entrainment threshold expected in the diluted limit $\phi \simeq 0$. Indeed, in this limit particles should not interact with each other and the criteria $h \sim \ell Ca_I^{2/3} \sim d$, i.e. $Ca_I \sim (d/\ell)^{3/2}$, derived by Colosqui

et al. (2013) for an isolated particle should apply. The latter limit, indicated in figure 5(a), is found to be in line with our measurements for $\phi \leq 0.30$.

Conversely, for larger volume fractions, Ca_I plateaus and becomes almost independent of ϕ . For a given particle size, all concentrated suspensions ($\phi \geq 0.30$) are found to have a very similar particle entrainment velocity threshold. This sharply contrasts with the evolution of $U_{II} \propto 1/\eta$, which strongly depends upon ϕ , in particular close to the critical volume fraction ϕ_{\max} where it is expected to vanish (Guazzelli & Pouliquen 2018). The value, denoted $Ca_{I,\phi \geq 0.30}$, of this large- ϕ plateau is determined as the mean of Ca_I over the range $0.30 \leq \phi \leq 0.50$ (over which the relative standard deviation is smaller than 7% for each value of d). It increases with increasing particle sizes, which means that, similarly to the diluted case, small particles are more easily entrained than large particles. As shown in the inset of figure 5a, this dependance of Ca_I on d is found to be pronounced. For d ranging from 80 to 550 μm the value of $Ca_{I,\phi \geq 0.30}$ increases by two decades, which suggests a dependance close to $Ca_{I,\phi \geq 0.30} \propto d^2$ as highlighted in the inset of figure 5(a). Although no model could be derived to explain these experimental results, the latter suggest that the dependance of Ca_I on d at large ϕ is stronger than for the diluted case ($Ca_I \propto d^{3/2}$). Besides, in the present case where a liquid film is always observed below U_I (see §3.6), the same transition velocities (U_I) is obtained whether the plate is of PMMA or glass.

So far, the content of the coating has been characterized and discussed on the basis of averaged measurements performed at a large distance (~ 30 mm) from the initial position of the triple line on the plate ($x = 0$). However, further qualitative information about the no particle entrainment transition can be obtained by observing the structure of the film that is formed at the onset of the plate withdrawal. As illustrated in the insets of figures 5(c-d), transition I is actually found to proceed differently depending on the particle size. For the largest particles ($d = 550$ μm) a transitory film containing no particle is observed close to $x = 0$, which length l increases as U decreases around U_I . By contrast, for smaller sizes ($d \leq 145$ μm), the first line of particles appears to be pinned at $x \simeq 0$. As a consequence a transitory entrainment of particles is observed even below U_I , but this entrainment is not steady for $U < U_I$: the width of the particle monolayer shrinks with x with a characteristic angle $\alpha > 0$ depending on U (see the inset of figure 5(d)). The reason for this transitory entrainment is not known. It might be related to differences between the static and dynamic shapes of the meniscus, but we cannot exclude influences of minute evaporation at the triple line for the few seconds the plate is immobile before it is withdrawn. Nevertheless, although the transitory coating actually differs between different particle sizes, it is consistent in all cases with the particle content observed at large distances (large x). As shown by the confrontation with the measurements of the dimensionless surface concentration \tilde{c}_s in figures 5(c-d), both the particle-free length l and the narrowing angle α increase abruptly around the value of U_I determined previously (figure 5(a)), which explains why \tilde{c}_s vanishes at large distance for small withdrawal velocities.

3.6. No particle entrainment regime (i)

The no particle entrainment regime has not been characterized quantitatively but an important remark has to be made. In all the cases studied a continuous liquid film was formed below the no particle entrainment transition (U slightly lower than U_I). This observation suggests that the no entrainment particle entrainment transition discussed above is not directly related to the threshold velocity for the wetting of the plate by the suspending liquid (de Gennes 1985; Bonn *et al.* 2009; Snoeijer & Andreotti 2013).

4. Conclusions

Three regimes of coating have been observed experimentally as a plate is withdrawn from a bath of a particulate suspension. For an increasing withdrawal velocity (i) no particle, (ii) a monolayer of particles, and (iii) a thick film of suspension are successively entrained with the plate.

In regime (iii), the particle size is unimportant. The coating has the same particle content as the bath and its thickness follows the Landau-Levich-Derjaguin law, provided the dependence of the suspension bulk viscosity on ϕ is considered (1.1). This conclusion has also been drawn very recently by Gans *et al.* (2019) and suggests that the net interfacial stresses experienced by a suspension of totally wetted and neutrally-buoyant particles are not very different from the Laplace pressure experienced by a pure liquid, as also reported for other types of capillary flow (Furbank & Morris 2004; Bonnoit *et al.* 2012; Mathues *et al.* 2015; Château *et al.* 2018; Château & Lhuissier 2019).

Naturally, the particle size d determines the transition velocities to regimes (ii) and (i). As also reported very recently by Gans *et al.* (2019), the transition II between (ii) and (iii) simply occurs when the film thickness $h/\ell \sim (\eta(\phi)U/\sigma)^{2/3}$ given by (1.1) is equal to d and, thus, always depends on ϕ . Conversely, the particle entrainment threshold velocity U_I separating (i) and (ii) is found to depend on ϕ only for sufficiently low volume fractions ($\phi \lesssim 0.30$). These measurements are consistent with the entrainment criteria for an isolated particle (Colosqui *et al.* 2013), which is expected to describe the diluted limit ($\phi \simeq 0$). The observation of a plateau in U_I at large ϕ ($\gtrsim 0.30$) suggests that the bath volume fraction becomes unimportant for the entrainment threshold and that the latter could be related to a local accumulation of particles in the meniscus. Nevertheless, the value of this plateau and its experimental dependence $\propto d^2$ on the particle size remain to be rationalized from first principles. Further work is also required to address the case of other types of suspensions, such as suspensions of partially wetted or non spherical particles.

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