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Abstract: There is little literature on the flow properties of the isotropic phase of liquid crystalline fluids. However, this phase is an ideal tool to bridge the physics of liquid crystals with those of (ordinary) fluids. Optical and mechanical studies are presented, demonstrating that away from any phase transition, the isotropic phase of liquid crystalline molecules (LCs) and liquid crystalline polymers (LCPs) can work as an optical oscillator in response to low-frequency mechanical excitation, establishing the elastic origin of the flow birefringence and “visualizing” the very existence of the elastic nature of the liquid state. Additionally, mimicking the excellent anchoring ability of liquid crystals, an alternative rheological protocol optimizing the fluid/substrate interfaces is presented to access the low-frequency shear elasticity in various one-component liquids and salt-free aqueous solutions.

Keywords: low- and high-molecular weight liquid crystals; flow birefringence; wetting; molecular liquids; low-frequency shear elasticity; solid-like properties

1. Introduction

Liquid crystalline molecules (LCs) are typically made of one or several flexible alkyl chains linked to rigid and polar cores (~5.0 D). The repetition of this antagonistic coupling along or within a polymer chain forms the so-called liquid crystalline polymers (LCPs). The symmetry and the characteristics of the liquid crystalline phases of LCPs and low molecular weight LCs are similar, being strongly related to short-range intermolecular liquid crystal interactions. While the flexible nature of the alkyl part favors amorphous glasses at low temperature, the rigid part self-assembles to form a crystal. These antagonistic properties are the key parameter to produce intermediate states between liquid and crystalline solid materials; the liquid crystallinity results from frustrated states. The frustration releases away from the phase transitions, in the isotropic phase, where the liquid crystal is thermodynamically, crystallographically, and hydrodynamically similar to an ordinary liquid.

The present contribution investigates newly elastic properties firstly identified in the non-mesomorphic phase of liquid crystals; i.e., in the isotropic phases of thermotropic LCs (including LCPs) or of lyotropic LCs, and then transposed to ordinary liquids or melts. While the elastic properties of the nematic phase of LCs and LCPs are largely documented via the dimensional Frank elastic constants [1], there is little literature on the mechanical behavior of the isotropic phase of liquid crystalline fluids. The main reason is that in the isotropic phase, the fluid is free from long-range liquid crystalline correlations, and therefore is undifferentiated from ordinary viscous liquids or from ordinary viscoelastic melts [2]. The investigation of the isotropic phase is however extremely rich: elastically-induced mechanical and optical properties are experimentally revealed.
The search for hidden elastic properties in the isotropic phase of liquid crystals was primary motivated by non-elucidated observations in steady-state flow conditions of non-linear stress behaviors, and of the emergence of flow birefringence above a critical shear rate. Systems as varied as wormlike micellar solutions [3–5], rigid-rod suspensions [6,7], and isotropic phases of thermotropic liquid crystal polymers (shear-induced isotropic to nematic [8–10] or isotropic to smectic phase transitions [11]) exhibit abrupt shear-induced transitions. These spectacular non-linear effects cannot be explained on the basis of flow coupling to a molecular relaxation time or a pretransitional lifetime [12–15] since, for example, the flow birefringence of LCPs is observed before reaching shear rates corresponding to the pretransitional lifetimes and the viscoelastic relaxation times [8–10,16–18]. Theoretical predictions based on a coupling with molecular dynamics can neither account for non-extensive parameters like the dimensionality (shear-induced phase transitions have been found to be thickness-dependent) nor for external conditions (boundary conditions such as surface wetting, surface curvature) [19]. These spectacular flow effects hide a different mechanism. Since the time scales are much larger than individual relaxation times, long-range collective processes are involved. The present work gathers some experimental results and theoretical developments, indicating that intermolecular interactions might play an important role in the dynamic response of the liquid to a flow field or a mechanical strain field. As a result, upon low-frequency excitation, the intermolecular forces act as a weak elastic network in which liquid molecules do behave not dynamically freely, but elastically (at the submillimeter scale).

The identification of elastic properties of the isotropic phase is of prime importance. Static shear elasticity tells that the molecules remain strongly elastically correlated even when the orientational (liquid crystal) interactions are lost in the (isotropic) liquid state. This article focuses on the fact that this property is not specific to liquid crystalline materials but concern fluids in general. Indeed, the isotropic phase bridges the physics of LCs with those of fluids, highlighting the route to access generic shear elasticity in the liquid state. Shear elasticity is extremely important to understand fluidics: it reveals that the liquid state is a low-threshold elastic medium; molecules are not free in the liquid state but dynamically elastically correlated. Shear elasticity sheds a new light on a comprehensive approach toward flow properties, involving flow birefringence, optical banded textures, flow instabilities, shear-induced stratification in liquid crystals, complex fluids (lyotropic solutions, colloids, vesicle membrane), and simple liquids (hydrodynamics . . . ). Additionally, the liquid phase of usual liquid crystals can work as a low-frequency (low-energy) opto-active material, and this is as such a property immediately available for macroscopic applications.

The first part of this contribution is devoted to the new identified strain optical properties induced at low frequency in the isotropic phase of LCPs and LCs, while the second part describes the origin of the low-frequency birefringence on the basis of the identification of shear elasticity in LCPs and LCs and in various fluids away from any phase transition. Both optical and stress behaviors challenge the Maxwell (molecular) definition of liquids (that are supposed to exhibit shear elasticity at high frequency only (typically at MHz or GHz)) and show that low-frequency (around Hz) shear elasticity exists. This long wavelength excitation reveals collective effects largely ignored in fluidics and points out a new no man’s land to explore.

2. Isotropic Phase under a Low-Frequency Mechanical Field: Spectacular Optical Effects

Low-Frequency Optical Response in the Isotropic Phase

We describe recent developments indicating that it is possible to produce a strong strain-induced optical signal of the isotropic phase of low molecular weight LCPs upon applying low-frequency (Hertz-range) mechanical excitation. This spectacular property was unknown to liquid crystal physics since dynamic correlations are assumed to be lost in the liquid phase.

The isotropic phase of liquid crystals is an ideal tool to explore liquid properties. From conventional rheological, thermodynamic, and crystallographic perspectives, it is an ordinary liquid. The liquid crystal/liquid transition is a first-order transition (the phase transition occurs at less than
0.1 °C). This implies that the pretransitional fluctuations, which are the phase precursors, do not mix with the liquid and coexist within the isotropic phase. The latter form clusters of randomly dispersed birefringent molecules. The strategy is to use them as optical tracers of the deformation field during the oscillating stress, similarly to bioluminescent phytoplankton organisms that emit light under oscillatory beach waves (Figure 1).

![Image](https://www.youtube.com/watch?v=0NPjNG6FkTE)

**Figure 1.** Like bioluminescent phytoplankton organisms that emit light under stress (see beach waves), pretransitional fluctuations produce birefringence by reorientation under shear strain stress (image from https://furthermore.equinox.com/articles/2014/10/seven-incredible-bodies-of-water).

Figure 2 illustrates that a strain-induced optical transmittance can be observed in the isotropic liquid phase of a 12-units LC upon applying an oscillatory strain wave at low frequency (0.5 Hz; true colors were obtained between crossed polarizers with a polychromatic incident light). This molecule is made of 12 liquid crystal moieties attached to an acrylate backbone. It is a commercially available product used in LC displays under the name LCP95 [20]. With a cyanobiphenyl side-chain moiety of 14 Å in length, a propyl spacer, the liquid crystal part is nearly as long as the repetitive 12-unit acrylate backbone. Its short length and the strong lateral hindrance do not enable several backbone conformations (no entropic conformation) and the smectic phase at lower temperature indicates that side-chain moieties are interdigitated in the bulk state [4,20,21].

![Image](https://www.youtube.com/watch?v=0NPjNG6FkTE)

**Figure 2.** The isotropic phase exhibits a “mechano-stimuli responsive” behavior upon applying an oscillatory strain wave $\gamma = \gamma_0 \sin(\omega \cdot t)$, where $\gamma_0$ is the rate of the displacement $\delta$ to the slab thickness $\varepsilon$ ($\gamma_0 = 10\%, \omega = 0.5$ Hz, $\varepsilon = 0.250$ mm, quartz substrate). Photos recorded between crossed polarizers using a polychromatic light, sample: 12 monomer units of cyanobiphenyl acrylate displaying the following phase sequence: Tg–54 °C–S_A–80 °C–I (from [22]). Link for the video: https://www.youtube.com/watch?v=0NPjNG6FkTE. LC: liquid crystalline molecule.
The low strain amplitude stress field stretches the isotropic phase that transits reversibly from a non-birefringent state (at rest) to a birefringent state (stretched state) [22]. The induced signal is reversible and synchronous with the strain wave, indicating that the involved mechanism is conservative and not dissipative. The remarkable point is that pretransitional fluctuations reorient under deformation at low frequencies (0.5 Hz) at timescales that do not enable a dynamic coupling with their lifetime ($10^{-9}$ s in usual LCs [23] and about $10^{-4}$ s for LCPs [24]). The analysis of the strain dependence provides information on the underlying mechanism that gives rise to the low-frequency birefringence.

Figure 3 quantitatively details the low-frequency optical response of the isotropic phase [22]. The signal is observed at $\omega = 0.5$ Hz as a function of the strain amplitude:

1. At the smallest strains ($\gamma_0 < 5\%$), the birefringence is harmonic and in phase with the applied strain.
2. In the intermediate regime ($5\% < \gamma_0 < 25\%$) the signals are also harmonic but are phase-shifted by $\pi/2$ (in phase with the strain rate).
3. At larger strains ($\gamma_0 > 25\%$), the signals become distorted, exhibiting higher harmonics. The waves no longer relax between two periods and saturated. The observed, almost continuous signal, as shown for $\gamma_0 > 80\%$, indicates a nearly strain-independent value. The asymptotic behavior at high strain amplitude of the birefringence corresponds to the flow birefringence.

**Low-frequency birefringence induced in the isotropic phase versus strain amplitude**

![Low-frequency birefringence induced in the isotropic phase versus strain amplitude](image)

**Figure 3.** Strain dependence of the birefringent signal (peak value of the signal) in the isotropic phase of the 12-units liquid crystal (T-TS$_{AI} = +1^\circ$C, quartz substrate) at 0.5 Hz. The strain amplitude is the maximum displacement length $\delta l$ divided by the sample thickness ($\gamma_0 = \delta l/e$).

The oscillatory signals at $\gamma_0 = 4\%, 10\%$, and $80\%$ strain amplitude displayed at the top (the applied strain is represented by the continuous black sine wave) indicate that:

- At a very low strain regime ($\gamma_0 < 4\%$), the birefringent signal is in phase with the applied strain wave (upper left inset).
- For $4\% < \gamma_0 < 30\%$, the optical signal is $\pi/2$ phase-shifted in respect to the strain and increases linearly up to $25\%$ strain amplitude (upper medium inset).
- Above $25\%$ strain amplitude, the optical signal does not relax, reaching an asymptotic value corresponding to the flow birefringence.
The three regimes pointed out in Figure 3 can be interpreted as follows:

- The birefringence at very small strain amplitudes \( \gamma_0 < \gamma_{\text{crit}} \) is in phase with the excitation, indicating an elastic mechanism alternating stretching state and relaxation under oscillatory strain.

- The second regime \( \gamma_0 > \gamma_{\text{crit}} \), characterized by a \( \pi/2 \) phase-shifted birefringence that increases linearly with the strain, is also harmonic with the excitation. The conservation of the shape of the strain wave (harmonicity) indicates that the strain-induced birefringence is associated to a conservative mechanism (as opposed to a dissipative process). The linearity with the increasing strain amplitude characterizes an elastic process. Finally, the \( \pi/2 \) shift of the phase of the signal indicates a two-step process wherein the first step is achieved in the first elastic regime identified at very low strain rates \( \gamma_0 < 4\% \) close to the transition.

- At higher strain amplitudes, the optical wave is not more harmonic, does not relax between two successive oscillations, and saturates to an asymptotic birefringence value, indicating a dissipative regime. The asymptotical limit of large strains is the steady state shear flow. In this regime, the nearly constant asymptotic value of the birefringence corresponds to the so-called flow birefringence.

Similar strain-induced optical behavior is observed with high molecular weight side-chain LCPs but without necessarily exhibiting higher optical signals. Figure 4 compares the signals of the strain-induced oscillatory birefringence of the 12-units LC to an 80-units LCP [25].

![A 12-units LC](image1)

![An 80-units-side-chain LC polymer](image2)

**Figure 4.** Low-frequency birefringence is larger for the small molecular weight LC under the same stress conditions \( \omega = 0.5 \text{ Hz}, 250 \mu m, \gamma_0 = 10\% \), +1 °C above the isotropic transition. (a) A 12-unit cyanobiphenyl side-chain acrylate molecule. (b) An 80-units cyanobiphenyl side-chain polyacrylate molecule (polydispersity: 1.1). In the insert: the optical signals of (a) and (b) of the isotropic phase of the 12-units and 80-units LCs are reported (double scale—the birefringence is normalized to the strain amplitude).

The identification of strain-induced optical birefringence in the isotropic phase at low frequency is new. The effect has been easily observed for side-chain liquid crystalline polymers of various chemical formulae [22,24,25] and is much less accessible on low molecular liquid crystals, likely because the pretransitional fluctuations are much less extended in space and in temperature range compared to larger molecular liquid crystals (Figure 5).
However, the higher molecular weights do not provide the highest strain-induced optical signal (Figure 4). While the elastic nature is reinforced by the increase of the degree of polymerization, the anchoring is weakened and generates instabilities (interfacial slippage) and therefore optical anharmonicity. A good compromise seems to be a highly viscous isotropic phase while avoiding the typical sliding ability of long polymer chains. The 12-units LC (Figure 3) allows effective interdigitation without being a polymer. Interdigitation is a key word; i.e., strong intermolecular interactions play a key role in such collective optical responses that imply long range correlations.

The low-frequency optical response of the isotropic phase is incompatible with the lifetime of pretransitional fluctuations (of the order of \( \tau \approx 10^{-9} \) s for the usual liquid crystals or \( \tau \approx 10^{-4} \) s for the liquid crystal polymers). Similarly, surface or capillary effects cannot explain the low-frequency birefringence; Thicknesses probed far exceed the coherence lengths that are of the order of several molecular lengths.

Since the strain-induced optical birefringence cannot be explained on the basis of conventional timescales, it contains important fundamental information. The succession of events from in-phase birefringence to this asymptotic (flow) birefringence is instructive with respect to the mechanism. It indicates that the strain-induced birefringence exhibits the characteristics of an elastic process (at low frequency) and thus is not necessary coupled to any particular time.

Indeed, the long-range order evidenced by the optical birefringence and the harmonicity of the response are in opposition to a dissipative state (the birefringence signal immediately relaxes back once the stress is released). Although the material gains energy under deformation, the induced order indicates that there is a loss of entropy compared to the isotropic state (and not an entropy gain). This result can be explained by considering that the molecules are elastically correlated. The energy transferred under deformation is accumulated to produce an ordered phase (orientation of pretransitional fluctuations) and not to reinforce a disordered liquid. The stretching process decreases the entropy, which is why the material relaxes immediately once the deformation is removed (entropy gain). The isotropic phase behaves like an elastic material alternating entropic loss and elastic relaxation during the round-trip motion. The free energy of the isotropic phase can be expressed according to the

\[
\begin{align*}
F = F_0 + \frac{1}{2} \cdot \gamma_0 \cdot \tau \cdot (\omega - \omega_0)^2
\end{align*}
\]
formalism of the liquid crystal elastomers by adding a term coupling the orientational fluctuations to
the deformation (at small amplitudes):

$$F = F_0 + \frac{1}{2} G_0 \gamma^2 - \sigma \gamma - k S(\gamma) \gamma$$

where $S$ is the order parameter assumed to be proportional to the birefringence ($S \equiv 0$ without
constraint), $G_0$ the elastic shear modulus identified in the isotropic phase, $\sigma$ is the applied stress, and $k$
is the coupling constant binding the parameter from order to deformation $\gamma$. This expression indicates
that the energy is lowered under deformation by an increase of the order parameter (birefringence)
and thus a decrease of the entropy.

Beside the study of the isotropic phase under oscillatory shear strain demonstrates that
pretransitional fluctuations are efficient probes to visualize, via the optical birefringence, the strain field
during the mechanical excitation. The strain-induced optical signal is detectable far above the clearing
point (at least above $T_{SAI} +15 \, ^\circ C$) and at frequencies as low as 0.01 Hz in viscous isotropic phases [5].
The usage of the pretransitional swarms as an optical probe is however limited by their temperature
dependence. Since the optical response of the isotropic phase reveals an elastically-induced process,
viscous (LC) or viscoelastic (LCP) spectra should contain an elastic response to an applied mechanical
stress. This point is developed in the second part.

3. Introduction to the Viscoelastic Approach: From the Macroscopic to Sub-Millimeter Scale

A Young Discipline

The spectral analysis versus frequency of fluid dynamic properties is a recent discipline resulting
from the need to characterize a plethora of materials for which flow behaviors are intermediate between
Newtonian liquids and Hookean solids following the time of observation; i.e., versus frequency. While
the general framework has existed since the 19th century to describe the linear behavior of these
intermediate materials in particular via mechanical models of springs (Poynting, Thomson [26]),
Boltzmann [27]), the principle of a time-dependent measurement relating the strain to the stress
and associated with the design of specific apparatus, first called rheogoniometers, is due to Weissenberg
and coworkers [28]. The rheology with the emergence of the rheometers, rapidly became the technique
for characterizing the dynamic properties of fluids, in particular for viscoelastic materials. Its principle
consists in the analysis of the response transmitted by the material subjected to dynamic mechanical
stress. With the stress being transferred to the sample by the molecular contact to the substrate, this
technique is entirely dependent on conditions of the quality of interaction between the material and
the substrate.

Rheological measurements are generally carried out applying a small amplitude oscillatory
motion to keep the sample as close as possible to equilibrium conditions (in agreement with the
causality-linearity principles). The fluid is placed in contact with and between two surfaces (generally
metallic substrate); one oscillating, the other one fixed measuring the stress transmitted by the sample
via a sensor (Figure 6). In conventional measurements (generally using aluminum, stainless steel,
or glass substrates), the dynamic relaxation spectrum is measured on millimeter-thick samples. From
the difference between the input and the output signals and supposing the sine wave is (harmonically)
conserved, two parameters are extracted: the component in phase with the strain determines the
shear elastic (or storage) modulus ($G'$), whereas the out-of-phase component defines the viscous
(or loss) modulus ($G''$) following the relationship: $\sigma(\omega) = \gamma_0 \cdot (G'(\omega) \cdot \cos(\omega \cdot t) + G''(\omega) \cdot \sin(\omega \cdot t))$.
The representation of $G'(\omega)$ and $G''(\omega)$ versus frequency provides the dynamic signature of the
material with its eigenmodes.
The analysis of the viscoelastic spectrum serves as the basis of the elegant theoretical approaches for polymer physics such as the tube model (Doi-Edwards 1978 [29]; de Gennes 1971 [30]) and earlier the Rouse theory (Rouse 1953 [31]) that was elaborated for dilute solutions, linking conformational polymer dynamics and viscoelasticity (Figure 7). Since relaxation spectra of dilute solutions, concentrated solutions, and polymer melts present similar features; i.e., the character of the frequency dependence seen was essentially similar, Ferry’s works extended the Rouse theory to try to explain bulk polymer behavior, developing the concept of a direct link between the rheological viscoelastic properties and the molecular structure (Ferry 1970 [32]).

Polymers in dilute, concentrated solutions or in the molten state exhibit versus frequency the typical viscoelastic curve [33]. The low-frequency range characterizes the terminal behavior and is called flow behavior. It is depicted by a $\omega$-scaling decrease of the viscous modulus ($G''$) and a $\omega^2$-scaling of the elastic modulus ($G'$). The flow behavior thus describes the frequency part where the viscous component becomes major. The interception of the two curves defines the terminal time; i.e., the largest time before the material enters in a flow regime. This characteristic time is interpreted as a single molecular relaxation time on the basis of the Rouse theory or the reptation concept. The viscoelasticity is thus a molecular theory interpreting macroscopic mechanical responses in terms of molecular-scale properties.

These elegant theoretical works are essentially based on a single chain picture where the relaxation modes (generating viscous and elastic contributions) originate mainly from the intrachain properties.
The intermolecular interactions are neglected in agreement with the early Rouse model of diluted polymer solutions (Rouse 1953 [31]).

The primary assumption of the Rouse theory is that the viscoelastic spectrum reflects the single chain dynamics. The chains are supposed sufficiently away from each other to not interact in a diluted solution; i.e., the theory assumes that the solvent has a negligible contribution, while it is however the vector of transfer of the stress from the substrate. The chain is seen as a succession of independent elastic springs (“bead-spring” model). Each spring representing a group of monomers (subchain) is sufficiently long to be decoupled from others (Gaussian statistics).

The elastic modulus takes the form of the Maxwell expression:

\[ G'(\omega) = nkT \sum_{p=1}^{Z} \frac{\omega^2 \tau_p^2}{1 + \omega^2 \tau_p^2} \]

where \( \tau_p \) is the relaxation time of the group \( p \), \( Z \) the number of springs, \( n \) the number of chains per volume unit, and \( T \) the temperature.

At low frequency, \( G' \) exhibits a \( \omega^2 \)-scale behavior (Figure 1) and the zero-frequency limit predicts a collapse of the elastic component.

The viscous part is expressed as:

\[ G''(\omega) = \eta_s + nkT \sum_{p=1}^{Z} \frac{\omega \tau_p}{1 + \omega^2 \tau_p^2} \]

where \( \eta_s \) is the solvent viscosity.

One can note that the \( G'' \) zero-frequency limit gives also rise to a collapse of the viscous part. To distinguish viscoelastic liquids from viscoelastic solids, a term \( G_e \) is added to the viscoelastic function (Ferry 1980):

\[ G'(\omega) = nkT \sum_{p=1}^{Z} \frac{\omega^2 \tau_p^2}{1 + \omega^2 \tau_p^2} + G_e(T) \]

\( G_e \) is the equilibrium modulus. It expresses the existence of infinite relaxation times (i.e., of infinite correlation ranges), that defines the elastic character of solid-like materials (typically cross-linked polymers). It is taken as \( G_e \equiv 0 \) for liquids and viscoelastic liquids at low frequency.

4. The Optical Response of LCs and LCPs in the Isotropic Phase Challenges the Single Molecular Approach

The optical response of LCs and LCPs in the isotropic phase (2) challenges this theoretical frame since it suggests an elastic behavior that is not compatible with the single molecular picture (elementary timescales in low molecular weight liquid crystal are extremely short of the order of \( \tau \approx 10^{-9} \) s for the usual liquid crystals or \( \tau \approx 10^{-4} \) s for the liquid crystal polymers compared to the low-frequency range).

In the following, it is demonstrated that LCs and LCPs challenge the expected viscous or viscoelastic responses described above and that there is a multiscale behavior in which the conventional viscoelastic behavior represents only a part of the dynamic response; i.e., the asymptotic stress response at large thickness.

5. Mechanical Response of LC and LCPs in the Isotropic Phase

Gallani et al. reported as early as 1994 on “abnormal” viscoelastic behavior in the isotropic phase of liquid crystalline polymer [34]. The gel-like response \( (10^6 \text{ Pa}) \) was measured on thin films of 13–20 \( \mu \text{m} \) thicknesses on different LCPs and firstly interpreted as a reminiscence of a liquid crystalline network structure [35]. A couple of years later, using a conventional rheometer, solid-like responses were reported up to the millimeter-length scale in the isotropic phase of a liquid crystalline polymer (L. Noirez 2005 [17,36]) while the molecular dimensions are less than 100 Å. The shear elasticity was
Low-frequency shear elastic behaviors have been reported actually on several occasions but restricted to very low scales and are thus interpreted as surface-induced effects. In this sense, LCs or LCPs are fascinating since they enable to access the elasticity at much larger scales. The strong anchoring ability of the liquid crystal molecules reinforces the boundary contacts between the fluid and the substrate whereby the stress is transmitted and facilitates the measurement. This might explain why the elastic response is easily measurable in mesomorphic fluids. For polymer melts, beginning in 1991 Granick and coworkers \[37–39\] measured a solid-like component at nanoscales and lower frequency, Collin et al. reported, using treated glass surfaces and small strains delivered by a piezorheometer, a gel-like response of up to 50-µm thicknesses in a low molecular weight polystyrene melt that was interpreted as reminiscent of the glass transition, i.e., clusters of finite size \[40\]. The very first analysis in terms of artefacts attributed to trapped dust particles \[40\]. The first analysis in terms of reminiscent glass transition effects. Figure 8 illustrates and compares the elastic behavior at a 3–4 µm thickness by micro-rheology, but these observations were mostly interpreted as resulting from surface-induced effects. The disappearance of the solid-like response at larger thicknesses was interpreted by a transition from surface to bulk properties. Other authors reported on an elastic behavior at a 3–4 µm thickness by micro-rheology, but these observations were mostly interpreted as artefacts attributed to trapped dust particles \[40\]. The very first analysis in terms of physical property was performed by Derjaguin \[41,42\] revealing in different fluids, including polymers and liquid water, an elastic response at the micron scale which was for the first time interpreted as an intrinsic property due to the force of intermolecular interactions. At larger scales and lower frequency, Collin et al. reported, using treated glass surfaces and small strains delivered by a piezorheometer, a gel-like response of up to 50-µm thicknesses in a low molecular weight polystyrene melt that was interpreted as reminiscent of the glass transition, i.e., clusters of finite size \[43\]. Since 2006, with the consideration of the wetting conditions to the substrate (paragraph 6), decisive steps have been taken for easy access to shear elasticity, generalizing its identification to a wide panel of liquids and elucidating its intermolecular interaction origin as a condensed matter property \[44–54\].

In this framework, the study of liquid crystalline fluids is very instructive, since low-frequency shear elasticity was identified both in the isotropic phases of low molecular weight liquid crystals \[49\].

**Figure 8.** A strong solid-like response is measured above the isotropic–nematic transition by a liquid crystal polymer (viscoelastic moduli \(G'(\bullet), G''(\bigcirc)\) recorded at 14 °C above the transition and 0.150 mm gap thickness). The lower inset displays for comparison the conventional polymer melt behavior fulfilling the Maxwell model \[32\]. From Mendil, Noirez, Baroni 2006 \[36\]). With kind permission from The European Physical Journal (EPJ).
and of high molecular weight liquid crystals of side-chain architecture [17,22,25,34–36,46,49,51], ruling out a reminiscence of glass transition effects. Figure 9 illustrates and compares the elastic response displayed by 4-octyl-4-cyano-biphenyl (8CB) [49] to the one of a side-chain liquid crystal polymer (methoxy-phenyl benzoate substituted polyacrylate of 85 repetitive units [36]). In both cases, the low-frequency regime exhibits an elastic behavior ($G'$ is higher than $G''$ and is weakly frequency dependent). The elastic response is the signature of a collective response; that is, intermolecular interactions dominate the mechanical response. They act as connectors creating a three-dimensional physical network in the isotropic state. The comparison of the low-frequency shear moduli indicates that the branched architecture of the side chain polymer intensifies the elastic signal ($\cong 900$ Pa) which is about three decades over the signal of the small molecule modulus (8CB; 2–3 Pa). The shear elasticity therefore strongly depends on the molecular architecture and the interdigitation ability.

Both measurements were carried out at about 0.050 mm. At larger thicknesses, the shear elasticity weakens, leaving room for the viscous behavior conventionally observed. The conventional viscous (or viscoelastic) behavior is thus the asymptotic behavior of the large-scale elastic regime. At small scales (several tens of microns), shear elasticity dominates and indicates that the liquid reacts like a solid at the length scale, far from several molecular lengths; that is, it is a macroscopic property. During mechanical excitation, the resistance of the cohesive forces diminishes as the thickness increases (Figure 5), becoming hidden at the millimeter scale. The following paragraph illustrates that the strain amplitude produces an effect similar as the thickness weakening the cohesive forces as the strain stress increases.

Figure 10 shows the evolution of the shear elasticity of the isotropic phase of 8CB as a function of the amplitude of deformation (from reference [34]). The mechanical signal analysis informs on the strain-induced transition of a solid-type behavior to a viscous-like behavior. At large stress amplitude,
the viscous modulus dominates the elastic modulus, the latter becoming negligible (less than 1%). The conventional viscous behavior of the isotropic phase is recovered by applying high deformation amplitudes, thus far away from mechanical equilibrium conditions. As a result, a linear solid-type regime precedes the conventional flow regime. The solid type response collapses by increasing the strain amplitude. The deformation and the thickness produce a similar effect on $G'$. The two parameters are linked by the relation: $\gamma = \delta l/e$ indicating that $\delta l$, the displacement is the relevant parameter, and suggesting a transition to a dissipative process (slippage effects, shear banding, band structuration) above a critical strain $\gamma_{\text{crit}}$ or a critical thickness $e_{\text{crit}}$ that defines the limit of the linear regime of shear elasticity.

Isotropic phase of 8CB: From elastic to conventional viscous behavior

![Isotropic phase of 8CB](image)

**Figure 10.** Mechanical response of 4-octyl-4'-cyanobiphenyl (8CB) in the isotropic phase at a 0.050-mm gap thickness (reproduced with permission from reference [50]). Upper figure: The elastic response is evidenced by in-phase behavior of strain and stress waves. At larger strain amplitudes, the strain (black line) and stress (red line) waves become progressively $\pi/2$ phase-shifted, indicating a liquid-like behavior characterized by the tabulated viscosity of 14 mPa.s. Bottom figure: Strain dependence (logarithmic scales) of the viscoelastic moduli ($G'(\star), G''(■)$): (a) At low strain amplitude (typically $\gamma_0 = 6\%$), the isotropic liquid exhibits an elastic response with $G' > G''$ and $G', G''$ nearly constant. The grey dotted line indicates the reference value of the stress modulus in nearly equilibrium conditions and the grey vertical bar indicates the modulus loss with respect to the elastic regime.

The second example is the low-frequency behavior reported in the isotropic phase of the 12-units LCs (Figure 11). With a cyanobiphenyl side-chain moiety of 14 Å length, a propyl spacer, the liquid crystal part is nearly as long as the backbone. This molecule in solution has a spherical shape with a 1.4-nm hydrodynamic radius. Its short length and the strong lateral hindrance do not enable conformational entropy, but the smectic phase at lower temperature indicates that side-chain moieties are strongly interdigitated in the bulk state [20,21] in agreement with its relatively large viscosity in the isotropic melt ($\eta \approx 160$ Pa·s at +25 °C up to 800 Pa·s at +1 °C above the isotropic–smectic transition).
Isotropic phase of 12-unit LCs: From elastic to conventional viscous behavior

![Graph showing viscoelastic moduli (G', G'') of the 12-unit LC in the isotropic phase (T = T_{SAI} + 25 °C) at a 0.170-mm gap thickness and ω = 0.1 Hz (from reference [22]). The solid-like response at small strain amplitudes is progressively replaced by a liquid-like behavior with increasing strains. This behavior is highlighted by the strain (black line) and stress (red line) waves that are in phase in the elastic regime and π/2 phase shifted in the viscous regime (top figure). The grey dotted line indicates the reference value of the stress modulus in nearly equilibrium conditions.](image)

Figure 11. Strain dependence (logarithmic scales) of the viscoelastic moduli (G' ( ), G'' ( )) of the 12-unit LC in the isotropic phase (T = T_{SAI} + 25 °C) at a 0.170-mm gap thickness and ω = 0.1 Hz (from reference [22]). The solid-like response at small strain amplitudes is progressively replaced by a liquid-like behavior with increasing strains. This behavior is highlighted by the strain (black line) and stress (red line) waves that are in phase in the elastic regime and π/2 phase shifted in the viscous regime (top figure). The grey dotted line indicates the reference value of the stress modulus in nearly equilibrium conditions.

Similarly, as for 8CB, the isotropic phase of the 12-units-LC exhibits an elastomeric behavior at low strain amplitude (Figure 11). By increasing the strain amplitude, the signals become slightly distorted (signals for γ₀ = 50%) and phase-shifted with respect to the applied strain. The shear elasticity is lost above a critical strain amplitude γ_{crit}, and by further increasing the strain amplitude, the strain/stress signals become phase shifted by π/2, in agreement with a viscous behavior. The viscous modulus dominates while the elastic modulus becomes negligible, recovering a viscous behavior (flow regime). The modulus of elasticity in shear of this liquid crystal of 12 units is about 150 Pa [22], which is an intermediate value between those reported for the isotropic phase of the side-chain polymers reaching thousands of Pa [17,31,34–36] and 8CB of around 1 Pascal [49]. In conclusion, 8CB and 12-units LCs, two examples of untangled non-crosslinked isotropic fluids, show that elastomer-like behavior can be obtained in the low-frequency regime provided that the isotropic liquid is excited at the scale of tens or hundreds of microns by a low strain stress. In addition, the elastomeric character of the isotropic phase is reinforced by a moderate branching of the liquid crystal moieties.

This overview of shear elasticity in liquid crystalline fluids would not be complete without mentioning lyotropic liquid crystal polymers. The low concentration (isotropic) phase of the lyotropic phase is the counterpart of the thermotropic isotropic phase. We show here that low-frequency shear elasticity has been identified in worm-like micellar solutions (Figure 12) bringing possible new input in the long debate on the origin of shear-induced phase transitions in lyotropic solutions. Figure 12 displays the low-frequency behavior in the isotropic phase of CTAB–water (Cetyl TrimethylAmmonium Bromide solution). Similarly, as for the isotropic phase of the thermotropic systems, the elastic modulus (G') is higher than the viscous modulus (G''), with G' and G'' relatively independent of the frequency, indicating a dominant elastic response [51].

The identification of shear elasticity in both thermotropic and lyotropic systems indicates that the molecules are not dynamically free but long-range correlated via the intermolecular interactions. These electrostatic interactions between molecules provide the liquid cohesion. The dynamic behavior of surfactant solution (Figure 7b) is in agreement with what was found on various liquids, including
ionic liquids, alkanes, and liquid water [47,50]. This was obtained by strongly interacting surfaces to optimize the stress transmission (see Section 6.).

![Figure 12](image-url) Using total wetting conditions, the liquid phase (dilution 18%) of salt-free CTAB-water (Cetyl TrimethylAmmonium Bromide solution) measured at 33 °C (isotropic phase) and the 0.300-mm gap thickness exhibit solid-like behavior with G’ independent of the frequency and exceeding G” [51].

6. Optimizing the Stress Transmission and Accessing Shear Elasticity in Ordinary Fluids

Up-to-date advances in instrumentation in mechanical rheometry have considerably widened the frequency window and the modulus range, and therefore enable the detection of subtle properties that would not been considered at the time of the first concepts of the viscoelasticity. However, the validity of a dynamic relaxation experiment is also primary depending on the efficiency of the stress transmission which is ensured by molecular contact between the sample and the surfaces. For symmetry reasons, surface properties differ from the bulk properties. Therefore, looking for ideal boundary conditions is a challenge. To lower the energy barrier at the solid/liquid interface when molecules do not anchor on substrate as liquid crystalline molecules usually do, reaching total wetting can supply by reinforcing the liquid/substrate interaction, and thus prevents the slippage.

In the framework of this, the wetting protocol has provided easier access to the solid-like response hidden in conventional mechanical measurements. The viscoelastic moduli using the total wetting boundary conditions (alumina surfaces) are higher and reveal the low-frequency shear elasticity in fluids and liquids. The low-frequency shear elasticity (regime of invariance of the dynamic response versus frequency) is observed far away from any phase transition, thus in the liquid state at typically submillimeter (0.025–0.5 mm) thicknesses. It has been reported both in unentangled [36] and in high molecular weight polymers [51,52], in glass formers [53,54], ordinary alkanes [47], and liquid water, highlighting its generic character related to the liquid cohesion energy.

Figure 13 illustrates the response obtained using full wetting conditions for H-bond oligomer polypropylene glycol (PPG4000). The superposition of the stress wave to strain stress wave confirms directly the instant transmission of the stress to the sensor, which characterizes a solid-like behavior. This result is coherent with the conclusions in terms of elastic contribution carried on the same liquid on the analysis of the dynamic of the capillary waves by synchrotron radiation [54].

If the shear elasticity of the fluid is observable by improving the wettability of the substrate, it is progressively lost by increasing the thickness or by increasing the strain amplitude, giving rise asymptotically to the viscous or in the case of polymer melts to the conventional flow behavior in agreement with what was observed in the mechanical behavior of liquid crystals. The shear strain acts as a selector with respect to the boundary contacts between the fluid and the substrate. Fast relaxation time contacts are easily restored and give rise to the conventional flow behavior, whereas long relaxation (solid-like) contacts bear only small strains and exhibit the elastic response. Finally, the analysis of the stress wave instructively shows that the transition from elastic to viscous regime by increasing strain rate generates non-harmonics, as for example in the case of the heptadecane (Figure 14).
7. Conclusions

Because flow is eminently an interface problem, the consideration of the boundary conditions between the surface and the sample is an important challenge. The optical response of the isotropic
phase under mechanical oscillatory excitation at macroscopic scale is a splendid illustration of the physics revealed by strong anchoring effects. The isotropic phase of liquid crystals submitted to low-frequency excitation exhibits an optical birefringence synchronized at low applied strains [22,25]. Because this effect is visible at low frequency and at length scales much larger than molecular lengths (at a scale of several hundreds of microns), it rules out the pertinence of a coupling to pretransitional modes (the latter of \( \tau \approx 10^{-9} \) s for (low molecular weight) rod-like liquid crystals corresponding to GHz or MHz excitation [23] and about \( \tau \approx 10^{-4} \) s for side-chain liquid crystalline polymers [24]) or surface-induced effects. Because the optical signal reproduces the shape of the applied strain wave, a conservative mechanism is suggested (as opposed to a dissipative process). This optical property is the visual demonstration of the very existence of an elastic process. This process gives rise at very high strain rate to the flow birefringence, which is the asymptotic elastic regime. A similar mechanism is reproduced by the stress behavior of the shear elasticity in the isotropic phases of LCs and LCPs which exhibit at low-strain-value elastic behavior, and viscous (low molecular weight) or viscoelastic (high molecular weight) behavior at large strain values, corresponding to asymptotic stress regimes.

Mimicking the excellent anchoring properties of liquid crystals by using total wetting substrates, a similar strain dependence is observed in various one-component liquids and salt-free aqueous solutions; a dominant shear elasticity is identified in the low-frequency regime, suggesting that the conventional viscous or viscoelastic regimes identified at large strain values correspond to the asymptotic part of a wider rheological scheme [36,41,42,47,49–53]. The experimental evidence that liquids do possess low-frequency shear elasticity and thus that the flow is obtained at the price of an overpassing an elastic threshold was already provided a couple of years ago by the pioneering group Derjaguin [41,42]. These works seem to have been ignored. This resistance of the fluid can be revealed when the molecules have a strong interaction with the surfaces. The boundary conditions play thus a key role that is rarely taken into consideration and is integrated in very few hydrodynamic models only [55]. Because shear elasticity is intrinsically linked to the compressibility, it enables the identification of shear-induced cooling in liquid water [56] and of thermal shear bands in polymer melts (Figure 15) [57] and is likely at the origin of stronger well-known effects [58,59], as well as shear-induced stratification or transverse phonon modes in the isotropic phase of liquid crystals using inelastic scattering [60]. These effects introduce the possibility of a stretched liquid state, in agreement with the excitation of long-range elastic interactions.

\[
\begin{align*}
\gamma &= 0 & \gamma &= \gamma_{\text{max}} & \gamma &= 0 \\
V &= V_{\text{max}} & V &= 0 & V &= V_{\text{max}}
\end{align*}
\]

**Figure 15.** Polymer slab of 0.185-mm-thickness under oscillatory strain: the melt exhibits non-uniform temperatures with the emergence of cold thermal bands (dark blue) coexisting upon applying an oscillatory shear stress of \( (\gamma = 1200\%, \omega = 2 \text{ rad/s}) \). The bottom curves illustrate the strain and the velocity over a period. Complementary information is available in references [58,59].

In this context, it is urgent to consider not only single molecular dynamics but also collective effects in liquids and thus reintroduce intermolecular interactions since they are responsible for long-range correlations. In polymer physics, this implies taking into account also interchain non-covalent
interactions [61] and not only intrachain interactions despite the dominant single (non-interacting) chain concept. Simulation models [62] foresee that the dominant viscoelastic contribution should be due to excluded volume interactions, i.e., interchain forces. The simulation is in agreement with NMR results [63] and fluorescence polarization measurements [64], showing that free or dangling chains become locally oriented in an anisotropic chain network.

In (generic) liquids, long-range elastic correlations were predicted at equilibrium [65] much prior the recent experimental identification at the sub-millimeter scale of low-frequency elasticity [17,34–36,44–54]. In this frame the density fluctuations are not simply linked to thermal fluctuations but are also correlated, introducing dynamic and dimensional scaling. New experimental approaches have already emerged describing at the molecular scale possible elastic-like mechanisms in liquids [66,67]. New modelling inspired from liquid crystal elastomers, revisiting solid melting [68] or current molecular models to elaborate an alternative solid-like gap-based approach [69,70], have already converged to integrate the dynamic role of the intermolecular interactions to understand liquid properties. Experimentally, the continuous emergence of new liquid crystalline molecules and the correlative discovery of unsuspected properties around the isotropic phase [71,72] highlight day after day the need for understanding the key role of intermolecular interactions.

**Author Contributions:** L.N. develops researches highlighting elastic correlations in liquids. She wrote this chapter on the basis of the last advances, in particular the results concerning the low-frequency birefringence identified and analyzed by P.K. in the frame of his PhD training.

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