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A Molecular-Dynamics Simulation of Sliding Liquid Nanodrops

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Dynamic contact angle θ^{d} at all points around drop depends on normal velocity of contact line U_{cl}

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Hypothesis: That the behavior of sliding drops at the nanoscale mirrors that seen in macroscopic experiments, that the local microscopic contact angle is velocity dependent in a way that is consistent with the molecular-kinetic theory (MKT), and that observations at this scale shed light on the pearling transition seen with larger drops.

Methods: We use large-scale molecular dynamics (MD) to model a nanodrop of liquid sliding across a solid surface under the influence of an external force. The simulations enable us to extract the shape of the drop, details of flow within the drop and the local dynamic contact angle at all points around its periphery.

Findings: Our results confirm the macroscopic observation that the dynamic contact angle at all points around the drop is a function of the velocity of the contact line normal to itself, $U_{cm}\sin\phi$, where U_{cm} is the velocity of the drop's center of mass and ϕ is the slope of the contact line with respect to the direction of travel. Flow within the drop agrees with that observed on the surface of macroscopic drops. If slip between the first layer of liquid molecules and the solid surface is accounted for, the velocity-dependence of the dynamic contact angle is identical with that found previous MD simulations of spreading drops, and consistent with the MKT. If the external force is increased beyond a certain point, the drop elongates and a neck appears between the front and rear of the drop, which separate into two distinct zones. This appears to be the onset of the drop is far removed from its equilibrium value but non-zero and approaches a more-or-less constant critical value as the transition progresses.

Keywords: Wetting, moving contact lines, avoided critical behavior, dynamic contact angle, slip, pearling transition, molecular-kinetic theory (MKT).

1. Introduction

Raindrops running or sliding down a windowpane are so much part of everyday experience that one may rarely stop to consider the mechanisms that might determine their passage. Casual inspection reveals that on a well-wetted surface, the drops move down nearly vertical paths. If the window is initially dry, a drop may slide with an irregular trajectory, diverting first to one side and then the other as its leading edge is hindered, generating unsteady internal flows. New drops arriving on the same path may follow the track of their predecessor, or diverge, pioneering their own trail. On a dry, but less easily wetted surface, the drops may stick and not start to move until another drop arrives to increase their mass. Once sliding starts, the drop may take on a teardrop shape, with a tapering, triangular tail from which even smaller drops are shed, as illustrated in Figure 1a. Such shedding may seem unsurprising; is not the drag of the glass bound to cause some fraction of the drop to be left behind? Nevertheless, this behavior is far from simple and some aspects of the underlying physics remain unknown, or at least contentious.



Figure 1. a) Sketch of a sliding drop showing a trailing vertex and a detached drop. b) Schematic of a saw-tooth wetting line formed when $U > U_{crit}$. c) Image of a triangular film entrained when a partially wetted surface is pulled vertically out of a bath of liquid [1].

A related phenomenon can be seen when a partially wetted plate or tape is pulled vertically out of a pool of liquid. At sufficiently low speeds, the solid surface emerges from the pool in an apparently dry state. However, if the speed of withdrawal exceeds a certain value, then a film of liquid is entrained. As the plate is pulled upwards, the film, including its upper boundary (the contact line) drains downwards, but at a slower rate, so that the wetted area increases. Of particular interest is that the receding contact line does not usually remain horizontal, but inclines, taking on a saw-tooth configuration. If the speed is increased still further, the film lengthens and the vertex angle of each triangular section becomes increasingly acute. Eventually, discrete drops of liquid are pulled from each trailing vertex.

Blake and Ruschak [1] showed that this behavior is evidence of a maximum velocity of dewetting, U_{crit} beyond which a film will be pulled. In order to minimize the energetically unfavorable creation of a liquid film on a poorly wetted surface, the contact line lengthens to form the saw-tooth shape, such that the normal velocity of each segment remains constant at its maximum value. The general effect is quite predictable and, as illustrated in Figure 1b, there is a simple geometric relationship between U_{crit} , the withdrawal velocity of the plate U and the angle of inclination ϕ of each segment with respect to the direction of motion:

$$U_{crit} = U \sin\phi. \tag{1}$$

In these experiments, a smooth, uniform 50 mm polymer tape was withdrawn continuously at a steady rate from a pool of aqueous glycerol solution. Above U_{crit} , a single, steady triangular

film was obtained across the width of the tape (Figure 1c). Drops were entrained from the trailing vertex once ϕ was less than about 45°. At the vertex, where the two straight-line segments appear to intersect, the curvature of the contact line is large but finite; thus, the tangent at this point will be horizontal and a local forced wetting transition leads to the entrainment of a narrow rivulet of liquid by the solid. This subsequently breaks into individual droplets due to Rayleigh-Plateau instability. The details of this region and exactly how the flow in the vicinity of the contact line avoids this critical behavior along the inclined segments is not yet fully explained, although progress has been made within certain simplifications, such as the use of the lubrication approximation to describe the flow and a fixed local, microscopic angle [2–6]. The situation is complicated by incomplete agreement on how a contact line moves across a solid surface: in particular, the relative importance of viscous and surface frictional forces at the contact line and whether or not it is indeed sufficient to assume that the microscopic contact angle remains constant at its equilibrium value [7–11].

Since the pioneering work [1], there have been further experimental studies of both film deposition [12–15] and sliding drops [3,16–20]. Recent papers [21,22] provide useful reviews, as well as detailed theoretical analyses. Although the phenomenology of sliding drops has much in common with film deposition, such as the avoided critical behavior and droplet shedding, there are several potentially important differences, in particular their small size and the fact that the liquid system is initially closed and surrounded by a highly curved surface. With respect to flow near the trailing vertices and droplet shedding (the so-called 'pearling transition') good agreement has been found between theory and experiment with moderately viscous silicone oils, but discrepancies, such as non-physical length scales, have been found for the less viscous liquid

water [19]. Whether this is due to the three-dimensionality of the flow in this region, the assumption of a fixed microscopic contact angle, or some other factor, remains to be resolved.

One approach that shows promise to further our understanding is to use large-scale molecular dynamics (MD) to model droplet sliding. MD has proved uniquely successful in illuminating the molecular mechanism by which a contact line moves across a solid surface and demonstrating the importance of contact-line friction [23–37]. Indeed, a very recent paper by Lukyanov and Pryer [38] may have successfully reconciled MD results with macroscopic hydrodynamics yielding a regularized solution to the moving contact line problem. Here, we apply MD to model a liquid nanodrop sliding across a molecularly flat solid surface under the influence of a uniform force that acts parallel to the solid-liquid interface and is applied to all the atoms of the liquid; thus, mimicking a drop sliding under the influence of gravity. We demonstrate that our results are compatible with the physical experiments of Limat and co-workers [39] and extend our understanding of the underlying processes down to the nanoscale.

2. Molecular dynamics

The simulation methods, base parameters and potentials we employ have all been used previously by De Coninck and co-workers to successfully model a range of wetting problems such as droplet spreading [27,34,35], the wetting of fibers [31], dewetting dynamics [32], and forced wetting in Couette flow [36]. Full details are given in these publications and work cited therein, where we have shown that the system, though very simple, has all the necessary features to model wetting on the nanoscale and recover established macroscopic laws governing liquid behavior. To summarize, the liquid (L), the solid (S) and their interactions are modelled using Lennard-Jones 12-6 potentials defined by

$$V(r_{ij}) = 4\epsilon C_{AB} \left(\left(\frac{\sigma}{r_{ij}} \right)^{12} - \left(\frac{\sigma}{r_{ij}} \right)^6 \right).$$
(2)

Here, r_{ij} is the distance between any pair of atoms *i* and *j*. The parameters ε and σ are, respectively, the depth of the potential wells and an effective atomic diameter. For both solid and liquid atoms, $\sigma = 0.35$ nm and $\varepsilon = k_B T$, where k_B is the Boltzmann constant and T = 33 K is the temperature. The pair potential is set to zero for $r_{ij} > 2.5\sigma$. The coupling parameter C_{AB} enables us to control the relative affinities between the different types of atoms and is given the value 1.0 for both L-L and S-S interactions but varied for S-L interactions in order to explore the influence of wettability on drop dynamics. Three values were selected: $C_{SL} = 0.7$, 0.8, and 0.9, yielding equilibrium contact angles 90°, 75°, and 55°, respectively.

The solid plate, which forms the bottom of the simulation box, comprises 69048 atoms arranged in a cubic lattice having three atomic layers with a lattice parameter $\lambda = 2^{1/6} \sigma \approx 0.393$ nm, i.e., the equilibrium distance given by the Lennard-Jones potential. To maintain rigidity, while permitting momentum exchange with the liquid, the solid atoms are allowed to vibrate thermally around their initial positions harmonic potential: by а strong $V_h(r) = 1000\epsilon |\mathbf{r} - \mathbf{r}^0|^2 / \sigma^2$, where *r* is the instantaneous position of a given solid atom and \mathbf{r}^0 is its initial lattice position.

The liquid is modelled as 5000 8-atom molecular chains, with adjacent atoms linked by a confining potential: $V_{conf} = \epsilon (r_{ij}/\sigma)^6$. This increases its viscosity compared with a monomer liquid and minimizes evaporation within the timescale of the simulation, so that the vapor phase is effectively a vacuum. The dimensions of the simulation box are L_x , L_y , $L_z = 107.6$, 33.0, 30.0 nm, respectively, with periodic boundary conditions imposed in the *x* and *y* directions. To

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investigate whether our results are independent of drop size, we also study a system comprising 10643 liquid molecules on a 3-layer cubic solid formed from 76608 atoms in a simulation box of dimensions L_x , L_y , $L_z = 88.0$, 44.7, 30.0 nm. The volumes of the smaller and larger liquid drops are $(2.081 \pm 0.003) \times 10^3$ nm³ and $(4.201 \pm 0.002) \times 10^3$ nm³, respectively, computed as the volumes of spheres fitted to the equilibrated surfaces of the drops before contact with the plate.

In order to compare our simulations with real, physical systems, all the atoms of both the liquid and the solid are given the mass of the carbon atom (12 g/mol). The simulated liquid has a density of $\rho_L = 18.26 \pm 0.07$ atoms/nm³, equivalent to 363.9 ± 1.4 kg/m³. Its surface tension is $\gamma_{LV} = (2.49 \pm 0.65)$ mN/m. This was found by an independent simulation of a free liquid film with planar surfaces from the integral of the difference between the normal and tangential pressures through the interface [40]. We have also performed a simulation of the bulk liquid with no interface to determine its viscosity $\eta_L = (0.249 \pm 0.004)$ mPa·s from the diffusion coefficient *D* via the Stokes-Einstein relation [41]. *D* is measured from the slope of the mean square displacement of liquid atoms versus time [42] and has the value (0.562 ± 0.021) nm²/ns. Over the range of our simulations the liquid remains Newtonian: all its properties, including its viscosity, are independent of the applied force and the velocity of the drop. Previous studies of Couette flow have also confirmed this [36].

In the simulation, Newton's equations of motion are solved using a 5th order Taylor expansion with a time step of 5 fs. The liquid molecules are initially distributed in a cubic lattice close to the plate and the entire system equilibrated using a thermostat based on velocity scaling for 10^6 time steps (5 ns). During this period, the liquid atoms rearrange to form an equilibrium droplet, as characterized by a stable contact angle and constant total energy. Once equilibrium has been

achieved, the thermostat is applied to the solid atoms only (to mimic an isothermal solid, as in a physical experiment) and we introduce an external force field in the *x* direction, parallel to the S-L interface and acting on each liquid atom: $F_0 = F_0 \hat{x}$, where \hat{x} is the unit vector in the *x* direction and F_0 is given one of 8 values from 0.83 to 6.64 fN. This causes the liquid drop to translate across the solid surface at a velocity that depends on both the strength of the field and the S-L coupling. The velocity attains a steady value well within the 5 × 10⁶ time steps (25 ns) allowed for this stage of the simulation. During this period, the drop also acquires constant overall dimensions and shape. Finally, we continue the simulation for another 5 × 10⁶ time steps, saving the positions of the liquid atoms at intervals of 10³ time steps. The resulting data enable statistical analysis of the sliding drops over 5 × 10³ saved configurations.

Molecular-dynamics modelling has the advantage over experiment that all the material properties and kinematic behaviors can be determined independently down to the molecular scale under a very wide range of conditions. This includes the degree to which a liquid droplet wets the solid and the way this may change when the droplet moves. In our simulations, wetting is controlled by the solid-liquid coupling C_{SL} . Figure 2 illustrates instantaneous (unaveraged) snapshots of a simulated drop for $C_{SL} = 0.7$, which yields an equilibrium contact angle θ^0 of 90°, and various values of the force defined by F_0 . The forces and the resulting motions are from left to right in the snapshots. The caption also gives the velocity of the drop's center of mass U_{cm} and the equivalent capillary number Ca = $\eta_L U_{cm}/\gamma_{LV}$. The drop shapes and their evolution closely resemble those seen in experiments [16–20,39,43]. As the drops are very small, F_0 has to be orders of magnitude greater than that caused by gravity to overcome the very large capillary forces generated as the drops slide and their configurations and contact angles change in response to the increasing velocity of the contact line. The velocities are also larger than for

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sliding raindrops, however the equivalent capillary numbers are realistic and not significantly larger than observed in experimental studies of forced wetting. We discuss these aspects of the study in more detail below.



Figure 2. Instantaneous snapshots for $C_{SL} = 0.7$. a) lateral and e) top view for $F_0 = 0.83$ fN, $U_{cm} = 2.7$ m/s, Ca = 0.27. b) lateral and f) top view for $F_0 = 1.66$ fN, $U_{cm} = 4.86$ m/s, Ca = 0.49. c) lateral and g) top view for $F_0 = 3.32$ fN, $U_{cm} = 9.9$ m/s, Ca = 0.99. d) lateral and h) top view for $F_0 = 4.98$ fN, $U_{cm} = 11.1$ m/s, Ca = 1.11.

3. Results and Discussion

3.1 Drop velocities and the shape of the contact line.

In order to analyze the dynamics of a sliding drop, we need to determine the location of the three-phase contact line, corresponding to the intersection of the liquid-vacuum interface with the solid surface. To compute this at all points around the drops, we refer the position vector of each liquid atom *i*, $r_i(t)$ to the location of the drop mass center at time *t*, $r_{cm}(t)$, i.e., $r'_i(t) = r_i(t) - r_{cm}(t)$. The liquid-vacuum interface may then be defined as the surface over which the local liquid density $\rho_L(r'_i, t)$ falls to half that of the bulk liquid (i.e., the equimolar surface). To

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measure the density $\rho_L(\dot{r}_u, t)$, we subdivide the available volume of the drop into cubic cells of size dx, dy, dz = 0.3 nm and calculate the average number of atoms per cell over 500 configurations at intervals of 10^3 time steps. More details are given in Supporting Information.

At equilibrium and in the absence of an external force, the contact line has circular geometry. When the external force is applied, it evolves into an elongated shape in the *x* direction as shown in Figure 2. Once the drop attains a steady regime, all points on the contact line move in the *x* direction at the same velocity with respect to the solid, and the shape of the drop remains constant. We measure the velocity and its standard deviation from linear fits to the displacement over time of sets of points, regularly spaced along the contact line. We also fit the displacement of the drop's center of mass to determine its velocity with respect to the solid surface U_{cm} . Figure 3 compares the velocity of points on the contact line and the center of mass as a function of F_0 for $C_{SL} = 0.7$. It is clear that the velocities are identical. Note that at $F_0 \sim 3.6$ fN the drop begins to elongate and its area of contact with the solid increases. The resulting increase in drag accounts for the change in slope and the intermediate dip in velocities. The possible significance of this transition is discussed later.



Figure 3. Velocities and corresponding capillary numbers Ca of the contact line U_{cl}^x and the drop's center of mass U_{cm} in the *x* direction versus the external force F_0 and the associated Bond number for $C_{SL} = 0.7$. The arrow marks the force at which the drop begins to elongate.

Raindrops typically have diameters in the range 0.5–5 mm [44]. However, the size of a drop that will begin to slide down a vertical windowpane depends on the wettability of the glass and the extent of static contact angle hysteresis. Sliding occurs when the gravitational force exceeds the capillary resistance caused by the difference between the advancing and receding contact angles, θ_A and θ_R , respectively. The gravitational force will scale as $\rho_L g l^3$, where g is the acceleration due to gravity and l is the characteristic size of the drop, whereas the capillary resistance will scale as $\gamma_{LV}(\cos\theta_R - \cos\theta_A)l$. Thus, for example, if $(\cos\theta_R - \cos\theta_A)$ is order 1, the drop will slide when the Bond number Bo = $\rho_L g l^2 / \gamma_{LV} > 1$, i.e., when l > 2.7 mm. Casual observation shows that raindrops of this size often slide, while those a little smaller may stick.

The Bond number scaling law will hold whatever the cause of the difference between θ_A and θ_R . For simulated Lennard-Jones liquids on an atomistically smooth solid surface, as in our study, there is no static hysteresis [1,39]. Therefore, drops will begin to slide as soon as a force is applied, but any consequent changes in the and advancing and receding *dynamic* contact angle will have a retarding effect which will increase with speed. Based on our previous simulations of dynamic wetting [e.g. 27,34-36], we know that the difference between the advancing and receding dynamic angles can exceed 90° for the range of velocities and capillary numbers depicted in Figure 3. Thus, the expected capillary resistance can easily be of order $\gamma_{LV}l$, which is ~ 50 pN for the approximately 20 nm drops used in our study. If we equate this to $\rho_L g_{eff} l^3$, where g_{eff} represents the effective acceleration supplied by our force, we find that the to achieve the sliding speeds observed a value of g_{eff} is ~ 2 × 10⁹g is required. During sliding, there will also be significant viscous dissipation, exacerbated by the elongation of the drop, and we may, therefore, expect the force required to maintain sliding to significantly exceed the capillary resistance alone. The mass of the smaller drop in our study is 7.97×10^{-22} kg, so for the range of velocities investigated, g_{eff} varies from 4.25 \times 10⁹g to 2.55 \times 10¹⁰g, which is consistent with the scaling estimate.

Such high values of g_{eff} required to maintain sliding are the inevitable result of the small size of the drops and the consequent increase in the ratio of the perimeter of the drop to its mass when compared with physical systems. They do not disqualify MD from being used to study the sliding phenomenon. Precisely because of the small physical scale of the systems that can be studied, MD provides a consistent approach to aspects of dynamic wetting not directly accessible by experiment, such as the local microscopic dynamic contact angle and the detailed shape of any trailing vertex. Further confidence in our results can be gained from the fact that our

simulations, and those of others, have proved entirely effective in recovering standard *macroscopic* laws such as the Young and Laplace equations [37,45–47]. Realistic behavior has also been seen for Poiseuille [48] and Couette flows [26,36]. Another way of comparing our simulations with the behavior of real drops is to consider the Bond numbers required to maintain sliding. In the example of the 2.7 mm raindrop given above, sliding commences when Bo > 1. In our simulations, for a 20 nm drop, 0.5 < Bo < 19 for $0.8 < F_0 < 6.64$ fN, as it can be seen in Fig. 3. The larger values arise because of the relatively low surface tension of our liquid.

3.2 Contact angles.

We determine the local contact angle at points from the slope of the plane tangent to the liquid interface at a set of points p_i spaced regularly along the contact line. The detailed procedure is described in Supporting Information. At equilibrium, the contact angle of the drop is the same at all points along the contact line: θ^0 . When the drop is moving, the dynamic contact angle θ^d depends on the velocity of the contact line normal to itself. Since this varies around the drop, having maximum and minimum values at the leading and trailing points on the *x* axis, but is zero at equatorial points, the dynamic contact angle should also vary, a result confirmed experimentally by Rio *et al.* [39].

Figure 4 depicts two examples of the variation of the local contact angle with x for $C_{SL} = 0.7$, corresponding to an equilibrium angle of 90°. The data are for the lowest and highest forces studied: $F_0 = 0.83$ and 4.98 fN. The inset figures delineate the actual shape of the contact line in each case. Also indicated are the coordinate systems and their origin, which is at the position of the mass center projected onto the same x-y plane. With $F_0 = 0.83$ fN (Figure 4a), the drop remains nearly circular and the contact angle increases, nearly monotonically, from a minimum value at the trailing end of the drop to a maximum value at the leading edge, exhibiting its

equilibrium value at the mid-point, where the normal velocity is zero. With $F_0 = 4.98$ fN (Figure 4b), the larger external force induces much greater deformation of the drop, stretching it and inducing to a nearly parallel section, where the contact angle is equal to 90° and, therefore, identical with that of a drop at rest.



Figure 4. Local contact angle versus x for $C_{SL} = 0.7$. a) $F_0 = 0.83$ fN. b) $F_0 = 4.98$ fN. The inset figures show the corresponding shape of the contact line, the coordinate system and its origin.

3.3 Contact-line velocities.

As we have seen, once the drop has reached a steady state under the influence of the applied force, all points p_i on the contact line move in the x direction relative to the solid surface at the

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same velocity as the center of mass U_{cm} . However, the velocities normal to the contact line vary with position. If the unit vector normal to the contact line at point p_i is $\hat{n}(p_i)$ the normal component of the contact-line velocity is the projection of U_{cm} onto $\hat{n}(p_i)$:

$$\boldsymbol{U_{cl}}(p_i) = U_{cm} \big(\boldsymbol{\hat{x}} \cdot \boldsymbol{\hat{n}}(p_i) \big) \boldsymbol{\hat{n}}(p_i) = U_{cl} \boldsymbol{\hat{n}}(p_i).$$
(3)

At the leading and trailing points of the drop p_f and p_r , respectively, (see Figure 2 in Supporting Information) the normal vectors are $\hat{n}(p_f) = \hat{x}$ and $\hat{n}(p_r) = -\hat{x}$, and the contact-line velocity attains its maximum and minimum values, $U_{cl}(p_f) = U_{cl}^{max} = U_{cm}\hat{x}$ and $U_{cl}(p_r) = U_{cl}^{min} = -U_{cm}\hat{x}$, respectively.

In order to compare our results directly with the experiments of Rio *et al.* [39] for silicone oil on fluoropolymer treated glass, we may cast our equations in terms of the slope angle of the contact line ϕ with respect to the direction of travel:

$$U_{cm}\sin\phi = U_{cm}(\hat{\boldsymbol{x}}\cdot\hat{\boldsymbol{n}}(p_i)). \tag{4}$$

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In Figure 5, we plot the dynamic contact angle θ^d versus $U_{cm}\sin\phi$ and Ca sin ϕ at multiple points around the moving drop for $C_{SL} = 0.7$ and all 8 values of F_0 . The contact angles are computed in the same way as described for Figure 4. (See Supporting Information). As we can see, it is possible to determine a wide range of dynamic contact angles from a single sliding drop, which is a great advantage, both theoretically and experimentally. Significantly for our understanding of dynamic contact angles, all the points lie close to a single line irrespective of F_0 , indicating a common mechanism. The general trend is very like that reported by Rio *et al.* [39] and Le Grand *et al.* [18], but without the discontinuity caused by the contact angle hysteresis present in their experimental system. Another difference is that our results span a significantly wider range of capillary numbers than those observed in the silicone oil experiments (\pm 1, compared with \pm 0.01) for a comparable range of dynamic contact angles. The range is, however, very similar to that observed previously in comparable simulations of forced wetting and spreading nanodrops [34-36].



Figure 5. Dynamic contact angle θ^d versus $U_{cm}\sin\phi$ and Ca $\sin\phi$ at multiple points around the contact line for $C_{SL} = 0.7$ and all 8 values of F_0 investigated. As shown in the inset, ϕ is the angle between the direction of drop travel and the tangent to the contact-line at each point p_i .

3.4 Flow within the drop.

To determine the details of the flow within the sliding drop, we compute the mean local velocity of the liquid within each of the cubic cells used to determine the local density. We take two successive saved configurations at times $t = t_0$ and $t_0 + \Delta t$. Particle *i*, which at time t_0 is at $r_i(t_0)$ in cell c_l moves to $r_i(t_0 + \Delta t)$ in cell c_m . The velocity of this particle is then

 $u_i = (r_i(t_0 + \Delta t) - r_i(t_0))/\Delta t$, which is ascribed to both cells c_i and c_m . This procedure is carried out for all the liquid atoms in the drop and all saved configurations separated by Δt . Thus, we can generate the mean local velocity in each cell and its standard deviation. The value of Δt is chosen to ensure that the displacement of the atoms is not greater than the distance to the next adjacent cell, which maximizes our resolution. Time intervals of $\Delta t = 200$, 300 and 500 time steps were trialed, which yielded no significant difference in the resulting velocities. Once the local velocities have been established, the complete flow pattern can be constructed.

To visualize this, we first consider the flow within the frame of reference of the drop, i.e., referenced to its center of mass. Figure 6a shows the flow of the first layer of liquid atoms in contact with the solid for $C_{SL} = 0.7$ and $F_0 = 3.32$ fN, where the color indicates the x component of the velocity. A negative value shows that the liquid moves to the left in the figure, as does the solid surface in this frame. In all the simulations, there is at least one point on the contact line where the tangent is parallel to the x axis ($= 0^{\circ}$) and the normal velocity of the contact line is zero. Here, the contact angle should have its equilibrium value, as confirmed in Figure 4a and seen in experiments [39]. The flow in the x-z plane, bisecting the drop and passing through its center of mass is illustrated in Figure 6b for $C_{SL} = 0.7$ and $F_0 = 4.98$ fN. In this case, the color indicates the z component of the velocity and confirms that the drop does not slide but rolls about a stagnation point at its center of mass. However, as can be seen by close inspection of Figure 6a, the flow within the drop, including that within the first layer, is slower than the translational velocity of the solid surface in the same frame, $-U_{cm}$. In other words, there is slip between the first layer of liquid molecules and the solid. The presence of slip in MD simulations of solid-liquid interfaces has been noted since the earliest studies [23–26] and has been

investigated in its own right [49,50]. We explore its ramifications to our simulations of sliding drops in the next section.



Figure 6. Flow diagrams for $C_{SL} = 0.7$, $F_0 = 3.32$ fN, and solid velocity $U_S = -U_{cm} = 9.3 \pm 0.2$ m/s. The force F_0 acts from left to right in the images. a) flow in the first layer of liquid in contact with the solid. b) flow in the *x*-*z* plane at the center of the drop. c) the same drop as in a), but now with the velocities referenced to the frame of the solid. d) residual flow when we subtract the local slip velocities in c). e) flow pattern observed in the experiments of Rio *et al.*

[39]. In a), c), and d), the color represents the x component of the liquid velocity; in b) the color represents the z component of the liquid velocity.

3.5 Slip and contact-line friction.

To quantify the slip between the liquid and the solid, we compare the velocity of the solid surface relative to the drop, $U_S = -U_{cm}$, with that of the first layer of liquid atoms in the central region of the solid-liquid interface, away from the influence of the contact line. We compute the velocity of the first layer as follows. We divide the liquid in the *z* direction into arbitrary slices of thickness z = 2 nm parallel to the liquid-solid interface. In the central region, the average velocity of the liquid across the center of each slice is $U_c = U_c \hat{x}$, where the modulus of U_c is constant but depends linearly on *z*: $U_c = U_c(z)$. If we define $U_{c,S}$ as value of $U_c(z)$) extrapolated to the solid surface located at z_S , i.e., $U_{c,S} = U_c(z_S)$, the slip velocity in the *x* direction with respect to the solid at the center of the S-L interface is $U_{slip} = U_S - U_{c,S}$. A similar procedure was used in an earlier paper on forced wetting [36]. In Figure 7, we plot the computed value of U_{slip} against F_0 for the three liquid-solid couplings used in the simulations, and we can see that the slip velocity increases with the external force, but decreases with increased coupling, as expected based on current understanding.

To visualize slip and its consequences more directly, Figure 6c, shows the same drop as in 6a, but now with the velocities referenced to the frame of the solid. We see that all the flow is in the direction of the applied force, with the highest velocities at the leading and trailing boundaries where slip is greatest and the velocity is the same as that of the center of mass. However, if we subtract the local slip velocities then a different picture emerges, as revealed in Figure 6d. Now, the flow in the center of the drop is stationary and all the velocities at the edges of the drop are

normal to the contact line. This nanoscale flow is consistent with the macroscopic flow observed in the experiments of Rio *et al.* [39] for a physical system, as shown in Figure 6e. Thus, it would appear that for a sliding drop the asymptotic macroscopic flow pattern persists down to the contact line. Note that in figure 6e the arrow vectors refer to the velocities at the upper surface of the drop rather than at the solid surface. As the contact line is approached this distinction becomes irrelevant.



Figure 7. Slip velocity in the central region of the drop U_{slip} versus F_0 for the different S-L couplings C_{sL} considered. The dashed lines are linear fits.

As discussed below, slip has a significant effect on the dynamics of the contact line. However, slip in the x direction will affect the normal velocity of the contact line differently according to the peripheral position around the drop, i.e., it will vary with . Hence, the effect will be a maximum at the front and rear of the drop at points p_f and p_r , where $= 90^\circ$ and -90° , respectively, but will be zero at intermediate points where = 0. To determine the local effect at each point p_i around the drop, we first compute $U_{c,s}(p_i)$ defined as the velocity, in the frame of the drop, of the first layer of liquid at the center of the S-L interface $U_{c,S}\hat{x}$ projected over the normal to the contact line at point p_i , $\hat{n}(p_i)$; i.e., $U_{c,S}(p_i) = U_{c,S}(\hat{x} \cdot \hat{n}(p_i)) = U_{c,S}(p_i)\hat{n}(p_i) = U_{c,S}(p_i)\hat{n}(p_i)$. Thus, the local slip velocity normal to the contact line will be

$$\boldsymbol{U_{slip}}(p_i) = U_{slip}(p_i)\boldsymbol{\widehat{n}}(p_i) = -\left(U_{cl}(p_i) + U_{c,s}(p_i)\right)\boldsymbol{\widehat{n}}(p_i).$$
(5)

Our previous MD studies of dynamic wetting [27,31,32,34–36], and those of others [28-30,33,37,38] have shown that at the scale of the simulations the dominant cause of the velocitydependence of the contact angle is contact-line friction due to the interaction of the liquid molecules with the potential energy landscape of the solid surface. Many of these studies have also shown that the molecular-kinetic theory (MKT) of Blake and Haynes [51], further developed by Blake [52] and Blake and De Coninck [53], provides a good model for the underlying mechanism. According to the MKT, there is a direct relationship between the velocity of the contact line normal to itself $U_{cl}(p_i)$ and the unbalanced surface tension force $\gamma_{LV}(\cos\theta^0 - \cos\theta^d)$ that arises when the dynamic contact angle θ^d deviates from its equilibrium value θ^0 . If the surface tension is low and/or the interactions with the substrate fairly weak, as in our simulations, the MKT reduces to a simple linear relation that can be applied at each point p_i along the contact line:

$$U_{cl}(p_i)\widehat{\boldsymbol{n}}(p_i) = \gamma_{LV}(\cos\theta^0 - \cos\theta^d) / \xi \,\widehat{\boldsymbol{n}}(p_i), \tag{6}$$

where ξ (Pa·s) is the coefficient of contact-line friction per unit length of the contact line. Since $U_{cl}(p_i)$ varies with position around the drop, the local dynamic contact angle θ^d must also vary.

In a recent MD study of forced wetting [36], we have shown that the propensity towards slip between the liquid and the solid has a strong influence on the relationship between the microscopic dynamic contact angle and contact-line velocity. The effective contact-line velocity is reduced by the local slip velocity normal to the contact line: $U_{cl}^{eff}(p_i) = U_{cl}(p_i) - U_{slip}(p_i)$. It follows from Eq. (5) that

$$\left(U_{cl}(p_i) - U_{slip}(p_i)\right)\widehat{\boldsymbol{n}}(p_i) = \gamma_{LV}(\cos\theta^0 - \cos\theta^d)/\xi\,\widehat{\boldsymbol{n}}(p_i).$$
(7)

To compute the relevant slip velocities, we take the mean of the velocity of the first layer of liquid across the center of the liquid-solid interface and that at the contact line. This provides a good estimate of the slip velocity within the small but finite three-phase zone, which constitutes the contact line at the molecular scale [36].



Figure 8. Unbalanced surface tension force $\gamma_{LV}(\cos\theta^0 - \cos\theta^d)$ versus the effective contactline velocity U_{cl}^{eff} for each value of the external force F_0 . a) $C_{SL} = 0.7$ (data for small and large drops). b) $C_{SL} = 0.8$. c) $C_{SL} = 0.9$. The dashed lines indicate the slope of data obtained from simulations of spreading drops at the same S-L couplings [35].

Once we have established the local contact angles and effective contact-line velocities at multiple points around the moving drops (using the bins as described Supporting Information), we can use Eq. (7) to calculate the contact-line friction. In each case, the data fall on an acceptably straight line, from the slope of which we can determine ξ . In Figure 8, we plot our results for each solid-liquid coupling $C_{SL} = 0.7, 0.8$, and 0.9 versus the external force F_0 . As confirmed by the dashed lines in Figures 8 and 9a, the coefficients of contact line friction are consistent with those found in previous MD simulations of spontaneous spreading of liquid drops with the same C_{SL} values [35]. Perhaps the most interesting result is that over the range studied, the contact-line frictions are independent of the external force, and since the contact-line velocities are measured around the entire circumference of the drop, independent of the local slope and curvature of the contact line, i.e., they appear to be material properties of the system, as envisaged by the MKT. Figures 8a and 9a contain the results obtained from the two drop sizes studied (comprising 5000 and 10643 8-atom molecular chains); thus, it would appear that the results are not size-dependent at this scale. Indeed, apart from the strength of the liquid-solid interaction, the only factor that affects the dynamic contact angle is the effective velocity of the contact line normal to itself. A corollary of this result is that if we know the advancing and receding dynamic contact angles at the front and rear of the drop, we can predict the angles at all other points around the drop where the local normal contact-line velocity will be given by $U_{cm}\sin\phi$.



Figure 9. a) Contact-line friction coefficient versus the external force F_0 for the three values of C_{SL} and the two drop sizes investigated. The dashed lines represent the value of the friction coefficient obtained from simulations of spontaneous spreading [35]. b) Apparent friction coefficient ξ^{app} computed from the simulations without considering the effect of slip. Here, the dashed lines represent the average values of the apparent friction coefficient for all values of the external force.

As shown in Figure 9b, were we not to take account of the slip in our system, i.e., if we were to use Eq. (6) instead of (7), then we would compute apparent friction coefficients ξ^{app}

significantly lower than those observed in the simulations of droplet spreading. As argued previously [36], the reduction in apparent contact-line friction due to slip induced by the flow is ultimately because both share the same underlying mechanism, namely the dynamic interaction of the liquid molecules with the energy landscape of the solid surface. The weaker this interaction, the smaller the friction and the greater the slip. And the greater the slip, the weaker the velocity-dependence of the contact angle. As also pointed out, the reduced apparent friction is a possible source of so-called hydrodynamic assist, whereby liquid coating speeds can be increased substantially by manipulating the coating flows to avoid air entrainment that follows when the dynamic contact angle approaches 180°.

3.6 Pearling.

Up to this point, we have considered primarily drops that maintain a simple oval shape. However, as the external force is increased, the droplet becomes elongated in the direction of travel: Figures 2d and 2h. If the force is increased still further, then a neck develops between the front and rear of the drop, which begins to separate into two distinct regions with separate circulation patterns and an intermediate stagnation zone, as shown in Figures 10a and b. We do not see a sharp angle at the trailing edge (there is no corner or "cusp") at the nanoscale. We therefore suggest that the separation and the inception of the intermediate stagnation zone provides the microscopic details of the pearling mechanism, i.e., the shedding of droplets, which is seen at sufficiently high sliding speeds with real macroscopic drops and liquid entrainment on partially wetted surfaces. If this is the case, then it is helpful to understand at what microscopic receding contact angle this dynamic wetting transition occurs.

The flow patterns shown in Figure 10 reveal rapid changes in velocity within the tail of the drop, characteristic of high shear stresses. Since one of the factors that determine this geometry

is the local dynamic contact angle, which we have shown to be velocity dependent, it is of interest to know how its limiting receding value evolves with F_0 and liquid-solid affinity.



Figure 10. Flow diagrams for $C_{SL} = 0.9$ and $F_0 = 3.32$ fN showing the development of a neck. a) Flow in the lateral *x-z* plane along the axis of the drop. The color represents the *z* component of the liquid velocity. b) Flow in the first layer of liquid in contact with the solid. Here, the color represents the *x* component of the liquid velocity.

Strong affinity leads to a small equilibrium angle and a high friction, but other factors, such as liquid viscosity, also enhance friction [49,50]. Thus, in principle, one may have a high friction, but still be in the partially wetting regime. If the friction were sufficiently high, the local dynamic contact angle might approach zero, leading inevitably to the entrainment of a liquid film; whereas, if the contact-line friction were comparatively small, the local angle at which the viscous stresses became dominant would be finite and potentially large, as seen here. One might consider the two outcomes as, respectively, second-order (i.e., continuous) and first-order

dynamic wetting transitions in terms of the way in which the surface free energy of the system evolves with velocity. However, this requires further investigation.

Figure 11a, illustrates the way in which the receding contact angle at the back of the drop varies with the applied force for the three couplings studied. In each case, we see that beyond a certain point (indicated by an arrow), which coincides with the appearance of a neck, the contact angle remains essentially constant at what we interpret to be the critical local dynamic contact angle for a pearling transition. Beyond this transition, the elongation of the drop simply becomes more pronounced as F_0 is increased. This is illustrated in the plots of drop length *L* versus F_0 in Figure 11b. The same transition is also seen in the plot of velocity versus F_0 in Figure_3. Presumably, at still higher driving forces, the drop would eventually bifurcate, but our computational resources were insufficient to explore this.



Figure 11. a) Dependence on F_0 of the receding contact angle measured along the *x* axis. b) Length of drop *L* versus F_0 . The arrows show the point at which a neck appears.

In our simulations we measure the local contact angle and find that its value is highly dependent on the velocity of the contact line. In theoretical investigations of the pearling transition [2,3,5,16,18,54] this local angle is usually taken to be the equilibrium angle and invariant, contrary to what we have observed. In experiments, the contact angles are apparent angles measured with a resolution of a few microns, at a scale greater than that at which viscous bending occurs. The local angle can only be inferred. We have the opposite limitation. We can

measure the local dynamic angle, but since we see no evidence of viscous bending at the scale of our simulation, can only infer what effect this will have on the apparent angle at greater scales. Further progress requires either much larger simulations or multi-scale modelling. Thus far, our simulations have revealed only forced wetting transitions at finite local angles; but it would certainly be of interest to investigate the effect of stronger S-L couplings and contact-line frictions, which would drive the system towards smaller dynamic contact angles.

4. Conclusions

We have performed large-scale molecular-dynamics simulations of nanoscopic liquid drops moving steadily across a flat solid surface under the influence of a uniform external force field acting parallel to the liquid-solid interface. Three different liquid-solid affinities and two drop sizes have been studied at 8 values of the external force F_0 . The simulations enable us to extract the velocity of the contact line normal to itself and the local, microscopic dynamic contact angle at all points around the drop. In contradiction to the assumptions of existing theoretical models of sliding drops [2,3,5,16,18,54], we find that the local contact angle measured at this scale varies continuously, from a maximum advancing angle at the front of the drop to a minimum receding angle at the rear.

Nevertheless, our results confirm the experimental observation [1,39] that the contact angle is given by some function of the local contact-line velocity in the normal direction $U_{cm}\sin\phi$, where U_{cm} is the velocity of the drop and ϕ is the slope of the contact line with respect to the direction of travel. We also show that this velocity-dependence can be modelled by the molecular-kinetic theory. A complication is that the simulated drops exhibit slip between the first layer of liquid molecules and the solid surface. However, once the effects of this are included, the contact-line frictions recovered are identical with those found in previous MD studies of spontaneously

spreading drops. Moreover, despite the small scale of the simulations, flow within the drop with respect to the solid surface is consistent with that observed by Rio *et al.* [39] and Le Grand *et al.* [18] in macroscopic experiments.

If the external force is increased beyond a certain value then the nanodrop elongates, its velocity increases more slowly with F_0 and a neck appears between the front and rear of the drop, which separates into two distinct zones. We suggest that this indicates the nanoscale mechanism of the pearling transition at the tip of a macroscopic drop. While the receding contact angle at this hydrodynamic transition is far removed from its equilibrium value, it is greater than zero and approaches a more-or-less constant value as the transition progresses. It would appear that this angle provides a system-specific critical condition for pearling. We conclude, therefore, that any complete theory of dynamic wetting transitions and associated avoided critical behavior at any scale should consider the impact of a velocity-dependent local microscopic contact angle.

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Supporting Information

S1. Finding the density and position of the liquid-vacuum interface.

To calculate the density of the liquid for each position vector $\rho_L r_i(t)$, we subdivide the available volume of the drop into cubic cells of size dx, dy, dz = 0.3 nm and calculate the average number of atoms per cell over 500 configurations at intervals of 10^3 time steps. From these we extract 10 independent density profiles, which we use to establish the location of the interface, the position of the contact line, the local contact angles, and the associated errors. The drop is sliced into k layers parallel to the L-S interface, as shown in Figure S1a. The density in each slice depends on the x-y coordinates; therefore, we decompose the slices into bins perpendicular to the x axis, as indicated in Figure S1b and compute the density profile along the y coordinate. A typical example is shown in Figure S1c. Finally, this profile is split into two

symmetrical regions about the x axis and we fit sigmoidal functions to determine the position of the interface where the density falls to half that of the bulk liquid. This is done for each slice in the z direction to locate the complete liquid-vacuum interface.



Figure S1. a) Density map profile for $C_{SL} = 0.7$ and $F_0 = 3.3$ fN computed in the *x-z* plane which cuts the mass center of the drop. The region contained between the two parallel lines represents an arbitrary layer *k*. b) Density map of the selected *k*-layer in a) in the *x-y* plane. c) Density profile versus *y*, together with the fit and the interface location (marked with crosses) of the selected bin *j* of b).

S2. Measuring the local contact angle.

We determine the local contact angle from the slope of the plane tangent to the liquid-vacuum interface at a set of points p_i spaced regularly along the contact line. The first step is to establish the normal to the contact line at each point $p_i = (x_i, y_i)$, which is defined by $y = y_i - (x - x_i)/f'(x_i)$, and we approximate the derivative by $f'(x_i) \approx (y_{i+1} - y_{i-1})/(x_{i+1} - x_{i-1})$.

Next, we calculate the point of intersection of this normal with the *x*-*y* projection of the liquidvacuum interface obtained from the *k* slices along *z*, $(z_1, z_2, ..., z_k)$, as shown in Figure S2a. The normal at each point p_i on the contact line intersects the projection of each layer *k* at $p_k = (x_k, y_k, z_k)$ and the interfacial profile is given by z_k as a function of the distance in the *x*-*y* base plane $r = \sqrt{(x_i - x_k)^2 + (y_i - y_k)^2}$. Finally, a circular arc is fitted to the profile omitting the first two layers of atoms in contact with the solid, as illustrated in Figure S2b, and we measure the contact angle as the tangent to this arc at its intersection with the solid. The mean value and standard deviation of each contact angle is calculated by repeating this procedure for the 10 density profiles determined as described above.



Figure S2. a) Calculation of the normal to the contact line at the point p_i and its intersection with the projection of the L-V interface for a sequence of layers on the base plane. b) Interfacial profile computed along the normal shown in a) and its circular fit to give the local dynamic contact angle $\theta^d(p_i)$.