Comprehensive thermodynamic study of the calcium sulfate-water vapor system. Part 1: Experimental measurements and phase equilibria.

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ABSTRACT

The calcium sulfate-water vapor system is of great scientific and technological importance due to its applications in several fields such as the construction materials industry, geology, and planetary sciences. While much effort has been consecrated during the past decades in characterizing the crystallographic structure of the different calcium sulfate polymorphs, some questions concerning their thermodynamic aspects as phase equilibria and their capability to increase their overall water content continuously beyond structural water content seem to have been left aside. Nevertheless, the comprehension of these aspects is of the utmost importance if we want to understand this chemical system fully. The present two-part work investigates these phenomena experimentally and by a thermodynamic modeling approach. In this first part, we develop a rigorous experimental protocol by thermogravimetric analysis under controlled temperature and water vapor partial pressure. We use this protocol to obtain thermodynamic equilibrium values for the overall water content of calcium sulfate hydrates. To ensure that the equilibrium was reached, we verified that these values could be obtained by distinct thermodynamic paths. With the equilibrium data, we were able to propose an updated equilibrium curve between phases AIII- CaSO_4 and $\text{CaSO}_4 \cdot 0.5\text{H}_2\text{O}$ and estimate the thermodynamic parameters $\Delta_r H^\circ = (35.5 \pm 1.0) \text{ kJ} \cdot \text{mol}^{-1}$ and $\Delta_r S^\circ = (80.0 \pm 2.8) \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$. After that, we were able to quantify the extent of water adsorption as a function of $(T, P_{\text{H}_2\text{O}})$, and we observed that it could represent a significant part of the overall water content of calcium sulfates.

KEYWORDS

adsorption, thermodynamics, phase equilibrium, calcium sulfate

1. Introduction

The chemical system composed by calcium sulfate and water is of paramount relevance for several industrial, technological, and scientific domains. Gypsum, the mineralogical term for the material mainly constituted of calcium sulfate dihydrate (DH, $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$), has extensive annual production and is mostly used in plaster (material mainly constituted of calcium sulfate hemihydrate, HH, $\text{CaSO}_4 \cdot 0.5\text{H}_2\text{O}$), and cement industries.¹⁻³ Apart from that, due to the high abundance of calcium sulfate on Earth's crust, calcium sulfates transformations are linked to several geological processes.^{4,5} Recent discoveries of calcium sulfate in Mars also inspired research about the transformations within the $\text{CaSO}_4\text{-H}_2\text{O}$ system.⁶⁻⁹

One recurrent area in $\text{CaSO}_4\text{-H}_2\text{O}$ system research concerns the quantity of water contained by calcium sulfates obtained from the dehydration reaction of gypsum and the determination of their structural water content. A considerably large amount of work has been dedicated to these issues. Many authors wrote extensive reviews on these points as, for example, Bezou¹⁰, Freyer and Voigt¹¹, Christensen et al.^{12,13}, Ballirano¹⁴, and Schmidt et al.¹⁵. Calcium sulfate dihydrate dehydrates to hemihydrate or anhydrite (CaSO_4) depending on temperature and humidity conditions. The hemihydrate prepared by this technique is normally referred to as β -hemihydrate ($\beta\text{-HH}$). There is also another kind of hemihydrate normally obtained by hydrothermal conditions and identified as α -hemihydrate ($\alpha\text{-HH}$). These forms of hemihydrate show some differences in their properties due to their microstructure, but they are considered to be chemically identical due to their similar X-ray powder diffraction pattern.^{1,16,17} The hemihydrate has also been reported to increase its structural water content to form a higher hydrate of the form $\text{CaSO}_4 \cdot 0.625\text{H}_2\text{O}$ (0.625-H).¹⁵ Three kinds of anhydrites have been reported: soluble anhydrite (AIII- CaSO_4), insoluble anhydrite (AII- CaSO_4), and anhydrite I (AI- CaSO_4). AIII- CaSO_4 is known to be unstable

and hydrate back to hemihydrate under atmospheric conditions. AII-CaSO₄ is produced by placing AIII-CaSO₄ under temperature conditions superior to 350°C and takes a long time to hydrate back to DH when mixed with liquid water. AI-CaSO₄ is less present in the literature and was reported to be stable for temperature values superior to 1180°C.^{18,19}

However, for a long time the phases HH, AIII-CaSO₄ and 0.625-H were thought to belong to the same crystalline phase, and the system was thought to be bivariant. That is, the crystalline water content of the compounds could vary continuously with temperature and water vapor pressure without any change in their crystalline system (e.g., this effect was recently observed for MgSO₄ hydrates.)²⁰ Discussions about the accuracy of this interpretation of the CaSO₄-H₂O system is found in several works as, for instance, the reviews presented by Posnjak²¹ or Ramsdell and Partridge²². We can also find the works from Gardet et al.²³ and Soustelle et al.²⁴ that reported calcium sulfate hydrates of the form CaSO₄ · εH₂O for which the water content would vary in the interval $0 \leq \varepsilon \leq 0.67$ depending on two intensive parameters: temperature and water vapor pressure. According to their interpretation of crystallographic data, they concluded that this variation in water content would take place without any change in the crystalline phase and that the system was bivariant. Bunn²⁵ also measured the overall water content in calcium sulfate hydrates up to $\varepsilon = 0.67$. Water vapor sorption studies carried out by Gregg and Willing²⁶ also showed a change in water retention of calcium sulfate hydrates with temperature and relative humidity. Published works from Bezou et al.¹⁰, Christensen et al.¹², Weiss and Bräu²⁷, and Schmidt et al.¹⁵ list a series of studies for which calcium sulfates can show water contents in the interval of $0 \leq \varepsilon \leq 0.8$. Currently, however, after an extensive number of studies in the characterization of calcium sulfate polymorphs, the existence of at least six distinct calcium sulfate polymorphs seems to be acknowledged in the scientific literature: dihydrate (DH, CaSO₄ · 2H₂O), hemihydrate (α-

and β -HH are identical), soluble anhydrite (AIII- CaSO_4), insoluble anhydrite (AII- CaSO_4), anhydrite I (AI- CaSO_4) and a higher hydrate “0.625-hydrate” (0.625-H , $\text{CaSO}_4 \cdot 0.625\text{H}_2\text{O}$). Therefore, the structural or crystalline water content of calcium sulfate obtained from gypsum calcination can be 0, 0.5, or 0.625 mol H_2O /mol CaSO_4 .^{15,27–30} Moreover, the transitions between these forms were shown to be univariant, and Bezou et al. reported thermogravimetric curves showing considerable overall water content variation in calcium sulfates (beyond the crystalline water content) caused by water vapor adsorption.^{29,31}

Overall, we can retain that a considerable amount of effort has been dedicated to the identification of the crystallographic forms of calcium sulfate hydrates so far. As a consequence, one can find considerably reliable data regarding the nature of the crystalline phases of these compounds. On the other hand, to the authors’ knowledge, no rigorous quantitative analysis of the water vapor adsorption on calcium sulfate hydrates has yet been published to complement the current state-of-the-art knowledge of crystalline forms of calcium sulfate. The unawareness of the extent of the water adsorption phenomenon can be problematic for several applications. For example, measuring the mass of a calcium sulfate without taking into account the adsorbed water content, this could bring important errors depending on the magnitude of the adsorption phenomenon. Moreover, simple operations such as storing calcium sulfate hydrates for later use can also compromise the nature of the material if parameters such as temperature and water vapor pressure are not controlled.^{15,32,33}

In this context, the present work aims at providing a quantitative investigation concerning the behavior of water vapor adsorption on calcium sulfates polymorphs obtained from the dehydration of synthetic and highly pure $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$. For this reason, we separated the work in two parts. The first part presents an experimental technique to study water sorption by the use of isothermal

and isobaric thermogravimetric analysis. We employed this method at atmospheric pressure to verify the extent of the water adsorption phenomenon and to quantify the adsorbed water content for calcium sulfate hydrates. We also discuss the thermodynamic variance of the system and perform phase equilibrium calculation. The second part of the present study is dedicated to the thermodynamic modeling of the water adsorption phenomenon.

2. Materials and Methods

The source of calcium sulfate for this work was a synthetic calcium sulfate dihydrate powder with high purity (Sigma-Aldrich, reagent grade, purity > 99.9%). We sieved this material and retained the fraction between 20 μm - and 50 μm -mesh.

2.1. Phase and chemical composition analyses. Powder X-ray Diffraction (XRD) pattern for the initial sample was measured in the range $5^\circ \leq 2\theta \leq 40^\circ$ using a diffractometer (Bruker-Siemens D5000) with monochromatic Cu – K_α radiation ($\lambda = 1.5406 \text{ \AA}$) and a scan time of 2.5 s. The experimental diffraction pattern was compared to the calcium sulfate dihydrate pattern (JCPDS 33-0311) to verify the phase purity of the initial sample.

The elemental composition of the initial sample was also evaluated to verify the purity of the sample by Inductive Coupled Plasma Mass Spectrometry (ICP-MS, JY 138 Ultrac, ISA Jobin Yvon).

2.2. Thermogravimetric analysis (TGA) protocols. To investigate the interaction between water vapor and calcium sulfate, we performed thermo- gravimetric analysis (TGA) experiments under isothermal and isobaric conditions. We used a high- performance symmetrical thermobalance (TAG 16, Setaram) instrumented for low-temperature experiments. We carried out the experiments under atmospheric pressure with a constant flowing mixture of dry Helium and

water vapor (50 cm³/min). The thermobalance has two parallel furnaces in which we place at the same time and under the same conditions one empty crucible (reference) and another crucible filled with the sample. Therefore, this dual furnace apparatus prevents buoyancy effect perturbations and the total carrier gas flow rate is divided equally between these two furnaces (25 cm³/min each). The choice of working with a Helium- atmosphere is due to the advantageous thermal properties of this gas (such as the thermal conductivity that is about eight times superior to the value for Argon and about six times superior to the values for nitrogen and air³⁴). This significantly reduces perturbations in the mass signal during the temperature program. We controlled the humidity of the gas stream by connecting an automated humidity generator (Wetsys, Setaram) to the entry of the thermobalance. The water vapor pressure in this work is represented by P_{H_2O} and corresponds to water vapor partial pressure values. The thermobalance's precision is of 10⁻³ mg. We used quantities between 5 and 12 mg of powder for the experiments. The sample holder was a quartz crucible with a diameter of 9 mm and with a fritted glass bottom. The fritted glass bottom is porous and lets the gas both pass through and be in contact with the lower part of the powder bed. The quantity of powder was sufficiently reduced so that the sample was dispersed in the crucible's fritted bottom without the formation of a thick layer, minimizing the impact of heat and mass transfer.

We employed two experimental protocols to obtain thermodynamic equilibrium points for different water vapor partial pressure (P_{H_2O}) and temperature (T) conditions. The first employed protocol consisted of keeping a constant value of T and using stepwise P_{H_2O} values.

Figure 1(a) shows one example of this protocol for increasing values of P_{H_2O} . We also employed decreasing stepwise values of P_{H_2O} in some experiments. The second protocol consisted of maintaining a constant value of P_{H_2O} and performing stepwise T values.

Figure 1(b) shows an example of this protocol using increasing T values. Similarly as for the first protocol, we also performed experiments for decreasing stepwise T. Therefore, we can consider experiments carried out under constant T and stepwise $P_{\text{H}_2\text{O}}$ as obtained by protocol (a), and experiments carried out under constant $P_{\text{H}_2\text{O}}$ and stepwise T as obtained by protocol (b). For both protocols, the samples of calcium sulfate dihydrate were initially fully dehydrated towards the AIII- CaSO_4 phase at 200°C at dry carrier gas conditions to establish a repeatable initial state for the experiments. To determine whether the equilibrium was reached, we waited until the stabilization of the mass signal for each pair $(T, P_{\text{H}_2\text{O}})$. The use of different protocols with different thermodynamic paths has the objective to ensure these mass values corresponded to the equilibrium values. The equilibrium was then reached by different thermodynamic paths, and the obtained mass values were compared. The experiments were carried for $5 \text{ hPa} \leq P_{\text{H}_2\text{O}} \leq 60 \text{ hPa}$ and for $34^\circ\text{C} \leq T \leq 250^\circ\text{C}$. However, due to water condensation limitations (due to the existence of cold spots within the experimental apparatus), it was not possible to obtain mass values at equilibrium conditions for the highest $P_{\text{H}_2\text{O}}$ and the lowest T values combined.

Figure 1. Schematic representation of the experimental protocols for (a) stepwise water vapor partial pressure and (b) stepwise temperature.

2.3. Characterization of samples textural properties. The textural properties of three sets of samples were analyzed. The first set was composed by the initial sample. The second set was prepared by dehydrating this sample at 200°C (to repeat the first dehydration step employed for the TGA protocol) under dry Argon stream (10 L/h) using a horizontal tubular furnace (Carbolite). The third set was prepared in two steps: (i) dehydration of the initial calcium sulfate powder at 200°C under dry Argon stream (10 L/h) and (ii) hydration of the powder at 50°C and humid Argon stream (10 L/h, $10 \text{ hPa} \leq P_{\text{H}_2\text{O}} \leq 60 \text{ hPa}$). These three sets of samples were prepared using a tubular horizontal furnace (Carbolite) instrumented with an automated humidity generator (Wetsys, Setaram).

The specific surface area of samples and their pore size distribution were estimated by nitrogen adsorption data at 77 K using an automated sorption system (ASAP 2020, Micromeritics). We obtained the adsorption data for the relative pressure range between 0.01 and 0.99. We employed the Brunauer-Emmet-Teller (BET) theory to estimate the surface area of samples.³⁵ We estimated

the pore size distribution and the total pore volume using the method by Barret, Joyner, and Halenda (BJH method).³⁶ We verified the presence of micropores for the second and third sets of samples by using the t-plot method of Lippens and de Boer.^{37–39} We observed the general aspect and the texture of the sample before and after dehydration using scanning electron microscopy (FEG Zeiss SUPRA 44VP).

2.4. In-situ XRD experiments. Powder X-ray patterns of the sample under different (T, P_{H_2O}) conditions were measured with a diffractometer (Bruker D8 Advance) with monochromatic Cu – K_α radiation ($\lambda = 1.5406 \text{ \AA}$). For this, we placed the samples in a closed chamber, and we instrumented the diffractometer with an automated humidity generator (Wetsys, Setaram). The patterns were obtained for the interval $13^\circ \leq 2\theta \leq 30^\circ$ with a scan time of 2 s. We compared the results to the patterns of calcium sulfate dihydrate (JCPDS 33-0311), hemihydrate (JCPDS 41-0224) and AIII- CaSO_4 (JCPDS 45-0157).

3. Results and discussion

3.1. Initial sample composition. Figure 2 shows the diffractogram obtained for the initial sample compared to the powder diffraction file for calcium sulfate dihydrate (JCPDS 33-0311). No other crystalline phase apart from $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$ was detected. The concentration of elements was measured by ICP-MS as shown in Table 1. The proportions of Ca and S are very close to the stoichiometric quantities in calcium sulfate dihydrate (23.3% and 18.6%, respectively) and other elements are present as traces. These analyses confirmed the high purity of the sample used for the experiments.

Figure 2. XRD diffractogram of the calcium sulfate dihydrate powder sample.

Table 1. Concentration of elements in the calcium sulfate dihydrate sample by ICP-MS

Elements	Concentration (wt.%)
Ca	22.7
S	19.8
K	0.4
Na	0.2
Si	0.01

3.2. Thermogravimetric analysis results. Figure 3(a) shows an example of a curve obtained by TGA for an experiment carried out at constant P_{H_2O} and stepwise T , i.e., protocol (a). The sample mass (represented by m_i) is shown as a function of time, T , and P_{H_2O} . Firstly, the initial sample of DH was fully dehydrated towards the form AIII- $CaSO_4$ at 200°C under a dry Helium stream. The percentage of mass loss measured was of $(20.74 \pm 0.01)\%$, that corresponds approximately to the stoichiometric value of 20.9% for complete dehydration of DH. This initial dehydration step was carried to set a repeatable starting point for all the experiments. After that,

the temperature was reduced, and the carrier gas was inserted with controlled humidity. In this middle part of the experiment, P_{H_2O} was kept constant, and increasing T plateaus were performed throughout the experiment. The (T, P_{H_2O}) conditions were maintained until stabilization of the mass signal. We observe an almost instantaneous 8% mass uptake with the insertion of humid gas (the mass of the sample increases from 4.20 mg to 4.54 mg). Afterward, we observe that for each increasing T step, the sample loses mass and m_i reaches a new equilibrium value. This systematic behavior can be observed in the areas identified as zones 1 and 2, better shown in Figure 3(b) and Figure 3(c), respectively. According to (T, P_{H_2O}) , the overall mass m_i of the sample can increase or decrease by hydration or dehydration processes. This behavior can be identified as bivariant, as the equilibrium values of m_i depend on both intensive parameters of the system, T and P_{H_2O} (two degrees of freedom).

The average mass at equilibrium $m_i(T, P_{H_2O})$ is then computed by averaging the mass m_i values over about one hour after the stabilization of the mass signal. This treatment of the TGA data also allows the determination of a standard deviation value for the calculated average mass at equilibrium. In the end, the sample is fully calcined at 600°C to produce an anhydrous reference mass (represented by m_{AH}). The observed difference between m_i and m_{AH} during the experiments were attributed to the water content of the sample at given (T, P_{H_2O}) conditions. Therefore, the overall water content of the sample ε (considering both structural and adsorbed water) at equilibrium for each set of conditions T and P_{H_2O} is then calculated as

$$\varepsilon = \frac{n_{H_2O}(T, P_{H_2O})}{n_{CaSO_4}} = \frac{[m_i(T, P_{H_2O}) - m_{AH}]/M_{H_2O}}{m_{AH}/M_{CaSO_4}} \quad (1)$$

where:

- $n_{H_2O}(T, P_{H_2O})$ is the equilibrium water content in moles present in the sample,

- n_{CaSO_4} is the quantity of anhydrous calcium sulfate in moles in the sample (calculated from m_{AH}),
- $M_{\text{H}_2\text{O}}$ and M_{CaSO_4} represent the molar mass of water and calcium sulfate respectively ($M_{\text{H}_2\text{O}} = 18.015 \text{ g} \cdot \text{mol}^{-1}$ and $M_{\text{CaSO}_4} = 136.14 \text{ g} \cdot \text{mol}^{-1}$).

(a)

(b)

(c)

Figure 3. (a) TGA curve of dehydration-hydration using measurement protocol (a) (stepwise increasing T and constant $P_{\text{H}_2\text{O}}$). The two highlighted zones show mass signal stabilization: (b) zoomed portion zone 1; (c) zoomed portion zone 2. The mass signal from 5 to 9 hours for the

beginning of zone 1 is not considered to have reached equilibrium (not stable) and is disregarded in further calculations.

As previously stated in the experimental section, we also performed TGA experiments using protocol (b) (under constant T and stepwise P_{H_2O}) as shown in Figure 4(a). Again, the initial sample is fully dehydrated towards the form $Al(OH)_3$ at 200°C under a dry Helium stream to ensure a repeatable starting point for the experiments. Afterward, the temperature was reduced and kept constant at 50°C . Humid gas was then introduced with increasing P_{H_2O} values according to the protocol shown in Figure 4(c). Similarly to the last protocol results, we observe that m_i increases for each change in P_{H_2O} . However, for this protocol, the sample undergoes hydration. That is, its mass increases and this variation is obtained by increasing P_{H_2O} . Figure 4(b) shows the region for which we observe the bivariate behavior of m_i for easier visualization. Again, we observed that the sample shows a bivariate behavior and the equilibrium values of m_i depend on both T and P_{H_2O} . At the end of the experiment, similarly to the previously shown protocol, the sample is fully calcined at 600°C to obtain an anhydrous reference mass, and the overall water content ε of the sample is calculated using (1).

Figure 4. (a) TGA curve for the dehydration-hydration using protocol (b) (stepwise increase in $P_{\text{H}_2\text{O}}$ and constant T). (b) The highlighted zone indicates mass signal stabilization. (c) Stepwise increase in $P_{\text{H}_2\text{O}}$ values.

We thoroughly verified whether the calculated values of ϵ for each set of conditions ($T, P_{\text{H}_2\text{O}}$) corresponded to equilibrium values. We performed these verifications by carrying out systematic repetitions of experiments and by attaining equilibrium conditions through different T and $P_{\text{H}_2\text{O}}$ paths. For instance, Figure 3 and Figure 4 show examples of how the equilibrium was reached by using different experimental protocols. Figure 5 shows the summary of results obtained for ϵ after reaching equilibrium for three experimental temperatures (50 $^{\circ}\text{C}$, 100 $^{\circ}\text{C}$, and 150 $^{\circ}\text{C}$) at different

conditions and with different protocols. The equilibrium values of ε obtained for different pairs (T, P_{H_2O}) are compared. The vertical axis corresponds to the values obtained under stepwise T and constant P_{H_2O} (protocol (a)) and the horizontal axis corresponds to the values under stepwise P_{H_2O} and constant T (protocol (b)). The experiments were then considered to reach equilibrium due to the observed correspondence of ε values for both protocols.

Figure 5. Values of equilibrium of the overall water content ε obtained under 50°C, 100°C, and 150°C by protocols (a) and (b): isobaric and stepwise isothermal measurements and isothermal and stepwise isobaric measurements, respectively.

The equilibrium values of ε for each (T, P_{H_2O}) conditions were then obtained for several experiments for the experimental ranges of $5 \text{ hPa} \leq P_{H_2O} \leq 60 \text{ hPa}$ and $34^\circ\text{C} \leq T \leq 250^\circ\text{C}$. Figure 6 shows the corresponding results by representing the measured overall water content values of ε as a function of (T, P_{H_2O}) (see Table S1 in the Supporting Information for data points). Three zones can be highlighted in this graph. The lower ($0 < \varepsilon < 0.15$) and the upper ($\varepsilon > 0.5$) zones are characterized by a continuous change in ε with temperature. On the other hand, in the middle zone ($0.15 < \varepsilon < 0.5$), there are no equilibrium points, and the isobar is step-shaped

indicating that the temperature of the hydration/dehydration transition in this zone is a function of the water vapor pressure.

Figure 6. Isobars showing the overall water content ε of the calcium sulfate sample as a function of the temperature T and the water vapor partial pressure P_{H_2O} . For a 3-D representation of the ε - P_{H_2O} - T curves, see Figure S4 in the Supporting Information.

This observed behavior can be interpreted by the existence of one univariant zone (in the middle part of the diagram) and two bivariant zones (identified as the lower and the upper parts of the diagram). The univariant zone represents the univariant transition between phases AIII- CaSO_4 and β -HH. It allows the determination of precise (T, P_{H_2O}) values for which this hydration/dehydration transition between these two phases takes place. The lower bivariant zone ($0 < \varepsilon < 0.15$), can be interpreted as the stability domain for the phase AIII- CaSO_4 and the evolution of ε in this zone can be interpreted as caused by water vapor adsorption. The upper bivariant zone ($\varepsilon > 0.5$) can be referred to as the stability domain for the phase β -HH. The variation in its water content can also be associated with water vapor adsorption.

Therefore, we can represent the overall water content ε measured by TGA for calcium sulfate compounds as produced by two contributions: structural (or crystalline) water and adsorbed water.

This can be expressed by the following expression

$$\varepsilon = n_{\text{structure}} + n_{\text{adsorption}}$$

where $n_{\text{structure}}$ and $n_{\text{adsorption}}$ correspond to the structural and adsorbed water contents, respectively. For our study, $n_{\text{structure}} = 0$ or $0.5 \text{ mol H}_2\text{O/mol CaSO}_4$ according to the calcium sulfate phase (i.e., AIII-CaSO₄ or β -HH, respectively).

Finally, as a matter of comparison, these two bivariant zones in Figure 6 are similar to zone 1 and 2 in Figure 3. Zone 1 corresponds to the upper bivariant zone caused by the water vapor adsorption on β -HH. Zone 2, on the other hand, corresponds to the lower bivariant zone that is related to water vapor adsorption on AIII-CaSO₄.

Overall, these observations confirm the univariant nature of the transition between distinct phases AIII-CaSO₄ and β -HH.^{27,29} From these observations, it is possible to determine for which T and $P_{\text{H}_2\text{O}}$ conditions this transition takes place and then use these data to perform phase equilibrium calculation. Furthermore, we can also complement these observations by verifying the crystalline phase in the lower and upper bivariant zones by in-situ XRD experiments. Both these aspects, phase equilibrium calculation and in-situ XRD experiments, are treated in the following sections.

Concerning the quantification of the adsorption phenomena, we observe that the quantities of adsorbed water are capable of changing the overall water content of the calcium sulfate sample considerably depending on the thermodynamic state $(T, P_{\text{H}_2\text{O}})$ of the system. For the experimental conditions in this work, we showed that β -HH can adsorb up to $0.25 \text{ mol H}_2\text{O/mol CaSO}_4$ beyond its crystalline water content of $0.5 \text{ mol H}_2\text{O/mol CaSO}_4$. That is, a β -HH sample could present a

quantity of adsorbed water that represents 50% of the crystalline water content. We also showed that AIII-CaSO₄ can adsorb water up to 0.15 mol H₂O/mol CaSO₄. These quantities are fairly significant and represent a challenge for the elaboration of gypsum products. For example, depending on the ambient temperature and humidity conditions, the water content in plasters due to adsorption may be more or less significant. However, it is known that the proportion of the adsorption phenomenon varies according to the textural properties of materials (specific surface area and porosity). Therefore, the adsorbed water quantity may also vary depending on the texture of a given material.

3.3. In-situ XRD study under isothermal and isobaric conditions. Figure 7 shows the results of an in-situ XRD study under controlled (T, P_{H_2O}) conditions. This study was performed to complement the results presented in the previous section. We checked the crystalline phase composition for some points in the diagram presented in Figure 6.

Figure 8 shows a TGA curve to illustrate the evolution of the overall water content ε of the sample throughout one experiment where the sample undergoes dehydration and hydration at different (T, P_{H_2O}) conditions. We observe that for the initial point X0, the sample corresponds to calcium sulfate dihydrate ($\varepsilon = 2$). After complete dehydration at 200°C (under dry Helium flow) and cool-down to 50°C, points X1 and X2 should correspond to phase AIII-CaSO₄ ($\varepsilon \approx 0$). Finally, after the introduction of the humid gas stream with P_{H_2O} values of 10 hPa and 20 hPa, the sample should be composed by β -hemihydrate ($\varepsilon \approx 0.5$).

Figure 7(a) shows the XRD diffractograms obtained for a similar sequence of (T, P_{H_2O}) conditions. Diffractogram X0 was obtained at the beginning of the experiment, at room temperature (RT) conditions. As expected, the sample showed the calcium sulfate dihydrate

pattern. After the initial dehydration at 200°C with dry Helium as a carrier gas, we verify that diffractogram X1 corresponds to AIII-CaSO₄ pattern. Diffractogram X2, obtained when the sample was cooled down to 50°C also shows a profile corresponding to the AIII-CaSO₄ pattern. Finally, as the P_{H₂O} value was set to 10 hPa and after to 20 hPa, we obtained diffractograms X3 and X4, respectively. Both of these diffractograms showed profiles corresponding to the phase CaSO₄ · 0.5H₂O. To better visualize the differences between the diffractograms X1 and X2 compared to X3 and X4, we can zoom and superpose some of the peaks and compare them with the patterns. Figure 7(b) shows the comparison for the peaks appearing in the range $25^{\circ} \leq 2\theta \leq 26.5^{\circ}$ for diffractograms X1 to X4. (Figure S5 in the supporting information document shows the comparison for other peaks in the ranges $14^{\circ} \leq 2\theta \leq 15.5^{\circ}$ and $29^{\circ} \leq 2\theta \leq 30^{\circ}$.) Hence, we verified the former premises: diffractograms X1 and X2 do correspond to the AIII-CaSO₄ patterns; diffractograms X3 and X4 do correspond to the CaSO₄ · 0.5H₂O pattern.

Figure 7. (a) Sequence of in-situ XRD diffractograms at controlled $(T, P_{\text{H}_2\text{O}})$ for calcium sulfate under different conditions. (b) Zoomed peaks at $25^\circ \leq 2\theta \leq 26.5^\circ$.

Figure 8. TGA curve corresponding to the in-situ XRD experiment shown in Figure 7.

3.4. Evolution of the sample textural properties. As water adsorption is a surface phenomenon, we have interested ourselves in the textural properties of the calcium sulfate samples at different moments of the TGA protocol. For this reason, three sets of samples were prepared. The first set was composed by the initial sample. The second set was prepared after the full dehydration of the initial sample at 200°C to represent the AIII-CaSO₄ phase. The third and last set of samples was prepared by the dehydration of the initial sample at 200°C and its subsequent hydration at 50°C and at different P_{H_2O} values with the objective of representing the β -HH phase ($15 \text{ hPa} \leq P_{H_2O} \leq 60 \text{ hPa}$). The nitrogen adsorption and desorption isotherms, the pore size distribution curves, and the t-plot (only for the second and third sets of samples) are shown in the supporting information document (cf. Figures S1-S3) Table 2 lists the BET specific surface areas $S_{BET}(N_2)$ and the BJH pore volume $V_{BJH}(N_2)$ calculated from the nitrogen adsorption isotherms. We observe that the dehydration reaction at 200°C increases the BET specific surface area of the sample by 35 times and the BJH pore volume more than 50 times. This increase in the textural properties of a sample has been previously observed for dehydration reactions.^{40,41} The departure of the water molecules from the initial sample creates a network of pores and cracks that are responsible for increasing the specific surface area of the sample. However, once the material

undergoes hydration, the crystallographic structure of the material changes and part of the pores are occupied by the water molecules. Therefore, the surface and pores of the hydrated material are less accessible to nitrogen molecules, and the calculated values $S_{\text{BET}}(\text{N}_2)$ and $V_{\text{BJH}}(\text{N}_2)$ for textural properties decrease. In terms of the general aspects of the powder before and after the dehydration process, we made observations by SEM (cf. Figure 9). Figure 9(a)-(b) shows the smooth overall aspect of the initial powder and Figure 9(c)-(d) shows the creation of pores and cracks with the dehydration process. Overall, the creation of surface and pores that are available for adsorption is expected considering the results presented in Figure 6.

Table 2. BET specific surface areas $S_{\text{BET}}(\text{N}_2)$ and BJH pore volume $V_{\text{BJH}}(\text{N}_2)$ calculated from nitrogen adsorption data at 77 K

Set	Sample	$S_{\text{BET}}(\text{N}_2)$ (m^2/g)	$V_{\text{BJH}}(\text{N}_2)$ (cm^3/g)
1	Initial sample	0.4 ± 0.1	$1.1 \cdot 10^{-3}$
2	Samples after dehydration at 200°C (anhydrous)	14 ± 1	$5.4 \cdot 10^{-2}$
3	β -hemihydrate samples prepared at 50°C	7.3 ± 1.6	$3.6 \cdot 10^{-2}$

Figure 9. SEM images of the powder: (a) general aspect of the initial powder, (b) texture of the initial grains of powder, (c) powder grain after calcination at 200°C, and (d) powder grain after calcination at 200°C and hydration at (100°C, 40 hPa).

3.5. Equilibrium between β -hemihydrate and soluble anhydrite. The univariant zone highlighted in the middle part of Figure 6 allows the determination of the equilibrium conditions for the transition between phases AIII-CaSO₄ and β -HH. To propose a simplified thermodynamic model of the equilibrium curve, the equilibrium equation between the two phases AIII-CaSO₄ and β -HH can be represented as

for which the equilibrium constant K_P is expressed in terms of the van't Hoff equation as follows

$$\ln K_P = -\frac{\Delta_r G^\circ}{RT} = -\frac{\Delta_r H^\circ}{RT} + \frac{\Delta_r S^\circ}{R} \quad (3)$$

where $\Delta_r G^\circ$, $\Delta_r H^\circ$, and $\Delta_r S^\circ$ are the changes in Gibbs free energy, enthalpy and entropy for the dehydration reaction in (2) at standard conditions. The law of mass action allows expressing the equilibrium constant as $K_P = (P_{\text{H}_2\text{O}}/P^\circ)^{0.5}$ (P° is the standard pressure here taken as the unit pressure in atm.) Therefore, the van't Hoff equation becomes

$$\ln\left(\frac{P_{\text{H}_2\text{O}}}{P^\circ}\right) = -\frac{2\Delta_r H^\circ}{RT} + \frac{2\Delta_r S^\circ}{R} \quad (4)$$

For this approximation, $\Delta_r H^\circ$ and $\Delta_r S^\circ$ are assumed to be independent of T for the investigated experimental temperature range (van't Hoff equation approximation.)⁴²

To determine the transition conditions for the equilibrium in (2), we plotted the stability points for each phase onto the $P_{\text{H}_2\text{O}}$ - T plane. Figure 10(a) shows these points in this $P_{\text{H}_2\text{O}}$ - T phase diagram. According to our previous hypotheses, the experimental points for which $\varepsilon \geq 0.5$ belong to the β -HH stability domain (red circles), and those for which $\varepsilon < 0.5$ belong to the AIII- CaSO_4 stability domain (red squares). The transition $(T, P_{\text{H}_2\text{O}})$ values can then be determined by considering the limits of the stability domains for these phases. We marked these values as blue squares and plotted the equilibrium curve by considering the van't Hoff plot in Figure 10(b) (and by applying Eq. 4). Moreover, the linear relationship shown in Figure 10(b) confirms the validity of the van't Hoff equation to represent the equilibrium $(T, P_{\text{H}_2\text{O}})$ values for the transition between β -HH and AIII- CaSO_4 . Therefore, we can estimate the values $\Delta_r H^\circ = (35.5 \pm 1.0) \text{ kJ} \cdot \text{mol}^{-1}$ and $\Delta_r S^\circ = (80.0 \pm 2.8) \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$ by a linear regression.

(a)

(b)

(c)

Figure 10. Pressure-Temperature phase diagrams for the equilibrium between β -HH and AIII- CaSO_4 . (a) The stability points for phases AIII- CaSO_4 and β - $\text{CaSO}_4 \cdot 0.5\text{H}_2\text{O}$ and the transition equilibrium values are presented. The line passing through the latter was fitted using the van't Hoff equation and represents the equilibrium line between these two phases. The dashed line on the top left-hand side represents the water vapor saturation line, and the liquid water stability domain is situated on the shaded area. (b) van't Hoff plot of the equilibrium data. (c) Comparison for the equilibrium curve for the transition between β -HH and AIII- CaSO_4 obtained by the present study and natural gypsum samples obtained by Kelley et al. (P, U, W, and LC), Oetzel et al., and Clifton.^{43–45}

The transition values were confronted with thermodynamic equilibrium data reported by Kelley et al.⁴³, Oetzel et al.⁴⁴ and Clifton⁴⁵, as shown in Figure 10(c). The first set of data for samples identified as P, U, W, and LC were published by Kelley et al. and correspond to hemihydrate samples. P and U correspond to β -hemihydrate samples prepared by heating up natural gypsum in the form of selenite; W probably corresponds to a mixture of α - and β -hemihydrate; LC corresponds to a set of data obtained from previous work by Lescoeur⁴⁶. We observe that the equilibrium points almost superpose for T values up to 90°C. For higher T values though, we observe that there is a shift between the conditions obtained from this study. For the same $P_{\text{H}_2\text{O}}$ value, data from Kelley et al. suggest that higher temperatures are necessary for the dehydration reaction onset. Although we cannot obtain specific information regarding the samples and methods employed by Kelley et al., we can list some hypotheses that might be at the cause of the differences obtained between this study and their results. At first, it is known that the presence of impurities can alter the thermodynamic activities of the components of a chemical system. Therefore, the observed differences could be linked to the purity of the samples. Moreover, as Kelley et al.

worked with dynamic vacuum conditions, some variations in water vapor pressure may occur throughout the experiment. As they have not shown their experimental errors for the pressure and temperature values, we cannot be sure of the real differences between all equilibrium points.

By employing the same methodology as for the experimental data from this study, we calculated values of $\Delta_r H^\circ$ and $\Delta_r S^\circ$ for Kelley et al. datasets in Figure 10(c). They are shown in Table 3 in comparison to the values calculated for the present study. As expected, some shifts are also observed for these values due to differences in the equilibrium points.

Other published P_{H_2O} -T diagrams for this reaction can also be found in the literature such as the ones from Oetzel et al. and Clifton also plotted in Figure 10(c). The results obtained by Oetzel et al. by in-situ XRD show higher transition values of T for the same values of P_{H_2O} compared to the data from the present work. This may be because they use flue-gas desulfurization (FGD) gypsum, obtained as a secondary product from coal-fired power stations, without specifying the impurities content of the material. For this reason, we calculated values of $\Delta_r H^\circ = (51.3 \pm 1.6) \text{ kJ} \cdot \text{mol}^{-1}$ and $\Delta_r S^\circ = (117.9 \pm 4.4) \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$, which are superior to the ones calculated for the synthetic highly pure calcium sulfate dihydrate. The study by Clifton, on the other hand, used highly pure reagent grade calcium sulfate dihydrate for his experiments. However, as they determined the transition using a non-isothermal protocol, the proper determination of the transition temperature can be problematic due to kinetic effects. Moreover, they were not able to measure and estimate $\Delta_r H^\circ$ values by DSC due to experimental limitations. In Figure 10(c), only one data point from Clifton can be seen as it is the only experimental points within the considered T and P_{H_2O} ranges.

Table 3. Values for $\Delta_r H^\circ$ and $\Delta_r S^\circ$ for the equilibrium between β -HH and AIII- CaSO_4

Experimental data	$\Delta_r H^\circ$ ($\text{kJ} \cdot \text{mol}^{-1}$)	$\Delta_r S^\circ$ ($\text{J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$)
This study	35.5 ± 1.0	80.0 ± 2.8
Sample P ⁴³	32.5 ± 0.6	70.4 ± 1.6
Sample U ⁴³	31.7 ± 0.3	67.8 ± 0.9
Sample W ⁴³	32.2 ± 0.2	69.4 ± 0.4
Sample LC ⁴³	32.5 ± 2.1	70.7 ± 5.3
FGD gypsum ⁴⁴	51.3 ± 1.6	117.9 ± 4.4

4. Conclusions

The present work is the first part of a study focusing on the thermodynamic aspects of the water vapor interaction phenomena on calcium sulfate compounds obtained from the dehydration of synthetic gypsum (highly pure $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$). The objective of this study was to propose an updated version of the phase diagram and quantify the water adsorption phenomena on calcium sulfate polymorphs as a function of $(T, P_{\text{H}_2\text{O}})$.

The results showed that the adsorbed water content on AIII- CaSO_4 and β -HH can vary beyond the crystalline water content of these compounds. Moreover, they evolve continuously with temperature and water vapor partial pressure within their stability domains. In the presence of water vapor partial pressure ranging from 5 hPa to 60 hPa and temperature from 34°C to 250°C, two bivariant zones were observed. We interpreted the lower bivariant zone ($0 \leq \varepsilon \leq 0.15$) as caused by water vapor adsorption on AIII- CaSO_4 and the upper bivariant zone ($\varepsilon \geq 0.5$) as caused by water vapor adsorption on β -HH. We provided in-situ XRD data to support these hypotheses. The transition between these two phases was also verified to be univariant. We proposed an

updated pressure-temperature diagram and calculate the values $\Delta_r H^\circ = (35.5 \pm 1.0) \text{ kJ} \cdot \text{mol}^{-1}$ and $\Delta_r S^\circ = (80.0 \pm 2.8) \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$.

We compared our equilibrium points and thermodynamic parameter values to previously reported points in the literature, and we could find some differences. We have attributed this to the kind of material that is used and its chemical composition. The thermodynamic activity of a component can vary if the samples presents impurities. Therefore, we may expect shifts in the equilibrium diagram for these cases. Therefore, if one is to use a specific raw material for an application, a targeted thermodynamic study should also be performed to take account of the possible observed shifts and reduce uncertainties in terms of process conditions and formulation of products.

We observed that calcium sulfate polymorphs can show considerably higher overall amounts of water compared to their crystalline water contents. Water adsorption on AIII- CaSO_4 represented up to about $0.15 \text{ mol H}_2\text{O/mol CaSO}_4$. For β -HH, this quantity represented up to $0.25 \text{ mol H}_2\text{O/mol CaSO}_4$ beyond the crystalline water content of $0.5 \text{ mol H}_2\text{O/mol CaSO}_4$. These amounts are indeed appreciable and should be considered in the formulation of gypsum products. However, the adsorbed water contents may change from sample to sample as a function of the textural properties of the material (specific surface and porosity).

Moreover, we also observed that the BET specific surface area and the BJH pore volume of calcium sulfate calculated from nitrogen adsorption data at 77 K increase with dehydration and decrease with hydration. This was associated with the departure and incorporation of water molecules. The initial departure of water molecules creates a pore network that is accessible by nitrogen. Once the material undergoes hydration, fewer pores are accessible to nitrogen adsorption.

In the second part of this work, we analyze the nature of the adsorbed water on AIII-CaSO₄ and β -HH by using adsorption thermodynamic models.

Supporting Information Additional experimental and characterization data.

This information is available free of charge via the Internet at <http://pubs.acs.org/>.

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NOMENCLATURE

T	Temperature (°C)
P _{H₂O}	Water vapor partial pressure (hPa)
P°	Reference pressure (1 atm)
m _i	Sample mass (mg)
m _i (T, P _{H₂O})	Average sample mass at (T, P _{H₂O}) (mg)
n _{H₂O} (T, P _{H₂O})	Quantity of water molecules in moles
m _{AH}	Mass of anhydrous calcium sulfate anhydrite (mg)
S _{BET} (N ₂)	BET area calculated from nitrogen adsorption data (m ² · g ⁻¹)
V _{BJH} (N ₂)	BJH pore volume calculated from nitrogen adsorption data (cm ³ · g ⁻¹)
n _{CaSO₄}	Quantity of anhydrous calcium sulfate in moles
M _{H₂O}	Molar mass of water (g · mol ⁻¹)
M _{CaSO₄}	Molar mass of calcium sulfate (g · mol ⁻¹)
K _p	Equilibrium constant
Δ _r G°	Change in Gibbs free energy of reaction (kJ · mol ⁻¹)
Δ _r H°	Change in enthalpy of reaction (kJ · mol ⁻¹)

$\Delta_r S^\circ$ Change in entropy of reaction ($\text{J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$)

R Universal gas constant ($= 8.314 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$)

GREEK LETTERS

ε Overall water content in moles of water per mole of anhydrous calcium sulfate

ABBREVIATIONS

DH Calcium sulfate dihydrate

HH Calcium sulfate hemihydrate

β -HH Calcium sulfate β -hemihydrate

XRD X-ray diffraction

ICP-MS Inductive coupled plasma mass spectrometry

TGA Thermogravimetric analysis

SEM Scanning-electron microscopy

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ε : Overall water content (structural + adsorbed)

$P_{\text{H}_2\text{O}}$: Water vapor partial pressure