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Adaptive Helmholtz resonator based on Electroactive Polymers: Modeling, Characterization, and control

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Abstract. This paper presents a new concept and strategy allowing adaptive control of a membraned Helmholtz resonator (HR) embedded in a melamine foam. The designed system aims to adapt the acoustic absorption performances and transmission loss in low frequencies (<500 Hz). The proposed concept consists in replacing the resonator front wall by an electroactive polymer (EAP) membrane. The stiffness of the membrane can be controlled by an electric field, resulting in a resonance frequency shift. A 2D axisymmetric numerical model based on the finite elements method is developed to characterize the complex structure-acoustic coupling between the membrane, the HR and the host foam to determine the potential of the concept. Experimental measurements are then performed in an impedance tube and compared to numerical results. A feedforward algorithm based on neural networks allows the adaptivity of the membraned HR to the acoustic excitation variation inside the impedance tube.

Keywords: Adaptive Helmholtz resonator, Electroactive polymer (EAP) membrane, Noise control, Acoustic efficiency, Neural network algorithm

1. Introduction

Helmholtz resonators (HR) are tunable devices widely used to amplify (e.g. in HI FI speakers) or absorb (e.g. in liners) sounds at a given frequency. They consist of an air filled cavity with an opening (or neck). They can be modeled as a single degree of freedom (SDOF) system with selective resonance frequency related to its neck geometry (associated to the inertial part of the resonator) and the cavity volume which acts as a spring thanks to its compressibility [1]. The mechanisms governing their performances in absorption [2] and transmission loss [3], limited to a single or very narrow frequency band, have been the subject of several studies [4, 5, 6]. Conventional HR have shown weakness when integrated into systems subjected to high frequency variations. Thus, to

overcome this issue, semi-active systems can provide a way to maintain the efficiency of the resonators to shift the resonance frequency in real time. Adaptive-passive methods have been proposed for narrow frequency band applications: resonators whose tuning frequency is controlled by varying its opening area [7] or its cavity volume [8, 9] have been proposed. For the latter, a DC motor controls a movable wall, which modifies its cavity volume. In addition, a feedback based control law is proposed as a tuning strategy. An in-situ, tunable-impedance based on an electromechanical acoustic compliant-backplate HR has been proposed as an alternative [10]. Additional resonances are observed in the impedance curves, leading to interesting sound pressure reduction in the duct. Liu et al. [11] investigated the use of a piezoelectric-composite backplate instead of the isotropic backplates to tune the resonance frequencies. This electromechanical HR was used to control the turbofan engine duct noise. Results show two principal resonance frequencies. The diaphragm geometry (thickness, radius) has been found to have a significant influence on the transmission loss because of the changes in effective cavity volume as a result of the diaphragm motion [12]. An active control is applied to an electronically tunable HR to modify its real impedance using an actuator installed in the resonator is proposed by [13]. It can suppress duct noise at tunable frequencies without increasing the resonator size. The developed control criteria gave a stable and robust active resonator. A theoretically semi-active noise control method (up to 1 kHz) for duct-borne transmission noise around various working conditions by the use of a periodic HR in ventilation systems was developed by [14]. The proposed control method combines band-gap attenuation using the side-branch resonators array with the self-adaptive system of noise control. However, the main drawbacks of this type of devices lies in the weight and the complexity of the mechanism which might restrain the practical implementation of these technologies.

In this paper, electroactive polymers (EAPs) [15] have been proposed as solutions to tune a membrane-cavity resonator (EAP membrane coupled with a back cavity). A very common EAP material is made from 3M VHB 4910 (acrylic) [16], however, other silicone-based film have been proposed in the literature [17]. Membranes are typically obtained from stretched dielectric materials where two compliant electrodes (carbon powder, grease,...etc.) are added on both sides of the film. When a high voltage is applied (in the kilo-Volt range), an in-plane expansion results leading to a reduction of the internal stress and change of the tangent stiffness [18, 19, 20]; leading in turn to a change in the membrane natural frequency. Thus, the natural frequencies of a dielectric elastomer can be varied by changing the membrane stretching ratio, or by varying the applied electrical voltage [21]. This electroactive polymer material behavior has already been demonstrated for membranes in different works [22, 23]. The use of EAP has become widespread in the recent years [24, 25]. Many applications in different engineering fields have emerged because of the remarkable features of these materials (lightness, high strain and fast response [26]). Among the most frequent uses, one can mention mechanical actuators, artificial muscles [27], sensors and energy harvester [28, 29], but also acoustic actuators [30]. Hence, introducing smart materials in acoustic systems offers a real potential for designing adaptive devices. Thus Lu et al. [31] studied the transmission loss performances of a duct silencer using a dielectric membraned cavity. The obtained peaks were tuned by both varying the membrane stretch ratio (λ) and the applied voltage. Other works were interested in electroactive membranes based metamaterials. Yu et al. [32] studied a network of four acoustic cavity resonators with a stretching ratio varying from 3.2 to 4. The peaks observed in the acoustic transmission loss curves can be shifted to lower frequencies when the applied voltage increases. In addition, a broadband control is obtained, showing a promising potential for adaptive noise control in ventilation systems and for other engineering applications. Recently, Yu et al. [33] investigated the acoustic cavity performances installed on a duct and tuned by a dielectric membrane. A three-dimensional analytical model based on the Patch Transfer Function (PTF) method [34] has been developed to characterize complex fluidstructure coupling between the membrane and the surrounding acoustic media. The peaks in the transmission loss curves are shifted to lower frequencies as the applied voltage is increased. Integrating an electroactive membrane on a HR has never been studied before, the main difference with the acoustic cavities consists on the possibility of tuning the "Helmholtz resonance" by varying the applied voltage. In this paper, the upper rigid part of a HR is replaced by an electroactive membrane and embedded in a melamine foam. Acoustic absorption and transmission loss at normal incidence are experimentally measured and results compared to the finite elements model (FEM). The model takes into account the dissipation mechanism in the foam [35] as well as the membraned HR [36].

Following this introduction, the effect of introducing voltage control to the membrane is investigated through a series of experimental measurements to determine the absorption coefficient as well as the transmission loss of the electroactive membraned HR with two stretch ratios i.e., $\lambda=3$ and 4 (see Section 2). Open-loop measurements are performed to control the resonance frequency shift to determine the limits of the proposed device. The frequency shifting phenomenon is analyzed in both absorption and transmission loss cases. The damping loss factor contribution is studied and a link with the acoustic performances is established. The detailed FE modeling of the proposed resonator is described in Section 3, including the porous treatments, the membrane and acoustic domains. In Section 4, a feedforward control with a neural network algorithm is developed for real-time calculation of the applied voltage giving the desired shift of the resonator.

2. Adaptive Helmholtz resonator

The front rigid wall of a HR is replaced by an electroactive membrane as shown in figure 1. The cylindrical cavity is 70 mm depth and 30 mm radius. The circular membrane is 30 mm radius and 0.11 mm and 0.0625 mm thick for respectively $\lambda=3$ and $\lambda=4$. The cylindrical cavity of the HR is characterized by its depth l_{cavity} and radius r_{cavity} , while the neck dimensions are given by its length d_{neck} and radius r_{neck} . Values are listed in

Table 1. Geometrical dimensions of the Helmholtz resonator.								
	$l_{\rm neck}$	$\mathbf{r}_{\mathrm{neck}}$	$d_{\rm cavity}$	$\mathbf{r}_{\mathbf{cavity}}$				
Dimension (mm)	30	9	70	30				

Table 1 Geometrical dimensions of the Helmholtz resonator

table 1. The resonator is embedded in a 75 mm depth and 50 mm radius ultralight



Figure 1. Helmholtz resonator with a front membrane made of electroactive polymer embedded in a melamine foam host support: (a) Real configuration, (b) 3D schematic of the HR components.

melamine foam.

2.1. Experimental setup

A loud speaker installed in a 100 mm diameter tube generates a white noise wave. NI 9263 A/D converter (0-5 V) controls a DC high voltage converter based on EMCO A series generating 0 to 5 kV. The three microphones, two cavities method [44] is used to determine the absorption coefficient and transmission loss. Acoustic data acquisitions are operated in the frequency range of interest [100-1200] Hz. The experimental measurement setup is shown in figure 2.

2.2. Experimental results

2.2.1. Characterization of non active membraned HR

In this section, the membrane is not activated. The contribution of the membraned HR (λ =3 and λ =4) embedded in melamine foam is shown in figures 3 (a, b). The figures also show a reference result corresponding to a melamine sample occupying the full volume (i.e., without resonator). The melamine curve obtained from absorption measurement (solid black line) shows a maximum absorption peak of 30% at 200 Hz and a resonance at 250 Hz attributed to the mechanical resonance of the melamine matrix



Figure 2. Experimental setup for the characterization of the embedded membraned HR in a 100 mm impedance tube.

(Biot frequency). Above this resonance, the foam contributes by 5 dB for transmission loss in the frequency range 200 to 1200 Hz. The contribution to the sound absorption can be positive or negative at the resonator resonances [35]. The absorption curves of $\lambda=3$ depict one peak at f=184.5 Hz and one dip at f=688 Hz at the resonance frequencies (respectively f=186 Hz and f=798 Hz for $\lambda=4$) as shown in figure 3 (a), while two peaks are observed for TL (figure 3 (b)). The first peak arises from the Helmholtz resonance modified by the added membrane, which can be considered as an elastic resonator (detailed modeling can be found in [45, 46, 47]). The added elastic wall contributes to decrease the resonator effective compliance and therefore to shift its resonance to lower frequencies. The dip corresponds to the membrane resonance [48]: the membrane is highly damped leading to a large attenuation in transmission and a poor absorption because of the high reactance of the host foam and to the RH filling ratio [35]. The acoustic pressure distribution corresponding the $\lambda=3$ case is computed at f=184.5 Hz (which corresponds to the Helmholtz type resonance) and f=688.5 Hz (membrane resonance) is shown in figure 3 (c).



Figure 3. Experimental (a) absorption coefficient and (b) transmission loss of the membraned HR for $\lambda=3$ and $\lambda=4$ compared to a full melamine foam; (c) Snapshot of the sound pressure field at the two resonances (1) and (2).

At resonances, the sound pressure observed inside the resonator is much larger than in the rest of the tube, demonstrating, thus, the ability of the device to attenuate certain frequencies by localizing the acoustic energy in the resonator.

The resonator enhances the sound transmission loss of the melamine foam because of the added mass and the two resonances. A first peak of 9 dB amplitude is observed at the first resonance frequency, beside, the second peak improves the transmission loss efficiency with a 33 dB amplitude.

The next section discusses the open-loop results for different applied voltages.

2.2.2. Static identification

The application of the electrical voltage V [Volt] changes the EAP membrane stiffness and therefore its mechanical and acoustical properties. Variations of the sound absorption and transmission loss are obtained. Analysis of this effect is carried out in an open-loop in the section. The applied electric voltage varies from 0 to 5 kV and the sound absorption (α) and TL are investigated. Results are shown in figure 4 (a,



b). The acoustic device depicts one peak and one dip at the resonance frequencies

Figure 4. Experimental (a) absorption coefficient and (b) transmission loss for various voltage values for $\lambda=3$ both compared to a full melamine foam.

on the absorption curve, while two peaks are observed in the case of transmission loss. As expected, the variation of the electrical voltages induces a to shift of the

						0	
V(kV) $f_r(Hz)$	0	1	2	3	4	5	
f_{res1}	184.5	183.0	180.0	174.5	165.5	152.5	
f_{res2}	688.5	687.0	682.6	673.8	663.6	635.7	

Table 2. First and second resonances as function of the applied voltage for $\lambda=3$.

resonances of the resonators. The peak shifts are explained by the interactions between the electroactive membrane of variable stiffness (equation (5)) and the resonances of the cavity. Absorption coefficient curves for the electroactive membrane Helmholtz resonator (λ =3) are plotted in figure 4 (a). Outside the resonance frequencies, the Helmholtz resonator behavior is independent from the electrical voltage. The first zero voltage resonance is observed at a frequency of 184.6 Hz with an amplitude of 0.85. For the maximum voltage of 5 kV, this frequency is lowered to 152.5 Hz with an amplitude of 0.5. Hence, 32 Hz offset is obtained (around 20 %). On the transmission loss curves (figure 4 (b)), two peaks are observed. The application of a voltage has the same effect as for the absorption coefficient, since a frequency shift is observed. For a null voltage, the first peak has an amplitude of 8.7 dB. It is reduced to 6 dB for 5 kV. The second resonance has an amplitude around 33 dB. This value decreases to 17.9 dB when 5 kV is applied. All resonances frequencies values are listed in table 2.

The shift of the first resonance as function of the applied voltage is listed in the following table 3.

∧-J.						
Voltage (kV)	0	1	2	3	4	5
Frequency shift (Hz)	0	1.5	4.5	10	19	32





Figure 5. Experimental (a) absorption coefficient and (b) transmission loss as function of the applied voltage variation for $\lambda=4$ both compared to the full melamine foam.

V (kV) f_r (Hz)	0	1	2	3	4	5	
$ \begin{array}{c c} f_{res1} \\ f_{res2} \end{array} $	186 798	186 798	183 792	179 785	170 772	158 750	

Table 4. First and second resonances as function of the applied voltage for $\lambda=4$.

The expected effect is thus clearly observed: a shift towards the low frequencies of the first resonance results from the increase in the electrical voltage. It should be noted that this property of interest results in a reduction in efficiency, whether in terms of absorption or transmission. A similar analysis for $\lambda=4$ leads to identical conclusions. The values of the resonant frequencies are listed in table 4. The first resonance frequency (0 kV) is 186 Hz, higher than that for $\lambda=3$ (184.6 Hz) with a tiny difference of just 1.4 Hz. The gap becomes larger for the second resonance with 798 Hz for $\lambda=4$ and 688.5 Hz for $\lambda=3$. This difference of 109.5 Hz is justified by the fact that this resonance is due to the membrane vibration which has a smaller thickness for $\lambda=4$ (0.0625 mm) than in the $\lambda=3$ (0.11 mm). For $\lambda=4$, the first resonance of the absorption curve has an amplitude of 90%. For 5 kV, a shift of 32 Hz and an amplitude drop of 66% are observed. For transmission loss (figure 5 (b)), peaks amplitudes are generally higher than ones obtained for $\lambda=3$. The amplitude falls to near extinction at 5 kV is due to the loss factor increase

	5. Frequency shift	t as func	tion of the a	pplied vol	tage for $\lambda = 4$.		
$V(\rm kV)$	0	1	2	3	4	5	
Frequency shift (Hz)	0	0	3	7	16	32	

resulting from the applied voltage. The different mechanisms related to resonances, and the loss factor increase are studied in section 2.3. With regard to the second resonance, the transmission loss efficiency remains high, the resonant frequency is shifted, which is synonymous with a change in the electroactive membrane internal stress, without necessarily bringing a large change in peak amplitudes except in the case of 5 kV. Therefore, the stretch ratio λ affects the absorption coefficient and the transmission loss of the resonator. The first frequencies (Helmholtz resonances) are quite close comparing $\lambda=3$ and 4 results, the difference is more apparent for the second (membrane) resonances. For possible applications, the targeted resonant frequencies determine the choice of the stretch ratio to use. Having found the possibility of controlling the resonator behavior by varying the applied voltage, the next section is focused on the validation of the numerical model.

2.3. Membrane damping analysis

Phenomenon linked to the absorption (respectively the transmission loss) amplitude fall noticed during the resonance shift towards the low frequencies are investigated. Experimental setup is shown in figure 6. The membraned HR are settled on a frame itself fixed on an impedance tube, a white noise excitation is generated by a speaker installed in the end of the tube in which a reference microphone is located. A 1D laser vibrometer (Doppler Polytec-PDV100) measures the membrane velocity, the transfer function between the membrane velocity and the reference pressure is thus established. The analysis is carried out to determine the effect of the membrane damping on the resonator performances. The fall in amplitude has already been mentioned in the literature: Dubois [19] studied the electrical voltage effect on the membrane (made from Sylgard 184 PDMS) resonance frequency with a resonance drop of up to 40%; Hochradel [30] reported the resonances dependency of dielectric elastomer actuators such as VHB 4905 on the applied voltage, 30% shift is observed for 3 kV; but to our knowledge, no identification of damping of EAP membranes under applied voltage is available in literature.



Figure 6. Experimental setup for measuring the velocity of the electroactive membranes.

The loss factors η are determined by the -3dB bandwidth method applied on the measured transfer function. figure 7 illustrates the identification of the first mode of the



Figure 7. Identification of the first eigenmode's loss factor η of the electroactive membrane for a null voltage ($\lambda=3$).

zero voltage membrane (λ =3). This latter step is repeated for voltage values from 1 to 5 kV.

The obtained loss factor η values are listed in table 6, η increases with the applied voltage. This trend is consistent with previous observations on the absorption factor and TL measurements: whether it is the first or the second resonance, an amplitude

drop is observed for the two resonators ($\lambda=3$ and $\lambda=4$) when the voltage increases. The

the applied voltage for A=3 and A=4.							
η V (kV)	0	1	2	3	4	5	
$ \begin{vmatrix} \eta_{\lambda=3} \\ \eta_{\lambda=4} \end{vmatrix} $	$0.020 \\ 0.030$	$0.030 \\ 0.031$	$0.036 \\ 0.031$	$0.038 \\ 0.034$	$\begin{array}{c} 0.040 \\ 0.034 \end{array}$	$0.050 \\ 0.045$	

Table 6. Variation of the loss factor η of the electroactive membrane as a function of the applied voltage for $\lambda=3$ and $\lambda=4$.

loss factor η contributes to lower the peak amplitudes of the absorption coefficients. The study allows to establish a link between the frequency shift and the amplitude fall. Observations made by Zhu [21] concerning the reduction of the resonant frequencies with the applied voltage are confirmed, this is explained by the increase of the membrane stiffness.

3. Numerical model

A 2D axisymmetric numerical model capable of describing the structural acoustic coupling is developed in order to predict the acoustic performances of the proposed device. A schematic of the geometry in the calculation is shown in figure 8. The numerical model simulates a 100 mm diameter impedance tube test for the measurement of the absorption coefficient and the transmission loss on frequency range 100 to 1200 Hz. At the impedance tube walls, a rigid wall boundary condition is imposed in the longitudinal direction. The mesh is based on quadratic triangular elements for the tube, the foam and the resonator. The element size is chosen in order to have 6 elements per wavelength on the whole model [37]. A multiphysics modeling of the foam as well as HR are needed. The resonator cavity walls are considered rigid as well as for the neck, the melamine foam behavior and the viscous loss in the resonator neck are modeled using the Johnson-Champoux-Allard model (JCA) model [35]. In addition the stretched membrane is modeled in the model by considering its in-plane force for different electrical voltage values.



Figure 8. Geometry of meshes used in the finite element model with plane wave source at one end and rigid backing at the opposite end. The two microphones are used to estimate absorption coefficient of the membraned HR embedded in melamine foam.

3.1. Acoustic model

The acoustic fields inside the tube and resonators cavities are described by Helmholtz's equation

$$\Delta p + k^2 p = 0, \qquad k^2 = \frac{\omega^2}{c_0^2},$$
 (1)

where p is the acoustic pressure, k is the wave number and $c_0=340$ m/s the sound speed in air.

The melamine foam is modeled as an equivalent fluid with a rigid frame based on the Johnson-Champoux-Allard model (JCA) [38]. This model is described by the Helmholtz equation in which the squared sound speed c_0^2 is replaced by $K_{\rm eff}/\rho_{\rm eff}$, where $K_{\rm eff}$ and $\rho_{\rm eff}$ are respectively the frequency-dependent effective bulk modulus and effective density. The JCA model is based on five intrinsic experimentally measured properties i.e., the flow resistivity σ , the porosity Φ , the tortuosity α_{∞} , the viscous Λ and thermal Λ' characteristic length. The intrinsic properties given in table 7 are obtained experimentally from the measurements carried out on the porous materials characterization benches at GAUS (Universit de Sherbrooke). The visco-thermal losses in the resonator neck are considered by using its effective complex and frequency dependent parameters [39] based also on the JCA model: the neck is assimilated to a cylindrical pore [40]. where corresponding parameters are given as $\Phi_{\rm neck}=1$, $\alpha_{\rm neck}=1$, $\sigma_{\rm neck}=\frac{8\eta_{\rm air}}{r_{\rm neck}^2}$ ($\eta_{\rm air}$ being the air viscosity), and $\Lambda_{\rm neck}=\Lambda'_{\rm neck}=r_{\rm neck}$.

3.1.1. Membrane modeling A structural FE model was developed in order to determine the membrane in-plane force T_0 . This latter is a key parameter to adapt the acoustic device performances. Ogden model with experimentally determined parameters (listed in table 8) is used to describe the hyperelastic material model [41]. In the present Nparameters model, the first Piolla-Kirchoff stress tensor P_1 of the material is given in

	foam identified exper				
σ	Φ	$lpha_{\infty}$	Λ	Λ'	
$(N.s.m^{-4})$			(μm)	$(\mu { m m})$	
8432	0.99	1.02	138	154	

Table 7. Johnson-Champoux-Allard model parameters of the ultralight melaminefoam identified experimentally.

 Table 8. Parameters of the 3M VHB 4910 acrylic described by Ogden hyperelastic model.

Parameter	Value	
$\overline{\mu_1[\text{kPa}]}$	104.5	
α_1 [-]	0.93	
$\mu_2 \; [\mathrm{kPa}]$	0.0529	
α_2 [-]	5.38	

terms of the stretch ratio λ and the empirically determined Ogden parameters μ_i and α_i .

$$P_1 = \sum_{i=1}^{N} \mu_i (\lambda^{\alpha_i - 1} - \lambda^{-\frac{\alpha_i}{2} - 1}).$$
(2)

The $t_0=1$ mm thick square $(l_x^0 = l_y^0 = 10 \text{ cm})$ membrane is stretched 3 and 4 times in both X and Y directions. The obtained thickness in the stretched state t_s is calculated by

$$t_s = t_0 / \lambda^2, \tag{3}$$

where $\lambda = l_x^s / l_x^0$, l_x^s being the membrane length after stretching. The obtained thicknesses are 0.11 mm and 0.0625 mm for $\lambda = 3$ and $\lambda = 4$, respectively. Simulation yields an in place force of $T_0 = 30.5$ N/m for $\lambda = 3$ and 26.4 N/m for $\lambda = 4$.

Introducing a voltage control to the membrane, in pursuing a possible tuning of the resonator acoustic performances is investigated. When a voltage is applied between the two electrodes, a Maxwell pressure is created upon the dielectric layer. The membrane become thinner, expends in the planar directions and increases its surface, causing a decrease in its internal stress σ and therefore the in-plane force T_0 . Thus, the voltage effect is taken into account according to [19]

$$\sigma_p = \sigma_0 - \varepsilon \frac{V^2}{t_s^2},\tag{4}$$

where σ_p is the membrane stress due to the applied voltage, σ_0 is the membrane initial stress, ε the elastomer relative permittivity [42] and t_s the membrane thickness.

Equation (4) is equivalent to

$$T_p = T_0 - \varepsilon_p V^2, \tag{5}$$

where T_0 and T_p are respectively, the membrane in-plane force before and after applying the voltage, $\varepsilon_p = \frac{\varepsilon}{t_s}$ values are determined based on the linear regression function. T_p values for 0, 3 and 5 kV are first obtained numerically by identification process based on the Least Mean Square method, then a linear regression function is used in order to generalize the evolution of T_p as a function of the applied voltage V [33].

The acoustic fields inside the tube, the resonator cavity and neck satisfy the Helmholtz's equation, the circular membrane is governed by its dynamic equation of flexural vibration, which amplitude w(x, y) under harmonic difference pressure load Δp at angular frequency ω is governed by equation 6

$$T_0 \bigtriangledown^2 w(x, y) + \omega^2 t_s \rho_m w(x, y) = \Delta p, \tag{6}$$

The density of the 3M VHB 4910 is 960 kg/m³ following [16], while Poisson's ratio is 0.49. The damping effect is taken into account in the FE model by using a complex inplane force $T_0^* = T_0(1+j\eta)$ with η the membrane loss factor determined experimentally as detailed in Section 2.3, values are listed in table 6.

3.2. Acoustic indicators

The aim of the model is to estimate two acoustic indicators: absorption coefficient α and transmission loss (TL). Two virtual microphones are used to determine the magnitude of the forward and backward traveling waves, from which sound absorption coefficient may be determined. It is assumed that only plane waves propagates in the tube from the right end and the specimen being in the other end. The sound absorption coefficient α is defined as the ratio of sound power absorbed by a surface to the incident sound power [43]. The sound absorption coefficient for a plane wave at normal incidence is obtained from the reflection coefficient R, and is given by

$$\alpha = 1 - |R|^2. \tag{7}$$

The acoustic attenuation capability, which is often referred to as TL in decibels is one of the most important factors in designing acoustic resonators. Hence, an anechoic termination condition $Z=\rho_0c_0$ ($\rho_0=1.213$ kg/m³ is the air density and $c_0=340$ m/s is the sound velocity in air) is applied at the end of the tube and the average pressures on two parallel surfaces to the acoustic excitation in upstream p_1 and downstream p_2 of the tested devices are raised. Transmission loss is determined as

$$TL = 20 \log_{10}(\frac{p_2}{p_1}).$$
(8)

3.3. EAP membrane behavior

The EAP membrane is described by equation (5). The model being quite simple and sensitive to mounting conditions, a linear regression is performed to identify two models (for $\lambda=3$ and $\lambda=4$) allowing correct estimation of the resonance frequencies identified in tables 2 and 4. These models are:

$$T_p^{\lambda=3} = T_0^{\lambda=3} - 0.48 \ V^2,\tag{9}$$

and

$$T_p^{\lambda=4} = T_0^{\lambda=4} - 0.4 \ V^2. \tag{10}$$

The value of the membrane in-plane force T_p as function of the applied voltage obtained both from numerical and linear regression approach are reported in figure 9. The evolution is non-linear with a tendency which is in adequacy with the two equations (9) and (10). T_p and V units used in the above equations are kilo-pascal (kPa) and kilo-volt (kV), respectively. For zero voltage, the membrane in-plane force values are $T_0=29$ N/m for $\lambda=3$ and $T_0=28$ N/m for $\lambda=4$. These values are obtained from identification process to fit the experimental measurements. They are lower compared to those obtained from the stretch process FEM simulation ($T_0=30.5$ N/m for $\lambda=3$ and $T_0=26.4$ N/m for $\lambda=4$). This adjustment can be explained considering the added electrodes (which is not taken into account in the FE model) and the membrane-frame assembly process subject to experimental uncertainties.

The figure 9 shows the identified values of the membrane in-plane forces and the corresponding regressions. The values of the membrane in-plane force T_p as function of



Figure 9. Membrane in-plane force T_p as function of the applied electric voltage (V) for $\lambda=3$ and $\lambda=4$: linear regression result compared to the numerical model.

the applied voltage V for $\lambda=3$ and $\lambda=4$ are listed in table 9. In the following, these models are used to estimate the effect of the applied voltage on the absorption coefficient factor and TL curves. Results are presented for 2 kV and 5 kV only.

$\lambda = 3$ and $\lambda =$	±.						
$\begin{array}{c c} & V(\mathrm{kV}) \\ \hline & T_p^{\lambda}(\mathrm{N/m}) \end{array}$	0	1	2	3	4	5	
$ \left \begin{array}{c} T_p^{\lambda=3} \\ T_p^{\lambda=4} \end{array} \right $	29.0 28.0	29.0 27.6	27.6 26.4	$25.2 \\ 24.4$	$\begin{array}{c} 21.8\\ 21.6\end{array}$	$17.5 \\ 18.0$	

Table 9. Membrane in-plane force T_p as function of the applied electric voltage V for $\lambda=3$ and $\lambda=4$.

3.4. Results

3.4.1. Absorption

In figure 10 (a, b), a good agreement between numerical and experimental curves for $\lambda=3$ is observed, the vibroacoustic behavior is faithfully described and resonance peaks are well estimated. For $\lambda=4$ (figure 11 (c, d)), the numerical model predicts the two



Figure 10. Absorption coefficients of the electroactive Helmholtz resonator: comparison of results from experimental and numerical model. (a) $\lambda=3$ for 2 kV, (b) $\lambda=3$ for 5 kV.

main resonances of the system, while a mean frequency difference is observed over the interval [200-700] Hz, which could be attributed to the uncertainties during experiments (resonator dimensions and it's mounting on the foam).



Figure 11. Absorption coefficients of the electroactive Helmholtz resonator: comparison of results from experimental and numerical model. (a) $\lambda=4$ for 2 kV and (b) $\lambda=4$ for 5 kV.

3.4.2. Transmission loss

Transmission loss results for $\lambda=3$ (2 kV and 5 kV) are compared in figure 12 (a, b). It is observed that numerical model fits well with the experimental data, peak resonances and amplitudes are correctly predicted with small differences for 2 kV (0.8% for the second resonance). This observation is similar to that made on the absorption curves. The differences are mainly due to experimental uncertainties.



Figure 12. Transmission loss of the electroactive Helmholtz resonator: comparison of results from experimental and numerical model. (a) $\lambda=3$ for 2 kV, (b) $\lambda=3$ for 5 kV, (c) $\lambda=4$ for 2 kV and (d) $\lambda=4$ for 5 kV.

For $\lambda=4$ (figure 12 (c, d)); the numerical model allows to estimate the two main resonances of the resonator for 2 kV and 5 kV voltages. It accurately describes the transmission loss behavior of the device. As concluded previously, the variation of the electrical voltage allows to shift the resonances towards the low frequencies. The obtained results show the potential offered by such devices for the control of resonances of the HR through an electromechanical system based on electroactive membrane. In the next section, a feedforward control algorithm is proposed to study the device's ability to adapt to a tonal noise excitation variation.

4. Closed loop control based on neural network algorithm

Shifts observed in open-loop measurements have allowed to assess the electroactive membrane resonator ability to control the resonance frequency. Therefore, a Feedforward based algorithm is proposed and experimentally tested. The control law is based on the Neural Networks (NN) algorithm of Matlab toolbox [49]. In the present case, the NN is composed of 10 neurons and 2 layers. The training of the NN is based

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on the optimization method of Levenberg-Marquardt combined with the Least Mean Square (LMS) performance function to better approximate the nonlinear function fit problems [50].

4.1. Control command

The control law is built for the two electroactive HRs ($\lambda=3$ and $\lambda=4$). Several steps are necessary for defining the control algorithm development as follow.

4.1.1. Step 1: generate the Input/Output data

Three measurements with an electrical voltage from 0.8 to 5 kV with 100 V step are performed to determine the frequency shift as a function of the applied electrical voltage $\Delta f = G(V)$ as shown in figure 13 (a, b). It is clearly observed from these figures that no membrane activation is made for voltage lower than 1.5 kV, which corresponds to a non linearities of the system. The effect appears for higher voltages. 50% of the obtained



Figure 13. Evolution of the frequency shift Δf (Hz) as a function of the applied voltage V (kV) for (a) $\lambda=3$ and (b) $\lambda=4$.

data (from measurements 1, 2 and 3) are used for the learning step, 25% for the test and 25% for validation.

4.1.2. Step 2: linear function approach

Assuming a quasi-static regime, the inverse non-linear function G^{-1} that links the control voltage V (to be applied) and the target frequency shift Δf is established using the NN algorithm such as

$$V = G^{-1}(\Delta f). \tag{11}$$

4.1.3. Step 3: Reference resonance frequency determination

Once the function G^{-1} assessed, a first measurement of absorption coefficient (black curve in figure 15) with white noise excitation for a zero voltage (V=0 kV) is carried

out. In order to determine the value of the first resonance f_0 (having a fixed value). Afterwards f_0 is used as the reference frequency in the following algorithm.

4.1.4. Step 4: test of the control algorithm

It consists, as depicted in figure 14 of exciting the device with a white noise combined with a tonal noise f_t . The latter being variable is chosen to be lower than that of the zero voltage resonator (f_0). The difference Δf between f_t and f_0 leads to the calculated



Figure 14. Diagram of the feedforward control applied to the adaptive HR based on EAP membrane (Resonance frequency shift process according to the desired command using the NN algorithm).

voltage value to be applied using the function G^{-1} from step 2. An absorption curve is plotted and compared to the reference one in order to check the command accuracy.

4.2. Results

Acoustic absorption results obtained from the control are presented for $\lambda=3$ and 4.



Figure 15. Feedforward algorithm response to the electroactive HR: frequency shift control (Case $\lambda = 3$) for (a) 20 Hz (4.53 kV) and (b) 51 Hz (6.26 kV).

For $\lambda=3$, 20 Hz (corresponding to a tonal noise of $f_t=164.5$ Hz) then 51 Hz ($f_t=135$ Hz) offsets are targeted. As shown in figure 15 (a, b), the command correctly estimates the adequate voltage to be applied (4.53 kV and 6.26 kV, respectively for the first and the second offset). Considering now $\lambda=4$, for 30 Hz corresponding to $f_t=156$ Hz, the 0 kV ($f_0=186$ Hz) peak (black curve) is well shifted to f=156 Hz as shown in figure 16 (a). On the other hand, the frequency is shifted to 121 Hz corresponding to a 65 Hz (with 5.93 kV voltage). Thus, the developed command accurately adapts to the tonal excitation variation even for voltages not belonging to the set interval of step 1 ([0.8-5]kV), demonstrating the effectiveness of the proposed algorithm.



Figure 16. Feedforward algorithm response of the electroactive Helmholtz resonator: frequency shift control of $\lambda=4$ for (a) 30 Hz (4.46 kV) and (b) 65 Hz (5.96 kV).

For the two ratios $\lambda=3$ and $\lambda=4$, the frequency corresponding to the fall of the absorption coefficient (in the neighborhood of 800 Hz) is also shifted, since it corresponds to the membrane resonance. A 6.26 kV is needed to accomplish the 51 Hz shift for $\lambda=3$, or, 65 Hz shift ($\lambda=4$), a lower voltage is applied. This is explained by the in-plane

forces T_0 and membrane thickness differences that modify the electrical permittivity of the material. It can also be observed that resonance amplitudes decrease drastically when the shift control is important. Thus, for 65 Hz, the first absorption resonance amplitude is decreased by 59% (89% amplitude at 0 kV and 30% at 6.26 kV) which is in accordance with the membrane damping analysis presented in Section 2.3.

Giving the obtained results, the NN algorithm based control seems to be very effective for adaptive HR response to the acoustic tonal excitation variation.

5. Conclusion

In this paper, the acoustic response of an electroactive membraned Helmholtz resonator embedded in melamine foam has been investigated numerically. Experimental validation have shows a good agreement between measurements and simulations, which definitely demonstrates the effectiveness of the proposed model.

Results for absorption and transmission loss have shown the potential of the electroactive polymer membrane integration to control the Helmholtz resonator frequency by varying the applied voltage. In addition to the Helmholtz type resonance, other peaks are observed at higher frequencies resulting from the membrane vibration. A drop is observed in acoustic absorption, while a high amplitude peak effect is obtained in transmission loss. The neural network algorithm allows the control of the resonance shift as function of the tonal acoustic excitation variation with a high accuracy. In the absence of disturbance, control by neural networks may be sufficient to obtain adaptive Helmholtz resonator and could open the control of the proposed system by taking into account the variation of conditions (temperature, humidity, etc.).

For future applications, and although resonators provide control over a narrow band, the combination of multiple tuned resonator at multiple frequencies could provide a potential solution for broadband control.

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