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Contactless Characterization of Coplanar Stripline Discontinuities by RCS Measurement

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Abstract—The article presents a contactless approach to characterize coplanar stripline discontinuities based on a radar cross-section (RCS) measurement method. With this approach, the values of the equivalent lumped element models are determined for two discontinuities often encountered in practice: open-circuit and short-circuit. The discontinuities are incorporated into two different very simple resonators. But contrarily to what is usually done, here the resonators are considered as radar resonant targets and are illuminated by a plane wave. The incremental electrical length due to the discontinuities causes a shift of the resonance frequency which is used for the extraction of the parameters. The values obtained from full-wave simulations are compared to measurements and to other data available from previous studies.

Index Terms—Coplanar stripline discontinuities, RCS measurement, resonator, wireless method.

I. INTRODUCTION

A COPLANAR stripline (CPS) is a uniplanar transmission line (TL) whose structure consists in two conductor strips separated by a gap and placed on a dielectric substrate of finite thickness $D$ [Fig. 1(a)]. This configuration corresponds to the dual structure of the coplanar waveguide (CPW) and provides the same advantages, including small losses, easy mounting of series lumped component and no need for via due to the uniplanar configuration.

CPSs are commonly used in monolithic microwave integrated circuits [1], as well as in microwave components such as filters [2]. Lately, CPSs have been used in various application fields such as antennas [3], chipless radio frequency identification (RFID) [4], or for medical sensors [5].

Compared to the extensive work carried out on microstrip and CPW structures, only few studies have been made to obtain lumped equivalent circuits of CPS discontinuities. The first characterization of simple CPS discontinuities has been reported in [6]. The values of the model elements were extracted from simulations (finite-difference time domain (FDTD) method) and measurements by using, in both cases, a thru-reflect-line (TRL) calibration algorithm. Some limitations concerning the de-embedding procedure of [6] are highlighted in [7] such as the parasitic effects of the calibration standards which are ignored. To correct that, Zhu and Wu present in [7] a second characterization method based on a deterministic method of moment (MoM) combined with a short-open calibration (SOC) technique for a more accurate assessment of the parameter values. Up to now, those two methods ([6], [7]) are the only ones existing for an experimental characterization of CPS discontinuities. They are both based on guided approaches that need an accurate de-embedding procedure.

Approximate analytical approaches were also proposed for a theoretical evaluation of open and short circuit discontinuities. A general quasi-TEM model is proposed in [8] for two wire transmission lines. It yields simple closed-form expressions that can be applied to the case of CPS. Another work presents a computation method based on the quasi-static concept of excess charge solved by MoM [9].

This article presents a novel experimental approach to characterize short circuit (SC) and an open circuit (OC) discontinuities of CPS based on RCS measurements. Compared to previous approaches, it does not need any de-embedding techniques or complex feeding network [7]. Indeed, this method simply uses a resonant scatterer that incorporates the discontinuity to be tested. The shift of the resonance frequency due to the discontinuity is then used to extract the values of the lumped equivalent elements. We note that this method belongs to the more general “resonator approach” used to analyze the microstrip discontinuities [1], [10], [11]. But contrarily to what is classically done with microstrip, here, the resonator does not need to be coupled to a feed line through a gap. The resonator is considered as a radar target which is illuminated by a plane wave [Fig. 1(b)]. This way of doing eliminates the possible errors due to the gap perturbation and the de-embedding techniques. Similar RCS measurement method have been used for the characterization.

Fig. 1. (a) Transverse section of coplanar stripline (CPS). (b) RCS measurement principle. A resonator that incorporates the discontinuity to be tested is illuminated by a plane wave $E_0$. The backscattered field $E_s$ is measured.

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of antennas with small electric length, scatterers, or chipless RFID tags [12]–[15].

The characterization method base on the resonator approach is presented in detail in section II. Section III is dedicated to the RCS measurement approach. Simulation and measurement results are compared to each other and also with published data.

II. CHARACTERIZATION METHOD

A. Discontinuity Models

The discontinuities under study are the SC and the OC.

First, a CPS short circuit is realized by interconnecting the strips with a conductor at the plane $P_1$ as it is shown in Fig. 2(a). At radiofrequency, magnetic energy is stored behind the termination so that the structure departs from an ideal SC. This can be modeled either by a lumped inductance $L_s$ or by an incremental length $\Delta l_s$ of the strips terminated with and ideal SC. This double modeling of the SC is the basic idea of the proposed method. Indeed, $L_s$ is the element which will be experimentally evaluated while the extra length, $\Delta l_s$, is the element that will be detected through the measurement of a frequency shift, like it will be seen in the following section.

Obviously, the impedance seen at the plane $P_1$ has to be the same for both models [10]. So considering no loss:

$$\omega L_s = Z_0 \tan(\beta \Delta l_s),$$

where $\omega$ is the pulsation, and $Z_0$ and $\beta$ are the characteristic impedance and the wavenumber of the CPS line.

Second, a CPS OC is formed by abruptly ending the metallic strips at the plane $P_2$ as it can be seen in Fig. 2(b). The dominant phenomenon associated with OC is the apparition of fringing fields which are extending beyond the physical termination of the metallic strips [6]. This gives rise to a capacitive reactance which can be modeled either by a lumped shunt capacitance $C_0$ or by an incremental length $\Delta l_o$.

Like in the previous case, those two equivalent representations are essential. With the same argument as for the SC case [10], we find:

$$-1/\omega C_0 = -Z_0 / \tan(\beta \Delta l_o).$$

A simpler expression of $L_s$ and $C_0$ is obtained using the first term of the expansion of the tangent function:

$$L_s = Z_0 \Delta l_s \sqrt{\varepsilon_{\text{eff}}} / \varepsilon,$$

$$C_0 = \Delta l_o \sqrt{\varepsilon_{\text{eff}}} / c Z_0,$$

where $\varepsilon_{\text{eff}}$ is the effective permittivity of the CPS line.

B. Resonator Approach

The SC and OC discontinuities are incorporated into two different resonant scatterers represented in Fig. 3. The loop resonator [Fig. 3(a)] can be considered as a TL section terminated at both ends by a SC. The C-like resonator [Fig. 3(b)] is a TL section terminated by a SC at one end and by an OC at the other end. A third kind of resonator terminated at both end by an OC could be theoretically used but it is hardly excited by a plane wave illumination and therefore it is not applicable for the present kind of measurement. For the study,

$$l_A + 2\Delta l_s = m \lambda_r / 2,$$

where $m$ is an integer.

The C-like scatterer behaves like a quarter-wavelength resonator:

$$l_B + \Delta l_s + \Delta l_o = \lambda_r / 4 + m \lambda_r / 2.$$
and \(C_0\) are functions of the frequency which directly depends on the physical length of the strips.

The guided wavelength is related to the resonant frequency \(f_r\):

\[ \lambda_g = \frac{c}{f_r \sqrt{\varepsilon_{\text{eff}}}}, \]

where \(c\) denotes the speed of light in free space and the effective permittivity \(\varepsilon_{\text{eff}}\) is calculated from the physical dimensions of the TL using the closed form equation given in [16]. Considering the first resonance for each scatterer, we have:

\[ l_A + 2 \Delta l_A(f_A) = \frac{c}{2 f_A \sqrt{\varepsilon_{\text{eff}}}}, \]  \(8\)

\[ l_B + \Delta l_B(f_B) + \Delta l_O(f_B) = \frac{c}{4 f_B \sqrt{\varepsilon_{\text{eff}}}}, \]  \(9\)

where the parenthesis denote the dependence on the frequency.

As it can be seen from (8)-(9), the incremental length due to the discontinuities causes a shift of the resonance frequency compared to the perfect SC and OC models. The value \(\Delta l_A\) corresponding to the resonant frequency \(f_A\) can be calculated from (8). If the physical length \(l_A\) and \(l_B\) are chosen such that the resonant frequency of both scatterers \(f_A\) and \(f_B\) are equal, we can replace \(\Delta l_A\) by its expression in (9), and then calculate \(\Delta l_O\). Considering that \(\varepsilon_{\text{eff}}\) and \(Z_0\) are constant with frequency which is a classic approximation for quasi-TEM lines, the corresponding values of \(L_A\) and \(C_0\) can then be obtained from (1) and (2).

### III. RCS MEASUREMENT

#### A. Realized scatterers

Two series of resonant scatterers having different geometrical dimensions have been realized for experimental validation of the characterization method. For the series n°1, the geometrical dimensions of the CPS elements are taken identical to the one of [6] for comparison with previously published data. A picture of the scatterers realized for the series n°1 is given in Fig. 4. Until now, only the discontinuities with dimensions given in [6] have been measured in the literature. However they are difficult to realize with good accuracy for low cost realization process which can result in poor quality prototypes, like it can be seen in the expanded view in Fig. 4(b). A second series of resonators (series n°2) has been designed to have geometrical dimensions simple to achieve with a chemical etching realization process which can be interesting for future measurement and comparison.

The geometrical parameters of the CPS lines are indicated in Fig. 1 and their values are indicated for both series in Table I. The dielectric substrate of the series n°1 consists in RT-Duroid 6010 of thickness 0.76 mm and permittivity \(\varepsilon_r = 10.2\). The dielectric substrate of the series n°2 consists in RO3003 of thickness 0.76 mm and permittivity \(\varepsilon_r = 3\). The electrical parameters \(\varepsilon_{\text{eff}}\) and \(Z_0\) in Table I are calculated from the closed form equations given in [16] which are generally considered accurate for quasi-TEM lines.

The series n°1 is composed of 4 Loop scatterers and 4 C-
like scatterers. The length of the strips has been calculated assuming that the discontinuities behave like perfect SC or OC. The length of the strips and their corresponding approximate resonant frequencies are indicated in Table II. Here, for each couple, the length of the strips are such that \( l_A = 2 \cdot l_B \). As a consequence, \( f_A \) is not exactly equal to \( f_B \) but close enough to it. It is thus assumed that \( \Delta l_s(f_A) = \Delta l_s(f_B) \). Solving (9) thus gives an approximate value \( \Delta l_\lambda(f_B) \). It is easy to show from (8)-(9) that the error on \( \Delta l_\lambda \) can be expressed as:

\[
\Delta l_\lambda(f_B) - \Delta l_\lambda(f_B) = \Delta l_s(f_B) - \Delta l_s(f_B) \tag{10}
\]

From simulations, we have observed that the approximate approach gives a maximum error of 3% on \( \Delta l_\lambda \) compared to the rigorous method for the frequency range of interest.

The series n°2 is composed of 6 Loop scatterers and 6 C-like scatterers. The lengths of the resonators have been chosen to obtain exactly \( f_A = f_B \). Fifteen EM simulations have been performed for each resonator to determine the curves of the resonance frequency in function of the physical length presented Fig. 5. The simulation results are compared to the perfect SC and OC models. Six couples of scatterers having the same resonance frequencies have been determined based on this parametric study. The resonance frequencies and associated lengths of the realized scatterers are indicated in table II.

The simulations have been performed using the time domain solver of the commercial full-wave simulator CST-Microwave-Studio 2016. A plane wave port is placed at a distance \( d = 1 \, \text{m} \) from the resonator and a pulse of 1W is delivered in the frequency band 0 GHz - 20 GHz. A typical RCS level of −30 dBsm has been computed for the two scatterers at resonance for both series. It can be seen from simulations that the re-radiation pattern of the scatterers is nearly isotropic for small values of the gap \( g \). The opposite current flows arising along the strips indicate a negligible horizontal component of the backscattered E-field (-150 dBsm in simulation). The re-radiation properties of the C-like scatterer have been studied in detail in [17]. There is no detailed study about the Loop used as a scatterer in the literature but simulations are showing a similar behavior for both kinds of scatterers.

B. Extraction of the natural frequencies

The extraction of the lumped element values relies on the accurate measurement of the resonance frequency of the scatterers. It is thus necessary to ensure a robust detection which does not depends on environmental factors.

The singularity expansion method (SEM) [18] is well adapted to the description of resonant target. It is based on the observation that the scattered field response of a conducting object in the late time can be written as a sum of damped sinusoids like:

\[
r(t) = \sum_{n=1}^{N} a_n e^{\sigma_n t} \cos(\omega_n t + \phi_n), \quad t > T_L
\]

Where \( T_L \) is the beginning of the late time response, \( a_n \) and \( \phi_n \) are the aspect dependent amplitude and phase of the \( n \)th mode, and \( s_n = \sigma_n + j\omega_n \) is the complex natural resonance associated to the \( n \)th mode. In (11), only \( N \) resonant modes are assumed excited by the incident field waveform. A major finding of the SEM theory is that the natural resonances are not dependent on excitation or aspect. The set of natural frequencies is unique to a specific target and provides an interesting basis for target identification [18]. Simple resonant scatterers like the Loop or the C-like scatterers can be assimilated to a single scattering center and the summation (11) thus reduces to a single term. In this simple case, the natural frequency corresponds to the frequencies of the first resonant mode \( f_A \) and \( f_B \) appearing in (8)-(9).

Fig. 6. Measured spectrograms of scatterers operating around 7 GHz. (a) Loop scatterer. (b) C-like scatterer. The specular reflection due to the dielectric substrate is observed for time inferior to 12 ns and can shift the resonant frequency of the scatterers. A time-frequency window (in black) is applied to recover the natural resonance of the scatterer.
During the early-time of the response, the RCS of the resonator is comparable to the one of the dielectric substrate and a shift of the resonance frequency is observed due to this additional contribution. A method to recover the natural resonance is to observe the spectrogram of the signal and to isolate the resonant part (late-time) from the specular response of the substrate (early-time) by application of a time-frequency window [19]. Measured spectrograms of the loop and the C-like scatterers operating around 7 GHz (series n°1) are presented in Fig. 6. The specular reflection due to the dielectric substrate is observed in the region inferior to 12 ns. The resonance lasts longer than the specular reflection (approximately until 20 ns) and the time window is chosen to keep only the resonant part of the signal. In this manner, the natural resonance frequency of the scatterer is obtained. Application examples of this extraction method including discussion about the nature and size of the time window are given in [20].

C. Measurement Results

Measurements are performed in the frequency domain in an anechoic chamber, see Fig. 7, with the Agilent PNA Network Analyzer N5222A in bi-static configuration for the vertical polarization. The power delivered by the vector network analyzer is 0 dBm in the frequency band from 2 GHz to 8 GHz. The two horn antennas have a gain of 12 dBi within the frequency band of interest. The spacing between the antennas is e = 30 cm and the distance between the tag and the antennas is r = 60 cm. Using the coordinate system of Fig. 1, the aspect angles for the measurement are given by θ = 90° and ϕ = ±15°. An isolation measurement and a reference measurement with a metallic plate having a known RCS were performed for calibration [21].

The natural frequencies of the realized scatterers are extracted using the procedure described in the last section. The measured resonant frequency of the Loop is used to solve (8) which determines ΔLg. In the same manner the resonant frequency measured for the C-like scatterers is used along with the value of ΔLg in (9) to determine ΔLp. The corresponding lumped element values are then calculated with (1)-(2).

The measurement results obtained for the series n°1 are presented Fig. 8. The normalized reactance obtained in simulation and measurements for the SC discontinuities is compared to other results from previously published studies [6]–[9] in Fig. 8(a). A good agreement is observed between our results, quasi-static theoretical predictions and measurements. The agreement remains acceptable with the other extraction methods. A maximum relative error of 13% is obtained at 2.5 GHz. The relative error is inferior to 6 % for other frequencies. Fig. 8(b) gives a comparison between measurement results and theory can be explained by the poor quality of the realized prototypes, like it can be seen in Fig. 4(b). Furthermore, the derivation of ΔLg depends directly on the assessment of ΔLg. Therefore it cumulates the inaccuracies in the realization of the two scatterers. A better agreement between simulations and measurements would certainly be obtained with a more accurate realization process. The measurement results obtained for the series n°2 are compared with simulation Fig. 9 with a good agreement. The normalized reactance obtained in simulation and measurements for the SC are compared Fig. 9(a). A maximum relative error of 13% is obtained at 2.5 GHz. The relative error is inferior to 6 % for other frequencies. Fig. 9(b) gives a comparison between
measurements and theory for the normalized reactance of the OC discontinuity. A maximum relative error of 8% is obtained at 2.5 GHz. The results are in a better agreement for series n°2 which can be explained by the fact that the dimensions are simple to realize in practice. This study highlights that the extracted parameter depends strongly on the fabrication error for CPS structures. This problem also appears in [6], [7] but without particular mention.

IV. CONCLUSION

A novel contactless method based on resonators has been proposed for the extraction of CPS discontinuities equivalent lumped elements. Contrarily to what is classically done for microstrip, the resonators are not coupled to a feed line through a gap. The discontinuities are incorporated into simple scatterers whose resonant frequencies are determined by RCS measurements. This feeding eliminates the possible errors caused by the gap uncertainties and do not require any de-embedding. The measurement results have been compared with success to simulations and to available data from previous studies [6]–[9]. A new set of discontinuities has been designed with dimensions simple to realize. This technique could be easily extended to other type of discontinuities like those proposed in [6]. Furthermore, this approach does not necessarily require the use of expensive laboratory device like a VNA as it is possible to use commercial UWB radar with frequency resolutions compatible with the approach [22].

APPENDIX

Annex A: Derivation of the relation between geometrical length and guided wavelength at resonance.

The resonant frequency of the scatterer is obtained from the resonant equation:

\[ \tilde{Z} + \tilde{Z} = 0, \]  

where \( \tilde{Z} \) and \( \tilde{Z} \) are the impedances looking at the left and right, respectively, from an arbitrary reference plane. For convenience of calculation, the reference plane is chosen at the first termination \( y = 0 \) in Fig. 3(c). \( \tilde{Z} \) is thus equal to \( Z_1 \) while \( \tilde{Z} \) is easily obtained from classical TL result, giving the following equality:

\[ Z_1 = -\left[ \frac{Z_2 + jZ_0 \tan(\beta l)}{Z_0 Z_2 + jZ_0 \tan(\beta l)} \right]. \]

where \( Z_1 \) and \( Z_2 \) are the load impedances at both ends of the equivalent circuit, \( Z_0 \) is the characteristic impedance of the CPS, \( \beta \) and \( l \) are the wavenumber and the physical length of the TL as indicated in Fig. 3(c).

In the following, we consider that the terminations are only reactive:

\[ Z_1 = jX_1, \quad Z_2 = jX_2. \]

where \( X_1 \) and \( X_2 \) are reactances. By solving (4) for \( \tan(\beta l) \), we obtain:

\[ \tan(\beta l) = -\frac{Z_0 (X_1 + X_2)}{X_1 X_2 - Z_0^2}. \]

By replacing \( X_1 \) and \( X_2 \) thanks to (1) and (2), a relation between the electrical length of the scatterers to the guided wavelength at resonance \( \lambda_r \) can be found (\( \beta = 2\pi / \lambda_r \))

For the loop scatterer, \( X_1 = X_2 = Z_0 \tan(\beta \Delta l_s) \), which gives:

\[ \tan(\beta l_A) = -\tan(2\beta \Delta l_s), \]

which is solved by:

\[ l_A + 2\Delta l_s = m \lambda_r / 2, \]

where \( m \) is an integer.

For the C-like scatterer, after inserting (1) and (2) into (15), we have:

\[ \tan(\beta l_B) = \frac{1 - \tan(\beta \Delta l_c) \cdot \tan(\beta \Delta l_o)}{\tan(\beta \Delta l_c) + \tan(\beta \Delta l_o)}, \]

where \( l_B \) is the length of the C-like scatterer. Once again, the use of the properties of the tangent function gives:

\[ \tan(\beta l_B) = 1 / \tan[\beta (\Delta l_c + \Delta l_o)] = \tan[\pi / 2 - \beta (\Delta l_s + \Delta l_o)], \]

which is solved by:

\[ l_B + \Delta l_s + \Delta l_o = \lambda_r / 4 + m \lambda_r / 2. \]
REFERENCES


Olivier Rance (S’15) is a PhD student working under the supervision of Dr. Etienne Perret. He received his Master’s degree in Electronic Engineering from the Institute National Polytechnique de Grenoble (Grenoble-INP), and joined the LCIS in 2012. His main research interests are leaky-wave antennas and chipless RFID.

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He is authored and co-authored of more than 120 technical conferences, letters and journal papers, and books. He is IEEE senior member and Technical Program Committee member of the IEEE International Conference on RFID. He was keynote speaker and the chairman of several international symposiums. His research activities cover the electromagnetic modeling of passive devices for millimeter and submillimeter-wave applications. His current research interests are in the field of wireless communications, especially radio frequency identification (RFID) and chipless RFID. His interests also involve advanced computer aided design techniques based on the development of an automated co-design synthesis computational approach. He was named one of MIT Technology Review's French Innovator's under 35 in 2013 for his work on chipless RFID. He is also the recipient of the French’s Innovative techniques for the environment awards in 2013.