Macro-meso models for joint submitted to pyrotechnic shock

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Abstract

The work presented deals with the propagation of pyrotechnical shocks in complex structures and, more specifically, through joints between the stages of the Ariane 5 space launcher. As it is a failure cause for satellite equipment, the National Center for Spatial Studies (CNES) is interested in predicting the hardness levels of the shock. A computational difficulty appears near joints as phenomena deeply depend on fine geometrical and mechanical details that cannot be taken into account in the whole structure model. To carry out the calculation, a two scales strategy is used: a structure scale where the joint appears as a nonlinear interface between shells, depending on a few parameters, and a mesoscopic scale dedicated to the joint where each detail and local physical phenomena can be integrated.

Moreover, an appropriate and efficient strategy is used to take these two scales into account, identify the macro-model parameters and make it reliable. Each scale computation is described and first results are commented.

Keywords: Dynamic; Propagation; Joint; Macro-model; Multi-scale; Identification; Condensed model

1. Industrial context

The document reports on studies carried out in co-operation with the National Center for Spatial Studies (CNES-Evry) in the context of the “pyrotechnic shocks” interest group. The industrial goal is to better understand the shock phenomena due to the stage separation on an Ariane 5 launcher. A typical launcher structure consists of cylindrical stages coupled by bolted joints (Fig. 1).

The separation is achieved by three explosive ropes shearing the bolted joint at a speed of 7100 m/s. The crack generates a shock wave of wide frequency range and high acceleration levels. The hardness of the shock for the equipment is usually measured by shock response spectra (SRS) [1,9].

To perform a correct simulation on the whole structure of the launcher, a special attention must be paid to the joint where shock reduction appears. It is the place for complex propagation and strong nonlinearities so different works are in progress at LMT Cachan to build a joint macro-model, available for standard fast dynamic finite element programs, of which parameters are adjusted from a precise propagation analysis in the bolted joint.

2. Computational strategy

Two scales into the problem can be separated (Fig. 1):

- The launcher scale where the structure can be modeled by a shell assembly.
- The joint scale where nonlinearities and geometrical details need a fine description.

Our goal is to build a macro-model of the joint for the launcher scale computation, based on a few parameters with a strong mechanical meaning. Parameters have to be adjusted to fit the real behavior as well as possible. At this step, experiments would be of great help but in this case, it would be very costly to get enough data and tough to extract pertinent value from sensors. Instead of experiments, a fine 3D model of the joint, including all physical phenomena as friction, unilateral contact or plasticity is used.

Identification consists in a classical iterative method to minimize an error function. A similar approach can be found in [11]. The error function is based on the difference in the SRS responses.

3. Efficient macro-model simulation

The macro-model simulation consists in the calculation of the transmitted and reflected wave generated by an

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Fig. 1. Two scale strategy.

Fig. 2. Interface crossing by finite element method and analytical solution: i = incident, r = reflected, t = transmitted, p = pressure wave, and s = shear wave.

incident wave (Fig. 2). A classical finite element model made of two shells jointed by an interface can get the result, as far as the model takes care of the absorption of waves on each side to avoid a non-physical multi-reflection. Then a tricky job consists in extracting the P (pressure) and S (shear) waves from the known displacement field. This is an inaccurate and lengthy way that is not adapted with an iterative identification procedure.

Finite element calculation spends all efforts in the propagation of waves in shells while the only interesting values are into the interface. As propagated solutions in shells are well known, a costly finite element method is replaced by analytical solutions.

Fig. 2 shows an incident wave split in two transmitted waves (P and S) and two reflected waves. As the speed of the impact point I is fixed by the direction $\vec{n}_{ip}$ of the incident wave, direction of those four new waves can be deduced from the incident wave. For each wave, the displacement

field can be expressed by (c_p and c_s are wave speeds) [5]:

- P wave: $\vec{U}_p(M, t) = \vec{n}_p \cdot f_p(\vec{OM} \cdot \vec{n}_p - c_p \cdot t)$
- S wave: $\vec{U}_s(M, t) = \vec{t}_s \cdot f_s(\vec{OM} \cdot \vec{n}_s - c_s \cdot t)$

As the interface is a link between force and displacement (or speed) on each side, it is necessary to express the force on the border of the shell:

$$\vec{F}(t) = \boldsymbol{\sigma}(t) \cdot \vec{y} = \mathbf{K} \cdot \boldsymbol{\varepsilon}(\vec{U}(t)) \cdot \vec{y} = F \cdot \frac{\partial f}{\partial t}(t)$$

Therefrom, the problem can be expressed with four time functions to determine: $f_{ip}(t)$, $f_{is}(t)$, $f_{rp}(t)$ and $f_{rs}(t)$.

The resolution is processed by L^AIN method where a linear global step consists in the analytical propagation problem in semi-infinite media and a nonlinear local step consists in the interface resolution problem. The robustness of the method allows strong nonlinearities as friction and unilateral contact. The simulation of a macro-model with 5 parameters as shown in Fig. 1 can be solved in less than

Fig. 3. Interaction of substructures and interfaces.

2 s on matlab (1500 times less than FE calculation) on a standard workstation.

4. Meso-model calculation

The joint is studied on a small scale using a 3D meso-model which takes the small dimensions and the material details of the actual joint into account. Appropriate numerical tools are available from previous works: the simulation is carried out with the *QFAST* program [3,8], which uses the *LATIN* method [7]. The calculation is iterative and is performed globally on the whole structure and for the whole time interval. The assembly is decomposed into linear elastic substructures connected with one another through interfaces which incorporate the nonlinear phenomena (Fig. 3). This tool, which is regarded as very robust, is especially well-suited to highly nonlinear problems, such as unilateral contact or friction.

In order to solve the problem associated with the above decomposition, we use a non-incremental approach called the *LATIN* method first proposed by Ladevèze in 1985 (more details can be found in [6,7]). This method gives excellent results for quasi-static loading. Previous works reported computation times divided by 50 for 3D connection problems with many contact surfaces [2].

The *LATIN* method is based on three principles. The first consists of separating the difficulties in order to avoid having to deal with global and nonlinear problems simultaneously. By taking into account the mechanical properties of the equations, these can be split into two groups: the

equations involving the local space variables, which may be nonlinear (the associated space will be called Γ) and the linear equations, which may be global in space (the associated space will be called $\mathbf{A}_d$).

The second principle of the method involves a two-stage iteration scheme which solves each set of equations alternatively. The local stage solves the problem associated with Γ and leads to a non-unique solution; therefore, it is necessary to add other equations (E^+), called search direction equations. The linear global stage solves the problem associated with $\mathbf{A}_d$ and leads to an ill-posed problem. It is necessary to add more search direction equations (E^-).

The third principle of the method lies in the resolution of the global problem. A major characteristic of this computational technique is that the global operators involved at this stage remain constant throughout the iterations [8].

Fig. 4 shows a typical result of the propagation phenomena. The load is applied on the top and run at 7100 m/s. A transmitted and reflected wave can be noticed. Absorbing boundary conditions on each side avoid multiple reflection [4,10].

5. First results of identification

Identification process is a classic iterative scheme. Several test shocks are chosen and should be representative of pyrotechnic shocks range. For each, meso-model response is calculated and gives the reference response. An iterative procedure then optimizes parameters so that the macro-model response fits the reference response.

Fig. 4. Propagation phenomena in the meso-model of the joint.

Fig. 5. Identification result of a 1D model (left) and 2D model (right).

Three main points will ensure the success and quality of the macro-model:

- Choice of the macro-model component: it is fundamental to include all the major physical phenomena in the macro-model; in this case, unilateral contact, friction, bolt stiffness, ect. . .
- Choice of the test shocks: those shocks must be representative of pyrotechnical shocks. The comparison is done by way of SRS. Giving a typical SRS, an algorithm can generate several different shocks with the same SRS.
- Choice of the gap measurement between macro-model and meso-model responses: this gap will be the error quantification to minimize. This quantity must be pertinent with regard to shocks. Once again, the maximum distance between SRS response is used.

A simplex classical algorithm that does not involve gradients is used for the minimization. This method has first been tested on a 1D optimization of macro-model. Ten test shocks are used for identification (three are plotted on Fig. 5) and a good result of 10% medium error on SRS is obtained (Fig. 5). A first 2D identification led, on one test signal, to a 12% error (Fig. 5). This encouraging result will be followed with complete 2D identification and testing.

6. Conclusion

A two-scale approach of the modeling of a joint submitted to pyrotechnic shock has been presented. Several difficulties in the calculation and identification process have led to special efficient techniques that seems to be a promising approach.

To complete FE simulation, experimental tests are currently performed by the CNES “pyrotechnical shocks”

interest group. The final macro-model should easily be implemented in a classic explicit FR code.

Acknowledgements

The financial support of this work by the CNES-evry (DT99/CNES/5704) and the French Ministry of Education is gratefully acknowledged.

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