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3D-Aggregate Quantitative Imaging: Experimental Results and Polarization Effects
Christelle Eyraud, Jean-Michel Geffrin, and Amélie Litman, Member, IEEE

Abstract—We present reconstructions of an aggregate of small spheres from experimental scattered fields using a working frequency of 18 GHz. This target presents at the same time a complex 3D shape and a low-contrast permittivity. Concerted experimental and numerical efforts have enabled to obtain accurate reconstructions. In particular, we took into account the real random noise via a Bayesian framework. Reconstructions have been realized with scattered fields measured in different polarization cases; the results are compared and discussed.

Index Terms—Aggregate, Bayesian formulation, microwave analogy, microwave imaging, 3D inverse scattering problem.

I. INTRODUCTION

ELECTROMAGNETIC wave probing is a useful tool to obtain information from an object in a non-destructive way. Indeed, the physical features of an unknown target (position, shape, size, complex permittivity) can be retrieved from its scattered field thanks to the resolution of an inverse problem. This implies accurate measurements of the scattered field associated with an efficient inversion algorithm.

Nowadays, as several inversion procedures have been extended to 3D configurations (see [1]–[3] for example) and as scattered fields of 3D-objects can be precisely measured [4], [5], the characterization of complex shaped 3D-targets can thus be realized. In particular, different inversion algorithms were recently tested against the same experimental dataset (3D Fresnel database) measured with the Institut Fresnel setup and the results were published in a special section of the Inverse Problems review [6].

In the present work, we are interested in a specific target which presents a particularly complex geometry including small details: an aggregate of spheres. To our knowledge, it is the first time that a target with such a complex geometry has been reconstructed with such a high frequency (18 GHz). To give an example, in the special section of the 3D Fresnel database [5], [6], the highest frequency was 8 GHz. To reach such a goal, we took profit of a joint work between the inversion developments [6], [9], [10]. Here, we present reconstructions with different polarization cases and we discuss the interest and relevance of each case either taking each one separately or using various combinations.

This paper is organized as follows. In Section II, the aggregate and its specific characteristics are presented. Sections III and IV explain the experimental study and the inversion procedure, each one being influenced by the other. The results of the reconstructions are shown in Section V with a discussion on the polarization inference on the reconstructions. Finally, some concluding remarks are provided in Section VI.

II. THE AGGREGATE

The studied target is an aggregate of spheres (Fig. 1), composed by 74 dielectric spheres of 2.5 mm radius. It has a fractal dimension of 1.7 [11]. The spheres are made of polyacetal and the relative permittivity of this material was measured with the commercial kit Epsimu [12], [13]. The relative permittivity value was then refined comparing diffraction measurements of a single 50 mm diameter sphere made of the same material and Mie computations [14], [15] with a minimization process. The final value was found to be purely real and equal to $2.85\pm0.01$. More details concerning this object and accurate comparisons between simulated and experimental scattered fields can be
found in [16] and on this website: http://www.fresnel.fr/3Ddirect/database.php.

This aggregate presents several singular characteristics. Its geometry is entirely non-symmetrical (no symmetry axis or plane). This implies that this target necessitates measurements for several incident and receiver directions to provide the possibility of a good characterization. It is a depolarizing target [17] and thus that measurements of different polarization cases are interesting. These measurements can be realized with our experimental setup almost all around the 2 m radius sphere enclosing the object [5].

This target has a very low density, i.e., the volume of the material represents less than 3% of the volume of the minimum sphere including the target, so it is globally a low-contrasted object. This involves that high accuracy on the measured scattered fields is definitely needed. Taking profit of our previous works [4], we are able to eliminate the systematic errors, to correct for the drift errors [18] and to estimate the remnant noise (random noise) on each measured point [19].

This object includes small details compared to its size, i.e., each sphere diameter represents 1/20 of the diameter of the minimum sphere enclosing the target. As these spheres have small dimensions, we chose to realize the inversion process using scattered fields measured at a frequency such that the individual sphere has a diameter of about $\lambda/3$ (18 GHz) to be able to retrieve such a fine geometry. On the other hand, the perturbations disturbing the scattered field are becoming more important and all the geometrical imprecisions are more sensitive when the frequency increases. In particular, the random noise increases, thus it is specially important to take this noise into account in the inversion process.

### III. Experimental Study

#### A. System Overview

The measurements were performed in the faradized anechoic chamber (14.5 m $\times$ 6.5 m $\times$ 6.5 m) of the C.C.R.M. (Centre Commun de Ressources en Microondes) in Marseille (Fig. 2), already described in various papers [10], [20]. The equipment is based on a Vector Network Analyzer (HP 8510 B), used in a multiple sources configuration with two synthesizers and two external mixers.

This setup is represented on Fig. 2(a). The transmitting antenna can be moved along the vertical arch in a vertical plane ($\phi$ angle). The target – placed at the top of a cylindrical expanded polystyrene mast at the position (0, 0, 0) – can rotate on itself around the vertical z-axis ($\theta$ angle) which allows to increase the number of incident directions. ($e_{\theta}$, $e_{\phi}$) are the basis vectors of a spherical coordinate system (Fig. 2(b)), where the conventions for the polar and azimuthal angle notations ($\theta$, $\phi$) defined in [21]. To reduce the measurement time, two antennas (in orthogonal polarization) are placed in two different positions on the vertical arch and are selected alternatively as sources using a microwave switch, i.e., for each receiver position, the field is measured successively from two different illuminations without mechanical movements. The receiving antenna is positioned on an arm and can rotate in the horizontal plane $x0y$ around the target ($\theta$ angle). The distance between the source and the object (resp. between the receiver and the object) is 1629 $\pm$ 2 mm (resp. 1702 $\pm$ 2 mm).

The transmitting and the receiving antennas are two high gain pyramidal horns (ARA MWH1826B) – to have a scattered field signal as high as possible – with a working frequency between 18 GHz and 26 GHz. The cable lengths and the power levels have been optimized so that the level of the forward scattering signal is just below the mixer saturation. These antennas are linearly polarized and can be rotated on their support to change the polarization direction (along $e_{\theta}$ or $e_{\phi}$).

#### B. Choice of the Experimental Parameters

As this target is a depolarizing one, its scattered field was measured in the four polarization cases: $\phi_{\theta}$, $\theta_{\phi}$, $\theta_{\phi}$ and $\phi_{\theta}$ ($h_{\theta}$ means that the emitter has the polarization $e_{\theta}$ and the receiver is sensitive to the polarization $e_{\phi}$).

The angular step of the transmitting antenna movement and of the receiving one were chosen in accordance with the maximum spatial frequency of the scattered field at 18 GHz. Indeed, the scattered field $E_{\phi}$ of bounded induced sources presents the property of having a limited spectral bandwidth in a spherical configuration when this field is observed far enough from the target [22]. A minimum spatial sampling angle can thus be deduced for the emitter and for the receiver allowing to measure all available information on the target. Indeed, the fields were measured with the step $\Delta \theta = 5^\circ$ on 53 equidistant points placed on a circle in the horizontal plane $x0y$ – $100^\circ$ are excluded due to mechanical impossibilities. The aggregate was illuminated with 117 incident directions. For this, the transmitting antenna was moved with the step $\Delta \phi = 10^\circ$ in the vertical plane realizing 13 incidences and furthermore, for each of those positions, 9 more incidences were created by rotating the target around the $z$-axis with the step $\Delta \theta = 40^\circ$. This last step is larger than the maximum sampling criterion ($11^\circ$), but this choice was made to keep a reasonable measurement time.

Finally, a calibration process, using a single reference target (a metallic sphere), estimated in the $\phi_{\theta}$ case only for sake of simplicity [4], [23], was applied to every scattered field keeping the same coefficient in each polarization case.

### IV. Inversion Procedure

The experimental scattered fields, measured on the antennas sphere (far away from the target), are allowing to deduce the
3D relative permittivity map in the domain \( \Omega \) (box including the target) thanks to an appropriate inversion procedure. A Bayesian formulation was used to balance each data according to its accuracy and to describe all available information. To solve this non-linear inverse problem, an iterative scheme is adopted and this necessitates an accurate forward problem.

A. Forward Problem

We calculate the scattering of a 3D inhomogeneous structure in the frequency domain using a volume integral formulation [24]. The field inside the imaging domain is computed with a biconjugate gradient stabilized FFT method [25] based on a 1D FFT to improve the calculation speed [26]. The computation complexity is then of \( O(N \log_2 N) \) and the memory requirement is \( O(N) \). The free space dyadic Green tensor is used.

B. Inversion Algorithm

We chose to introduce information on the effective random noise which disturbs the scattered field measurements in the inversion procedure using a Bayesian formulation. The experimental noise was characterized on the measured fields (the total and incident fields) as explained in a previous study [19]. The results established that the deduced noise on the scattered field can be described by an additive complex random variable whose real and imaginary parts are normally distributed and with associated standard deviations depending on the total field magnitude, on the incident field magnitude and on the frequency. The noise disturbing the scattered field data, for a given frequency, depends thus strongly on the incident direction and on the receiver position. Indeed, the standard deviations can vary with the knowledge of the measured scattered field and of the measured one is balanced with a weighting coefficient – depending on the potential noise disturbing the measurement on this point.

The 3D-complex relative permittivity map of the considered domain \( \Omega \) was obtained through an iterative procedure which minimizes the cost-functional \( F \) of (2). The minimization is realized with a conjugate gradient algorithm using a positivity constraint and with the standard Polak-Ribiere coefficients [31], [32]. More details about this algorithm can be found in [30].

C. Reconstruction Error Quantification

To give a criterion of the reconstruction quality, we have considered different error functions comparing the reconstructed 3D relative permittivity maps and the true one (due to the difficulty to extract a significative one). It can be noticed that if there is a difference – even weak – between the expected position of the aggregate (considered in the following criteria calculations) and its real position in the experiments, the influence on the criteria can be dramatically strong. Thus, the first step consists in detecting this possible geometrical shift.

1) Estimation of the Real Target Position: We have determined the real position of the center of mass of the aggregate \( \mathbf{d} = (x_d, y_d, z_d) \) using a 3D cross correlation between the reconstructed contrast map \( \varepsilon_r + 1 \) and the expected one

\[
R_{\text{cr}}(\mathbf{d}) = \sum_{\mathbf{r}} (\varepsilon_r^{\text{true}}(\mathbf{r}) - 1)(\varepsilon_r^{\text{reco}}(\mathbf{d}) - 1) \quad (3)
\]

where \( \varepsilon_r^{\text{true}} \) is the true relative permittivity value, \( \varepsilon_r^{\text{reco}} \) is the reconstructed value at the end of the inversion process and \( \mathbf{r} \) describes the position of the considered cell in the \( \Omega \) domain. It can be noticed that the cross correlation has been calculated on the \( \varepsilon_r + 1 \) maps (and not on the \( \varepsilon_r \) maps) in order to compare only the voxels where some material can be found.

2) Relative Permittivity Map Error Criteria: Once this operation has been realized, we can evaluate the similarity between the two maps. We have considered here four different criteria (the first and the second are standard ones and we propose also two other ones). The first one (resp. second), is a comparison between the two relative permittivity maps with a relative L2 norm (resp. L1 norm)

\[
C_i^{L2} = \frac{\| \varepsilon_r^{\text{true}} - \varepsilon_r^{\text{reco}} \|_{L2}}{\varepsilon_r} \quad i = 1,2 \quad (4)
\]

The third criterion \( C^{CC} \), corresponds to the expression of the cross correlation normalized on the contrast maps – for the best position \( \mathbf{d}^* \) (previously determined)

\[
C^{CC} = \frac{C_{\text{cr}}(\mathbf{d}^*)}{C_{\text{cr}}(\mathbf{0})}. \quad (5)
\]

Its interest is to provide a value linked to the similarity between the two maps comparing only the voxels containing some material with respect to the true map.

To consider the reconstructed relative permittivity also for the empty voxels, we consider a fourth criterion, \( C^e \) which corresponds to the correlation between the two maps

\[
C^e = \frac{C_{\text{cr}}(\varepsilon_r^{\text{reco}}, \varepsilon_r^{\text{true}})}{\sqrt{\text{Var}(\varepsilon_r^{\text{reco}}) \text{Var}(\varepsilon_r^{\text{true}})}} \quad (6)
\]

We have det
where $\text{Cov}(u, v)$ is the covariance between $u$ and $v$ and $\text{Var}(u)$ the variance of $u$. All those parameters have been estimated for each of the reconstructions presented below.

The more similar the two maps are, (i) the closer to 0 the criteria $C_{L1}$ and $C_{L2}$ are, (ii) the closer to 1 the criteria $C^{cc}$ and $C^c$ are.

**D. Inversion Parameters**

The initial guess of the relative permittivity map was chosen to be equal to the one of the background medium (more precisely, a small constant value was added to avoid the case where the gradients vanish due to the positive constraint expression). The inversion process was stopped when the cost functional is below $3\sigma$ ($\sigma$ being the average of the measured noise standard deviation values). For the following reconstructions, the convergence was reached at (or before) the 3rd iteration. An investigated domain $\Omega$ of $(75 \times 50 \times 75)$ mm$^3$ centered at $(x = 0, y = 0, z = 0)$ mm was considered with a cubic lattice spacing equal to 1.6 mm ($\lambda/10$).

**V. Results**

The inversions were performed in three cases: (i) with or without any information on the real random noise, (ii) separately for different polarization cases of the measured scattered fields and (iii) for several combined polarization cases of the measured scattered fields. The different reconstructions are presented and discussed in this section. Note that, for every reconstruction, the real position of the object was found with the cross-correlation criterion.

**A. Target Position**

The cross-correlation criterion $R_{txt}$ (3) allows to determine the real position that the aggregate had during the experiments. For all the polarization cases, the same position was found: $d^* = (1.3, -1.2, 2.9)$ mm. This positioning error is very small considering the fact that the target has to be placed at the center $(0,0,0)$ mm of our setup, a 4000 mm diameter sphere.

**B. Single Polarization Cases**

1) $\phi\phi$ Polarization: In this section, we present the reconstruction results obtained using the scattered fields in the $\phi\phi$ polarization case only.

The first reconstruction was realized without any use of the random noise knowledge, i.e., which amounts to taking $\sigma_{\text{Re}(R_0, R_T)} = \sigma_{\text{Im}(R_0, R_T)} = 1$ in (2). This reconstruction is presented with a 3D visualization in Fig. 4. For this figure (and all the similar figures in the following), the iso-surface threshold value is taken when the relative permittivity is different from the free space one and the angles plotted at the top of each view correspond to the (azimuth, elevation) coordinates of the viewpoint. This figure has to be compared with the one of the expected aggregate (Fig. 3). This inversion allows to reconstruct a 3D structure but the fine geometry of the aggregate is not really well obtained, i.e., the outlines are not distinct. Moreover, the maximum relative permittivity value of the reconstructed map is weak: 1.94 (the true one being 2.85).

Secondly, we took into account the experimental random noise in the inversion process with the formulation explained in Section IV-B. As it can be seen on Fig. 5, the reconstruction is strongly improved and now the form of the reconstructed object is very close to the real one even if parts of the target (4 spheres) are still missing. The relative permittivity of the target is also very close to the real one even if parts of the target (4 spheres) are still missing. The relative permittivity of the target is also very close to the real one even if parts of the target (4 spheres) are still missing. The relative permittivity of the target is also very close to the real one even if parts of the target (4 spheres) are still missing. The relative permittivity of the target is also very close to the real one even if parts of the target (4 spheres) are still missing.

Fig. 3. Real aggregate representation with an iso-surface threshold function.

Fig. 4. Reconstruction result at 18 GHz using only the scattered field in the $\phi\phi$ polarization and without taking into account the random noise.

Fig. 5. Reconstruction result at 18 GHz using only the scattered field in the $\phi\phi$ polarization and taking into account the random noise.

Fig. 6. Relative permittivity maps reconstructed in the $\sigma_{\phi\phi}$ plane at 18 GHz and at several altitudes $z$ using scattered fields in the $\phi\phi$ polarization and taking into account the random noise (the colorbar/grayscale is the same for the three plots). (a) $z = -20$ mm. (b) $z = -15$ mm. (c) $z = +21$ mm.
quantify the reconstruction error is improved (Table I, line 2). This means that both permittivity estimations of the voxels with and without material are better.

Thus, all the other reconstructions presented in this paper, were obtained taking into account the random noise in the procedure as this knowledge of the real noise does improve the results.

2) \(\phi\theta\) Polarization: We now only consider the data measured in the \(\phi\theta\) polarization case. As it can be seen in Fig. 7, the horizontal zones are preferentially and almost solely reconstructed. The maximum value of the reconstructed relative permittivity is weak (1.4). For these two reasons, the \(C^{x_c}\) and \(C^c\) criteria are low (Table I, line 3). The surprising values of the \(C^{L2}\) and \(C^{L1}\) criteria are due to the fact that these criteria are mainly sensitive to the great number of well reconstructed empty voxels. Physical reasoning is derived in Section V-D to understand the obtained results.

C. Two Polarization Cases

In this paragraph, we consider two polarization cases together in the inversion process. As the \(\phi\theta\) polarization brings more information than the \(\phi\phi\) one, we have kept this polarization and we have tried to add another polarization to see if we can improve the results.

1) \(\phi\phi\) and \(\phi\theta\) Polarizations: In this case, the scattered field in the \(\phi\phi\) polarization is used in combination with the field measured in the \(\phi\theta\) case. As it can be seen on Fig. 8, the reconstruction is very close to the one obtained considering only the scattered field in the \(\phi\phi\) polarization. The cross correlation, the correlation, \(L2\)-norm and the \(L1\)-norm criteria are also similar to the ones obtained in the \(\phi\phi\) case (Table I).

2) \(\phi\phi\) and \(\theta\theta\) Polarizations: In this case, the scattered field in the \(\phi\phi\) polarization is used in combination with the measured field in the \(\theta\theta\) case. The reconstruction is presented in the Figs. 9–10. As it can be seen, the voxels including material are more precisely reconstructed (in comparison with the \(\phi\phi\) polarization case) and the relative permittivity value is also higher in these zones. The cross correlation criterion \(C^{x_c}\) is also improved compared to the \(\phi\phi\) polarization case (Table I). It can be noticed that some artefacts did appear, but their values are very weak (the relative permittivity values of these voxels being less than 1.2) and they are emphasized by the threshold representation. Nevertheless, their influences are also visible on the \(C^c\), \(C^{L2}\) and \(C^{L1}\) criteria which are worse in this case.

The combination of the \(\theta\theta\) polarization with the \(\phi\phi\) one is not presented here because this is not an interesting case as explained in Section V-D.

D. Discussion of the Polarization Interest

We propose here two tools to analyze and understand the reconstructions obtained with the various polarizations.

1) First Tool: The first interpretation (Fig. 11) is based on a representation of the different incident field vectors (in black) for all the source positions. To clarify the representation, only the end of these vectors are plotted (with the + marker) – each vector being brought back at the center of the setup. The projection of the scattered field vector which is measured by the receiving antenna is overlaid (in cyan/gray) for all the receiver positions. These vectors are normalized in order to focus on information provided by the projection angle. This representation was realized for the four polarization cases.

2) Second Tool: The second tool concerns the induced currents in the \(\Omega\) zone. It therefore takes into account the depolar-
with the marker source and receiver positions – each vector being brought back at the center of vectors (black) and of the received scattered vectors (cyan/gray) for all the directions (7) for the four polarization cases and we have plotted them in terms of histograms (Fig. 12).

Fig. 11. Representation for $\phi \theta$, $\phi \theta$ and $\theta \phi$ polarizations of the incident vectors (black) and of the received scattered vectors (cyan/gray) for all the source and receiver positions – each vector being brought back at the center of the setup – (for the incident vectors, only the end of these vectors are plotted with the marker $+$).

Fig. 12. Histogram of the normalized induced currents projected on the receiver polarization direction for the four polarization cases $I^{\phi \phi}$, $I^{\phi \theta}$, $I^{\theta \phi}$ and $I^{\theta \theta}$ in (7).

To summarize this part, we can remark that these results are not intuitive. Indeed, in our configuration, due to the sources and receivers displacements, the co-polarizations are not intuitive. Indeed, in our configuration, due to the sources and components along the same polarization vector than in the $\phi \theta$ case – thus the scattered ones.

3) Discussion: We can first observe that the incident polarization along $\phi$ allows to double the number of incident polarization directions (Fig. 11(a)) – compared to the incident polarization along $\theta$ (Fig. 11(d)). Furthermore, the $\phi \phi$ case is also the case containing the highest values of the induced currents (Fig. 12) and thus the signal level is higher and less sensitive to noise [19]. In consequence, the most interesting polarization case is $\phi \phi$. This is in agreement with the quality of the reconstruction obtained using this polarization (Section V-B.I).

Looking to the $\theta \theta$ case (Fig. 11(d)–(f)), the incident field vector is contained in the $x0y$ plane for all the source positions. Moreover, all the receivers are only sensitive to the fields contained in the $x0y$ plane. Thus, it seems natural that the horizontal geometrical zones of the object are preferentially reconstructed (Section V-B.II). In comparison, it can be noticed that in the $\phi \phi$ case, even if the scattered field is always measured along the $z$ axis, the incident vector has both components in the $x0y$ plane and components along the $z$ axis (Fig. 11(a)–(c)).

Considering now the reconstruction with the $\phi \phi$ and the $\theta \theta$ polarizations, we can first note that this combination does not add new incident direction in comparison with the $\phi \phi$ case (Fig. 11(a)–(f)). Looking then to the induced currents (Fig. 12), we can see that, contrarily to our first intuition, the $\theta \theta$ case contains only middle range values. These two points can explain why we did not see real improvements in the reconstructions when adding the $\theta \theta$ fields to the $\phi \phi$ ones.

Considering the reconstructions obtained with the $\phi \theta$ and the $\phi \phi$ measurements, it appears that the $\phi \theta$ data are bringing new – non redundant – information on the object (Fig. 11(g)–(i)), with respect to the $\phi \phi$ measurement (Fig. 11(a)–(c)). Indeed, in the present case, for the $\phi$ incident wave polarization, the scattered field is measured along the two orthogonal polarizations $\phi$ and $\theta$ – instead of only the $\phi$ one in the $\phi \phi$ case – thus the scattered vector is entirely measured on the receivers for a given illumination. This can explain the improvement of the reconstruction. It can be furthermore noticed that all the incident vector directions in the $\theta \theta$ case are contained in the $\phi \theta$ case as well as all the receiving vector projections.

Finally, looking to the Fig. 11(j)–(l), in the $\theta \phi$ polarization case, (i) the incident and the receiver field vector are always orthogonal, (ii) the target is illuminated with polarization vectors already contained in the $\phi \phi$ polarization and the field is received along the same polarization vector than in the $\phi \phi$ case. Moreover, considering the induced currents, this polarization contains only very few non negligible values (Fig. 12). So, for targets which are not highly depolarizing objects – as the present one, the $\theta \phi$ polarization measurement is not interesting and can be omitted. This can allow to remove a quarter of the measurement time.

To summarize this part, we can remark that these results are not intuitive. Indeed, in our configuration, due to the sources and receivers displacements, the co-polarizations $\phi \phi$ and $\theta \theta$ are not equivalent at all. Moreover it is more useful to add the cross-polarization $\phi \theta$, than the co-polarization $\theta \theta$, to the $\phi \phi$ in this case.

VI. CONCLUSION

In this paper, our work is based on a good complementarity between the numerical part (positive constraint, Bayesian approach) and the experimental part (number of measurements, calibration, precision of the measurements). This allows to realize faithful reconstructions from measured data of a 3D complex shape target which is, in the present case, an aggregate of 74 spheres. We have also performed similar reconstructions of this object from synthetically generated data – using the same positions of the transmitters/receivers than the ones used in the...
experiments – and as the results are very close to the ones obtained with the measurements, this tends to demonstrate that the concerted experimental and numerical efforts have been properly made.

The evaluation of the reconstructions is not a trivial problem. Four criteria have been considered to evaluate the results. The usually adopted criteria (relative L1 and L2-norms) are not very adapted to evaluate the quality of the reconstruction of the present target. Indeed, their values are particularly dependent on the reconstruction of the empty voxels which are not the most interesting voxels. For these two reasons, we have proposed two other criteria: the cross-correlation $C^{ex}$ and the correlation $C^r$. Their variations are more significant and in particular the $C^{ex}$ allows to compare only the voxels within the material.

In this study, inversions have been presented using experimental scattered fields, measured with different polarizations. The results have shown that the choice of the polarizations has a great influence on the reconstruction results and the more the polarizations of the emitter and of the receiver are describing a diversity of directions, the better the results are. With our setup, the $\phi$ polarization is the most interesting case as it contains a larger diversity of polarization directions of the incident wave and because the measured values are relatively high (compared to the other polarization cases). If a second polarization case can be added, the most favorable one seems to be the $\phi$ polarization case even if it corresponds generally to weaker measurement values. It would be interesting, in future work, to corroborate these conclusions with the inversion results obtained with other complex-shape targets.

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REFERENCES
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