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SAR TOMOGRAPHY OF URBAN AREAS:
3D REGULARIZED INVERSION IN THE SCENE GEOMETRY

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ABSTRACT
Starting from a stack of co-registered SAR images in interferometric configuration, SAR tomography performs a reconstruction of the reflectivity of scatterers in 3-D. Scatterers seen within the same resolution cell in each SAR image can be separated by jointly unmixing the SAR complex amplitude observed throughout the stack. In urban areas, Compress Sensing (CS) approaches have been applied to achieve super-resolution in the estimation of the position of the scatterers. However, even if all the local information coming from a stack at a given pixel is used, the structural information that is inherent to the image is not directly used to improve the rendering of the scene. This paper addresses the problem of adding structural constraints to sparse tomographic reconstructions of urban areas. We derive an algorithm allowing the inversion of tomographic data under structural constraints and illustrate its performances on a stack of Spotlight TerraSAR-X images.

Index Terms— SAR tomography, structural information, spatial regularization

1. INTRODUCTION
SAR tomography is the extension of the 2-D SAR imaging to three dimensions. As conventional 2-D SAR imaging uses a synthetic aperture in azimuth direction, 3-D SAR imaging is performed by a synthetic aperture in the elevation direction by collecting several images from parallel tracks. Using multi-baseline interferometry techniques on the well-calibrated SAR images stack, it is possible to retrieve the localization of the scatterers in the third dimension. This approach allows separating scatterers mapped in the same resolution cell, which is likely to happen on the dense urban area due to the layover phenomenon.

To perform 3-D SAR focusing, application of the inverse discrete Fourier transform gives a resolution inversely propo-

\begin{equation}
\varphi_n(x, r) = \int_{(y, z) \in \Delta(x, r)} u(x, y, z) \exp(-j \xi_n h(y, z)) \, dy \, dz + n
\end{equation}
3. TOMOGRAPHIC INVERSION

In this part we will derive the inversion of equation (3) using some basic priors on the urban topography. To achieve super resolution, we will have a number of unknowns variables far more important than the size of \( \mathbf{v} \). To be able to estimate \( \mathbf{v} \) we will add two constraints. First, we will assume that the 3-D scene is sparse which is the same hypothesis as in CS. Second, we will make the assumption that the objects are smooth in the \( x, y \) and \( z \) directions. Those hypothesis express the fact walls and roofs are seen as punctual objects in at least one direction and are smooth in the other two directions. We then want to solve the following minimization problem

\[
\hat{\mathbf{u}} = \arg\min_{\mathbf{u}} \left\| \mathbf{\Phi} \mathbf{u} - \mathbf{v} \right\|_2^2 + \mathcal{R}(\mathbf{u})
\]

with

\[
\mathcal{R}(\mathbf{u}) = \mu_x \cdot \left\| D_x \mathbf{u} \right\|_2^2 + \mu_y \cdot \left\| D_y \mathbf{u} \right\|_2^2 + \mu_z \cdot \left\| D_z \mathbf{u} \right\|_2^2 + \mu_L \cdot \left\| \mathbf{u} \right\|_1
\]

\( \mu_x, \mu_y, \mu_z \) and \( \mu_L \) are the parameters allowing to tune the impact of each term in \( \mathcal{R} \). Here the regularization is applied to the modulus of the 3-D reflectivity. One big reason is that we don’t want to risk to converge to zero as we smooth two neighboring scatterers with opposite phase. The introduction of the modulus add a lot of complexity to this problem even with a relatively simple prior. To be able to solve (4), we introduce two more variables and chose an alternating minimization scheme. We now want to solve

\[
\hat{\mathbf{u}} = \arg\min_{\mathbf{u}} \left\| \mathbf{\Phi} \mathbf{u} - \mathbf{v} \right\|_2^2 + \mathcal{R}(\mathbf{w})
\]

s.t. \( \mathbf{f} = \mathbf{w} \)

The real image \( \mathbf{w} \) will converge to the modulus of the image \( \mathbf{u} \) and the complex image \( \mathbf{f} \) links them. We solve (5) using a modified ADMM [5] algorithm by jointly optimizing over \( \mathbf{u} \) and \( \mathbf{w} \) and updating the two Lagrange multipliers:

- \( \langle \mathbf{\tilde{u}}, \mathbf{\tilde{w}} \rangle \left\{ \frac{1}{2} \left\| \mathbf{\Phi} \mathbf{u} - \mathbf{v} \right\|_2^2 + \beta_1 \left\| \mathbf{\Phi} \mathbf{u} - \mathbf{v} \right\|_2^2 + \beta_2 \left\| \mathbf{w} - \mathbf{f}(\mathbf{u}, \mathbf{w}) \right\|_2^2 + \mathcal{R}(\mathbf{w}) \right\} \)
- \( \mathbf{\tilde{d}_2} \leftarrow \mathbf{\tilde{d}_2} + \mathbf{\tilde{w}} - \mathbf{f}(\mathbf{\tilde{u}}, \mathbf{\tilde{w}}) \)
- \( \mathbf{\tilde{d}_1} \leftarrow \mathbf{\tilde{d}_1} + \mathbf{\tilde{f}(\mathbf{\tilde{u}}, \mathbf{\tilde{w}})} - \mathbf{\tilde{u}} \)
$\beta_1$ and $\beta_2$ are two parameters needed for the optimization and $f(u, w)$ is given by

$$f(u, w) = \left[ \frac{\beta_1 \cdot |u - \hat{d}_1| + \beta_2 \cdot (w + \hat{d}_2)}{\beta_1 + \beta_2} \right]^+ \cdot \exp \left[ i \cdot \arg (u - \hat{d}_1) \right]$$

(7)

The first step in (6) is easy to optimize as it is a sum of quadratic and linear functions. As the modulus is positive, the $\ell_1$ norm can be seen as the sum of all the elements in the vector. The algorithm described in (6) gives a new tool capable to inverse a tomographic problem under structural priors. Even if the model we choose is still simple, it gives good results on urban areas as shown in the next section. As the framework is completely independent of the regularization chosen, the structure of the algorithm can be used to add even more sophisticated priors on the reconstructed data.

4. EXPERIMENTAL RESULT

The algorithm described in the previous section has been implemented and tested on a dataset of 40 TerraSAR-X images over the front de Seine in the south-west of Paris, France. The observed scene is presented Fig. 3. The spatial (orthogonal component) and temporal baseline are shown in Fig. 2. The total spatial baseline span is more than 775m and the total temporal baseline more than 5 years with a large gap of almost two years in it.

Fig. 4 we present the intensity of the 3-D inversion over the Mirabeau Tower and we also plot in Google Hearth the height of the discretized reconstruction obtained by thresholding the intensity. Fig. 5 we present the intensity of the 3-D inversion over the Ministry of Foreign Affairs and the height of the discretized reconstruction in Google Hearth.

5. CONCLUSION

In this paper, we have proposed a new algorithm for the inversion of a stack of tomographic images. In this approach, we add structural constraints on the modulus of the 3-D reflectivity in order to describe more accurately a dense urban scene. This algorithm has been implemented and gives good results on real images. Finally, as the priors we add can be changed, we introduce a framework capable of performing 3-D tomographic inversion under spatial constraint.

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1These data have been provided by the DLR in the framework of the project LAN1746
Fig. 4. (top) Intensity of the 3-D reconstruction of the Mirabeau Tower [6]. (bottom) height of the brightest points in the 3-D reconstruction plotted in Google Hearth.

Fig. 5. (top) Intensity of the 3-D reconstruction of the Ministry of Foreign Affairs [6]. (bottom) height of the brightest points in the 3-D reconstruction plotted in Google Hearth.

6. REFERENCES


