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Linear Hyperfine Tuning of Donor Spins in Silicon Using Hydrostatic Strain

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We experimentally study the coupling of group V donor spins in silicon to mechanical strain, and measure strain-induced frequency shifts that are linear in strain, in contrast to the quadratic dependence predicted by the valley repopulation model (VRM), and therefore orders of magnitude greater than that predicted by the VRM for small strains $|e| < 10^{-5}$. Through both tight-binding and first principles calculations we find that these shifts arise from a linear tuning of the donor hyperfine interaction term by the hydrostatic component of strain and achieve semiquantitative agreement with the experimental values. Our results provide a framework for making quantitative predictions of donor spins in silicon nanostructures, such as those being used to develop silicon-based quantum processors and memories. The strong spin-strain coupling we measure (up to 150 GHz per strain, for Bi donors in Si) offers a method for donor spin tuning—shifting Bi donor electron spins by over a linewidth with a hydrostatic strain of order 10^{-6} —as well as opportunities for coupling to mechanical resonators.

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Donors in silicon present an attractive spin qubit platform, offering amongst the longest coherence times in the solid state [1,2] and single-qubit control with fault-tolerant fidelity [3,4]. As with the conventional semiconductor industry, the majority of efforts in donor-based spin qubits are focused on ³¹P donors [5–12]. The heavier group V donors ⁷⁵As, ¹²¹Sb, and ²⁰⁹Bi have recently received substantial interest [13–19], offering larger nuclear spins (up to $I = 9/2$ for ²⁰⁹Bi) and correspondingly richer Hilbert spaces that enable up to four logical qubits to be represented in a single dopant atom. Furthermore, “atomic clock transitions” have been identified in ²⁰⁹Bi where spin resonance transition frequencies become first-order insensitive to magnetic field noise, resulting in coherence times of up to 3 sec in ²⁸Si [20].

The exploitation of donor spins in silicon as qubits typically requires their incorporation into nano- and micro-electronic devices. This has been used to demonstrate the single-shot read-out of a single ³¹P donor spin using a

tunnel-coupled silicon single-electron transistor [21,22], and to create hybrid devices in which donor spins are coupled to superconducting resonators [23–25] to develop interfaces between microwave photons and solid-state spins. In both cases, the use of metal-oxide-semiconductor (MOS) nanostructures [26], or patterned superconducting films on silicon [27], involves a combination of materials with coefficients of thermal expansion that differ by up to an order of magnitude [28–32]. The presence of strain in the silicon environment around the donor spin is therefore pervasive when studying such nanodevices at cryogenic temperatures. Furthermore, factors such as optimizing spin-resonator coupling or spin-read-out speed motivate the placement of donors close to features such as single-electron transistors [33] or resonator inductor wires [34] where strain is maximal.

Strain modifies the band structure of silicon [35,36], and it has been shown, for example, to contribute to the confinement of single electrons in silicon under nanoscale aluminium gates [37,38]. The donor electron wave function is also modified by strain: following the valley repopulation model (VRM) developed by Wilson and Feher [39] within the framework of effective mass theory, an applied uniaxial strain lifts the degeneracy of the six silicon valleys leading to a mixture of the donor ground state $1s(A_1)$ with the first excited state $1s(E)$. In this excited state, the hyperfine

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coupling between the donor electron and nuclear spin is zero; therefore, the VRM predicts a quadratic reduction in A as a function of uniaxial strain, as well as a strain-induced anisotropic contribution to the electron g factor. Strain-induced perturbations of the donor hyperfine coupling have been observed for P-donor spins in ^{28}Si epilayers, grown on SiGe to yield built-in strains of order 10^{-3} [40]—piezoelectric contacts on such material have been used to modulate this built-in strain to shift the electron spin resonance frequency by up to ~ 400 kHz [41].

In this Letter, we report the observation of a strain-induced shift in the hyperfine coupling of group V donors in silicon that is linear (rather than quadratic), and therefore orders of magnitude greater than that predicted by the valley repopulation model of Wilson and Feher [39] for small strains ($|\epsilon| \lesssim 10^{-5}$). We present experimental studies showing strain tuning of the coherent evolution of each of the group V donor spins (^{31}P , ^{75}As , ^{121}Sb , and ^{209}Bi), extracting the strain-induced shifts of the hyperfine coupling and electron spin g factor for each, and corroborate the results with a combination of both tight binding and density functional theory calculations that reveal the crucial role of hydrostatic strain in this novel mechanism [42]. In addition to providing essential insights for the use of donor spins in nano- and micronscale quantum devices, our results provide a method for linear tuning of the donor hyperfine interaction with coupling strengths of up to 150 GHz/strain for ^{209}Bi donor spins.

The spin Hamiltonian for a group V donor in the presence of an external magnetic field $\mathbf{B} = B_0 \mathbf{z}$ is

$$\hat{\mathcal{H}} = (g_e \mu_B \hat{\mathbf{S}}_z - g_n \mu_N \hat{\mathbf{I}}_z) B_0 + A \hat{\mathbf{S}} \cdot \hat{\mathbf{I}}, \quad (1)$$

where g_e and g_n are, respectively, the electronic and nuclear g factors, μ_B and μ_N are the Bohr and nuclear magnetons, and $\hat{\mathbf{S}}$ and $\hat{\mathbf{I}}$ are the electronic and nuclear spin operators. The Fermi contact hyperfine interaction strength, $A = 1.4754$ GHz in Si:Bi, can be expressed as

$$A = \frac{8\pi}{3} g_0 \mu_B g_n \mu_N |\psi(0)|^2, \quad (2)$$

where $\psi(0)$ represents the amplitude of the electronic wave function at the nucleus and $g_0 = 2.0023$ is the free electron g factor. The eigenstates of this Hamiltonian describe a Hilbert space of dimension $(2S + 1)(2I + 1)$ with $S = 1/2$ and I determined by the nuclear spin species, illustrated for the case of ^{209}Bi :Si in Fig. 1(a). Transitions between these eigenstates obeying the selection rule $(\Delta m_S, \Delta m_I) = (\pm 1, 0)$ in the high field limit can be driven and detected using pulsed electron spin resonance (ESR) [43].

We use samples of isotopically enriched ^{28}Si doped with Bi, Sb, As, and P (see Ref. [44] for more details), mounted with crystal orientation shown in Fig. 1(b). The sample is situated inside a dielectric microwave ESR resonator in an

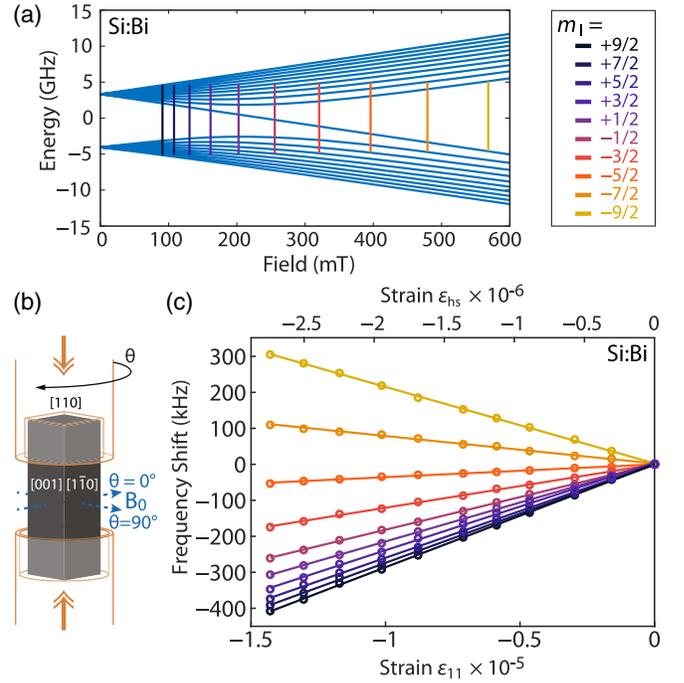


FIG. 1. (a) Energy levels of Si:Bi spin eigenstates as a function of magnetic field, with the ten allowed ESR transitions at 9.7 GHz highlighted and labeled according to their high-field nuclear spin projection m_I . (b) Schematic of experimental setup. The silicon single crystal sample is mounted between two engineered plastic rods with the ability to apply compressive stress. θ , the angle of the applied magnetic field to the [001] direction, can be varied by rotating the sample. (c) Observed linear frequency shifts for each of the ten allowed ESR transitions shown in panel (a), as a function of strain ϵ_{11} , with $\theta = 30^\circ$.

Oxford Instruments CF935 liquid helium flow cryostat, and is held between two plastic (polyether ether ketone) rods whose end faces have been milled using computer numerical control to match the profile of the sample allowing it to be rotated with respect to the magnetic field. Using calibrated masses, a uniaxial stress is applied to the sample perpendicular to the [110] face, via the upper rod, which extends outside the cryostat. The resulting strain tensor can be derived from the generalized form of Hooke's law for anisotropic materials and the compliance matrix for silicon [65]: in the ([110], $[1\bar{1}0]$, [001]) coordinate system per kilogram of applied mass, $\epsilon_{11} = -1.45 \times 10^{-5}/\text{kg}$, $\epsilon_{22} = 9.02 \times 10^{-7}/\text{kg}$, $\epsilon_{33} = 5.24 \times 10^{-6}/\text{kg}$, and $\epsilon_{i \neq j} = 0$. While the VRM predicts frequency shifts only from uniaxial strain, we shall see that the new mechanism presented here arises from hydrostatic strain $\epsilon_{\text{hs}} = (\epsilon_{11} + \epsilon_{22} + \epsilon_{33})/3$. In our setup, we estimate a strain per unit mass of $\epsilon_{\text{hs}} = -2.78 \times 10^{-6}/\text{kg}$.

We use a home-built pulsed ESR spectrometer [66] at 9.7 GHz to apply a Hahn echo sequence $\pi/2 \rightarrow \tau \rightarrow \pi \rightarrow \tau \rightarrow \text{echo}$ [67] with $\tau = 15 \mu\text{s}$ and a π pulse duration of 130 ns. The time-domain Hahn echo signals (top of Fig. 2) obtained while systematically increasing the applied strain

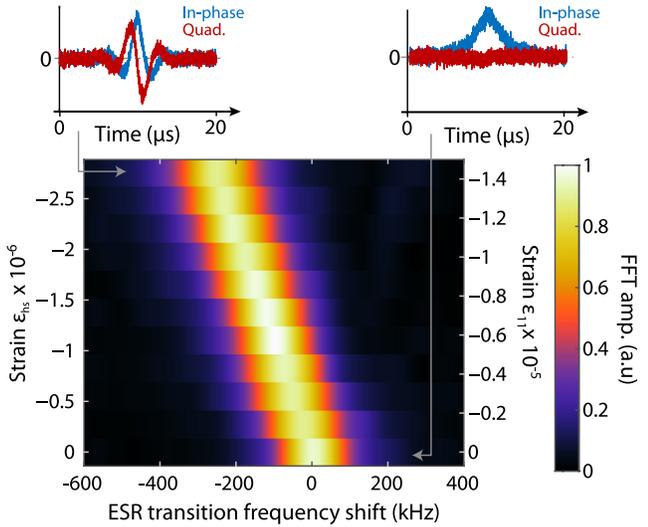


FIG. 2. Electron spin echo signals in the frequency domain measured in $^{28}\text{Si}:\text{Bi}$ as a function of compressive strain (shown in terms of the uniaxial strain ϵ_{11} and hydrostatic strain ϵ_{hs}) arising from the applied stress in our experiment. Time-domain echoes for zero strain and $\epsilon_{11} = 1.4 \times 10^{-5}$ are shown as insets. Data shown are from the $m_I = -1/2$ transition with $\theta = 45^\circ$, taken at $T = 8$ K.

are then Fourier transformed to yield the strain-induced shifts in spin resonance frequency [44].

First, we observe in Fig. 2 that the Bi donor ESR transition can be shifted by more than a linewidth (in ^{28}Si) for strains of order 10^{-5} (uniaxial) or 10^{-6} (hydrostatic). We fit the frequency-domain echo signals to a Voigt profile, and then plot the center-frequency shifts as a function of strain, for each of the ten allowed ESR transitions [see Fig. 1(c)]. Strikingly, the ESR frequency of each transition shows a linear dependence on strain, rather than the expected quadratic dependence. In Fig. 3, we plot the experimentally determined $\partial f/\partial \epsilon_{11}$ for each transition against the first-order sensitivity of each transition frequency to the isotropic hyperfine coupling $\partial f/\partial A$. Remarkably, all ten points fall on a single line, demonstrating that the dominant effect we observe in Si:Bi is a strain-induced shift in the isotropic hyperfine coupling that is linear in strain, and equivalent to $\partial A/\partial \epsilon_{11} = 5.4 \pm 0.3$ GHz or $\partial A/\partial \epsilon_{\text{hs}} = 28.2 \pm 1.6$ GHz.

Multivalley effective mass theory has been successful in describing many aspects of the donor electron wave function [68–70], including close agreement between theory and experimental measurements of the Stark effect [71] and predictions of exchange coupling between neighboring donors [72]. Within this framework, the wave function is expanded in terms of Bloch functions concentrated around the six degenerate [100] conduction band minima (valleys) such that $\psi = \sum_{\mu=1}^6 \alpha_{\mu} F_{\mu} \phi_{\mu}$, where μ indexes over the valleys in the basis $[+x, -x, +y, -y, +z, -z]$, F_{μ} is a hydrogenlike envelope function, and ϕ_{μ}

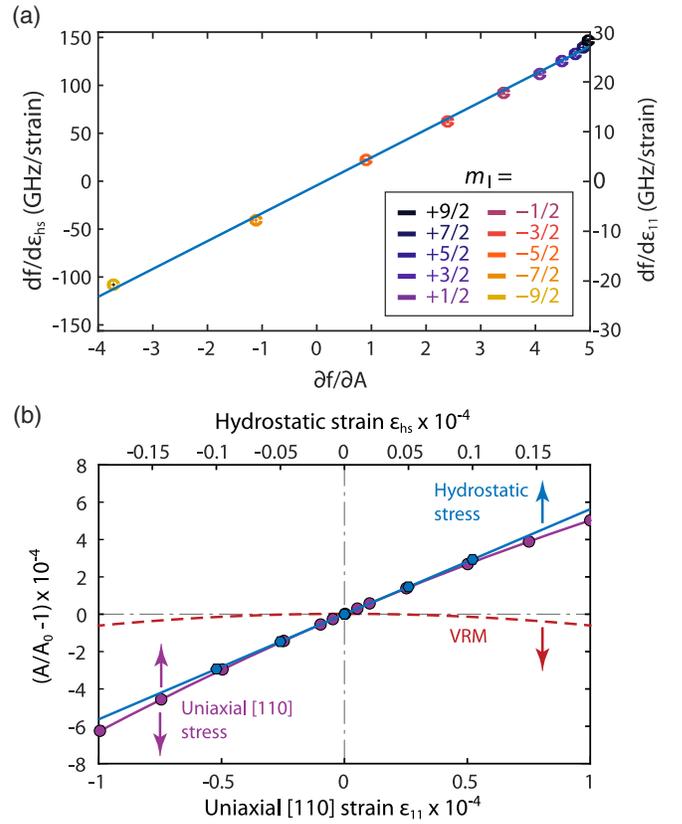


FIG. 3. (a) The gradient of the strain-induced frequency shifts ($df/d\epsilon$) for each of the ten Si:Bi ESR transitions is shown as a function of the first-order sensitivity of each transition to the hyperfine coupling ($\partial f/\partial A$). The linear relationship confirms the observed strain-induced shifts in Si:Bi result from tuning the hyperfine coupling, A , with a gradient $\partial A/\partial \epsilon_{11} = 5.4 \pm 0.3$ GHz or, equivalently, $\partial A/\partial \epsilon_{\text{hs}} = 28.2 \pm 1.6$ GHz. (b) Calculations showing the relative change in hyperfine coupling strength A/A_0 as a function of strain, comparing TB and valley repopulation models. To mimic the experiment, we show TB calculations of A/A_0 under uniaxial stress along [110] (purple curve and circles), which produces a hydrostatic component of strain (ϵ_{hs} , top axis) in addition to a uniaxial component along [110] (ϵ_{11} , bottom axis). This behavior can be understood by comparing with TB calculations for pure hydrostatic stress (blue curve and hexagons), plotted on the same axis of ϵ_{hs} , as well as calculations from the VRM (red dotted curve), plotted on the same axis of ϵ_{11} . The arrows indicate the relevant axes for each trace.

is the valley Bloch function. The donor impurity potential breaks the symmetry of the crystal and induces a coupling between the valleys, leading to a valley-orbit splitting of the $1s$ -like donor state into three sublevels. The ground state is singly degenerate with A_1 symmetry and has $\alpha_{\mu} = 1/\sqrt{6}$, while one of the excited states is doubly degenerate with E symmetry and has $\alpha_{E_1} = 1/2[1, 1, -1, -1, 0, 0]$ and $\alpha_{E_2} = 1/2[1, 1, 0, 0, -1, -1]$. The valley repopulation model assumes that uniaxial strain applied along a valley axis results in the corresponding pair of valley energies being decreased or increased for compressive or tensile

strain, respectively [39]. This modification of the valley energies results in a redistribution of the amplitude of each valley contributing to the ground state, which can be represented under strain as an admixture of the $1s(A_1)$ and $1s(E)$ states, resulting in a quadratic reduction of A as a function of uniaxial strain. At our maximum applied strain of $\epsilon_{11} = -1.45 \times 10^{-5}$, the VRM predicts a reduction in A of 1.9 kHz, while we measure a reduction in A of 78 kHz—this discrepancy is even more pronounced for smaller strains. Therefore, in addition to predicting a different functional form of the dependence of A against strain, the VRM predicts shifts that are approximately 2 orders of magnitude smaller than what we measure in this strain regime, implying that another physical mechanism must dominate the changes to the structure of the donor electron wave function we observe.

In order to understand these trends, we have computed the bound states of bismuth impurities in silicon using the $sp^3d^5s^*$ tight-binding (TB) model of Ref. [45]. This model reproduces the variations of the band structure of bulk silicon under arbitrary strains in the whole first Brillouin zone. The impurity is described by a Coulomb tail and by a correction of the orbital energies of the bismuth atom (similar to a central cell correction in the effective mass approximation) [46]. The TB ratio A/A_0 between the strained (A) and unstrained (A_0) hyperfine interaction strengths is plotted in Fig. 3(b) under uniaxial stress along [110], as a function of the resulting uniaxial [110] and hydrostatic strains. Surprisingly, and in agreement with the experiments performed here, A/A_0 behaves linearly with small strain, and this trend can be assigned to the effects of the hydrostatic stress. Although not predicted by the VRM, the existence of a linear hydrostatic term is compatible with the symmetries of the system [42]. A symmetry analysis indeed suggests that, to second order in the strains ϵ_{ij} in the cubic axis set,

$$\begin{aligned} A/A_0 = 1 + \frac{K}{3}(\epsilon_{xx} + \epsilon_{yy} + \epsilon_{zz}) \\ + \frac{L}{2}[(\epsilon_{yy} - \epsilon_{zz})^2 + (\epsilon_{xx} - \epsilon_{zz})^2 + (\epsilon_{xx} - \epsilon_{yy})^2] \\ + N(\epsilon_{yz}^2 + \epsilon_{xz}^2 + \epsilon_{xy}^2). \end{aligned} \quad (3)$$

A fit to the TB data yields $K = 29.3$, $L = -9064$, and $N = -225$. L mostly results from the coupling of the $1s(A_1)$ with the $1s(E)$ state by the uniaxial strain. The TB L is close to the VRM $L = -2\Xi_u^2/(9\Delta^2) = -9720$ [39], where $\Xi_u = 8.6$ eV is the uniaxial deformation potential of the conduction band of silicon and $\Delta = 41$ meV is the splitting between the $1s(A_1)$ and the $1s(E)$ state of the Bi impurity. The quadratic shear term N is usually negligible with respect to L . $K = \partial(A/A_0)/\partial\epsilon_{hs}$ results from the coupling of the $1s(A_1)$ with the $2s(A_1)$ state (and higher A_1 states, since hydrostatic strain preserves the symmetry of the system) due to the change of the shape and depth of the

central cell correction under strain. A/A_0 is dominated by this hydrostatic term at small strain, as evidenced in Fig. 3(b). The TB $K = 29.3$ is larger than the experimental $K = 19.1$. At variance with L (which mostly depends on a deformation potential of the silicon matrix), K indeed depends on details of the potential near the impurity, which must be specifically accounted for in the TB model in order to reach quantitative accuracy [44]. In order to better capture the central cell correction around the bismuth impurity, we also performed first principles calculations using density functional theory (DFT) to describe the atomic relaxations not accounted for by our TB calculations [44]. The DFT calculations further corroborate the linear dependence of the hyperfine coupling on hydrostatic strain (for $\epsilon_{hs} \leq 10^{-3}$), and predict a coefficient $K = 17.5$, in good agreement with our experiments. Full details concerning the models and calculations can be found in Ref. [44].

To test our model further and explore the expected anisotropy of a g factor coupling to strain, we extend our study over a range of magnetic field orientations [as defined in Fig. 1(b)] and for the other group V donors: ^{31}P , ^{75}As , and ^{121}Sb . In all cases we find the observed ESR transition frequency shifts f are linear as a function of hydrostatic strain ϵ_{hs} , with the resulting coupling strengths ($df/d\epsilon_{hs}$) summarized in Fig. 4 and Table SI, along with values predicted from tight-binding calculations and full data sets [44]. While we find no significant anisotropy in Si:Bi, the data from Si:Sb, Si:As, and Si:P display strain effects that clearly depend on the magnetic field orientation, attributed to a strain-induced anisotropic electronic g factor. Following Wilson and Feher [39], our model for this anisotropy includes a term accounting for the effect of valley repopulation, and another accounting for the effect

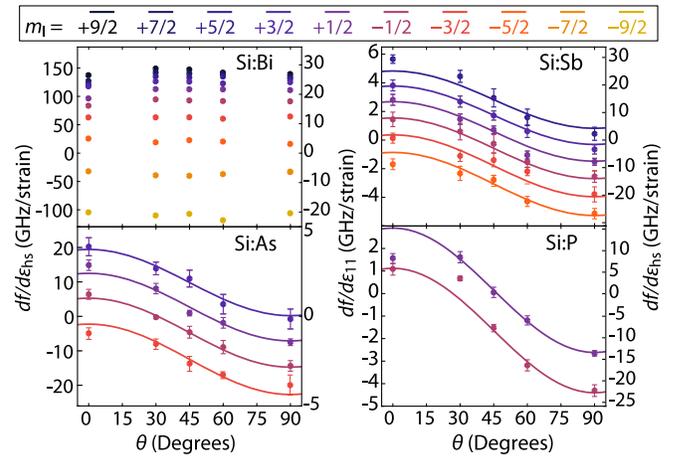


FIG. 4. Extracted linear fit gradients $df/d\epsilon_{11}$ for each transition for all four donors under consideration as a function of the angle of B_0 with respect to the crystal θ . For Si:Sb, Si:As, and Si:P, these fits are overlaid with a model taking into account the linear shift of hyperfine interaction strength A as well as an anisotropic g factor as a function of ϵ_{11} .

of spin-orbit coupling in the sheared lattice. Fits of this model to our experimental data reproduce the predicted strength of both of these effects to within a factor of 2 [44].

Through experiments and calculations, we have demonstrated that hydrostatic strain in silicon leads to a strong, linear tuning of the hyperfine interaction in group V donors, through coupling between the $1s(A_1)$ and $2s(A_1)$ states. The ability to shift the ESR transition frequencies by over a linewidth with hydrostatic strain in the order of 10^{-6} opens up new possibilities for conditional “A-gate” control of donors as well as coupling to mechanical resonators. In addition, these insights will be crucial in supporting the design of quantum memories and processors based on donors in silicon, enabling the ability to accurately predict ESR transition energies as a function of donor position within the device structure.

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