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Nonequilibrium radiation from a recombining nitrogen plasma

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Previous experiments performed at Stanford University studied the properties of a recombining non-equilibrium nitrogen plasma at atmospheric pressure. They used an inductively coupled plasma torch to create an equilibrium plasma and then imposed rapid cooling within a water-cooled tube in order to force rapid recombination and generate non-equilibrium distributions of ground and excited species. Emission spectroscopy was used to measure the plasma properties. Comparisons with numerical simulations showed that CFD codes did not correctly predict the temperature drop and the radiative flux leaving the plasma. This paper discusses a re-analysis of these experiments using new temperature measurements performed using Raman spectroscopy. A key result is that the measured temperature drop due to the imposed cooling is even higher than that measured by prior emission spectroscopy measurements. In addition to the Raman measurements, optical emission measurements were also performed and used to measure the atomic nitrogen density. From these measurements, we show that a large portion of the plasma enthalpy is stored in non-recombined nitrogen atoms. This is an important consideration for CFD codes looking to model atmospheric reentry dynamics.

I. Introduction

During atmospheric entry, a capsule enters the atmosphere of a planet (Earth, Mars...) at a velocity that can exceed 10 km/s. The strong shockwave that forms in front of the capsule heats the gas to temperatures that can exceed 10,000K. The high temperature of the gas leads to ionization, molecular dissociation, excitation and intense gas radiation. The study of the radiative and convective heat transfer of such a plasma is critical for the design of the heat shield (or thermal protection system, TPS) of a reentry capsule. These heatshields are carbon-based and represent a significant constraint for the mission, particularly in regards to their cost and weight. The heat flux to the forebody of the capsule has been the primary focus of past research and is now relatively well understood [1] [2]. However, predictions of the heat flux to the afterbody surface suffer from large uncertainties. This is due mainly to two factors. The first is the presence of significant quantities of carbon in the plasma, introduced via the ablative heat shield in the front of the capsule. The carbon sublimates from the forebody heat shield on the capsule and recombines in the flow, forming molecules such as CN and CO, that radiate in the afterbody region. This is currently the focus of some studies; see for example [3] [4] [5]. The second phenomenon is the expansion of the plasma into the afterbody region. This expansion rapidly cools the plasma, forces plasma recombination and departure from chemical equilibrium. The prediction of this nonequilibrium and the resulting radiation from such a plasma is not accurately modeled at the moment. Experiments conducted at Stanford University between 1995 and 2003 in atmospheric pressure recombining nitrogen plasmas showed that the radiation of certain transitions could emit up to 30 times more than the corresponding equilibrium radiation [6] [7]. CFD simulations were also performed to reproduce the N recombination and gas cooling but were not in agreement with the measurements [8] [9] as shown in Figure 1. In particular, the CFD calculations predicted that the gas temperature decreases by about 400K between the tube entrance and exit for a tube length of 15cm. In contrast, the measurements show more than 2400K of temperature decrease.

Figure 1: CFD simulations vs experimental results for several CFD simulations. Figures taken from

The combined effect of these two phenomena leads to large uncertainties on the heat flux to the afterbody surface. For earth reentry, simulations performed by Johnston et al [2] [10] show that uncertainties on the radiation heat flux to the afterbody can be up to 100% for velocities around 14 km/s. The velocity in the case of a real Mars reentry scenario could be higher, particularly for a Mars aerocapture mission [11]. This would increase the uncertainty resulting from these phenomena.

Although the heat flux per unit area to the afterbody surface is lower than on the forebody (for example, for the Stardust reentry, the total heat flux on the afterbody is about 20 W/cm² as compared to 100 W/cm² in the forebody), the afterbody surface represents approximately 2/3 of the total area, and therefore significant heating may occur on the afterbody. Uncertainties on these heat fluxes cause an overestimation of the TPS shield due to design margins, which can lead to a significant cost increase and added weight. This, in turn, can affect the feasibility of a mission. A fundamental study of the mechanisms governing the plasma dynamics in the afterbody of a spacecraft is therefore needed in order to

reduce these uncertainties. This work will focus on the radiation of a non-equilibrium recombining plasma flow to better understand this mechanism.

In this paper, we revisit the previous experiments conducted by Laux, Gessman et al [6] [7]. To this end, we have now implemented a new Raman scattering diagnostic to complement emission spectroscopy measurements. We used our 50 kW plasma torch to supply a high enthalpy plasma, at conditions reproducing those of the Stanford experiments. The plasma is then cooled in a water-cooled tube to force the plasma to recombine, resulting in a nonequilibrium plasma at the exit of the tube. We use emission and Raman spectroscopy to study the departure from equilibrium and the resulting radiation from the plasma. This experiment provides a simple test case for a recombining plasma and can be used to validate CFD codes: in particular, it serves as a validation case for the chemical kinetics being used in the CFD codes. We performed experiments for a variety of conditions, ranging from equilibrium to nonequilibrium cases, in order to try and assess the impact of the chemical kinetics on the plasma properties.

II. Experimental setup

The plasma torch facility is a TAFE Model 66 inductively coupled plasma (ICP) torch powered by a 120 kVA radio frequency LEPEL Model T-50-3 power supply. The power supply operates at 4 MHz and can supply a maximum of 12 kV DC and 7.5 A to the oscillator plates. Details of the plasma torch facility are provided in previous publications [4] [7] [12]. The plasma produced within the torch exits through a 1-cm diameter nozzle at a speed of approximately 600 m/s. The plasma studied here are comprised of 90 slpm of N_2 or air premixed with 50 slpm of argon to provide stable operating conditions for the torch. A water-cooled tube (15 cm length) made of brass is mounted on top of the plasma torch. Instead of creating a strong expansion as with a reentering capsule, the plasma is forced to recombine by imposing rapid cooling via the cold wall (maintained at approximately 300 K). This setup is therefore intended as a simplified experimental model of a real reentry scenario. Details of the experimental setup are presented in figure 2. We will compare the results between the N_2/Ar and the Air/Ar plasmas.

Figure 2: Water-cooled test-section mounted on the top of the plasma torch

Measurements were performed for several tube lengths:

- A 0-cm tube length corresponds to measurements directly at the exit of the torch nozzle (no water-cooled tube). It has been shown that the plasma is in equilibrium at this location [7] [13]. The plasma temperature is measured by optical emission spectroscopy (see Figure 3) of atomic lines [12]. Measured molecular spectra are then compared with theoretical ones generated using the radiation code SPECAIR [14] assuming the equilibrium measured temperature and the known pressure (1 atm). The good agreement between theory and experiment validates the equilibrium assumption. Raman measurements recently performed in our group for these conditions have also confirmed the temperature obtained by emission spectroscopy [14].
- At 10-cm and 15-cm tube lengths, temperature measurements are performed using both emission and Raman spectroscopy. At 10 cm, the temperature is measured from the absolute emission of atomic lines. The temperature at 15 cm is measured using emission spectroscopy of N_2^+ rotational lines using the procedure

Figure 4: Experimental setup for Raman UV scattering measurements. The laser is focused above the torch exit. The periscope consists of two quartz prisms for adjusting the height and direction of the laser beam. The 90° image rotator serves to horizontally align the laser beam with the spectrometer entrance slit.

III. Results

- 0 cm (water-cooled tube inlet)

Temperature profiles in both nitrogen and air plasmas are presented in figure 5. The profile labeled “Gessman *et al*” corresponds to the temperature measured by Gessman *et al* [16] of a N₂/Ar plasma using emission spectroscopy and for the same flow rate as used in this paper. Results from Raman spectroscopy are also presented in Fig. 5. The temperature measurements using emission spectroscopy are performed using the absolute intensity of the atomic nitrogen line at 746 nm (labeled N746) in the case of the nitrogen plasma, and O777 in the case of the air plasma. Also, temperature measurements using N742, N744, Ar751 and Ar763 were performed and confirmed these temperature measurements: these are not presented here for the sake of clarity. Results from Raman spectroscopy are also presented. At these high temperatures, the gas is highly dissociated, and the density is low, leading to a small population of N₂(X). Therefore, the Raman signal is weak, and the associated uncertainty is large.

Figure 5: temperature profiles measured using both emission and Raman spectroscopy at tube inlet ($x=0$ cm).

The temperature measurements of Gessman et al and our own for an N_2/Ar plasma are in good agreement. A slight difference is observed between the two sets of results, although the torch power and the mass flow rates were identical in both experiments. This difference can be attributed to different injection conditions in the plasma torch: in the experiments of Gessman et al, 50% of the gas was injected in swirl mode, and 50% in radial mode, whereas in the present experiments we used 20% swirl / 80% radial. Swirl can slightly change the temperature profiles, as seen from the computations shown in Fig. 1.

The Raman measurements for Air/Ar using Raman spectroscopy are not presented as they give the same profile as for the N_2/Ar plasma. Temperature profiles of the Air/Ar plasma obtained using emission and Raman spectroscopy are in agreement to within the uncertainty bars. The good agreement between temperature measurements using different atomic transitions and Raman scattering gives confidence that the plasma is in equilibrium.

- **10 cm water-cooled tube exit**

Temperature profiles at 10 cm were performed using the same techniques as those used at 0 cm and are presented in figure 6.

Figure 6: temperature profiles measured using both emission and Raman spectroscopy at 10 cm water-cooled tube exit.

The temperature profiles of Gessman *et al* and our emission measurements for the N_2/Ar plasma are in good agreement again as expected. Both Raman and emission spectroscopy temperature profiles remain in good agreement for the Air/Ar plasma. However, the temperature profiles measured using emission and Raman spectroscopy now differ for the case of the N_2/Ar plasma: this is the case despite the relatively large uncertainty bars. This was unanticipated. Note that the temperatures measured using Raman spectroscopy are more representative of the temperature of the gas because they are a measurement of the ground state of N_2 . The emission measurements are in agreement with those of Gessman et al. However, the Raman measurements show that the bulk gas temperature is much lower than previously thought. Also note that the Raman measurements, rather than reducing the discrepancy with the CFD model predictions in Fig. 1, amplify this discrepancy.

- **15 cm water-cooled tube exit**

Temperature profiles at 15 cm are presented in figure 7.

Figure 7: temperature profiles measured using both emission and Raman spectroscopy at 15 cm water-cooled tube exit.

Once again, all temperature profiles are in good agreement with the exception of the Raman measurement in the N_2/Ar plasma. The differences between the temperatures measured using Raman spectroscopy and emission spectroscopy for the N_2/Ar plasma are now even more pronounced than for the case at 10 cm. Emission spectroscopy measurements are based on emission from the N_2^+ B state. Previous work suggested that the ion may recombine before it equilibrates to the background rotational/translational temperature [17]. This would mean that this emission is not representative of the bulk gas temperature. Indeed, the Raman measurements show that the bulk gas temperature is much lower than previously thought. This confirms that a recombination mechanism in the N_2/Ar plasma causes a rapid temperature decrease that is not accounted for in the CFD models (Fig. 1). Note that, for the case of the Air/Ar plasma, the temperatures measured using both techniques provide similar results and give confidence in the temperature measured by Raman for the N_2/Ar case.

In both the air and N_2 plasma we measured N_2 first positive emission in the visible wavelength range for comparison with SPECAIR modeling. Figure 8 shows the results. We computed with SPECAIR the theoretical spectrum for an air/Ar and a N_2/Ar plasma under local thermodynamic equilibrium conditions at the measured temperature and 1 atm. For the N_2/Ar plasma case, we computed two theoretical spectra: one with the temperature measured using emission spectroscopy, and the second with the temperature measured using Raman spectroscopy.

Figure 8: calibrated measured spectra for the N_2/Ar and Air/Ar plasmas and the corresponding computed spectra using SPECAIR, assuming equilibrium at the exit of the 15 cm tube. The measured spectra are Abel-inverted and only the emission of the 0.5 mm thick center slab is plotted.

There is good agreement between the measured and computed spectra for the case of the Air/Ar plasma, confirming equilibrium at the exit of the 15 cm tube. However, there is a large discrepancy for the case of the N₂/Ar plasma. Note that this discrepancy is large even with the higher temperature obtained using emission spectroscopy. This shows that the plasma is not in equilibrium. Considering only the N₂ first positive transition, it appears that the measured radiation from this transition is about 5 times more than the equilibrium value if a temperature of 4570 K is assumed (temperature measured with emission). If we assume that the plasma is at 3200 K, which corresponds to the temperature obtained using Raman spectroscopy, the measured radiation is now about 10000 times more than equilibrium. In term of CFD simulations, this shows that the plasma is not in equilibrium and that the temperature is not the only relevant physical quantity to be modeled. A vibrationally specific collisional-radiative model is essential to correctly predict the radiative heat flux. Note that Gessman *et al* showed, for the case of the Air/Ar plasma, that the additional presence of oxygen tends to keep the recombining plasma at equilibrium via the recombination reaction: $N + O + M \leftrightarrow NO + M$ [16].

To quantify the degree of departure from equilibrium in the vibrational levels of the N₂ B state, we used SPECAIR and altered the population of the vibrational levels of N₂B to reproduce the experimental spectrum. This was done by using the previously defined overpopulation factor ρ_v to increase the population of a given vibrational level. The experimental spectrum was reconstructed by introducing overpopulation factors for the various contributing vibrational levels. This was done using an optimization algorithm. The results of the measured population and the corresponding spectra are presented in figure 9. Note that we used the temperature measured using Raman as it is the most representative of the gas temperature. Note that the level N₂⁺ (A ²Σ_g⁺) is also overpopulated as the transition N₂⁺ Meinel is stronger than at equilibrium.

Figure 9: Left: Measured and theoretical spectra in the case of the N₂/Ar at the exit of the 15 cm tube. The blue curve represents the computed SPECAIR spectrum assuming equilibrium and the red one is the computed spectrum assuming a non-equilibrium distribution of N₂B. Right: The population of vibrational levels of N₂B taken in SPECAIR for calculation of theoretical spectra.

The good agreement between the spectrum assuming non-equilibrium and the measured one validates our measurement of the population distribution of the vibrational levels of N₂ B. Note that N₂ B is highly overpopulated as compared to its equilibrium value because N does not have time to recombine in the tube due to the high velocity imposed. Note also that the vibrational population distribution in N₂ B is no longer given by a Boltzmann distribution. It is therefore not possible to characterize the plasma using a single temperature. This is a challenge for CFD simulations as all vibrational levels should be included in the chemistry model to predict the correct radiative flux. This was also observed

by Gessman *et al.* However, in their case, they calculated the overpopulation factors based upon the temperature measured using N_2^+ emission. Given that this temperature is much higher than the Raman measurement, the overpopulation factors in their case were much lower. On the other hand, the populations measured by Gessman *et al.* are very close to those measured in the present work.

It is also possible to measure the atomic nitrogen density from this spectrum. As explained in Ref [7], the vibrational level $v=13$ of $N_2 B$ is a predissociating state $N_2(B, v = 13) \leftrightarrow N(^4S) + N(^4S)$. Considering that this reaction is equilibrated, the overpopulation of level $\rho_{N_2, B, v=13}$ gives the overpopulation of atomic N via the equation: $\rho_N = \sqrt{\rho_{N_2, B, v=13}}$. With the Abel-inverted spectra, we measured the overpopulation of $N_2, B, v=13$ versus radius to infer the population of N across the tube diameter. Populations of N measured using this technique are plotted in figure 10.

Figure 10: radial population distribution of atomic nitrogen atoms, measured and calculated assuming an equilibrium population at the temperature measured using Raman spectroscopy

The density of atomic nitrogen is highly above its equilibrium value at 10 cm and it does not change substantially between 10 and 15 cm, suggesting that the N population is effectively frozen. Furthermore, a significant amount of enthalpy is stored in the unrecombined N. This is an important consideration for the energy balance of the flow, as shown below. The nitrogen atomic density was also measured by Gessman *et al* in the center of the tube. They measured a density of $1.62 \pm 0.3 \cdot 10^{17} \text{ cm}^{-3}$ against $1.02 \pm 0.06 \cdot 10^{17} \text{ cm}^{-3}$ in our case. Both values are in good agreement despite using different temperatures conditions (we used temperature measured with Raman spectroscopy while Gessman *et al* used emission spectroscopy).

The enthalpy stored in unrecombined nitrogen atoms is given by the following relation:

$$\Delta H_{chem} = (n_N - n_N^*) E_{diss N_2}$$

where n_N is the measured number density of N, n_N^* is the equilibrium density of N, and $E_{diss N_2}$ the energy of dissociation of N_2 . This enthalpy is divided by the residence time of the gas in the tube to obtain a power:

$$\Delta P_{chem} = \frac{\Delta H_{chem}}{\tau_{residence}} = \frac{\Delta H_{chem}}{\frac{x}{V_{gas}}}$$

where x is the length of the tube (10 or 15 cm) and V_{gas} the mean velocity of the gas. Note that the velocity has not been measured directly and is estimated by matching the mass flow rate assuming a radial velocity profile self-similar to that of the measured temperature (justified by the fact that the Prandtl number, equal to 0.7, is close to unity). However, to account for any potential error due to this assumption, a large uncertainty (20%) on the velocity is taken for each calculation involving this parameter.

Based on the measured temperature profiles at the inlet and outlet of the tube, the power variation across the tube assuming equilibrium conditions is:

$$\Delta P_{gas (equilibrium)} = \left[\int_{r=0}^{r=5 \text{ mm}} \rho_{gas} V_{gas} c_{p_{gas}} T_{gas} 2\pi r dr \right]_{outlet} - \left[\int_{r=0}^{r=5 \text{ mm}} \rho_{gas} V_{gas} c_{p_{gas}} T_{gas} 2\pi r dr \right]_{inlet}$$

In addition, we also performed a calorimetric power balance on the water that traverses the water-cooled tube. This gives the power removed via the wall during the experiment and is equal to:

$$\Delta P_{water} = \dot{m}_{water} * c_{p_{water}} * (T_{wo} - T_{wi})$$

where $\dot{m}_{water}$ is the measured water mass flow rate, T_{wi} and T_{wo} are the temperature of the water at the inlet and the outlet of the cooling tube, respectively.

Through a simple energy balance, this power must be equal to:

$$\Delta P_{water} = \Delta P_{gas (equilibrium)} - \Delta P_{chemistry}$$

where $\Delta P_{chemistry}$ represents the power stored due to chemical or thermal nonequilibrium: for example, the power stored in unrecombined nitrogen atoms.

Figure 11 shows the results obtained.

Figure 11: Power measurements using two different approaches for both plasmas cases.

Blue: measured power removed by water cooling.

Red: Power change between the exit and the inlet of the tube assuming equilibrium throughout the tube.

Green: power stored into unrecombined N atoms using the measured overpopulation factors.

Black: Red minus green curve: this represents the total power removed from the gas if only atomic nitrogen is responsible for the discrepancy in power.

For the N_2/Ar plasma the good agreement between the black and the blue curves indicates that the unrecombined N accounts for the missing energy. Note that all the calculations were done using the temperature measured via Raman spectroscopy. The chemical energy stored in the overpopulated vibrational levels of $N_2 B$ and $N_2 C$, measured using emission spectroscopy, was also considered. However, this energy is negligible compared to the enthalpy stored in the unrecombined N. This energy balance gives us confidence in the fact that the temperature of the gas is indeed the temperature measured with Raman. However, although these measurements are consistent with the Raman measurements, they do not explain the mechanism that causes the rapid cooling of the nitrogen/argon plasma.

In the case of an air/Ar plasma, we showed that the plasma stayed at equilibrium in the tube: thus, there is no energy stored into unrecombined nitrogen atoms. At 10 cm, the power balance assuming equilibrium is in agreement with the power removed by the water as expected for an equilibrium plasma. However, there is a slight difference at 15 cm. This can potentially be explained by unrecombined atoms near the wall. Near the wall, the rate of cooling is faster and is more likely to lead to a nonequilibrium distribution. However, due to the lower temperature close to the wall, it was not possible to measure possible overpopulations of atomic nitrogen using emission spectroscopy. Emission spectra were only measured for radii less than 3 mm, where the emission was sufficiently strong.

These power balances show strong differences between the N_2/Ar plasma and the air/Ar plasma. Both experiments are interesting for CFD codes as they have similar input conditions (same flow rates, temperatures, pressure...) but significantly different results at the tube outlet.

IV. Conclusions

Experiments have been conducted in a plasma torch facility to study nonequilibrium recombining plasmas of nitrogen/argon and air/argon. These experiments may be used to validate CFD codes for atmospheric entry calculations.

Our results using emission spectroscopy are in agreement with earlier experimental results performed by Gessman et al [16]. We have also performed Raman scattering measurements to measure rotational and vibrational temperatures of N_2 ground state. The vibrational and rotational temperatures obtained with Raman spectroscopy are in equilibrium and are much lower than those measured using emission spectroscopy. The higher temperature obtained by emission spectroscopy for the rotational distribution of levels of the $N_2^+ B$ state is likely due to the rapid quenching of excited ions states, which do not have time to relax to the background temperature of the gas. This has been observed by Studer and Vervisch [17]. Bruggeman *et al* [18] studied other scenarios where emission spectroscopy gives an incorrect measurement of the gas temperature. Thus, the Raman temperature measurements should be more reliable than those obtained with emission spectroscopy.

Given the temperature measured using Raman spectroscopy, we were able to calculate a simple energy balance which showed that a large portion of enthalpy remains in unrecombined atomic nitrogen.

An important conclusion of this work is that the experimental results remain in strong disagreement with the CFD simulations. This is likely to come from modeling issues on the radial heat transfer in CFD codes. Indeed, analysis on CFD results showed that not enough heat is transferred from the plasma close to the wall at 300 K and the plasma in the center of the tube.

The N_2/Ar plasma case is complex as it couples fluid mechanics and non-equilibrium chemistry. Our experiments can be used to uncouple these effects. Indeed, the air/Ar plasma case gives experimental results for a plasma that stays close to equilibrium conditions which is easier to model. Disagreement between experiments and CFD simulations for this case is likely to come from fluid mechanics modeling of the reacting flow. This should be further investigated to understand the disagreement between CFD simulations and experiments. Then simulations on the N_2/Ar plasma case can be performed to validate the kinetic modeling.

It is clear that this nonequilibrium experiment done using a simple configuration raises many interesting issues about nonequilibrium recombining nitrogen flows. These issues are currently the object of our continued investigations.

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