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Novel three-dimensional carbon nanotube networks as high performance thermal interface materials

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ABSTRACT

Vertically aligned carbon nanotube (VACNT) arrays are considered as promising thermal interface materials (TIMs) due to their superior out-of-plane thermal conductivities. However the air gaps between adjacent CNTs within the CNT array...
hinder the in-plane heat transfer, thus significantly degrading the thermal performance of VACNT-based TIMs. To improve the inter-tube in-plane thermal conduction within of VACNT arrays, we propose a novel three dimensional CNT (3D CNT) network structure, where the CNTs in a VACNT array are cross-linked by randomly-oriented secondary CNTs. Three different catalyst preparation methods for the secondary CNT growth are compared in terms of their ability to produce a dense network of secondary CNTs. Among the tested methods, the chemical impregnation method shows a denser 3D CNT network structure. The 3D CNT network grown using this method is thus chosen for further thermal characterization via a framework especially developed for the evaluation of in-plane thermal properties of such devices. The temperature fields of the corresponding 3D CNT network under different heating powers are recorded using a 15 μm-resolution infrared thermal imaging system. The in-plane thermal conductivity is then derived from these fields using numerical fitting with a 3D heat diffusion model. We find that the in-plane thermal conductivity of the 3D CNT network is $5.40 \pm 0.92$ W/mK, at least 30 times higher than the thermal conductivity of the primary VACNT array used to grow the 3D CNT network.

**Keywords**: 3D CNT network, in-plane thermal conductivity, thermal imaging.

1. **Introduction**

Thermal interface materials (TIMs) play a significant role in the packaging of high power electronic devices. TIMs are generally positioned between heat generating devices and heat sinks to improve their thermal coupling via physical contact. For
state-of-the-art TIMs, such as thermal greases or phase change materials, the effective thermal conductivity ranges between 0.4 and 5 W/mK [1]. Although it is much better than air (~0.026W/mK), such thermal properties are still insufficient to satisfy the requirements of modern high power density devices.

Recent studies have investigated carbon nanotube (CNT) based TIMs in depth [2-4]. Carbon nanotubes possess superior thermal properties due to their strong sp² carbon bonding and long phonon mean free path. The thermal conductivity of individual CNTs has been measured to be 600–3000W/mK [5, 6]. Various kinds of CNT-based TIMs have been developed, such as CNT/polymer composites [3, 7] and CNT array [8]. Among the reported studies, vertically aligned CNT (VACNT) arrays stand out for their higher thermal conductivity [9] coupled with high mechanical compliance [10]. This helps in solving the issue of thermal stress caused by the mismatch in the coefficient of thermal expansion (CTE) between two contacting surfaces. Zhang et al. reported a reduction of 90% in the interfacial thermal resistance when replacing commercial TIMs with VACNT array-based TIM in high brightness light-emitting-diodes [11].

Despite the promising potential of VACNTs as TIMs, the thermal conductivity of a VACNT array is highly anisotropic. The air gap within the CNT array reduces the heat transfer between adjacent CNTs, which limits the in-plane thermal conductivity of VACNT arrays. From molecular dynamics (MD) simulations, Che et al. predicted that the in-plane thermal conductivity of VACNT array is as low as 0.056W/mK [12]. It reduces the applicability of VACNT as TIMs, as high in-plane thermal conductivity
is required when the sizes of the devices and their corresponding heat sources decrease. However, compared with the out-of-plane thermal measurements of VACNT-based TIMs, very few tools are available for the in-plane thermal characterizations of VACNT-based TIMs [13], which slows down the progress of improving the in-plane thermal properties of VACNT-based TIMs.

Considering the low in-plane thermal conductivity of the current state-of-the-art VACNT arrays as well as the lack of dedicated tools to evaluate this thermal property, the objective of the present work is two-fold: improving the in-plane thermal properties of VACNT array-based TIMs and developing a reliable framework for the quantitative evaluation of their in-plane conductivity. To this end, in this work, a novel three dimensional (3D) CNT network is proposed, where to enhance the in-plane thermal conductivity of VACNT array-based TIMs. In this novel structure, CNTs in a VACNT array are cross-linked by randomly-oriented secondary CNTs thus forming a three dimensional (3D) CNT network. The secondary CNTs provide an extra path for heat conduction in the in-plane direction and thus are expected to enhance the in-plane thermal conductivity of VACNT array-based TIMs. To verify this, The in-plane thermal conductivity of the 3D CNT network is evaluated by a method coupling infrared thermal imaging with 3D thermal modeling is developed so as to characterize the in-plane thermal conductivity of the proposed structure.

In what follows, three different catalyst preparation methods for the secondary CNT growth are compared in terms of their ability to produce a dense network of secondary CNTs. The 3D CNT network grown using the method yielding the denser
network is then chosen for further thermal characterization. Real-time temperature fields of the corresponding 3D CNT network heated by a metal wire are recorded using a high-resolution infrared thermal camera. A 3D thermal model of the system is then solved by finite element analysis. The obtained temperature data is fitted with the model outcome to yield the in-plane thermal conductivity of the material. The in-plane thermal conductivities of the 3D CNT network and the primary VACNT array used to grow the 3D CNT network are finally compared.

2. Experimental Details

2.1 Sample preparation

Figure 1 shows the preparation procedure for the samples. Quartz is chosen as substrate for its good heat insulation property (see Fig.1(a)). The thermal conductivity of the quartz substrate is measured to be 1.77 W/mK by the 3ω technique [14]. To serve as a heater, a metal bridge composed of a wire and two contact pads is deposited on top of a rectangular quartz sample (15 mm × 20 mm) (see Fig.1(b)). The metal bridge is 6 mm in length and 40 μm in width. Each contact pad measures 12.5 mm in length and 1.8 mm in width. Both the bridge and the contact pads are made of a 150 nm-thick Ti layer topped with a 30 nm-thick TiN layer. The high electrical resistivity of Ti enables a large electrical resistance (up to 3000Ω). The TiN layer protects Ti from oxidizing. A 20 nm Ni layer is then evaporated on top of the substrate and of the metal bridge as the catalyst for VACNT growth (see Fig. 1(c)). The contact pads of the metal bridge are protected with thermal tape during the evaporation.
The primary VACNT array is then grown by Aixtron Blackmagic Plasma Enhanced Chemical Vapor Deposition (PECVD) system. A detailed study about the VACNT growth has been reported previously [15]. The chamber pressure is kept as 5 mbar. A radio frequency (RF) electric field biased at 700V is applied with a power of 90W. After 5mins pre-growth annealing under 250sccm NH₃, the VACNT growth is conducted at 750°C under 250sccm NH₃ and 50sccm C₂H₂ for 30mins. The resulting “VACNT/heater/quartz” structure is depicted in Fig. 1(d).

![Fig. 1 Preparation procedure of the primary VACNT array: (a) the quartz substrate; (b) the metal bridge deposited on top of quartz as heater; (c) the Ni catalyst layer deposition; and (d) VACNT array/heater/quartz substrate structure.](image)

To achieve the cross-linked structure of the 3D CNT network, the Ni catalysts for the secondary CNTs growth within the primary VACNT array structure are prepared. In this study, three catalyst preparation methods are compared: (1) the sputtering method, (2) the direct transfer method, and (3) the chemical impregnation method:
(1) In the sputtering method (see Fig. 2(a)), the Ni catalyst is deposited onto the primary VACNTs through magnetic sputtering;

(2) In the direct transfer method (see Fig. 2(b)), a Ni foil is transferred onto the top of the primary VACNTs. Then the foil is annealed under H₂ atmosphere to break it down into Ni particles;

(3) In the chemical impregnation method (see Fig. 2(c)), the primary VACNT array is impregnated with 0.01mol/L Ni(NO₃)₂·6H₂O in acetone and then annealed under H₂ atmosphere. During the annealing, the Ni precursors contained in the above-mentioned solution are transformed into Ni particles. The reactive equations are described in Eq. 1 and Eq. 2:

$$\text{Ni(NO}_3\text{)}_2 = \text{NiO} + 2\text{NO}_2 + \text{O}_2 \quad (1)$$

$$\text{NiO} + \text{H}_2 = \text{Ni} + \text{H}_2\text{O} \quad (2)$$

After the Ni catalyst preparation (see Fig. 2(d)), the secondary CNTs are grown in a thermal furnace using an ethanol bubbler as the carbon source. The growth is carried out under 700°C for 10mins, and the 3D CNT network is formed (see Fig. 2(e)).

The electrical resistance of the metal wire is measured before and after the growth process of the VACNT array and of the secondary CNTs. Little change (<0.5%) is observed, suggesting that the presence of CNTs on top of the metal bridge does not induce significant parasitic conducting paths.
Fig. 2 Preparation procedure of secondary CNTs using three different Ni catalyst preparation methods: (a) the sputtering method; (b) the transfer method; and (c) the impregnation method. (d) The Ni catalyst attached on the sidewall of VACNT; and (e) the final 3D CNT network/heater/quartz substrate structure.

2.2 Infrared thermography characterization

Figure 3(a) shows the schematic diagram of the set-up for infrared thermal imaging of the samples. The temperature map of the sample surface is obtained using a FLIRX8400sc infrared camera equipped with a G1 lens and operating in the infrared wavelength range between 1.5 μm and 5μm. This system offers a spatial resolution of 15 μm and a temperature sensitivity of 25 mK. A black box surrounds the sample and the lens of the camera to minimize the noise from the radiation of surrounding objects.
The sample is maintained vertically in front of the camera by a holder made of aluminum alloy. The two contact pads of the metal bridge deposited on the quartz substrate are connected to a precision power supply (Keithley 2612B), as shown in Fig. 3(c). When a DC current is applied to the pads of the bridge, the bridge wire would act as a heater by Joule heating effect.

![Diagram of the set-up for the infrared thermal imaging](image1)

![Image of the system inside the black box](image2)

![Image of the sample clipped to the holder with electrical wire connections in place](image3)

**Fig. 3(a)** Diagram of the set-up for the infrared thermal imaging, (b) image of the system inside the black box, and (c) image of the sample clipped to the holder with electrical wire connections in place.

To convert the infrared radiation collected by the camera into temperature data, the emissivity value of each sample in the range of 1.5 μm to 5.1 μm is required. The
emissivities of the primary VACNT and the 3D CNT network are both measured to be 0.99 using an Perkin-Elmer Frontier FTIR system with an integrating sphere. The procedure has been well described elsewhere [16].

Temperature maps of sample surfaces are recorded under three different heating powers: 23mW, 47mW and 99mW. Temperature profiles corresponding to the thermal steady state are extracted for further thermal property analysis (see Section 3.3 for details).

3 Results and Discussion

3.1 Primary VACNT array

Figure 4(a) presents a cross-sectional SEM image of the primary VACNT array. It exhibits a high degree of vertical alignment, similar to other PECVD-grown CNTs such as those reported by Abdi et al. [17]. According to the TEM image shown in Fig. 4(b), Ni clusters are observed at the tips of the CNTs. This suggests the tip-growth mechanism of VACNTs by PECVD system [18]. From the top view (see Fig. 4(c)), sparsely-grown CNTs are observed, with visible air gaps between CNTs. This feature is expected from PECVD-grown CNTs, as described in our previous study [19]. This sparsely-grown nature of PECVD-grown CNT may exhibit inferior in-plane thermal properties, as discussed earlier.
3.2 3D CNT network

To explore the possibilities in improving the in-plane thermal conductivity of the VACNT array presented in Fig. 4, secondary CNTs are grown within the VACNT array to provide additional thermal conducting pathways. As described in Section 2.1, three different methods for Ni catalyst preparation have been investigated for the secondary CNTs growth within the primary VACNT array. The obtained 3D CNT networks using these three methods are compared in this section.

Figure 5(a) shows the SEM image of the 3D CNT network grown using the sputtering method. It can be observed that Ni nanoballs of 200 to 1000 nm in diameter...
are accumulated on the tips of the VACNTs, which can be explained by Cassie-Baxter model [20]. The presence of Ni nanoballs can possibly shield the underneath part of the primary VACNTs (see Fig. 5(b)), blocking the carbon feed stock gas to diffuse below the tips. As a result, minimal secondary CNTs are grown, as observed in Fig. 5(a).

![Fig. 5 3D CNT network grown using the sputtering method: (a) the cross-sectional SEM image; and (b) the schematic image.](image)

Since the formation of Ni nanoballs hinders secondary CNT growth, an alternative method is needed to incorporate Ni catalyst source on VACNTs for the growth of secondary CNTs. Therefore, we attempted to incorporate Ni catalyst using direct nickel foil transfer method. Figure 6 shows the SEM images of the 3D CNT network grown using the direct Ni foil transfer method. From Figure 6(b) and (d), it is observed that secondary CNTs are grown and bridged between adjacent primary VACNTs. This indicates that the Ni foil has been de-wetted into small nickel particles, scattering around VACNT to form catalytic particles for secondary CNT growth. As
compared to Fig. 5(a), a more significant growth of secondary CNTs can be observed in Fig. 6(d). However, the grown secondary CNTs are still sparse, and provide limited thermal pathways to bridge adjacent VACNTs. This can limit the enhancement in its thermal conductivity along the in-plane direction.

![SEM images of a 3D CNT network grown using the direct transfer method: (a) top view of the 3D CNT network; (b) zoom image of the red rectangular area in (a); (c) cross-sectional view of the 3D CNT network; and (d) zoom image of the red rectangular area in (c).](image)

To explore further improvement in the growth density of secondary CNTs, VACNTs are impregnated with Ni(NO$_3$)$_2$ solution as a catalyst source for secondary CNTs growth. Figure 7 shows the SEM images of the 3D CNT network obtained using the chemical impregnation method. Randomly oriented secondary CNTs are grown, filling up the gaps between adjacent VACNTs. As compared to direct transfer of Ni foil, this method provides Ni particles in solution state, which can be speculated to be
penetrated more readily through the VACNT film. As a result, dense secondary CNTs are obtained from the chemical impregnation technique.

![Fig. 7 SEM images of a 3D CNT network grown using the impregnation method: (a) top view SEM image of the 3D CNT network; (b) cross-sectional view of the 3D CNT network; and (c) zoom image of the 3D CNT network.](image)

To further investigate the morphological properties of 3D CNT network grown using the chemical impregnation method, we perform TEM imaging on the 3D CNT network (see Fig. 8). As shown in Fig. 8(a), the diameter of primary VACNT is around 150 nm. The diameter of the secondary CNT cross-linking the primary CNTs is around 20 nm. From the magnified TEM image (see Fig. 8(b)), both primary
VACNTs and secondary CNTs show multi-walled structure. To investigate the interface between primary VACNTs and secondary CNTs further, the zoom image of the red rectangle region in Fig. 8(b) is shown as Fig. 8(c). The spacing between each wall is 0.34 nm for both primary and secondary CNTs, which is in agreement with the wall spacing in MWCNTs [21]. It can be observed seems (zone circled in Fig. 8(c)) that the wall structure of secondary CNT is embedded into the wall pattern of primary CNT. Such a smooth continuation of CNT walls would suggest that the secondary CNT is grown directly from the sidewall of the primary CNT.
Fig. 8 (a) TEM image of 3D CNT network grown using the chemical impregnation method, (b) HRTEM image of the rectangular region in (a), and (c) HRTEM image of the rectangular region in (b).

From the obtained results, the 3D CNT network grown using the chemical impregnation method shows a network structure with the densest secondary CNTs among all three different methods. Since secondary CNTs can enhance the in-plane thermal conductivity of VACNT array, the 3D CNT network sample grown using the chemical impregnation method is the most desirable for superior in-plane thermal conductivity. Therefore, for the thermal property study conducted in what follows, we
will only focus on the 3D CNT network sample synthesized using the chemical impregnation method.

3.3 Thermal imaging characterization

A comparison of the high resolution thermal maps of the 3D CNT network as well as the primary VACNT array, which serves as a reference sample, are shown in Fig. 9 for different input powers. The temperature profiles along a segment perpendicular to the center of the wire heater (marked by the blue dotted line in Fig. 10(a)) are also extracted from the above-mentioned maps and shown in Fig. 10(b). Under different heating powers, the temperature of the 3D CNT network near the heating wire is always lower than that of the primary VACNT array. As the heating power increases, the surface temperature difference between the 3D CNT network and the VACNT array increases. Under the heating power of 99 mW, the temperature of the 3D CNT network at a distance of 0.5 mm away from the heating wire is 10 K lower than that of the VACNT array. This indicates that the 3D CNT network has a much better heat dissipation capability than the primary VACNT array. Compared to the primary VACNT array, the slopes of the temperature profiles for the 3D CNT network are much smaller, which indicates that the 3D CNT network has a lower in-plane thermal resistance than the primary VACNT array.

At a distance of 6 mm from the heater, the sample is clipped by an aluminum alloy holder (see Fig. 3(c)). This aluminum alloy holder acts as heat sink for the system, due to its high thermal conductivity. As a result, the temperature of the sample
surface near the heat sink is close to the ambient temperature. During the thermal measurements, the ambient temperatures are slightly different: 296.35K for the 3D CNT network and 295.45K for the VACNT array. This gives an explanation of the slightly higher temperature for the 3D CNT network than for the VACNT array at 5.1 mm from the wire.

Fig. 9 Left: Primary VACNT array under 23mW(a), 47mW(b), 99mW(c); Right: 3D CNT network under 23mW(d), 47mW(e), 99mW(f).
Fig. 10 (a) Model for the thermal system: the blue dotted line is perpendicular to the center of the wire heater, and (b) the temperature profile (extracted from the temperature maps of Fig. 9) along the blue dotted line as a function of the distance from the heater.
3.4 Extraction of the in-plane thermal conductivity of the CNT films

3.4.1 Thermal model

To extract the in-plane thermal conductivity of the CNT films from the temperature profiles given in Fig. 10(b), we use the following governing 3D heat equations for the thermal heater, the quartz substrate, the top and bottom parts of the holder, and the CNT film:

\[
\frac{\partial}{\partial x} (K_H \frac{\partial T_H}{\partial x}) + \frac{\partial}{\partial y} (K_H \frac{\partial T_H}{\partial y}) + \frac{\partial}{\partial z} (K_H \frac{\partial T_H}{\partial z}) + P = \rho_H c_H \frac{\partial T_H}{\partial t} \tag{3}
\]

\[
\frac{\partial}{\partial x} (K_S \frac{\partial T_S}{\partial x}) + \frac{\partial}{\partial y} (K_S \frac{\partial T_S}{\partial y}) + \frac{\partial}{\partial z} (K_S \frac{\partial T_S}{\partial z}) = \rho_S c_S \frac{\partial T_S}{\partial t} \tag{4}
\]

\[
\frac{\partial}{\partial x} (K_A \frac{\partial T_{th}}{\partial x}) + \frac{\partial}{\partial y} (K_A \frac{\partial T_{th}}{\partial y}) + \frac{\partial}{\partial z} (K_A \frac{\partial T_{th}}{\partial z}) = \rho_A c_A \frac{\partial T_{th}}{\partial t} \tag{5}
\]

\[
\frac{\partial}{\partial x} (K_A \frac{\partial T_{bh}}{\partial x}) + \frac{\partial}{\partial y} (K_A \frac{\partial T_{bh}}{\partial y}) + \frac{\partial}{\partial z} (K_A \frac{\partial T_{bh}}{\partial z}) = \rho_A c_A \frac{\partial T_{bh}}{\partial t} \tag{6}
\]

\[
\frac{\partial}{\partial x} (K_{CNT, in} \frac{\partial T_{CNT}}{\partial x}) + \frac{\partial}{\partial y} (K_{CNT, in} \frac{\partial T_{CNT}}{\partial y}) + \frac{\partial}{\partial z} (K_{CNT, out} \frac{\partial T_{CNT}}{\partial z}) = \rho_{CNT} c_{CNT} \frac{\partial T_{CNT}}{\partial t} \tag{7}
\]

In Eq. 3 to Eq. 7, the subscript \( H \) refers to the metal heater, \( S \) to the quartz substrate, \( A \) to the aluminum alloy holder, \( th \) to the top part of the holder, \( bh \) to the bottom part of the holder, \( P \) to the heat generation rate of the metal wire, \( \rho \) to the density, \( C \) to the heat capacity, and \( K \) to the thermal conductivity. Since CNT films show high anisotropy in their thermal property [22], we define \( K_{CNT, in} \) and \( K_{CNT, out} \) to represent respectively the in-plane and the out-of-plane thermal conductivity of the CNT film. For the holder, the quartz substrate, and the metal heater, \( K_A \), \( K_S \), and \( K_H \) represent their thermal conductivities, assumed to be isotropic.

In the thermal steady state, the time derivatives of the temperature in the different domains are null; so the right-hand side of Eq.3 to Eq.7 turns out to be 0.
Therefore, the 3D heat diffusion equations under thermal steady state are no longer dependent on the density ($\rho$) and the heat capacity ($C$) of the materials.

Regarding boundary conditions:

- As the bottom part of the holder is placed on a large steel stage, the temperature of the bottom surface of the bottom holder is fixed at ambient temperature $T_0$:
  $$T = T_0$$  \hspace{1cm} (8)

- For all the remaining external (exposed to air) boundary surfaces, there is heat flux caused by natural convection. The heat flux $\vec{q}_c$ of natural convection is:
  $$-\vec{n} \cdot \vec{q}_c = h(T_0 - T),$$  \hspace{1cm} (9)
  where $T_0$ is the ambient temperature; $T$ is the temperature of the boundary surface; $h$ is the heat transfer coefficient for natural convection.

- In addition to the natural convection, there is also heat loss due to the radiation on all the remaining boundary surfaces. The heat flux $\vec{q}_r$ caused by radiation is described as:
  $$-\vec{n} \cdot \vec{q}_r = \varepsilon \sigma (T_0^4 - T^4),$$  \hspace{1cm} (10)
  where $\varepsilon$ is the sample emissivity; $\sigma$ is the Stefan-Boltzman constant, $\sigma = 5.67 \times 10^{-8}$ W/m$^2$K$^4$. Since quartz is transparent in the mid-infrared range where the thermal camera operates, its emissivity at mid-infrared range is extremely low ($10^{-7}$–$10^{-5}$) and the radiation rate is negligible (around $10^{-5}$ mW) [23]. Based on our measurements, the temperature of the holder is close to the
ambient temperature $T_0$. The radiation rate of the holder is calculated from Eq. 10 to be around 10$^{-3}$ mW, which is three orders of magnitude lower than the heat generation rate of metal heater and is considered negligible too. The radiation loss of the whole system is thus dominated by the radiation from the CNT film.

Since the sample is clipped to the holder, there is thermal contact resistance between the sample surface and the holder. The heat flux $q_c$ across the contact surfaces is:

$$\vec{n} \cdot \vec{q}_c = -\Delta T / R_c,$$

where $\Delta T$ is the temperature jump between the two contact surfaces.

### 3.4.2 Solver

We perform the thermal simulations by solving Eq. 3 to Eq. 11 in 3D via the finite element method using software COMSOL Multiphysics™. The element size is set as 15μm, which is the same as the spatial resolution of the infrared thermal camera.

### 3.4.3 Parameter sensitivity check by numerical simulation

Numerical simulations are done to investigate the effect of various parameters on the temperature profiles. The values used in the simulations can be found in the Supplementary Table S1. The surface temperature profiles along a segment perpendicular to the center of the wire heater (marked as the blue dotted line in Fig.
10(a)) are plotted as a function of the distance from the heater. Variations in the holder thermal conductivity, in the contact resistance between holder and samples, and in the ambient temperature only induce a homogeneous shift of temperature by $\Delta T$ (see Supplementary Fig. S1, S2 and S3).

By contrast, a change in the slope of the temperature profile is observed when the quartz substrate thermal conductivity, the natural convection coefficient, the in-plane thermal conductivity of the CNT film, and the heating power vary. The relationships between the slope of the temperature profile versus these four parameters are shown in Fig. 12. The original temperature profiles can be found in Supplementary Fig. S4, S5, S6, S8.

![Fig. 12](image)

**Fig. 12** Slope of temperature profile versus (a) quartz substrate thermal conductivity; (b) natural convection coefficient; (c) CNT in-plane thermal conductivity; and (d) heating power.
heating power. (The original temperature profiles can be found in Supplementary Fig. S4, S5, S6, S8).

The surface temperature profile is not sensitive to the out-of-plane thermal conductivity of the CNT film (see Supplementary Fig. S7). It is because when the whole system is under thermal steady state, the net heat flux in the CNT film happens in the in-plane direction towards the holder (heat sink). Thus, the measured temperature distribution at the surface of the 3D CNT network is mainly governed by the in-plane thermal conductivity of the CNT film, and not sensitive to the out-of-plane thermal conductivity of the CNT film.

3.4.4 Derivation of the in-plane thermal conductivity

As discussed in Section 3.4.3, the variation in the CNT in-plane thermal conductivity will lead to a slope change in the surface temperature profile with a function of the distance from the heater (see Fig. 11(a)). However, the value of the natural convection coefficient, another unknown parameter, also has an influence on the slope of the temperature profile (see Fig. 11(b)). Therefore, both the CNT in-plane thermal conductivity and the natural convection coefficient need to be derived from the temperature profiles. The temperature profiles obtained at three different heating powers (23 mW, 47 mW, and 99 mW) are perfect candidates for the derivation, as they are non-linearly correlated to the heating power, as shown in supplementary Fig. S8.

To derive the in-plane thermal conductivity of the CNT film and the natural
convection coefficient, both of them are varied iteratively until the simulation matches the experimental data for the three different heating powers. The profile matching is achieved using the least mean-square fitting tool of COMSOL Multiphysics™.

Note that the thermal conductivity of the holder $K_A$ and the contact resistance $R_c$ are also not known during the measurements. However, the simulations show that the change in $K_A$ and $R_c$ only induce a homogeneous shift of the temperature by $\Delta T$ (as discussed in Section 3.4.3), and do not influence the slope of the temperature profiles. Thus, there is no impact on the derivation of the in-plane thermal conductivity.

### 3.4.5 Results for the in-plane thermal conductivity

Figures 13 (a) and (b) show the fitting curves of the temperature profiles for the 3D CNT network and the primary VACNT array. Under different heat generation rates, the fitting curves are in very good agreement with the temperature profiles obtained by the infrared thermal camera, with all the R-squared coefficient larger than 0.99.

The resulting in-plane thermal conductivities for the 3D CNT network and the primary VACNT array are respectively 5.40 W/mK and 0.10 W/mK. The thermal conductivity of the 3D CNT network is much higher than that of the primary VACNT array. The enhancement in the thermal conductivity is attributed to the extra thermal pathways provided by the secondary CNTs, which directly grown from the walls of the primary VACNTs. The natural convection coefficient $h$ for the 3D CNT network
and the primary VACNT array are both found to be 2.0 W/m²K, which is comparable to the conventional natural convection coefficient reported (2~25 W/m²K) [24].

The uncertainty in the derivation of the in-plane thermal conductivity of the CNT films is mainly related to the uncertainty on the values of the quartz substrate thermal conductivity (1.2%) and the heat generating rate (1.6%), since the variation of these two parameters may lead to changes in the slope of the temperature profile (as discussed in Section 3.4.3). The total uncertainty for the thermal conductivity estimation can be calculated using:

$$\frac{\delta K_{CNT,in}}{K_{CNT,in}} = \sqrt{\left[\frac{\partial f(K_{CNT,in})}{\partial K_S} \delta K_S\right]^2 + \left[\frac{\partial f(K_{CNT,in})}{\partial P} \delta P\right]^2},$$

(12)

where $K_S$ is the thermal conductivity of the quartz substrate, and $P$ is the heat generation rate. For the 3D CNT network, the total uncertainty is 17%. While for primary VACNT array, the total uncertainty is calculated to be 51%, which is due to the low sensitivity of the surface temperature profile to low $K_{CNT,in}$ around 0.10 W/mK.

Taking these uncertainties in the measurements into account, the thermal conductivities of the VACNT array and the 3D CNT network are, respectively, 0.10±0.05 W/mK and 5.40±0.92 W/mK, which corresponds to an improvement in the in-plane thermal conductivity is of at least 30 times higher.

### 3.4.6 Additional characterizations: Out-of-plane thermal conductivities

For the sake of completeness, the previous result shows clearly the advantage of using 3D CNT network to enhance the in-plane thermal conductivities. However, as the secondary CNTs appear to branch out from the primary CNTs, the possibility exists that they have a
detrimental effect on the thermal conductivity of the primary CNTs, and thus on the out-of-plane thermal conductivity of the 3D CNT network. To address this issue, the out-of-plane conductivities of the VACNT array and the 3D CNT network were evaluated via a method derived from the 3ω method [14] and reported fully here [1]. The out-of-plane thermal conductivity were found to be, respectively, 17.9 W/mK for the VACNT array and 21.5 W/mK for the 3D CNT network, corresponding to an improvement by 20% of the thermal conductivity thanks to the addition of secondary CNTs. This may be due to the random orientation of the secondary CNTs. Indeed, as they are not growing orthogonally to the VACNTs, but with a random angle to the CNT surface (as can be seen from the TEM pictures), they are also expected to create additional out-of-plane (vertical) thermal pathways via a method derived from the 3ω method [14]. More details on the method and results are the subject of a separate study to be published elsewhere.

3.4.7. Mechanical softness

Furthermore, nanodynamic mechanical analyses were performed on the VACNT array and the 3D CNT network using a Dynamic Mechanical Analysis (DMA) setup Q800 from TA instrument. No significant difference was observed in the viscoelastic properties (loss and storage moduli) of the two samples, thus indicating that the gain in in-plane thermal conductivity in the newly proposed 3DCNT network was obtained without degrading the softness of the system, an important point for its further use as a TIM.
Fig. 13 Fitting of the experimental temperature profile based on the 3D thermal model for different heating powers for (a) the 3D CNT network and (b) the primary VACNT array.
4 Conclusion

A novel 3D CNT network structure is proposed to improve the thermal performances of CNT-based TIMs. In the 3D CNT network structure, the primary VACNTs are cross-linked by randomly-oriented secondary CNTs grown directly from the walls of the primary VACNTs. Both VACNT and 3D CNT network structures are integrated with a local heating element and the temperature distributions of the 3D CNT network and the VACNT array heated under different heating powers are recorded in real time by a 15μm-resolution thermal imaging system. These profiles show that, the surface temperature of the 3D CNT network is much lower than that of the VACNT array, showing a much better thermal dissipation capability. The in-plane thermal conductivities of both types of material are further obtained by a full 3D numerical thermal model of the system. The in-plane thermal conductivity of 3D CNT network is found to be 5.40±0.92 W/mK, which is at least 30 times higher than that of the VACNT array (0.10±0.05 W/mK). The thermal conductivity enhancement is attributed to the extra thermal pathways provided by the secondary CNTs. The direct growth of these CNT from the walls of the primary VACNTs is thought to minimize the thermal resistance between primary and secondary CNTs. The obtained outcomes in this study demonstrate an effective approach in enhancing the in-plane thermal conductivity of CNT films, which gives an insightful view on the applications of CNTs as TIM materials.

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