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# Trajectory-Based Synthesis of Propulsion Systems for Fixed-Thrusters AUVs

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**Abstract.** This paper presents a synthesis method for the Autonomous Underwater Vehicle (AUV) propulsion system based on the features of a trajectory to follow. This method is based on solid/fluid dynamics analysis of a AUV performing the trajectory following task and gives actuation requirements to achieve it properly. This actuation is then used to generate a propulsion system under the form of a Thrust Configuration Matrix (TCM) that is compatible with the desired trajectory. From this matrix the number of thrusters, their position and direction can then be extracted to synthesis a fitted propulsion system. Thus, the propulsion capabilities of the robot will match the trajectory characteristics and it will be able to follow it. The objective of this work is to provide an evaluation as well as a design method to produce a controllable AUV for a given task. A second use of such an analysis is to provide an evaluation process allowing to perform AUV task-based design. The method is developed for generic fixed-thrusters AUVs on any trajectory, and is applied to an existing 4-thrusters AUV for a seabed scanning flat trajectory. The method shows why the initial AUV propulsion does not match the task and what is the solution solving the issue.

**Keywords:** AUV, Propulsion synthesis, Fixed-Thruster.

## 1 Introduction

Thanks to its autonomy, nowadays Underwater Autonomous Vehicles (AUVs) can perform long range surveillance missions and deep sea operations. This kind of vehicles are also used in off-shore installations, to map the sea floor, to secure harbors, to search for sea-mines, among other activities [1]. With enough effort in research, AUVs capabilities will be expanded allowing them to perform even more demanding tasks than the ones accomplished nowadays. Precisely, most AUVs are designed for specific applications as shown in [14]. In a long range type AUV, attention is focused on reducing drag forces and increasing thruster efficiency in order to reduce energy consumption and provide the AUV with more autonomy. Usually under-actuated, this type of vehicles are commonly propelled by a rear thruster and steered by control surfaces. The hull has a hydrodynamic

design in order to reduce drag forces and to improve the autonomy capabilities of the AUV. Fully maneuverable AUVs have at least as many thrusters as their operational space has degrees of freedom (DOF), usually six. Their design is focused on improving agility and multi-directional response (holonomy), which makes these vehicles energy-intensive ([16]).

Regarding the propulsion system, several architectures have been proposed. We can divide them into three categories: classical rear propeller and control surface architectures [23], bio-mimetic propulsion [25, 26, 8] and vector thrust [3]. The latter can be achieved by different means: Some authors use a steerable rear propeller for propulsion, maneuvering and control [2, 17, 18, 10, 9, 13]. Some others make collective and cyclic pitch propellers by using a swash plate [12] or by using shape-memory alloys [24]. Vector propulsion can be achieved by adding forces from fixed thrusters [19, 20] or using re-orientable (or reconfigurable) propellers [11, 4, 22]. Using vector thrusters, it has been shown that a dynamic reconfiguration of the propulsion would allow to adapt the AUV to different in-mission tasks specifications [5]. Meanwhile, finding the fitted propulsion configuration for a given task remain a challenge.

This work is focused on the analysis and synthesis of fixed-thrusters propulsion architectures for AUV in order to achieve a trajectory following task. It provides an analysis of the needed wrench to move the robot throughout all the trajectory following and gives the method to build a compatible thrust configuration matrix (TCM). This fundamental matrix is then used to deduce the propulsion system configuration. In this way, we obtain the minimum number of thrusters, their possible positions and their orientation. In this way we obtain controllable AUVs for the trajectory. The method is first applied to analyze an ill-conditioned AUV that cannot achieve the task, then to analyze and design modified AUVs fit for the task.

## 2 Dynamic Model of AUV and Propulsion System

### 2.1 AUV Kinematic and Dynamic Models

To model the AUV, two orthogonal coordinate systems are used:  $R_0$  ( $O_0, \mathbf{x}_0, \mathbf{y}_0, \mathbf{z}_0$ ) is the earth-fixed frame and  $R_b$  ( $O_b, \mathbf{x}_b, \mathbf{y}_b, \mathbf{z}_b$ ) is AUV body-fixed. In Fig 1 the AUV is depicted in its body-fixed coordinate system.

The vectors describing the motion of the AUV in 6 DOF are:

$$\boldsymbol{\eta} = (x \ y \ z \ \phi \ \theta \ \psi)^t, \boldsymbol{\nu} = (u \ v \ w \ p \ q \ r)^t$$

Here  $\boldsymbol{\eta}$  is the vector of position and orientation in  $R_0$ . The orientation in  $\boldsymbol{\eta}$  is defined using an Euler  $ZYX$  ( $\psi, \theta, \phi$ ) convention as described in [6].  $\boldsymbol{\nu}$  is the linear and angular absolute velocity vector in  $R_b$ .

To change the AUV velocity vector from one to another coordinate system we use a velocity transformation matrix as given in [6]:

Using this transformation matrix  $J(\eta)$ , we can obtain the AUV absolute velocity vector expressed in  $R_0$  from its expression in  $R_b$ , see [6]:

$$\dot{\boldsymbol{\eta}} = \left. \frac{d\boldsymbol{\eta}}{dt} \right|_{R_0} = \mathbf{J}(\boldsymbol{\eta}) \boldsymbol{\nu} \quad (1)$$

The nonlinear rigid-body dynamic equations of the underwater robot, can be formulated as in [1] and [6]:

$$\mathbf{M}\dot{\boldsymbol{\nu}} + \mathbf{C}\boldsymbol{\nu} + \mathbf{D}\boldsymbol{\nu} + \mathbf{G} = \boldsymbol{\tau} \quad (2)$$

where  $\mathbf{M} \in \mathbb{R}^{6 \times 6}$ ,  $\mathbf{C} \in \mathbb{R}^{6 \times 6}$  and  $\mathbf{D} \in \mathbb{R}^{6 \times 6}$  are the matrices of mass, Coriolis and centripetal terms, and damping respectively, including added mass terms.  $\mathbf{G}$  is the vector of gravitational forces and moments. Lastly,  $\boldsymbol{\tau}$  is the wrench of external forces and moments (6 DOF), it accounts for the propulsive wrench generated by the thrusters.  $\boldsymbol{\tau}$  is calculated as follows:

$$\boldsymbol{\tau} = \mathbf{B} \mathbf{u} \quad (3)$$

where  $\mathbf{B}$  is the thrust control matrix (TCM), which depends on the propulsion system configuration (number, position and orientation of the actuators).  $\mathbf{u}$  is the vector of the thrusters forces, i.e., the thrusts.

Added mass effects, drag forces and gravitational/buoyancy efforts are included in matrices of Eqn. (2) as described in Fossen [6] and Antonelli [1] and in our previous works [21].

## 2.2 Fixed Propulsion System Model

AUVs with this type of propulsion are powered by several thrusters placed along different axis in order to combine their thrust and provide six (or less) actuated DOF to the robot. This architecture uses a multi-directional propulsion based on force combination. Fig. 1 shows the ‘‘RSM’’ AUV which includes 4 thrusters: 2 horizontal thrusters are placed at the rear of the AUV and two vertical ones are centered symmetrically on the sides. This configuration provides actuation over the following DOF: Surge (linear motion along the  $\mathbf{x}_b$ -axis), Heave (linear motion along the  $\mathbf{z}_b$ -axis), Yaw (rotation along the  $\mathbf{y}_b$ -axis) and Roll (rotation along the  $\mathbf{x}_b$ -axis). Due to this configuration, 2 DOF are not actuated: Pitch (rotation along  $\mathbf{y}_b$ -axis) and Sway (linear motion along  $\mathbf{y}_b$ -axis). Roll and Pitch motions are mechanically stabilized thanks to the relative position of the buoyancy and gravity centers. Conversely to the Pitch, the Sway is not controlled and not stabilized, thus free motion on  $\mathbf{y}_b$ -axis (drift) is expected to occur.

The thrusters position vectors with regard to  $R_b$  are:

$$\mathbf{P}_1 = \begin{bmatrix} P_{1x} \\ P_{1y} \\ P_{1z} \end{bmatrix}, \mathbf{P}_2 = \begin{bmatrix} P_{2x} \\ P_{2y} \\ P_{2z} \end{bmatrix}, \mathbf{P}_3 = \begin{bmatrix} P_{3x} \\ P_{3y} \\ P_{3z} \end{bmatrix}, \mathbf{P}_4 = \begin{bmatrix} P_{4x} \\ P_{4y} \\ P_{4z} \end{bmatrix}$$

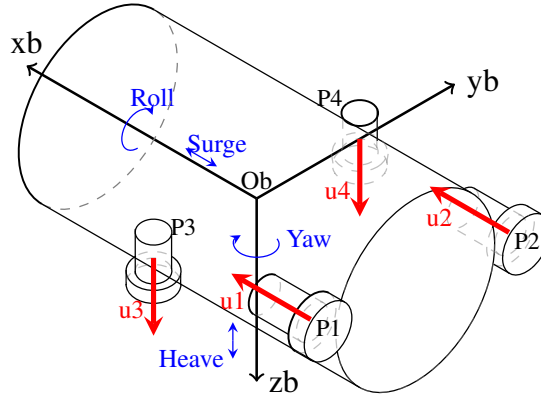


Fig. 1: RSM AUV: 4-fixed thrusters architecture

The RSM AUV thrust control matrix can then be calculated as:

$$\mathbf{B} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & P_{3y} & P_{4y} \\ P_{1z} & P_{2z} & -P_{3x} & -P_{4x} \\ -P_{1y} & -P_{2y} & 0 & 0 \end{bmatrix} \quad \text{with } \mathbf{u} = \begin{bmatrix} u_1 \\ u_2 \\ u_3 \\ u_4 \end{bmatrix} \quad (4)$$

where  $u_1$ ,  $u_2$ ,  $u_3$  and  $u_4$  are the thruster propulsion forces. If the AUV is controllable then  $B$  is invertible. In this case, it is possible to express the thrust control vector as:  $\mathbf{u} = B^{-1}\boldsymbol{\tau}$ , where  $\boldsymbol{\tau}$  is the required propulsive wrench.

### 3 Model-Based Anticipation

To analyze the propulsion system w.r.t. the trajectory, we need to estimate the efforts needed to move the AUV during the trajectory tracking. We use the kinematic and dynamic models to compute the needed (or anticipation) torque  $\boldsymbol{\tau}_a$  in order to follow the desired trajectory  $\boldsymbol{\eta}_d$ . The anticipation method we propose will simply “stick” the AUV on the trajectory such as  $\boldsymbol{\eta} \equiv \boldsymbol{\eta}_d$ . The corresponding vector  $\boldsymbol{\tau}_a$  can be understood as the “nominal control”, steering ideally the AUV on the reference trajectory (See Pino and Delaleau [15] in the design spirit and Hagenmeyer and Delaleau [7] in a control perspective). To proceed, we calculate the inverse kinematic and dynamic models to obtain trajectory-dependent anticipation speed  $\boldsymbol{\nu}_a$  and efforts (or wrench)  $\boldsymbol{\tau}_a$ .

The point  $O_e$  is an arbitrary point belonging to the AUV, with which we want to follow the trajectory. We can write the velocity of point  $O_e$  in  $R_b$ :

$$\boldsymbol{\nu}_e = \underbrace{\begin{bmatrix} 1 & 0 & 0 & 0 & \epsilon_z & -\epsilon_y \\ 0 & 1 & 0 & -\epsilon_z & 0 & \epsilon_x \\ 0 & 0 & 1 & \epsilon_y & -\epsilon_x & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}}_{\mathbf{T}} \underbrace{\begin{bmatrix} u \\ v \\ w \\ p \\ q \\ r \end{bmatrix}}_{\boldsymbol{\nu}}, \quad \mathbf{r}_e = \begin{bmatrix} \epsilon_x \\ \epsilon_y \\ \epsilon_z \end{bmatrix} = \overrightarrow{O_b O_e}$$

with  $\mathbf{r}_e$  the position of point  $O_e$  in  $R_b$  and  $\mathbf{T}$  the transformation matrix of velocity  $\boldsymbol{\nu}$  from  $O_e$  to  $O_b$ . Taking into account preceding equations leads to:

$$\dot{\boldsymbol{\eta}}_e = \mathbf{J}(\boldsymbol{\eta}) \boldsymbol{\nu}_e = \mathbf{J}(\boldsymbol{\eta}) \mathbf{T} \boldsymbol{\nu} \quad (5)$$

This allows us to determine the relation between the velocity at point  $O_e$ , namely  $\dot{\boldsymbol{\eta}}_e$ , and the robot anticipation velocity  $\boldsymbol{\nu}_a$  at  $O_b$ , expressed in  $R_b$ :

$$\boldsymbol{\nu}_a = \mathbf{T}^{-1} \mathbf{J}(\boldsymbol{\eta}_2)^{-1} \dot{\boldsymbol{\eta}}_e \quad (6)$$

Based on the dynamic model of the robot described before (Eq. 2), the following anticipation dynamic law is deduced (in  $R_b$ ):

$$\boldsymbol{\tau}_a = \mathbf{M} \dot{\boldsymbol{\nu}}_a + (\mathbf{C}(\boldsymbol{\nu}_a) + \mathbf{D}) \boldsymbol{\nu}_a + \mathbf{G} \quad (7)$$

Fig. 2 depicts a pipeline following trajectory and Fig. 3 shows the wrench  $\boldsymbol{\tau}_a$  we obtained by the anticipation method on the pipeline trajectory following task, applied on a generic AUV (6 DOF).

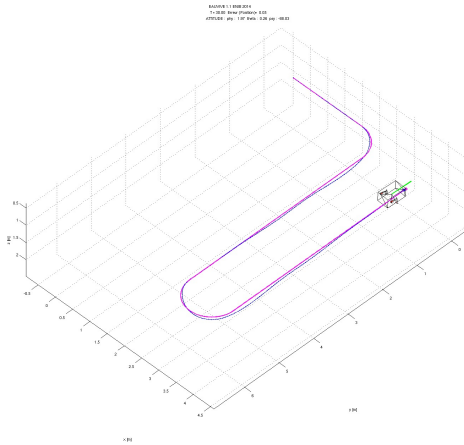


Fig. 2: 3D representation of the trajectory

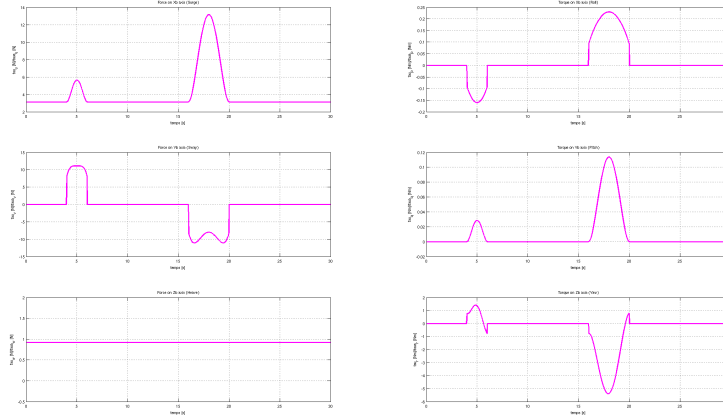


Fig. 3: Efforts in  $R_b$  required for the pipeline following task. First column : surge, sway and heave. Second column : roll, pitch and yaw motions.

We can see that for the forces (first column), the propulsion is required on 3 axes, since surge, sway and heave are necessary to maintain the  $O_e$  point on the trajectory. Inertia forces demand more efforts during the two turns. Considering the moments (second column), roll and pitch motions do not require any effort outside the turns (the trajectory being planar) while the turns generate small angular accelerations that should be compensated by mechanical stability. Finally, the yaw motion need an important moment during the turns. This can be summarized in the anticipated wrench  $\tau_a$  by writing:  $\tau_a = [* * * 0 0 *]^t$ . Note that all stars (\*) in a vector stand for independent non zero coefficients.

## 4 Synthesis of the Propulsion System

All the coordinates, forces and torques are expressed in the AUV frame  $\mathcal{R}_b$ . The robot is actuated by  $K$  thrusters located in points  $P_k = (P_{x,k}, P_{y,k}, P_{z,k})$  (see Fig. 1). The controlled force produced by thruster  $k$  is  $\vec{F}_k = u_k \vec{f}_k$ , where  $\|\vec{f}_k\| = 1$  and  $|u_k| = \|\vec{F}_k\|$ ;  $\vec{f}_k$  is the *force direction* and  $u_k$  is the *thrust* (control variable). Thruster  $k$  also produce the torque  $\vec{T}_k = \overrightarrow{O_b P_k} \wedge \vec{F}_k = u_k \underbrace{(\overrightarrow{O_b P_k} \wedge \vec{f}_k)}_{\vec{\tau}_k}$

where  $\vec{\tau}_k$  is the “normalized” torque.

Each thruster is completely described by its position  $P_k$ , its control variable (scalar)  $u_k$  and its force direction  $\vec{f}_k$ . The *normalized wrench* of thruster  $k$  is thus  $\vec{\omega}_k = (\vec{f}_k, \vec{\tau}_k)$ . The  $B$  matrix is constituted by the normalize wrenches: each column of  $B$  is precisely the normalized wrench of one thruster.

#### 4.1 Single Thrusters and Basic Configurations

One has seen that each thruster is potentially able to activate several DOF (not independently of course). For the sake of simplicity of the design one seeks for simple situations in which the thrusters could only activate 1 or 2 degree of freedom. In case of 2 DOF, this will be 1 translation and 1 rotation. The 9 configurations are listed and named in Table 1. One sees that a single thruster cannot activate a rotation without activating a translation.

In the sequel, the 3 basic thruster types that activate only translation are generically named as  $T_{\bullet}$  and the other 6 ones will be denoted  $T_{\bullet\bullet}$ .

Table 1: Wrenches associated to some thrusters.

Configuration name	$T_x$	$T_y$	$T_z$	$T_{yx}$	$T_{zx}$	$T_{xy}$	$T_{zy}$	$T_{xz}$	$T_{yz}$
Thruster position	$\begin{bmatrix} P_x \\ 0 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ P_y \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 0 \\ P_z \end{bmatrix}$	$\begin{bmatrix} 0 \\ P_y \\ P_z \end{bmatrix}$	$\begin{bmatrix} 0 \\ P_y \\ P_z \end{bmatrix}$	$\begin{bmatrix} P_x \\ 0 \\ P_z \end{bmatrix}$	$\begin{bmatrix} P_x \\ 0 \\ P_z \end{bmatrix}$	$\begin{bmatrix} P_x \\ P_y \\ 0 \end{bmatrix}$	$\begin{bmatrix} P_x \\ P_y \\ 0 \end{bmatrix}$
Force direction	$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$	$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$
Produced Torque	$\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$	$\begin{bmatrix} -P_z \\ 0 \\ 0 \end{bmatrix}$	$\begin{bmatrix} +P_y \\ 0 \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ +P_z \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ -P_x \\ 0 \end{bmatrix}$	$\begin{bmatrix} 0 \\ 0 \\ -P_y \end{bmatrix}$	$\begin{bmatrix} 0 \\ 0 \\ +P_x \end{bmatrix}$

#### 4.2 Thrusters Configuration Design

The aim of this paper is to find a thruster configuration which allows the robot to follow one or several given trajectories. Denotes by  $[t_i, t_f]$  the time interval on which the trajectory  $\tau_a$  is defined:  $t \in [t_i, t_f] \rightarrow \tau_a(t) \in \mathbb{R}^6$ . Denotes by  $\mathcal{J}(\tau_a)$  the vector subspace of  $\mathbb{R}^6$  defined by:

$$\mathcal{J}(\tau_a) = \text{span} \{ \tau_a(t) \mid t \in [t_i, t_f] \}$$

The design procedure consists in finding a family of wrenches  $\{\omega_1, \dots, \omega_K\}$  among the  $T_{\bullet}$ 's and the  $T_{\bullet\bullet}$ 's in Table 1 such that:

$$\mathcal{J}(\tau_a) \subset \text{span} \{ \omega_1, \dots, \omega_K \}$$

The family of thruster  $\{\omega_1, \dots, \omega_K\}$  is said to be **minimal** w.r.t. the trajectory  $\tau_a$  if the two following conditions<sup>4</sup> are satisfied:

$$\mathcal{J}(\tau_a) \subset \text{span} \{ \omega_1, \dots, \omega_K \} \quad \text{and} \quad \mathcal{J}(\tau_a) \not\subset \text{span} \{ \omega_1, \dots, \omega_{K-1} \}$$

<sup>4</sup> The second condition is valid up to a renumbering of the  $\omega_i$ 's.



**Design procedure<sup>5</sup>:**

- **Step 1:** Choose as many  $T_{\bullet\bullet}$  thrusters as needed rotations<sup>6</sup>.
- **Step 2:** Choose other  $T_{\bullet\bullet}$  thrusters in order to cover all/most translations.
- **Step 3:** If needed, choose  $T_{\bullet}$  thrusters in order to cover missing translations.

An analysis is done on two already designed AUVs and the design procedure is illustrated to generate a new one that matches the task and is minimal.

**4.3 Design Examples**

**RSM AUV:** This existing AUV has 4 thrusters and must follow the pipeline trajectory:

$$\boldsymbol{\tau}_a = \begin{bmatrix} * \\ * \\ * \\ 0 \\ 0 \\ * \end{bmatrix}, \quad \mathbf{B}_{\text{rsm}} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & Y_3 & Y_4 \\ 0 & 0 & 0 & 0 \\ -Y_1 & -Y_2 & 0 & 0 \end{bmatrix}, \quad \mathbf{u}_{\text{rsm}} = \begin{bmatrix} u_1 \\ u_2 \\ u_3 \\ u_4 \end{bmatrix}, \quad \boldsymbol{\tau}_{\text{rsm}} = \begin{bmatrix} * \\ 0 \\ * \\ * \\ 0 \\ * \end{bmatrix}$$

One sees that this design corresponds to the choice:

- 2 thrusters  $T_{xz}$  (one located at  $(X_1 \ Y_1 \ 0)^t$  and the other one at  $(X_2 \ Y_2 \ 0)^t$ );
- 2 thrusters of type  $T_{zx}$  (located in  $(0 \ Y_3 \ Z_3)^t$  and  $(0 \ Y_4 \ Z_4)^t$ ).

Finally one has  $\mathcal{J}(\boldsymbol{\tau}_a) \not\subset \mathcal{J}(\boldsymbol{\tau}_{\text{rsm}})$  and this AUV cannot perform the task properly. The second star in  $\boldsymbol{\tau}_a$  (sway motion) is not matched in  $\boldsymbol{\tau}_{\text{rsm}}$  due to the 0. Since this AUV is not suitable for task, we propose to add a fifth thruster to generate the missing surge actuation (see RSM2 below).

**RSM2 AUV:** The adjunction of a “bow thruster” to RSM gives the RSM2 AUV that has a 5 thrusters and thus can follow the trajectory:

$$\boldsymbol{\tau}_a = \begin{bmatrix} * \\ * \\ * \\ 0 \\ 0 \\ * \end{bmatrix}, \quad \mathbf{B}_{\text{rsm2}} = \begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & Y_3 & Y_4 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ -Y_1 & -Y_2 & 0 & 0 & X_5 \end{bmatrix}, \quad \mathbf{u}_{\text{rsm2}} = \begin{bmatrix} u_1 \\ u_2 \\ u_3 \\ u_4 \\ u_5 \end{bmatrix}, \quad \boldsymbol{\tau}_{\text{rsm2}} = \begin{bmatrix} * \\ * \\ * \\ * \\ 0 \\ * \end{bmatrix}$$

On sees that RSM2 is obtained from RSM by adding one thruster of type  $T_{yz}$  located at  $(X_5 \ Y_5 \ 0)^t$ . Here we have  $\mathcal{J}(\boldsymbol{\tau}_a) \subset \mathcal{J}(\boldsymbol{\tau}_{\text{rsm2}})$  and the AUV can achieve the task. However, the solution is not minimal as  $\mathcal{J}(\boldsymbol{\tau}_a) \neq \mathcal{J}(\boldsymbol{\tau}_{\text{rsm2}})$ . Here, the roll motion can be actuated whilst it is not a required DOF, which makes this configuration non-minimal w.r.t. the task and we will seek a 4-thrusters of the AUV achieving this task (see NEW AUV below).

<sup>5</sup> The procedure favors the  $T_{\bullet\bullet}$  are they are off-centered and more easily implementable than the  $T_{\bullet}$  ones.

<sup>6</sup> Rotation thrusters  $T_{\bullet\bullet}$  are chosen first as they generally induce translations.

**NEW AUV:** One seeks for a 4-DOF AUV able to track  $\tau_a = [**00*]$  trajectories. We here apply the design procedure given in previous section:

- **Step 1:** The needed rotation about  $z_b$  require either a  $T_{xz}$  or a  $T_{yz}$  thruster.
- **Step 2:** At this step we choose either  $T_{xz}, T_{yz}$  or  $T_{yz}, T_{xz}$
- **Step 3:** In the two cases,  $z_b$  is missing we end-up with the choice of  $T_z$ .

The two obtained configurations are:

$$\{T_{xz}, T_{xz}, T_{yz}, T_z\}, \{T_{yz}, T_{yz}, T_{xz}, T_z\}$$

Any other choice leads to more thrusters. Notice that same symbol appearing twice in the same configuration mean 2 thrusters of the same type at two different locations. In the next section, only the first case of this NEW AUV will be simulated. The corresponding TCM matrix  $B_{\text{new}}$  is explicitied below:

$$B_{\text{new}} = \begin{bmatrix} 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ -Y_1 & -Y_2 & X_3 & 0 \end{bmatrix}, \mathbf{u}_{\text{new}} = \begin{bmatrix} u_1 \\ u_2 \\ u_3 \\ u_4 \end{bmatrix}, \boldsymbol{\tau}_{\text{new}} \equiv \boldsymbol{\tau}_a = \begin{bmatrix} * \\ * \\ * \\ 0 \\ 0 \\ * \end{bmatrix}$$

## 5 Simulation and Results

The studied trajectory is depicted in Fig. 2. The 3 different configurations, namely “RSM”, “RSM2” and “NEW”, are considered and compared. Fig. 4 reports the propulsion efforts whilst Fig. 5 express the position and angular errors w.r.t. the desired reference trajectory. In the simulations, the control of the AUV is achieved by feedback linearization, however, the range of this work extends far beyond this method.

## 6 Conclusion

The main result of this work is to show that it is possible, knowing the dynamic model of the AUV to build an intrinsically controllable AUV thanks to a specifically designed propulsion system. We showed why some AUVs are unable to achieve a given family of trajectory tasks and how to make it fit to do so. Moreover, we proposed a mathematical and programmable method to build a rational and controllable AUV, using the minimum number of thrusters to perform a trajectory following task. Simulations have been achieved to validate the design. Future works will deal with the generalization to other propulsion modes (not only thrusters) and will improve the control techniques based on nonlinear models. Real word experiments for trajectory following missions will then be done to validate the propulsion synthesis.

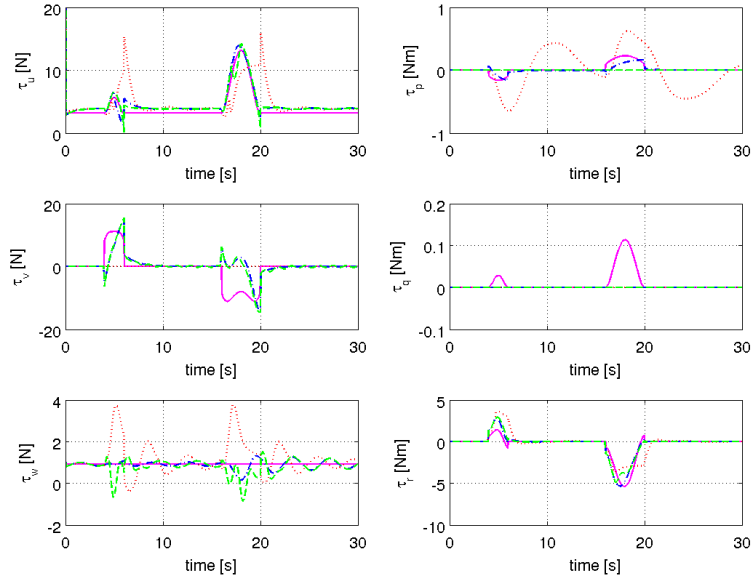


Fig. 4: AUV propulsion efforts : Ref - RSM - - RSM2 .- NEW ..

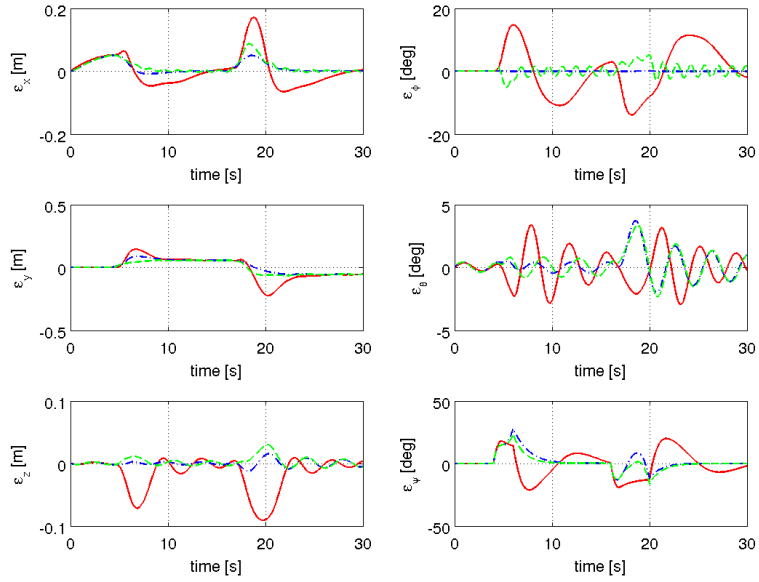


Fig. 5: AUV trajectory errors : RSM - RSM2 .- NEW - -

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