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Mumford-Shah Mesh Processing using the Ambrosio-Tortorelli Functional

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Figure 1: Our discretization of the MS functional along with our new vertex projection technique allows for applications such as mesh denoising, segmentation, inpainting and normal map embossing. (b) Our method removes heavy noise while preserving sharp features shown in yellow. (c) We remove vertices highlighted in cyan from the original mesh (a); our method finds sharp features (shown in yellow) and successfull inpaints the missing area. (d) We decompose the original mesh (a) into piecewise smooth segments whose boundaries are characterized by sharp features shown on edges in red. (e) We emboss a normal map into the mesh vertices.

Abstract

The Mumford-Shah functional approximates a function by a piecewise smooth function. Its versatility makes it ideal for tasks such as image segmentation or restoration, and it is now a widespread tool of image processing. Recent work has started to investigate its use for mesh segmentation and feature lines detection, but we take the stance that the power of this functional could reach far beyond these tasks and integrate the everyday mesh processing toolbox. In this paper, we discretize an Ambrosio-Tortorelli approximation via a Discrete Exterior Calculus formulation. We show that, combined with a new shape optimization routine, several mesh processing problems can be readily tackled within the same framework. In particular, we illustrate applications in mesh denoising, normal map embossing, mesh inpainting and mesh segmentation.

1. Introduction

The Mumford-Shah (MS) functional, originally intended for image segmentation [MS89], is a well-known functional which models an image as a piecewise-smooth function. Minimizing this functional recovers both a piecewise-smooth image that can be useful for applications such as image denoising, and the set of discontinuities can be useful for edge detection. Since the nineties, this model has seen a tremendous success in image processing and has found many applications from image segmentation [TYW01, VC02] to denoising [TYW01], inpainting [ES02], magnification [TYW01], deblurring [BSK06] or registration [BAS10].

This functional has however attracted little attention in geometry processing, where similar problems are encountered. Notable exceptions include the work of Zhang et al. [ZZWC12] that makes use of a convexified version of the MS model for mesh segmentation, and the finite element method of Tong and Tai [TT16] to construct feature lines on meshes. This lack of interest might have come from several challenges that need to be overcome. First, the model itself is not suited to a computational resolution. Hence, numerical methods only solve approximate MS models. Second, their computational complexity makes algorithms tuned for regular grids difficult to scale to large unstructured meshes. Third, the MS formulation, once adapted to manifolds, exhibits differential operators that need careful handling when discretized over triangular meshes. Last, the MS model represents a piecewise-smooth scalar function over a domain; it is thus not obvious what this function should be in the context of mesh processing and for which applications.
Fortunately, recent progress on the first two issues allows to paint a brighter picture. On the computational side, various approximations of the MS functional have recently been proposed. In this paper, we are interested with an accurate approximation of the MS functional: the Ambrosio-Tortorelli’s functional [AT90]. Recent advances have further made calculus on meshes practical and affordable. In particular, Discrete Exterior Calculus (DEC) [Hir03] has become popular for easily formulating and solving differential equations on meshes. We will formulate the MS functional as a discrete AT model in the language of DEC, in the spirit of the method of Coeurjolly et al. [CFGL16].

Regarding the choice of scalar function to use in the MS functional, it obviously depends on the targeted applications. For our applications, we take advantage of our DEC formulation to consider each component of the normal vector at each point of the surface as a 0-form stored on the faces of a dual mesh. This results in a set of three scalar functions, generalizing MS to vector functions [H11]. We will jointly minimize MS over these three scalar functions. Overall, this essentially allows to smooth out the normals of an input mesh so they better match the underlying continuous surface being approximated while preserving mesh discontinuities.

Benefitting from these advances, we formulate a set of classical mesh processing problems using the MS functional applied to the manifold’s normal vector field. From the resulting regularized normal vector field, we further introduce a shape optimization routine as an easy-to-implement projection operator which deforms the geometry so that geometric normals match the obtained regularized normals. We illustrate our method on a number of applications, such as mesh denoising, normal map embossing, mesh inpainting and mesh segmentation.

2. Related work

The Mumford-Shah Model. Mumford and Shah described a functional representing an input image by a piecewise-smooth approximation [MS89]. This functional reads:

\[ MS[u, C] = \alpha \int_{\Omega} (u - g)^2 \, dx + \beta \int_{\Omega \setminus C} |\nabla u|^2 \, dx + \gamma \int_{C} \, ds, \]

(1)

with \( g \) the input image on a two-dimensional planar domain \( \Omega \), \( u \) its (unknown) approximation, and \( C \) a set of (unknown) curves describing the set of discontinuities. The parameters of the model intuitively model the tightness \( \alpha \) of the approximation to the image, the smoothness \( \beta \) of the approximation, and the length of discontinuities \( \gamma \). While for segmentation purpose, it is often assumed that \( C \) forms a closed curve or is the boundary of some partition of the space, this is not a requirement of the model nor the optimal solution to it. In addition, this model is not restricted to images: in the general case, \( \Omega \) need not be a plane and can be an arbitrary surface, and \( g \) a real-valued function over this surface.

Unfortunately, except in limited scenarios, this functional is non-convex and very difficult to optimize.

Optimizing the MS functional. To avoid these difficulties, various approximations to MS have been proposed, and among them, the most natural ones are convex envelopes or convex approximations to MS functional. When restricting the problem to foreground / background extraction, the MS functional can be convexified by replacing the term accounting for the length of segment boundaries by the total variation of the gradient of a segment binary indicator function [CEN06]. Instead of a piecewise-smooth assumption, this assumes a piecewise constant function and precludes open segment boundaries or isolated discontinuities. This can be extended to multiple segments but still necessarily produces disjoint sets. While this assumption can be appropriate for certain segmentation applications and has indeed been successfully used for mesh segmentation [ZZWC12], this may not be suitable in our context where our function of interest is the normal field that varies relatively smoothly across the surface [ZZWC12] and may exhibit internal discontinuities (see Fig. 5, first row). Similarly, Tsai et al. [TYW01] directly optimize the MS functional using level sets, but also requires closed segments boundaries. These approaches thus lack the generality we are targeting. We instead resort to an early approximation from Ambrosio and Tortorelli [AT90] that relies on Γ-convergence results, and provably converges towards the MS functional. Its numerical optimization is nonetheless far from being trivial. For instance, Chambolle and Dal Maso [CDM99] and Bourdin and Chambolle [BC00] employ a Finite Element Method with adaptive mesh refinement and edge alignment is required for its optimization. Even with such advanced technique, these numerical methods are very sensitive to noise [FLT16]. Fortunately, new discretization schemes for the Ambrosio-Tortorelli (AT) model have been designed on grids [FLT16, CFGL16] and do not require FEM anymore nor adaptive mesh to get piecewise smooth solutions. This discretization has seen applications for image restoration [FLT16] and feature extraction on voxel-based digital geometries [CFGL16]. A first discrete differential calculus version of AT has been employed by Pokrass et al. [BBN011] to solve the partial matching of non-rigid 3D shapes. Their discretization is different from ours since discontinuities and values live on vertices, while the cross-term is evaluated on faces, resulting in smoother features. This is fine for their specific objective but limits its range of applications. In contrast our approach allows coarse-to-fine detection of features for a variety of geometry processing tasks. An alternative finite element discretization of AT has been recently proposed for triangle meshes [TT16]. This approach is the closest one to our formulation but it is not able to recover piecewise smooth patches on noisy data as illustrated in Figure 2. We propose a specific Discrete Exterior Calculus discretization of this functional, which achieves sharper and more robust features, as we show in our experiments.

Applications in image processing. The MS functional originated from the image processing community as a way to represent an image as a piecewise-smooth function. In the last 40 years, it has led to numerous applications, even if most of the time it is only simpler variants of the MS functional that are solved. Image segmentation [TYW01, VC02] and denoising [TYW01] are the two main applications that directly follow from the variables being optimized for (that is, discontinuity boundaries and piecewise smooth approximations). Image inpainting [ES02] is rendered possible by removing the data attachment term inside the inpainted area. A 3x image magnification [TYW01] is performed by interlacing the input image in a 3x upsampled grid, and inpainting the missing pixel values. Bar et al. extend a deconvolution functional by summing it with the MS functional [BSK06], hence leading to a new image
deconvolution method with piecewise smoothness prior. Similarly, Ben-Ari and Sochen integrate the MS model in a stereo-matching functional, resulting in piece-wise smooth disparity maps [BAS10].

Variational methods in mesh processing. Variational methods for mesh processing have long been studied. A variational method optimizes a given functional over a space of functions. The most common examples of such functionals used in mesh processing include Lloyd’s functional [CSAD04], Total Variation [ZWZD15], the variational problem associated with the Poisson equation [Y2004], the curvature energy [Zor05] or the MS functional [CFGL16, ZZWC12]. Individual mesh processing applications have their own set of priors, hypotheses and constraints, and it is illusory to search for an all-purpose functional. However, we show that the MS functional appropriately solves a number of problems and is of value to the geometry processing community.

3. Discretizing Mumford-Shah over Surfaces

This section describes our model for mesh processing, that extends the model of Coeurjolly et al. [CFGL16] tailored for voxel-based geometries. In particular, we briefly discuss the AT approximation, and expose our discretization over triangular meshes within the DEC framework.

3.1. Ambrosio-Tortorelli’s Approximation

Ambrosio and Tortorelli reformulates the MS functional [AT90] by working on a smoothness indicator function rather than the set of discontinuities C. This indicator function, denoted by ν in the following, is optimized such that it takes the value ν(x) = 1 wherever g(x) is smooth, and ν(x) = 0 on discontinuities. Therefore we call it the feature function. In their model, this function ν is smooth and kept close to 1 where g is smooth, and its oscillations are prevented by keeping ∇ν close to 0. Their functional can be written as follows:

\[
AT_e[u, ν] = \int_Ω \left[ α(u - g)^2 + |ν∇u|^2 + λε(∇ν)^2 + \frac{λ(1 - ν)^2}{4} \right] dx. \tag{2}
\]

This functional now depends on the same parameters α and λ (β is set to 1 without loss of generality), but also requires a parameter ε. Parameter λ is still such that 1/λ represents the length of discontinuities, and parameter ε controls the smoothness of the feature ν. Ambrosio and Tortorelli proved that when ε tends to zero, minimizers of this functional exactly corresponds to those of the MS functional. However, the problem is now quasi convex, and the integration domain is fixed and does not involve unknown curves.

3.2. Minimizing the Energy

For a fixed ε, since the energy (2) is quasi convex, we can minimize it by alternating minimizations over u and ν. We follow the AT energy formulation proposed in [CFGL16]. The feature scalar field ν is discretized as a primal 0–form, that is a collection of scalar values associated with each vertex of the mesh. The normal vector fields (both u and g) are each discretized as three dual 0–forms, one for each coordinate of the $\mathbb{R}^3$ embedding space. Note that Focardi and Iurlano showed that AT in the vectorial case also converges towards an approximation of MS [FI14]. Each of those three dual 0–forms can be seen as a scalar value associated with each primal face (or dual vertex) of the mesh. Denoting d and $\bar{d}$ the primal and dual exterior derivatives, it follows that dv is a primal 1–form and $\bar{du}$ corresponds to three dual 1–forms. Norms are induced by the natural inner products between k–forms. We rewrite then the AT functional as a sum of inner products on primal and dual 0 and 1–forms:

\[
AT_e[u, ν] = -α(u - g)^2 + \|νdu, νd\bar{u}\| + \lambdaε(\|dν\| + \|\bar{d}ν\|) + \frac{λ}{4ε}(1 - ν)^2. \tag{3}
\]

Note that we have discretized (2) such that our feature function ν does not not become identically one when epsilon tends to 0, and remains zero around feature edges. To achieve such discontinuities, the function ν acts as a rescaling of the derivatives of u and not as a rescaling of the squared gradient norm. Hence it operates directly on edges in (3) and it does not operate on vertices as would give a standard DEC discretization of (2). Our discretization of AT is thus more related to discontinuous FEM than to continuous and linear basis elements. For instance, the FEM approach of Tong and Tai [TT16] oversmoothes features (function ν becomes almost 1 everywhere) and requires post-processing to find its valleys.

We write the $AT_e$ energy in matrix form, using the following no-
4. Deforming a Mesh to a Prescribed Normal Field

Given a regularized normal field \( u \) over an input mesh (e.g., given by a first AT minimization), we wish to deform the mesh by moving its vertices such that the triangles normal vectors match the prescribed normal field \( u \). We perform this operation by minimizing an energy \( E \) consisting of three terms: a normal matching term \( E_m \), a fairness term \( E_f \), and a data attachment term \( E_d \), described in this section. Note that some terms may appear in various forms in other works [Tao01, FDC03, PAH+07, SRML07]. We describe them for self-containment and propose a fairness energy to take into account the feature field. Our method then proceeds by alternately solving for the unknown positions of the deformed mesh with a fixed feature field \( v \) and solving the AT functional to update the feature field \( v \) and piecewise smooth normals \( u \).

Matching normals. Let \( p \) be the vertices positions of the deformed mesh, and \( F = \{ f_j \}_{j=1}^N \) the set of triangles where \( f_j \) denotes the \( f^k \)th vertex of the \( f^k \)th triangle, with \( j \in \{0,1,2\} \). As we are deforming the mesh, the topology (and hence the set of triangles) of the deformed mesh is the same as that of the input mesh. We denote by \(|p|\) the number of vertices. Our goal is to find \( p \) such that per-triangle geometric normals match the prescribed normal field \( u \).

We formulate this condition by imposing that each edge of each triangle be orthogonal to \( u \):

\[
E_m = \sum_{j=1}^N \left( (p_{f_1} - p_{f_0}) \cdot u \right)^2 + \left( (p_{f_2} - p_{f_0}) \cdot u \right)^2 + \left( (p_{f_3} - p_{f_0}) \cdot u \right)^2
= \sum_{j=1}^N E_m(f_j).
\]

Note that the summation is performed over all triangles and not over edges since \( u \) is known per triangle. This induces sharper discontinuities. Its gradient with respect to each triangle vertex position is given by:

\[
\nabla_{p_{f_0}} E_m(f_j) = 2\left(2(p_{f_1} - \sum_{k \neq j} p_{f_k}) \cdot u\right) = A(f_j) p,
\]

where \( A(f_j) \) is a \( 3 \times 9 \) matrix, that can be assembled in a \( 3|p| \times 3|p| \) matrix \( A \) for all vertices of all triangles of the mesh.

Fairness. We additionally enforce the piecewise smoothness of the deformed mesh by adding a fairness term. This term forces neighboring triangles to share similar geometric normals, at least wherever the feature \( v = 1 \) and corresponds to a thin plate energy. Its effect can be appreciated in Fig. 4. For an edge \( e = (p_{i}, p_{j}) \) between triangles \( t_1 = (p_{i}, p_{j}, p_{k}) \) and \( t_2 = (p_{i}, p_{j}, p_{l}) \), the fairness energy reads:

\[
E_f(e) = \left( \frac{|v_{p_{i}}| + |v_{p_{j}}|}{2} \right)^2 \|p_{i} + p_{j} - p_{k} - p_{l}\|^2,
\]

and we obtain \( E_f \) by summing over all edges \( E_f = \sum E_f(e) \). Fixing \( v \), the gradient of \( E_f(e) \) with respect to \( p_{i} \) (resp. \( p_{j} \)) is:

\[
\nabla_{p_{i}} E_f(e) = 2\left(\frac{|v_{p_{i}}| + |v_{p_{j}}|}{2}\right)^2 (p_{i} + p_{j} - p_{k} - p_{l}) = B(e)p,
\]

Convergence and stability are improved by progressively reducing \( \varepsilon \) rather than directly solving the problem with a small \( \varepsilon \). We hence perform the above minimization repeatedly, dividing \( \varepsilon \) by 2 at each iteration (we typically start at \( \varepsilon_0 = 2 \) and decrease until \( \varepsilon = 0.25 \)). This allows to better infer the general position of features at a coarse scale (large \( \varepsilon \)), and then to better precisely delineate them at a fine scale (small \( \varepsilon \)). This coarse-to-fine optimization is especially important in the inpainting case, where the value of \( \varepsilon_0 \) should be around the radius size of the inpainted region.
where $B(e_i)$ is a $3 \times 12$ matrix. These matrices again be assembled in a $3|p| \times 3|p|$ matrix $B$ by summing contributions of all edges.

\[ E_d = \sum_i \|p_i - q_i\|^2. \]

Its gradient is $\nabla p E_d = 2(p - q)$.

\section{Data attachment.}
Data attachment. We finally prevent vertices to depart too much from their original position, and add a data attachment term. Denoting $q$ the original position of the vertices, this reads:

\[ E_d = \frac{1}{T} \sum_i \|p_i - q_i\|^2. \]

\section{Solving for positions.}
Solving for positions. Denoting $E = E_m + w_1 E_f + w_2 E_d$ the weighted sum of the energies, we can now obtain $p$ by solving $\nabla p E = 0$. This amounts to solving the linear system

\[ (A + w_1 B + w_2 Id)p = w_2 q, \]

where $Id$ is the $3|p| \times 3|p|$ identity matrix. The left-hand linear operator being positive and definite (as long as weights are positive), efficient inversion algorithms can be used to solve the system. Except for inpainting which requires large values of $w_1$ as discussed next, most results were obtained with $w_1 = 1$, though decreasing $w_1$ can be useful for large noise or unreliable vertex positions. We have kept $w_2$ fixed and small throughout all our experiments, with $w_2 = 0.05$. Note that meshes are uniformly scaled to fit the unit ball, so that parameters are comparable across meshes.

\section{Applications}

Inspired by image processing, our method serves various geometry processing applications illustrated in this section. This includes restoring noisy meshes, segmenting meshes, inpainting missing data, or embossing a normal map into the mesh vertices.

\subsection{Denoising}

Denoising the model of Fig. 2 without (a) and with (b) a small fairness term $E_f$ ($w_1 = 0.5$). The fairness term favors more regular near-Delaunay meshes. The colormap indicates the aspect ratio of each triangle ($1 - \frac{\alpha_T}{\pi}$ with $\alpha_T$ the minimum angle of triangle $T$).

\begin{figure}[h]
\centering
\includegraphics[width=\linewidth]{denoising.png}
\caption{Denoising the model of Fig. 2 without (a) and with (b) a small fairness term $E_f$ ($w_1 = 0.5$). The fairness term favors more regular near-Delaunay meshes. The colormap indicates the aspect ratio of each triangle ($1 - \frac{\alpha_T}{\pi}$ with $\alpha_T$ the minimum angle of triangle $T$).}
\end{figure}

\subsection{Segmentation}

Segmentation benchmarks.\cite{CGF09}

We segment meshes into piecewise smooth parts. Note that, contrary to semantic mesh segmentation, our segmentation is purely geometric and bears no semantic meaning. This can find applications in mesh parameterization where seams should remain as little visible as possible \cite{RNLL10}, or as a preprocessing for further feature extraction (see the mesh segmentation survey of Attene et al. \cite{AKM06}). However, this makes numerical evaluation difficult since no ground truth segmentation is available, in contrast to semantic segmentation benchmarks \cite{CGF09}.

To perform this segmentation, we make use of our MS solver to obtain the feature field $v$ for each vertex of the mesh. We further clamp $v$ since it can occasionally take values outside of the range $[0,1]$ due to approximations. We then make use of the method of Keuper et al. \cite{KLB15} which solves a minimum multicut problem in the triangle adjacency graph using the Kernighan Lin method. This method takes as input the probability of two adjacent triangles to belong to different segment, which amounts to bringing the feature $v$ from vertices to edges. For each edge, we obtain a splitting probability by averaging the value $1 - v$ of both vertices of the edge, while forcing this probability to 0.1% when adjacent triangles have their (regularized) normals further than $5^\circ$ apart. Segmentation results can be seen in Fig. 9.

In Fig. 10, we illustrate the differences between our geometric segmentation and state-of-the-art semantic segmentation meth-
5.3. Inpainting

Inpainting seeks to fill in missing areas of a mesh. To perform mesh inpainting, one should first triangulate the missing area. The first step is to recover the topology of the missing area, which we perform using the hole filling algorithm [Lie03] implemented in CGAL [FP09]. Then, we set the data attachment terms $\alpha$ and $w_2$ to a large value (typically, $\alpha = w_2 = 1000$) outside of the inpainted area to prevent known vertices from moving, and $w_2$ to zero inside. Since the hole filling tends to oversmooth the inpainted area, we...
set \( \lambda \) to one tenth of its original value inside the inpainted area, hence favoring longer features. We finally solve the MS problem and conform the mesh to the obtained normals. Inpainting results are shown in Fig. 11.

5.4. Embossing Normal Maps

Normal mapping is a useful technique for interactive applications, and allows for efficient low-polygon rendering by encoding geometric details as variations in normals stored in a high resolution texture. However, when it comes to realistic or physically-based rendering, this comes at the expense of several shortcomings. First, as these shading normal variations merely fake geometric details, silhouettes remain coarse, hence precluding renderings of close-ups. Second, as shading normals are not aligned with geometric normals, this can produce artifacts in physically-based renderers such as light leaks or black regions (Fig. 12, (b)), or artifacts due to the lack of energy conservation if not handled with particular care [Vea98, SHHD17]. Our projection step allows to recover finely detailed models for offline rendering from coarse assets along with their normal map. First, we increase the resolution of the input model (for subdivision surfaces, we apply a Catmull-Clark scheme). We then look up the normal value at each vertex from the normal map, and finally apply the projection step described in Sec. 4. Several embossing results are shown in Fig. 12.

6. Discussions

6.1. Implementation and Performance

We implemented our method in C++ using the DEC operators within the libDCC library [CdDS13]. Our implementation is mono-threaded, although fast parallel sparse linear solvers could be used instead [GJ*10]. Still, our unoptimized code already produces results in a reasonable amount of time. It processes meshes of nearly 300k triangles in less than 15 minutes, or in less than a minute if only the projection step is required (see Table. 2). Our implementation is available within our supplemental materials.

6.2. Limitations

First of all, to better capture the geometry, our approach requires to have meshes with enough triangles. For instance, low resolution shapes may lead to irrelevant segmentations (see Fig. 13, first row). For a more extreme case, since the feature vector \( v \) is represented as a \( 0^- \) form we may highlight as feature all edges of a thin triangular strip (see Fig. 13, second row).

We also believe the normal map embossing would benefit from a mesh refinement strategy that adapts to the local frequency content of the normal map. Some details from the normal map indeed appear to be lost, and this is due to a too coarse underlying mesh at some places. This could be investigated in the future.
Table 1: We provide numerical evaluation with state-of-the-art methods, with respect to the Hausdorff distance (RMS, normalized by the bounding box diameter), and the perceptual metric of Lavoué et al. [LGD∗06] (ranks are given as cell colors from dark blue –rank 1– to light-blue –rank 6–). Our method performs better according to perceptual distances. This is due to a slight shrinkage of our denoising results which drastically impacts purely geometric metrics. Parameters were not adjusted to perform well under these metrics. Columns are named following: Z15 [ZDZ∗15], S07 [SRML07], F03 [FDCO03], Z11 [ZFAT11], and H13 [HS13], and AT is our method.

Figure 9: Segmentation results. Edge splitting probabilities are shown in red.

Figure 11: Inpainting results. The recovered feature field v is shown in yellow.

Table 2: Performance of the MS solver and vertex projection steps with respect to the model complexity, using an unoptimized monothreaded implementation.

6.3. Conclusions and Future Work

We have introduced a discretization of a functional for mesh processing along with a series of preliminary applications, which produces state-of-the-art results in mesh denoising, segmentation, inpainting and embossing. We leave as a future work a more extensive validation of each individual application, and rather emphasize the broad scope of our method. In particular, we expect the features detected by our Mumford-Shah discretization to be useful for feature sensitive remeshing [NLG15]. We also believe that stitching meshes together [SBSCO06] and mesh super-resolution [TYW01] could be performed similarly to our inpainting application. More generally, we expect the success of the MS model in geometry processing could parallel its success in image processing.

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Figure 10: Comparison of semantic segmentations (a-f) with our geometric segmentation (g). While semantic segmentation produces parts of meaningful semantics such as the base, the neck, or the handle of this jar, our geometric segmentation detects sharp edges and results in piecewise smooth segments regardless of the underlying semantic.

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Figure 13: First row: multicut segmentation fails to capture the bunny ears geometry. Second row: a coarse mesh does not capture features (in yellow) computed per vertex accurately. As we subdivide the mesh, features become more accurate.