Chiral Spin Texture in the Charge-Density-Wave Phase of the Correlated Metallic Pb/Si(111) Monolayer

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We investigate the $1/3$ monolayer α -Pb/Si(111) surface by scanning tunneling spectroscopy (STS) and fully relativistic first-principles calculations. We study both the high-temperature $\sqrt{3} \times \sqrt{3}$ and low-temperature 3×3 reconstructions and show that, in both phases, the spin-orbit interaction leads to an energy splitting as large as 25% of the valence-band bandwidth. Relativistic effects, electronic correlations, and Pb-substrate interaction cooperate to stabilize a correlated low-temperature paramagnetic phase with well-developed lower and upper Hubbard bands coexisting with 3×3 periodicity. By comparing the Fourier transform of STS conductance maps at the Fermi level with calculated quasiparticle interference from nonmagnetic impurities, we demonstrate the occurrence of two large hexagonal Fermi sheets with in-plane spin polarizations and opposite helicities.

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Two-dimensional materials with spin-polarized surface states are promising candidates for spin-charge current conversion via the Edelstein effect [1]. Furthermore, efficient long-range spin coherent applications [2] require spin transport protected from backscattering. A first step in this direction using strong Rashba spin-orbit coupling (SOC) has been made in heavy-group atoms grown epitaxially on group IV surfaces, like β -Pb/Ge(111) [3,4] or Au/Si(111) [5]. Surprisingly, in less dense $1/3$ monolayer (ML) phases, effects produced by SOC were overlooked while reversible phase transitions with temperature were found [6–9], accompanied by metal-insulator transitions [10–12] and possible magnetic orderings [13,14].

At room temperature, $1/3$ ML coverage of Pb or Sn grown on top of Si(111) or Ge(111) displays an isoelectronic $\sqrt{3} \times \sqrt{3}R30^\circ$ reconstruction. The host atoms occupy the T_4 sites in an hexagonal array [6], the so-called α phase [see Fig. 1(d)]. The three Si dangling bonds in the top Si layer next to the metal atom are saturated, leaving a free unsaturated electron at each T_4 site. These systems are thus expected to present a half filled surface band well separated from Si bands. This expectation is in contrast with experimental evidence of an insulating ground state in Sn on Ge(111) [10] and Si(111) [11,16].

This contradictory behavior was attributed to electronic correlations [12,17]. At a low temperature, the situation is usually complicated by the presence of a reversible structural transition from $\sqrt{3} \times \sqrt{3}$ to 3×3 periodicity [6,7,18,19]. Its origin is still debated and could be either due to the freezing of an out-of-plane phonon mode [9] or produced by long-range

electronic correlations [17,20], both favoring a charge-density wave having the so-called one-up-two-down atom configuration. Surprisingly, despite the presence of heavy atoms and substrate-induced broken inversion symmetry, only one theoretical work (restricted to the $\sqrt{3} \times \sqrt{3}$ reconstruction) treats *ab initio* and on equal footing relativistic and correlation effects as well as the interaction with the substrate [21]. Finally, despite many theoretical calculations for $1/3$ ML Pb/Si(111) [9,17,21], the small size of the 3×3 domains has prevented, up to now, the experimental spectroscopy of their electronic structure.

Here we study the $1/3$ ML α -Pb/Si(111) by scanning tunneling microscopy and spectroscopy (STM and STS) and the fully relativistic density functional theory (DFT). Experimental results down to 300 mK reveal the 3×3 ground state to be a correlated metal not undergoing a Mott transition. It reveals a largely depressed density of states (DOS) at the Fermi level E_F , where well-defined quasiparticles exist, forming two large Fermi surfaces with dominant in-plane spin polarization and opposite helicities.

The preparation of the α -Pb/Si(111) surface is described in Supplemental Material [22]. It is known that large $\sqrt{3} \times \sqrt{3}$ areas with a low defect density cannot be grown [18,19] in contrast to Pb or Sn/Ge(111), or Sn/Si(111). Below 86 K, the $\sqrt{3} \times \sqrt{3}$ regions transit to a 3×3 structure [18,19] [see Fig. 1(d)]. The measurements were performed at 0.3, 2, and 4 K with metallic PtIr or W tips. The $dI/dV(V)$ spectra shown hereafter were obtained by a numerical

FIG. 1. Measurements at $T = 4.2$ K. (a) 900×900 nm² STM topographic map of the sample (scanning $V = -1.0$ V, $I = 20$ pA). (b) 48×48 nm² topography of a 3×3 area showing Pb up and down atoms. (c) STS $dI/dV(V)$ conductance spectra between $[-0.9, +0.9]$ V inside a 3×3 area, spatially averaged over 9 nm² (set point $V = -1.0$ V, $I = 200$ pA). (d) Top: Top view of the high-temperature $\sqrt{3} \times \sqrt{3}R30^\circ$ (red) and low-temperature 3×3 (blue) unit cells of $1/3$ ML Pb/Si(111). Bottom: Side view of the 3×3 . Small (large) circles represent Si (Pb) atoms. (e) Computed STS spectrum for the $3 \times 3a$ phase using Tersoff-Hamann (TH) theory [15] in the DFT + U approximation, including SOC effects for a supercell having three Si double layers. The gray region is the TH calculation for a semi-infinite Si(111) slab. (f) Color plot representing the conductance of 62 $dI/dV(V)$ spectra measured along the 13.8 nm white line shown in (b), across the interface between a 3×3 and a $\sqrt{7} \times \sqrt{3}$ domain. The right axis indicates the distance x from the boundary (being at $x = 0$ nm) at which each spectrum is measured. The voltage axis is identical to the one used in (c), enabling a direct comparison of all spectral features. Each spectrum is the average of 15 spectra measured over a width of 5 nm perpendicular to the white line. The 3×3 band structure establishes sharply over less than 1 nm from the interface. Periodic oscillations appear along x between $[-0.3, +0.4]$ V reflecting the different LDOS at the Pb up and down atoms, seen in (g) presenting the calculated LDOS projected on atomic sites. (h) presents cuts at various energies in map (f) enabling one to better see the oscillations in (f).

derivation of the raw $I(V)$ curves. Negative (positive) bias voltage corresponds to occupied (empty) sample states.

A 900×900 nm² STM topography of the studied samples is shown in Fig. 1(a). The 3×3 areas are surrounded by metallic $\sqrt{7} \times \sqrt{3}$ domains enabling efficient charge evacuation [30]. 3×3 regions of size 25–100 nm, such as the main one seen in Fig. 1(b), were chosen for the spectroscopic studies. This size range is similar to the one presented in Ref. [18]. Intrinsic 3×3 spectroscopic features were measured far enough from boundaries with neighboring $\sqrt{7} \times \sqrt{3}$ domains.

A characteristic dI/dV spectrum measured locally in clean 3×3 areas is presented in Fig. 1(c). It reveals a strongly depressed DOS at E_F not reaching zero, demonstrating the

correlated semimetallic character of the surface. The most prominent feature is a peak at +290 meV labeled U_3 . Kinks were always observed at -170 and -60 meV labeled O_1 and O_3 , respectively. At a larger binding energy ($-420 < V < -250$ meV), the conductance increases, forming a broad peak with internal fine features. The DOS then remains flat with small oscillations until $V \simeq -660$ meV and increases strongly for $V < -660$ meV due to Si bands [31]. In the unoccupied states, several reproducible small kinks are observed around the peak U_3 at +55, +180, and +400 meV denoted, respectively, U_1 , U_2 , and U_4 . For $V > 400$ meV, a continuous drop in conductance occurs until about 550 meV. The conductance remains low but nonzero until 650 meV and then drops, leading to negative dI/dV above $V \simeq 750$ meV and

below 1 V. Above 1 V, a strong increase signals Si bands (see Sec. II in Supplemental Material for additional data and a discussion of the small features [22]).

In principle, the absolute energies of these features must be taken with caution, as the electric field of the STM tip can induce a band bending at the surfaces of gapped solids like semiconductors [31] or Mott systems [32]. However, here 3×3 areas cover less than 10% of the surface, the remaining being the metallic $\sqrt{7} \times \sqrt{3}$ phase becoming superconducting below 1.5 K [30,33]. Furthermore, since 3×3 areas are semimetallic and not insulating, a small band bending effect is expected. The comparison between STS, ARPES, and DFT + U in 1/3ML Sn/Si(111) shows negligible band bending for the occupied states and a small effect for the unoccupied states [11]. The most important contributions that we found to influence the LDOS of 3×3 areas are (i) local or extended defects and (ii) dynamical motion of Pb atoms below the tip (see Sec. II in Ref. [22]).

To rationalize the experimental findings, we performed theoretical calculations using QUANTUM ESPRESSO [34]. We included relativistic effects, noncollinear magnetism in the DFT + U approximation, and the Si(111) substrate (see Supplemental Material [22] and Ref. [9] for more details). We first consider 1/3 ML Pb on Si(111) in the $\sqrt{3} \times \sqrt{3}R30^\circ$ structure within the spin polarized generalized gradient approximation (GGA). While the structural properties are not affected by relativistic effects (see Supplemental Material [22] and Ref. [9]), SOC has a strong impact on the electronic structure inducing a band splitting as large as 1/4 of the bandwidth [see Fig. 2(a)]. The electron-electron interaction treated in the DFT + U approximation or using the HSE06 has minor effects on the $\sqrt{3} \times \sqrt{3}$ surface-band electronic structure [22].

To understand the microscopic mechanisms behind the 3×3 reconstruction, we first neglect SOC and study the lattice deformation within the GGA and local-density approximation (LDA) approximations. Using the GGA, we find a stabilization of the 3×3 reconstruction (energy gain 5 meV per Pb atom, difference in height of Pb atoms $\Delta h \sim 0.24$ Å) in agreement with previous results [9]. Despite the indistinguishable electronic structure, the LDA does not lead to a structural transition, ruling out Fermi surface effects. Although the structural 3×3 distortion is well reproduced in paramagnetic GGA neglecting SOC, the resulting surface DOS is clearly metallic with no depressed DOS at E_F (see Supplemental Material [22]), in qualitative disagreement with the experiment. Including SOC splits the topmost peak in the empty DOS by ≈ 0.09 eV, generating a three-peak structure but keeping a metallic state [see Fig. 2(b)]. Within the GGA, we also considered possible magnetic instabilities. Even if we could stabilize different magnetic solutions, those were always higher in energy than the paramagnetic one [22]. We then consider the relativistic rotational-invariant formulation of the GGA + U approximation [35]. We evaluated the U parameter self-consistently and obtained $U \sim 1.75$ eV.

FIG. 2. Fully relativistic electronic structure for the $\sqrt{3} \times \sqrt{3}R(30^\circ)$ (a) and 3×3 (b) phases with $U = 0$ eV. In (c) 3×3 with $U = 1.75$ eV. Dots in (b) and (c) label the $\mathbf{k}$ points leading to peaks in the DOS (right panels). The projected Si bulk band structure (and DOS) is indicated by gray areas.

We optimized the internal parameters and again found that the paramagnetic 3×3 phase is the ground state (8 meV/Pb energy gain and $\Delta h \sim 0.32$ Å). Since the energy gain is larger at $U \sim 1.75$ eV than at $U = 0$ eV, the local Coulomb repulsion enhances the distortion. Figure 2(c) shows the electronic structure. The Hubbard repulsion lowers the energies of half of the occupied bands, reducing the DOS near E_F . It is possible to probe directly the SOC (Δ_{SOC}) and Hubbard (Δ_U) splittings at selected $\mathbf{k}$ points by looking at the corresponding features induced in the empty and occupied DOS. As presented in the right panel in Fig. 2(c), the main experimental features of the Pb- α phase DOS are reproduced by the calculations: one peak O_1 in the occupied states, a depressed DOS O_3 around E_F , and a three-peak structure U_2 , U_3 , U_4 centered around the prominent peak U_3 in the empty states. We underline that the spin-orbit splitting is about 50% of the Hubbard one, demonstrating the crucial importance of including both effects in the band structure calculation.

To compare in more detail the theory and experiment, the Tersoff-Hamann (TH) simulation [15] of the STS spectra is presented in Fig. 1(e). A good qualitative agreement exists for the energies at which spectral features are observed in

FIG. 3. (a) DFT + U Fermi surface of Pb-3 $\times$ 3/Si(111) including spins polarization (arrows). The out-of-plane spin component is at most 1% of the in-plane one. White arrows, 100% in-plane polarization; blue and red arrows, opposite out-of-plane components. Black arrows $\mathbf{q}_{\text{inter}}$ and $\mathbf{q}_{\text{intra}}$, scattering vectors corresponding to scalar impurities. (b) Symmetrized Fourier transform of a 60 $\times$ 60 nm² $dI/dV(V=0)$ map measured by STS at $T=0.3$ K and $B=0.5$ T, corresponding to quasiparticle interference at $E=E_F$. (c) Calculated quasiparticle interference map at $E=E_F$ assuming pure scalar impurity scattering.

the occupied states. The agreement concerning their amplitude and shape is less good, since O_1 is a kink in the experiment. Most likely, this is because the TH approximation is not valid anymore close to O_1 : Figure 2(c) shows that states close to O_1 have a large in-plane momentum $\|\mathbf{k}_{\parallel}\| \simeq \Gamma M'$. Thus, tip states with $l \neq 0$ angular momentum can significantly contribute to $dI/dV(V)$, invalidating the TH assumptions [36]. Below O_1 in STS, a broad peak with small oscillating features ends up around -0.43 eV in agreement with the calculated half-bandwidth. The small oscillations come from surface Si atoms [see Fig. 1(g)] and continue for $-0.70 < V < -0.43$ eV (see Fig. 8 in Ref. [22]). The LDOS increases further for $V < -0.70$ eV due to bulk Si bands. For the unoccupied states, the main shape of a large peak U_3 with three additional features U_1 , U_2 , and U_4 agrees with the calculations, although finite lifetime effects most likely broaden the real levels (see Sec. VIII and Fig. 10 in Ref. [22]). Energies U_i are found larger in STS due to small band bending, as observed in Refs. [10,11]. The measured upper half-bandwidth is 0.50 eV, while the calculated one is 0.35 eV. One cannot exclude that DFT + U slightly underestimates the bandwidth, because HSE06 calculations show a larger bandwidth mostly for empty states (see [22]).

We now address the conductance oscillations measured between the Pb up and down atoms shown in Fig. 1(f), which strongly support our interpretation of the LDOS structure. For electron energies $O_2 < E < U_4$, DFT + U predicts a larger LDOS on the two Pb down atoms than on the Pb up ones [Fig. 1(g)]. The opposite occurs for $E < O_2$. The local measurements presented in Fig. 1(f) and energy cuts in Fig. 1(h) agree well with these predictions in the range $[-0.3; +0.4]$ eV. Finally, the experimental V -shaped DOS around E_F on the meV scale is typical of correlated metals [37] and can be modeled using a dynamical Coulomb blockade [38].

The Pb- α phase being a correlated 2D metal, one may wonder whether or not it exhibits well-defined quasiparticle excitations at E_F . We answered this question by measuring quasiparticle interference (QPI) $dI/dV(V=0)$ map by STS and performing its Fourier transform (FT) [39]. Here we expect nonmagnetic scalar scattering to be the most dominant scattering process. We verified that magnetic scatterers and spin-orbit scatterers do not contribute significantly to the FT-QPI maps using a similar approach as in Ref. [40].

The calculated Fermi surface of the 3 $\times$ 3 reconstruction is shown in Fig. 3(a). It consists of two hexagons, carrying essentially in-plane spin polarization with opposite helicities: It is thus almost of pure Rashba type. We then calculated the joint DOS due to scattering by scalar impurities, namely, $\chi(\mathbf{q}) = (1/N_{\mathbf{K}}) \sum_{\mathbf{k}n, \mathbf{k}'m} |\mathbf{M}_{\mathbf{k}n, \mathbf{k}'m}|^2 \delta(\epsilon_{\mathbf{k}n} - E_F) \delta(\epsilon_{\mathbf{k}'m} - E_F)$, where $\mathbf{q} = \mathbf{k} - \mathbf{k}'$, $\epsilon_{\mathbf{k}n}$ are the relativistic DFT + U electronic bands, and $M_{\mathbf{k}n, \mathbf{k}'m} = \langle \mathbf{k}n | \sigma_0 \exp\{i(\mathbf{k}' - \mathbf{k}) \cdot \mathbf{r}\} | \mathbf{k}'m \rangle$ with σ_0 the identity matrix in spin space. In the pure Rashba case, one has $M_{\mathbf{k}n, \mathbf{k}'m} = 1 + (-1)^{n-m} \cos[\phi(\mathbf{k}) - \phi(\mathbf{k}')]]$ and $\phi(\mathbf{k}) = (k_x + ik_y)/k$. In Fig. 3(c), we display $\chi(\mathbf{q})$ as a color plot. The hexagonal feature corresponds to interband ($m \neq n$) scattering between segments of different hexagons of the Fermi surface having parallel spins [see $\mathbf{q}_{\text{inter}}$ in Fig. 3(a)]. Near $\mathbf{q} = \mathbf{0}$, a star-shaped feature occurs due to intra Fermi sheet scattering along the straight side of each hexagon [see $\mathbf{q}_{\text{intra}}$ in Fig. 3(a)].

The threefold symmetrized experimental FT-QPI map is shown in Fig. 3(b) (for raw data and details, see Sec. IV in Ref. [22]). A hexagon of maximal radius $\simeq 0.8 \text{ \AA}^{-1}$ is found, in good agreement with Fig. 3(c). Near $\mathbf{q} = \mathbf{0}$, a star-shaped feature is seen. The remaining weaker scattering signal probably comes from extended defects. We checked that it cannot be produced assuming unpolarized spin bands (see Sec. IV [22–29]). The good agreement between calculated and experimental FT-QPI maps demonstrates

(i) well-defined quasiparticles exist at E_F forming two large hexagonal Fermi sheets with opposite in-plane spin-helicities and (ii) mainly scalar scatterers.

In conclusion, using STS experiments and DFT calculations, we showed that the Pb-substrate interaction, non-collinear spin-orbit coupling, and correlation effects are all mandatory to describe the electronic structure of the 1/3 ML Pb/Si(111) surface and its reconstructions. The low-temperature ground state of the 3×3 reconstruction is a strongly correlated metal with well-developed lower and upper Hubbard bands coexisting with a charge-density wave. By comparing calculated quasiparticle interference with the Fourier transform of STS data, we demonstrated the occurrence of two large hexagonal Fermi surfaces with in-plane spin polarization and opposite helicities.

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Recently, we became aware of a work performed on a similar system to ours: 1/3ML Sn/Si(111) reaching a Mott insulator state for heavily n -doped substrate [42]. Following old [12] and new theoretical predictions [43] a very exciting perspective to our work is to study whether unconventional superconductivity could be induced or not in triangular lattice systems such as the 1/3 Pb or Sn grown on Si(111) or Ge(111).

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