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Magnetic dimerization in the frustrated spin ladder Li2Cu2O(SO4)2

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The magnetic properties of Li2Cu2O(SO4)2 are investigated in the framework of density functional theory. In its high-temperature tetragonal structure, this compound appears as a rare material realization of a frustrated spin-1/2 two-leg ladder, where magnetic frustration arises from competing nearest and next-nearest interactions along the legs. Through a large magnetoeelastic coupling, the triclinic distortion occurring around 125 K is shown to induce the formation of a staggered dimer structure, lifting most of the magnetic frustration.

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During the last few decades, a considerable effort has been devoted to the experimental and theoretical investigation of frustrated quantum antiferromagnets [1]. Among the different models studied as potential candidates in which new states of matter could occur, the frustrated $S = 1/2$ two-leg spin ladder has received considerable attention, as it combines low spin, low dimensionality, and magnetic frustration. The general Hamiltonian for this model can be written as

$$ H = J \sum_{\alpha=1,2} \sum_i S_{\alpha,i} \cdot S_{\alpha,i+1} + J_\perp \sum_i S_{1,i} \cdot S_{2,i} + J_x \sum_i (S_{1,i} \cdot S_{2,i+1} + S_{1,i+1} \cdot S_{2,i}) + J_2 \sum_{\alpha=1,2} \sum_i S_{\alpha,i} \cdot S_{\alpha,i+2}, \quad (1) $$

where the index $\alpha$ distinguishes left and right legs, $i$ labels rungs, and the $S_{\alpha,i}$ are the $S = 1/2$ operators at the rung $i$ on the $\alpha$th leg of the ladder. $J$ is the nearest-neighbor (NN) exchange coupling along the legs and $J_\perp$ the interleg coupling along the rungs. Frustration arises either through the next-nearest-neighbor (NNN) coupling along the legs $J_x$ or through the diagonal, interleg coupling $J_2$.

In the absence of next-nearest-neighbor coupling ($J_2 = 0$), the phase diagram for this model was originally shown to consist of two parts: a Haldane and a rung-singlet phase [2–4]. It was later suggested that this picture might be incomplete and that an additional, intermediate dimerized phase could also occur [5,6]. Vekua and Honecker [7] further showed that the addition of sufficiently strong next-nearest-neighbor couplings along the legs ($J_2 \neq 0$) stabilizes additional columnar dimer and staggered dimer phases. A rich phase diagram thus emerges from this quasi-one-dimensional (quasi-1D) lattice model depending critically on the relative signs and strengths of the various exchange couplings.

Unfortunately, only a very limited number of material systems can be considered as true realizations of frustrated $S = 1/2$ two-leg spin ladders and thus, provide experimental evidence to be confronted by these theoretical predictions. Whereas SrCu2O3 [8] or Sr12Cu23O41 [9,10] are prototypical realizations of nonfrustrated ladders, BiCu2PO6 [11] might appear as one of the very rare examples of $S = 1/2$ frustrated spin ladder where the frustration arises only from NNN interactions along the legs [12].

In this Rapid Communication, we show that the newly synthesized compound Li2Cu2O(SO4)2 [13] is an actual realization of $S = 1/2$ frustrated two-leg spin ladder. Moreover, we demonstrate that the tetragonal to triclinic structural transition occurring around 125 K [14] leads to the emergence of a staggered $S = 1/2$ dimer structure, lifting most of the magnetic frustration.

The crystal structure of Li2Cu2O(SO4)2 at room temperature is shown in Figs. 1(a) and 1(b). This compound crystallizes in a tetragonal structure, with space group $P4_2/m$ where Cu2+ ions occupy a slightly distorted square planar environment, as commonly observed for this strong Jahn-Teller ion. The resulting CuO4 squares are grouped by two, sharing an edge to form CuO6 platelets. These platelets are connected one to each other through an oxygen atom, after being rotated by 90° under the effect of the $4_2$ helical axis leading to infinite CuO4 chains running along the c axis of the crystal [see Fig. 1(b)]. Tetrahedral SO4 units further link every second platelet along the chains by sharing two oxygen ions with them. These chains are finally separated from each other by the Li+ ions. From a magnetostructural perspective, dominant magnetic couplings should occur in this structure either through intra-[J_\perp in Fig. 1(c)] or interplatelets ($J = J_x$) Cu-O-Cu superexchange mechanisms or through longer ranged interactions via the nonmagnetic bridging SO4 units ($J_2$), as such polyatomic groups are known to be efficient media for magnetic interactions [15]. As additional interchain interactions are expected to be weak due to the absence of well-defined covalent superexchange paths, this compound should exhibit a strong quasi-1D character. Note that the resulting geometry for such an isolated chain maps exactly on a $S = 1/2$ frustrated two-leg ladder described by (1) in the special case where $J = J_\perp$ as illustrated in Fig. 1(d).

Figure 2 shows the paramagnetic band structure and density of states (DOS) of Li2Cu2O(SO4)2 calculated close to the Fermi level. These density functional theory (DFT)
FIG. 1. (a) Tetragonal crystal structure of Li2Cu2O(SO4)2 at room temperature. Cu are in blue, O in red, S in yellow, and Li in green. (b) Detail of the atomic structure of the chains running along the c axis. (c) Magnetic model deduced from the atomic structure, with the three dominant interactions along the chain: $J_\perp$ in green, $J = J_{\perp} \times J$ in blue, and $J_2$ in red. (d) Topologically equivalent frustrated two-leg spin ladder.

calculations have been carried out using the pseudopotential plane-wave method as implemented in the QUANTUM ESPRESSO suite of codes [16]. Exchange and correlation has been accounted for in the generalized gradient approximation (GGA) parametrized by Perdew, Burke and Ernzerhof (PBE) [17]. Ultrasoft pseudopotentials [18] have been employed with a plane-wave and charge density cutoffs of 60 and 480 Ry, respectively. The four half-filled bands of dominant Cu-3$d_{x^2-y^2}$ character hybridized with the 2$p$ states of the neighboring oxygen ions are well separated from the continuum manifold. Strikingly, these bands are almost dispersionless except along $/\Gamma_1-Z$, i.e., along the chain direction, confirming therefore the marked quasi-1D character of these electronic states, expected from structural considerations. Maximally localized Wannier function [19] (MLWF) interpolation of the band structure was performed using WANNIER90 [20] and is shown in Fig. 2. This interpolation allows the extraction of the effective hopping integrals between magnetic orbitals and reveals that three interactions largely dominate the dispersion: the intraplatelet hopping $t_\perp = -146$ meV, the NN interplatelet hopping $t = 161$ meV, and the NNN hopping along the legs $t_2 = 101$ meV. Considering these three terms only, a tight-binding description of the band structure can easily be constructed leading to the analytical results

$$
\epsilon_{1,2}(\mathbf{k}) = \epsilon_{3d} - t_\perp + 2t_2 \cos(2\pi k_z),
$$

$$
\epsilon_3(\mathbf{k}) = \epsilon_{3d} + t_\perp - 4t \cos(\pi k_x) + 2t_2 \cos(2\pi k_z),
$$

$$
\epsilon_4(\mathbf{k}) = \epsilon_{3d} + t_\perp + 4t \cos(\pi k_x) + 2t_2 \cos(2\pi k_z). \quad (2)
$$

The corresponding bands are represented in Fig. 2 with red lines and clearly illustrate the excellent description of the electronic structure provided by this simplified 1D model. A mapping of the paramagnetic band structure onto a single-band Hubbard model at half-filling, eventually reducing to an antiferromagnetic (AFM) Heisenberg model in the strongly correlated limit, provides a direct link between these hopping parameters and the AFM component of the magnetic couplings, through the expression $J_{\text{AFM}} = 4t_2^2/U_{\text{eff}}$. One could therefore expect the three dominant couplings $J_\perp$, $J$, and $J_2$ to be essentially AFM and of the same order of magnitude. However, this simple analysis overlooks the presence of potentially large ferromagnetic (FM) contributions [21–23] which, depending on the detailed atomic arrangement supporting the superexchange mechanisms, could partially balance or even dominate their AFM counterparts. $J$ is primarily associated with a Cu-O-Cu bond forming an angle of 116° and is likely to be dominated by its AFM component. $J_2$ corresponds to a long-range interaction mediated by a bridging SO4 group, a geometry which usually favors antiferromagnetism too and might give rise to strong couplings [15,24]. The situation is, however, very different for $J_\perp$ where the Cu-O-Cu bond forms an angle of 97°, close to the FM-AFM crossover [25].

In order to investigate this point, the magnetic couplings were estimated within the broken symmetry formalism, i.e., by mapping total energies corresponding to various collinear spin arrangements within a supercell [15,26] onto...
the Heisenberg Hamiltonian (1) with \( J = J_a \) by symmetry. Total energies were calculated in GGA+\( U \) to improve the treatment of strongly correlated Cu-3d electrons. A value of \( U_{\text{eff}} = 10.85 \text{ eV} \) for the effective self-consistent Hubbard term was determined for a \( 1 \times 1 \times 2 \) supercell following the approach described in Refs. [27,28]. The mapping has been carried out using the total energies of 42 spin configurations calculated in a \( 1 \times 1 \times 2 \) supercell containing four formula units and based on the experimental structure determined at 300 K (see Supplemental Material [29]). The results give \( J = J_a \approx J_d = 127 \text{ K} \) confirming the expected AFM nature of these couplings. Note here that if the first equality is dictated by symmetry, the second is only numerical. Finally, \( J_\perp = -100 \text{ K} \); the intraplatelet coupling is ferromagnetic. Additional calculations performed using a \( 2 \times 1 \times 1 \) supercell confirm the absence of sizable interladder couplings.

The picture emerging from the calculated effective exchange interactions is therefore that of a quasi-1D and highly frustrated spin ladder system, where the frustration arises from competing NN and NNN interactions along the legs. This image is confirmed by the numerical calculation of the ground-state expectation values of the spin correlations \( \langle S_i \cdot S_j \rangle \) using Lanczos diagonalization on a finite lattice of 24 spins and imposing periodic boundary conditions. Finite-size effects were found to be small, particularly for the dimerized phase. In agreement with the FM nature of \( J_a \), the intraplatelet value of 0.241 is very close to the value expected for a triplet, i.e., 0.250. Values for the NN and NNN interactions along the legs of \(-0.269 \) and \(-0.046 \) reveal frustrated quasi-1D antiferromagnetic couplings. Setting \( J_2 = 0 \) is enough to entirely lift the magnetic frustration. The intraplatelet, NN, and NNN interactions then reach 0.250, -0.351, and 0.194, respectively, consistent with a Haldane ground state [2].

As recently reported, this compound undergoes a structural transition at 125 K from the tetragonal \( P4_2/m \) to the triclinic \( P1 \) symmetry [14]. This tetragonal to triclinic transition is not accompanied by any volume discontinuity and only involves a very weak modification of the lattice parameters from \( a = 8.325(1) \text{ Å} \) and \( c = 5.909(1) \text{ Å} \) at 300 K to \( a = 8.292(1) \text{ Å} \), \( b = 8.280(1) \text{ Å} \), and \( c = 5.067(1) \text{ Å} \) together with unit-cell angles of \( \alpha = 90.44(1)^\circ \), \( \beta = 90.60(1)^\circ \), and \( \gamma = 90.07(1)^\circ \) at 4 K. In order to evaluate the impact of this distortion on the magnetic couplings, broken-symmetry calculations performed using the experimental structure determined at 300 K have been extended to a set of 61 structures obtained from the Rietveld refinement of neutron powder diffraction experiments carried out from 2 to 300 K. The results are summarized in Fig. 3(a) where data points are represented by dots; the Boltzmann sigmoid fits are represented with lines. (b) Experimental temperature dependence of the interplatelet Cu-O-Cu superexchange angles. (c) Schematic representation of the staggered dimer structure deduced for the triclinic phase (below the transition temperature of \( \sim 125 \text{ K} \)). The inequivalent triclinic interactions along the legs \( J_a^\perp \) and \( J_b^\perp \), diagonal interactions between the legs \( J_c^\perp \) and \( J_d^\perp \), and between the legs along the rungs \( J_a^\parallel \) and \( J_b^\parallel \), are represented in dark blue, blue, and green, respectively. The same color convention has been used for the superexchange angles. The NNN interaction along the legs \( J_2 \) is represented in red.

FIG. 3. (a) Temperature dependence of the magnetic couplings in \( \text{Li}_2\text{Cu}_2\text{O}(\text{SO}_4)_2 \) calculated in GGA+\( U \). Data points are represented with dots; the Boltzmann sigmoid fits are represented with lines. (b) Experimental temperature dependence of the interplatelet Cu-O-Cu superexchange angles. (c) Schematic representation of the staggered dimer structure deduced for the triclinic phase (below the transition temperature of \( \sim 125 \text{ K} \)). The inequivalent triclinic interactions along the legs \( J_a^\perp \) and \( J_b^\perp \), diagonal interactions between the legs \( J_c^\perp \) and \( J_d^\perp \), and between the legs along the rungs \( J_a^\parallel \) and \( J_b^\parallel \), are represented in dark blue, blue, and green, respectively. The same color convention has been used for the superexchange angles. The NNN interaction along the legs \( J_2 \) is represented in red.

the ideal tetragonal structure already occur above the transition temperature [14].

Whereas the triclinic distortion has only a marginal effect on \( J_c^\perp \) and \( J_2 \) [33], it drastically impacts the interplatelet coupling \( J_\perp \). Firstly, the crystal symmetry lowering in the triclinic phase lifts its original degeneracy, leading to four distinct couplings instead of a single one in the tetragonal phase. Secondly, each of these couplings follows a distinct trend as the temperature is lowered: two of them largely reduce their amplitude \( J_c^\perp \) and \( J_d^\perp \), one remains almost constant \( J_a^\perp \), whereas the last one experiences a drastic increase \( J_b^\perp \), raising its amplitude to almost three times its room-temperature value. This very strong variation of the predicted magnetic couplings with the temperature is not surprising if we consider the detailed evolution of the atomic arrangement inside the unit cell. Indeed, although the triclinic distortion has only a modest
impact on the lattice parameters, it involves a sizable variation of the interplatelet Cu-O-Cu superexchange angle, as shown in Fig. 3(b). As the Cu-3d/O-2p hopping is directly related to this angle and as the superexchange interaction directly scales with this integral, the amplitude of the resulting AFM couplings correlates exactly with the Cu-O-Cu angle [see Figs. 3(a) and 3(b)]. The picture resulting from these calculations is therefore that the weak triclinic structural distortion involves a strong magnetic dimerization. The resulting staggered S = 1/2 dimer magnetic structure, lifting most of the frustration, is shown in Fig. 3(c). The temperature dependence of the expectation values of the spin correlations, based on the smooth interpolations of the magnetic couplings presented in Fig. 3(a), is shown in Fig. 4(b). The magnetic dimerization is evidenced at low temperature where the spin correlation associated with J_d reaches a value of −0.666, very close to the value of an isolated singlet, −0.750. The weaker magnetic correlations between the dimers result from the remaining interactions.

In order to verify the validity of these findings, the temperature dependence of the magnetic susceptibility has been calculated using full diagonalization on a finite lattice of 16 spins and imposing periodic boundary conditions (finite-size effects are relatively small; see Supplemental Material [29]). Three models based on the couplings obtained by DFT have been confronted to the experiments [14], corresponding respectively to (i) a set of fixed, i.e., temperature-independent couplings determined from the experimental tetragonal structure determined at 300 K; (ii) a set of fixed couplings determined from the experimental triclinic structure at 2 K; and (iii) a set of variable, i.e., temperature-dependent, couplings based on the interpolations presented in Fig. 3(a). The results are shown in Fig. 4(a) where the fit of the experimental data is solely based on the adjustment of the g factor, set to g ≃ 2.10, a reasonable value for Cu^{2+} [34]. The best agreement is clearly obtained for the model with the temperature-dependent exchange interactions, confirming the large impact of the structural distortion on the magnetism of this compound. Remaining discrepancies, particularly visible at low temperature through a substantial overestimation of the spin gap, are directly attributable to the semiquantitative nature of the magnetic couplings calculated in DFT. These quantities indeed strongly depend on the approximations used in the treatment of exchange and correlation and are often overestimated [35].

In summary, Li_2Cu_2O(SO_4)_2 appears, in its tetragonal structure, as a very rare realization of a S = 1/2 frustrated two-leg spin ladder where frustration arises from competing NN and NNN interactions along the legs. The unusual triclinic distortion occurring in this compound at about 125 K is accompanied by a drastic modification of its magnetic properties. We indeed showed that a strong magnetoelastic coupling is responsible for the formation of a staggered S = 1/2 dimer structure, lifting most of the magnetic frustration. This work should motivate further experimental investigations of Li_2Cu_2O(SO_4)_2, as this compound appears as a prototypical material system to study the physics of spin-lattice coupling in quasi-1D frustrated quantum antiferromagnets.

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[33] Note that, strictly, two distinct $J_2$ couplings, between crystallographically inequivalent Cu(1) and Cu(2) ions [14], respectively, should be considered in the triclinic phase. They are, however, numerically so close that they have been considered as a unique coupling here.
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