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CHARACTERIZATION OF MIXING IN A STIRRED TANK BY PLANAR LASER INDUCED FLUORESCENCE (P.L.I.F.)

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The mixing of two water feedstreams is investigated in a 0.02 m³ continuous stirred tank, from concentration measurements. These measurements are carried out with a laser sheet in a very thin vertical plane through the vessel tangent to the impeller. The proportionality between the grey level obtained by planar laser induced fluorescence and the local concentration has been previously determined. The fields of instantaneous concentration, temporal variance and mixing index are processed from the grey level images.

Keywords: mixing; mixing index; laser sheet; fluorescence; stirred tank.

INTRODUCTION

Solid particles obtained in industry by precipitation (reaction crystallization) are generally produced in mechanically stirred tanks, or in jet mixers. In these processes, two liquid streams come into contact, but the process is more or less controlled.

Precipitation supersaturations originate from a chemical reaction and thus are very high¹. Furthermore, the effects of contacting and mixing conditions of reactants play an essential role on the nucleation and crystal size distribution². Indeed, if the mixing of both reactants is imperfect in the stirred tank, the concentration pattern will not be homogeneous and supersaturation heterogeneities will be created. Consequently, nucleation and crystal growth rates will vary in the mixer from one point to another.

As a mixing model, the fluorescence properties of a solution mixed with pure water in a transparent tank are used, which is crossed by a planar laser sheet. During the first moments of mixing, the mixing of the two tracers is similar to the mixing of two reagents in ionic precipitation. Indeed, there is no significant consumption of the reactants during the first seconds of mixing, owing to the small size of nuclei produced and to the time scales of the crystal growth, which are much larger than those of nucleation³. As a result, mixing in ionic precipitation can be characterized by studying the mixing of two inert tracers, or the mixing of a single tracer in solution with pure solvent, each fluid being injected by two separate feed tubes. The laser sheet visualization method has been used by Mahouast⁴, and developed in a 0.02 m³ mechanically stirred tank by Houcine *et al.*⁵ and adapted at the pilot scale by Marcant *et al.*⁶. The laser induced fluorescence technique (L.I.F.), which is non-intrusive like tomography⁷, can help to optimize the geometry of the mixers, the feed rates or the positions and shape of the injectors. It is based on the stimulation of fluorescence by laser and the measurement of

the emitted light. For low tracer concentrations the fluorescent intensity is proportional to the local concentration and to the power of the incident laser light. Previous workers have used a CCD camera^{4-6,8}, a photomultiplier⁹, and a line scan camera¹⁰. They measured the fluorescent light intensity, respectively in a plane, at a point, and along a line. The planar laser induced fluorescence technique (P.L.I.F.) allows characterizing mixing in any plane crossing the flow defined by the laser sheet. This technique is based on the fluorescence of organic substances induced by a laser sheet and coupled with image analysis. The originality of this study, compared to previous works⁴⁻⁶, lies (a) in the fact that the laser sheet is very thin (down to 100 μm); (b) the camera is much more sensitive and finally; (c) more powerful tools are used for image processing.

The aim of this paper is to describe and validate the PLIF set up designed for fast and precise characterization of contacting and mixing of one inert tracer and pure water.

MEASUREMENT TECHNIQUE AND EXPERIMENTAL SET-UP

Principle

Several organic molecules in solution, like fluoresceine or rhodamine B exhibit a fluorescence phenomenon when they are stimulated by laser light. For low tracer concentrations the intensity of fluorescence is proportional to the local concentration of tracer and to the power of the incident laser light. The fluorescence is emitted with a wavelength (about 590 nm) higher than that of the laser (520 nm). Its intensity is filtered and monitored by a high sensitive camera.

Procedure

The first set measurements are performed to establish the grey level images in the following cases:

- the tank is filled with water. It provides for the grey level field of the background: $NG_{ob}(x, y, t)$;
- the stirred tank is filled with a fluorescent tracer solution. Its concentration is the mixing concentration during the experiment in the completely homogeneous state C_{mp} . It yields the grey level field corresponding to the perfect mixing images;
- finally, two water feedstreams (one containing the fluorescent tracer) supply the stirred tank, yielding the grey level field: $NG(x, y, t)$.

For a diverging laser sheet Houcine *et al.*⁵ derived the relations between:

- the instantaneous local concentration of tracer and the grey level $NG(x, y, t)$ of the image:

$$C(x, y, t) = \frac{NG(x, y, t) - \overline{NG}_{ob}(x, y)}{\overline{NG}_{C_{mp}}(x, y) - \overline{NG}_{ob}(x, y)} C_{mp} \quad (1)$$

- between the grey level $NG(x, y, t)$, the power of laser source P_o and the tracer local concentration $C(x, y, t)$:

$$NG(x, y, t) = KP_o C(x, y, t) \exp[-(\varepsilon_i L + \varepsilon_e L') C_{mp}] \quad (2)$$

Where $\overline{NG}_{ob}(x, y)$ and $\overline{NG}_{C_{mp}}(x, y)$ are the average grey levels of the background and the perfect mixing, respectively, ε_i and ε_e are the extinction coefficients of incident laser light and emitted fluorescence light, L is the depth of penetration of the laser beam into the tracer solution, L' is the optic path of the fluorescent light in the tracer solution, K is a constant grouping physical and geometrical parameters

Equation (1) takes into account the attenuation of the intensity along the optical path, approximately identical for $\overline{NG}_{C_{mp}}(x, y, t)$ and $NG(x, y, t)$. Equation (2) is intended to determine the operating conditions of tracer concentration and power favourable to obtaining a proportionality and a

great sensitivity between the grey level and fluorescent dye concentration. Thus, it was possible to determine the intensity of fluorescence emission as a function of:

- the tracer concentration: the tank is filled with different solution of homogeneous concentration, varying between 0 and $40 \times 10^{-6} \text{ kg m}^{-3}$;
- the laser intensity: the tank is irradiated at P_o increasing, varying between 0 and 2 W.

Experimental

The scheme of the apparatus used in this work is shown in Figure 1. The experiments are carried out in a standard type stirred tank of 0.02 m^3 . The cylindrical vessel of internal diameter $T=0.29 \text{ m}$ is placed inside a square vessel filled with water in order to reduce problems associated with refraction by curved surfaces. Both vessels are made of a transparent material of optical quality Altuglass (PMMA). Four baffles of width $T/10$ and thickness $T/100$ are provided at intervals of 90° against the wall of the inner tank. The six-bladed Rushton turbine in Altuglass is coupled to a stainless steel shaft which has an external diameter of 10 mm. The impeller diameter and bottom clearance are equal to $H/3$, where H represents the height of the liquid in the tank. The other dimensions of the stirred tank are represented in Figure 2. The stirring speed is fixed at $N=110 \text{ rpm}$. The optical device includes a laser diode, with an emission wavelength of 520 nm and with a maximum power $P_o=2 \text{ W}$. When crossing the diaphragm, the laser beam is focused by a mirror and is spread out into a very thin sheet (down to $100 \mu\text{m}$) using a POWELL lens. A CCD camera, of total exposure time 35 ms, fitted with a sharp cut-off high pass filter takes 9 images per second. It gives high resolutions down to ten micrometers, since it provides for images of 1280×1024 pixels encoded on 4096 grey levels. The camera and the laser are jointly assembled

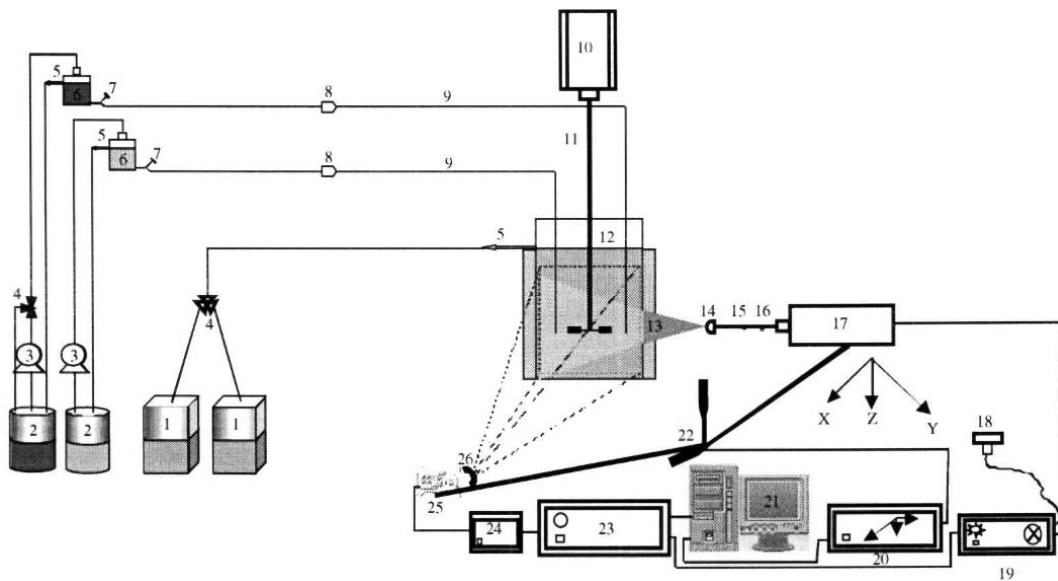


Figure 1. Experimental set-up: (1) storage tanks; (2) feed tanks; (3) pumps; (4) valve; (5) outlet; (6) reservoirs; (7) taps; (8) flow meter; (9) feed tubes; (10) motor; (11) stirrer; (12) mixing tank; (13) laser sheet; (14) Powell lens; (15) mirror; (16) diaphragm; (17) 2 W diode-pumped laser millennia IIs (Nd: YVO₄): excitation wavelength at 520 nm; (18) control module; (19) internal diode power supply; (20) displacement remote control; (21) computer; (22) displacement system; (23) processor; (24) video power supply; (25) DANTEC CCD-camera: HiSense[®] PIV/PLIF; (26) high-pass filter: Sharp-cut glass filter (570 nm) placed on the lens of the camera to remove reflections of the laser light from the fluorescent signal to achieve a high signal-to-noise ratio.

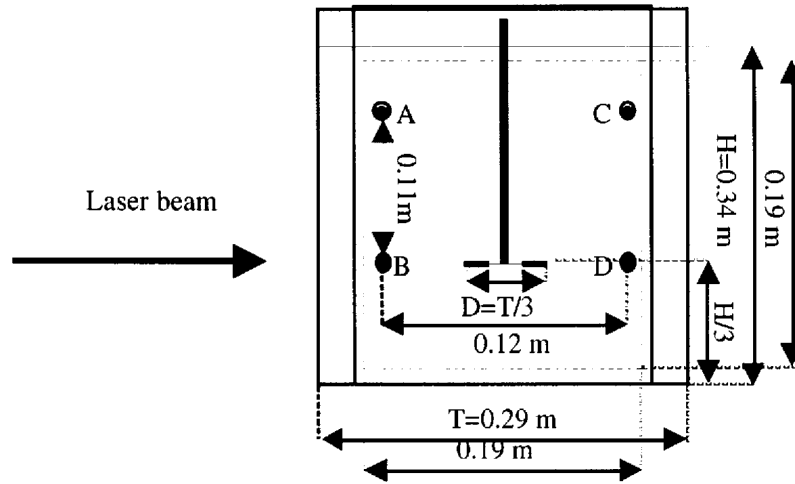


Figure 2. Mixing tank.

on a vertical and horizontal displacement system. This device is controlled by a computer with a total displacement of 0.54 m and a repeatability of 0.1 mm. Two reservoirs continuously supply the tank with equal flow rates ($Q_A = Q_B = 1.45 \times 10^{-3} \text{ m}^3 \text{ min}^{-1}$) by two incoming feed tubes. The tubes have an internal diameter of 6 mm and their axis are separated by a distance of 19.2 mm. The feed point locations are at a height of $2H/3$ and are situated on the tangential vertical plane to the impeller. In this plane, there is no significant orthogonal average velocity¹¹. The tracer concentration ($40 \times 10^{-6} \text{ kg m}^{-3}$) is selected in the range of linearity between concentration and grey level (see Figure 3). The fluorescence images are recorded with FlowManager[®]-Dantec software and then processed in Aphelion[®]-Adcis images analysis software with specific developed macros.

RESULTS

Before starting the experiments in the continuous stirred tank, the range of the linear response between the grey level and the tracer concentration were determined. This was done at four points in Figure 2. It can be seen in Figure 3 that the linearity is observed up to $40 \times 10^{-6} \text{ kg m}^{-3}$ ($8.35 \times 10^{-5} \text{ mol m}^{-3}$) with linear regression coefficient $R^2 > 0.99$ (least square method). For larger concentrations the response of the grey level becomes non-linear because of the exponential term of the equation (2). This result is in agreement with those obtained by Houcine *et al.*⁵, who used a laser power of 1.4 W. The linear response between the laser and fluorescence intensity is given on the Figure 4 (linear regression coefficient $R^2 > 0.99$). In the range of

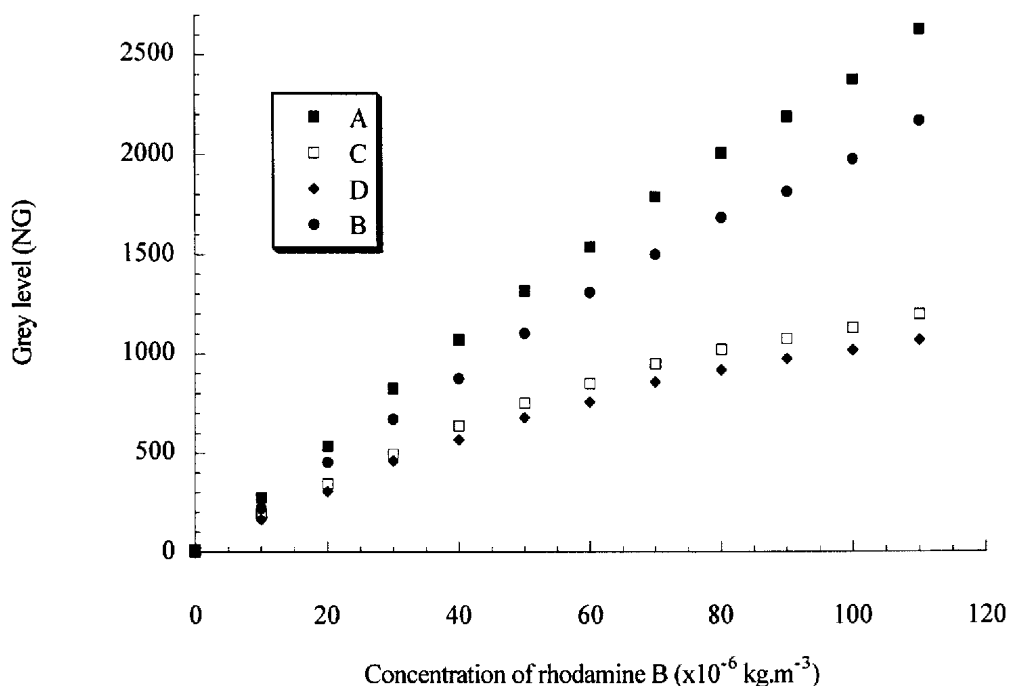


Figure 3. Grey level variation with tracer concentration.

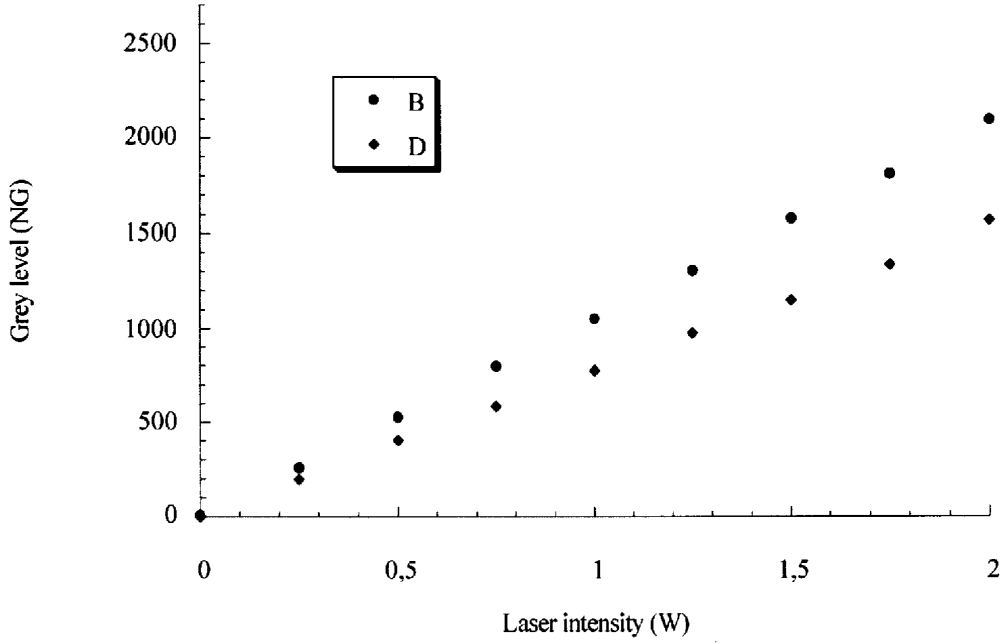


Figure 4. Grey level variation with laser intensity.

the tracer concentration ($0-40 \times 10^{-6} \text{ kg m}^{-3}$) and in the laser power range (0–2 W), there are no saturation problems.

An example of the instantaneous dye concentration field is shown in Figure 5 for the case of a continuously fed tank reactor: fluorescent tracer injected at $40 \times 10^{-6} \text{ kg m}^{-3}$ appears white, whereas pure water appears black. The mean concentration field $\bar{C}(x, y)$ is obtained by averaging a number $n = 100$ of successive instantaneous concentration fields $C(x, y, t)$. The reduced concentration $\bar{C}(x, y)/\bar{C}_{mp}(x, y)$, Figure 6, represents the relative deviation to perfect mixing. Along a line AB (see Figure 6), the ratio varies between 0 (black) and 2 (white): Figure 7, corresponding to the feed stream of water and fluorescent tracer, respectively. Perfect mixing is reached for the value 1.

The temporal variance is expressed by the following equation:

$$\sigma^2(x, y, t) = \frac{1}{n} \sum_{k=1}^n (C(x, y, t) - \bar{C}(x, y))^2 \quad (3)$$

This equation characterizes the mixing dynamics. Figure 8 shows the field of the temporal variance corresponding to the mixing layers of both jets. A white area means high variance, while black means low variance. The persistence of two zones of intensive mixing can be observed around the injection cones at the exit of the feed point locations. The rest of the tank is well homogenized. There is almost no deviation of concentration from the mean.

All the previously shown fields characterize different aspects of the mixing process from the tracer concentration field. It is also interesting to have comparison tools to study various mixing situations. Thus, a mixing index is defined. In the case of two species A and B, Ablitzer¹² proposed:

$$\alpha_{AB}(x, y, t) = 1 - \frac{|C_A(x, y, t) - C_B(x, y, t)|}{C_A(x, y, t) + C_B(x, y, t)} \quad (4)$$

In the case of a tracer water solution (A) and pure water (B), the equation (4) becomes (see appendix), with the tracer concentration $C_A(x, y, t)$:

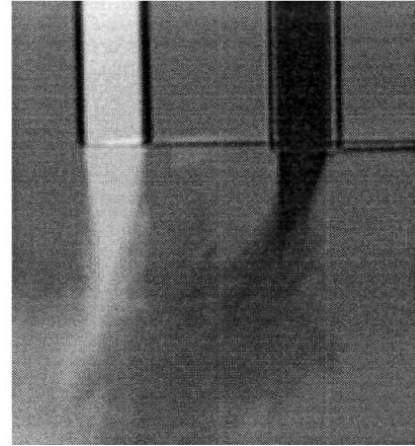


Figure 5. Instantaneous concentration field $C(x, y, t)$.

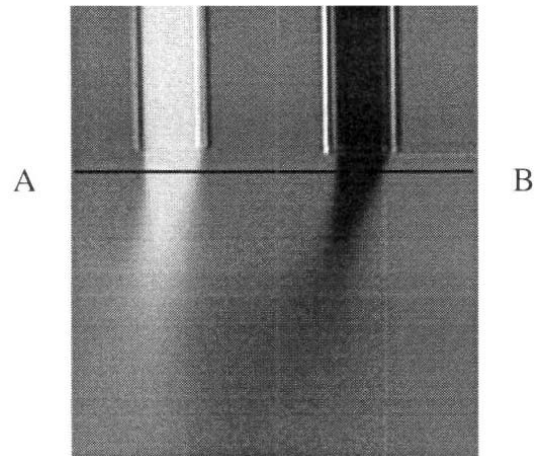


Figure 6. Reduced mean concentration $\bar{C}(x, y)/\bar{C}_{mp}(x, y)$.

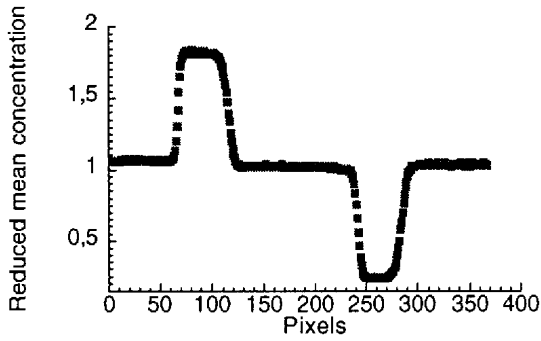


Figure 7. Reduced concentration variation along a line AB (in Figure 6).

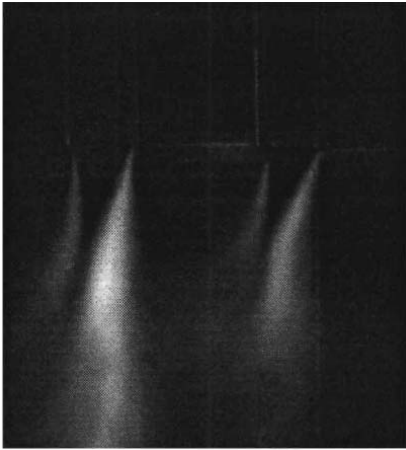


Figure 8. Field of the instantaneous temporal variance $\sigma^2(x, y, t)$.

$$\alpha_{AB}(x, y, t) = 1 - \left| \frac{C_A(x, y, t) - C_{A0}}{C_A(x, y, t) * (2 * \bar{f} - 1) + C_{A0}} \right| \quad (5)$$

where: $\bar{f} = Q_B / (Q_A + Q_B)$

Examples of the instantaneous and average mixing index fields are shown in Figures 9 and 10, respectively. This index varies from 0 (black), in the feed streams jets corresponding to no contact up to a value close to 1 (white) in the rest of the tank. Figure 11 illustrates the evolution of this contacting parameter along the straight line AB (shown in Figure 10).

CONCLUSION

This work describes a powerful non-intrusive technique based on the fluorescence spectroscopy using a very thin static laser plane (down to $100 \mu\text{m}$). The technique is validated for the case of a standard stirred tank reactor of 0.02 m^3 volume, continuously fed with a tracer solution and pure water. Images of instantaneous and average concentration, fields of temporal variance, and mixing index are very precise and illustrate the investigative power and resolution of the PLIF technique. Thus, this device can be used to study contacting and mixing fluid patterns. This will allow, the study of influence of parameters, like feed rate¹³, feed position in the tank, and also allow more sophisticated mixing devices to be characterized.

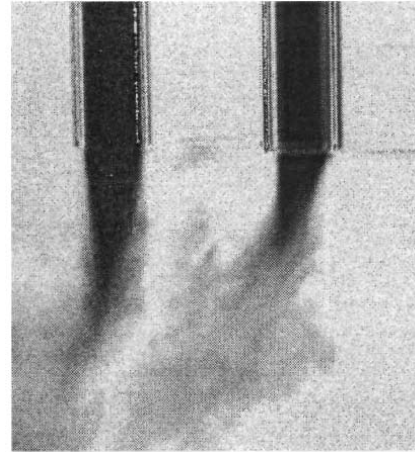


Figure 9. Instantaneous mixing index field.

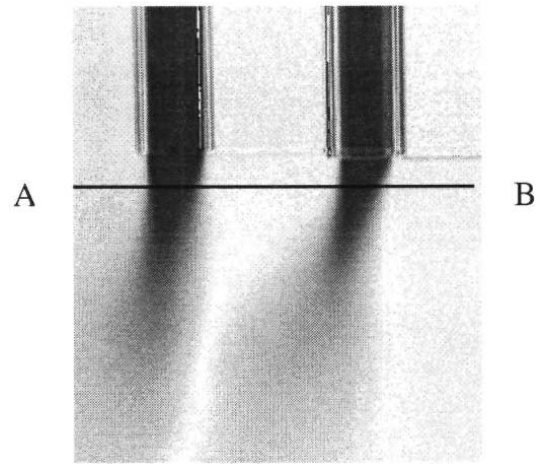


Figure 10. Mean mixing index field.

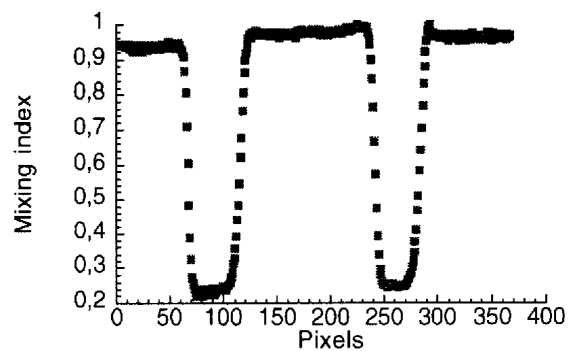


Figure 11. Variation of mean mixing index along a line AB (in Figure 10).

APPENDIX

The aim of this appendix is to derive the mixing index α (given by equation (5)) in this case, from the one defined by Ablitzer¹².

Consider the mixing of two inert tracers, without consumption, shown in Figure A1. If f represents the instantaneous fraction of molecule coming from the inlet B, at point M of coordinates (x, y) , the instantaneous concentrations of species A and B are respectively:

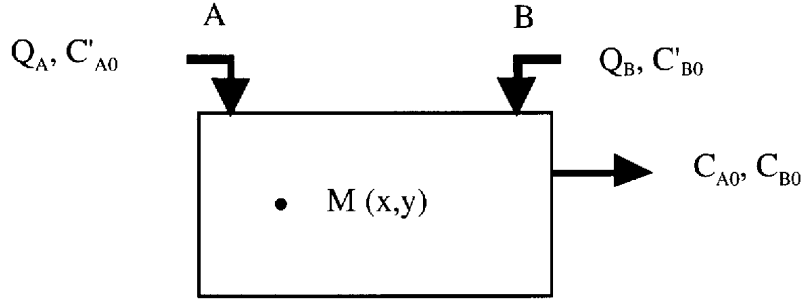


Figure A1. Mixing of two inert tracers without consumption.

$$C_A = C'_{A0}(1 - f) \quad (A1)$$

and:

$$C_B = C'_{B0}f \quad (A2)$$

Thus, at the outlet:

$$C_{A0} = C'_{A0}(1 - \bar{f}) \quad (A3)$$

$$C_{B0} = C'_{B0}\bar{f} \quad (A4)$$

where

$$\bar{f} = \frac{Q_B}{Q_A + Q_B} \quad (A5)$$

In the case of stoichiometry:

$$Q_A C'_{A0} = Q_B C'_{B0} \quad (A6)$$

When equation (A6) is divided by $(Q_A + Q_B)$, it becomes:

$$C'_{A0}(1 - \bar{f}) = \bar{f} C'_{B0} \quad (A7)$$

Addition of equations (A1) and (A2) leads to:

$$\frac{C_A}{C'_{A0}} + \frac{C_B}{C'_{B0}} = 1 \quad (A8)$$

averaging gives:

$$\frac{\bar{C}_A}{C'_{A0}} + \frac{\bar{C}_B}{C'_{B0}} = 1 \quad (A9)$$

For two species A and B, Ablitzer¹² proposed the following mixing index:

$$\alpha_{AB} = 1 - \left| \frac{C_A - C_B}{C_A + C_B} \right| \quad (A10)$$

Taking into account the equation (A8), gives:

$$\alpha_{AB} = 1 - \left| \frac{C_A - C'_{B0} \left(1 - \frac{C_A}{C'_{A0}}\right)}{C_A + C'_{B0} \left(1 - \frac{C_A}{C'_{A0}}\right)} \right| \quad (A11)$$

When C'_{B0} is substituted from equation (A7), equation (A11) leads to:

$$\alpha_{AB} = 1 - \left| \frac{C_A - C'_{A0} \frac{1-\bar{f}}{f} \left(1 - \frac{C_A}{C'_{A0}}\right)}{C_A + C'_{A0} \frac{1-\bar{f}}{f} \left(1 - \frac{C_A}{C'_{A0}}\right)} \right| \quad (A12)$$

After simplification, equation (A12) becomes:

$$\alpha_{AB} = 1 - \left| \frac{C_A - (1 - \bar{f})C'_{A0}}{C_A(2\bar{f} - 1) + C'_{A0}(1 - \bar{f})} \right| \quad (A13)$$

Finally taking into account equation (A3), gives:

$$\alpha_{AB} = 1 - \left| \frac{C_A - C_{A0}}{C_A(2\bar{f} - 1) + C_{A0}} \right| \quad (A14)$$

NOMENCLATURE

C	local concentration of the fluorescent dye, mol m^{-3}
C_X	tracer concentration in the feedstream X mol m^{-3}
C_{X0}	concentration coming in the feedstream X at outing of the tank, mol m^{-3}
C'_{X0}	initial concentration in the feedstream, mol m^{-3}
C_{np}	tracer concentration in the stirred tank in the completely homogeneous state, mol m^{-3}
NG	grey level
P_o	power of the laser source, W
$\varepsilon_i, \varepsilon_e$	extinction coefficient of incident laser light and emitted fluorescence light, $\text{m}^2 \text{mol}^{-1}$
K	constant taking into account physical and geometrical parameters
L	depth of penetration of the laser beam into the tracer solution, m
L'	optic path of the fluorescent light in the tracer solution, m
Q_X	feed rate of feedstream X entering the tank, $\text{m}^3 \text{s}^{-1}$
(x, y)	pixel coordinates, m, m
t	time, s

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