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# Navigation of Multi-Robot Formation in Unstructured Environment Using Dynamical Virtual Structures

Ahmed Benzerrouk\*, Lounis Adouane\*, Laurent Lequievre\* and Philippe Martinet\*

**Abstract**—In this paper, the control problem for a group of mobile robots keeping a geometric formation is considered. The proposed architecture of control allows to each robot to avoid obstacles and to rejoin the desired formation. To not complicate the control of such a system, it is proposed to divide the overall complex task into two basic tasks: attraction to a dynamical target, and obstacle avoidance. Thus, a desired geometric shape is defined and each robot has to track one node of this mobile shape. Each robot has to be autonomously able to avoid disturbing obstacles and to rejoin the formation in a reactive manner. Moreover, it chooses the optimal avoidance side thanks to limit-cycle method in order to reach as rapidly as possible its virtual target. The proposed control architecture is implemented in a distributed manner. In addition, this architecture uses the same control law (Lyapunov stable) for the two elementary tasks, and the switching from one task to another occurs only by changing the set-points. Experimental results validate the proposed control architecture.

## I. INTRODUCTION

Robots are requested to achieve more and more complex tasks. In the beginning of the robotics revolution, they were solicited to enlarge their workspace. Mobility was then a very desirable property. Once reached, another issue arises. Indeed, as the task is complicated, the robot structure becomes rapidly complicated too. An alternative of designing one complex robot is to use a set of simpler cooperating robots with more flexibility.

Many examples of multi-robot applications can be cited: pushing a heavy object [1], remover task [2], keeping a formation for AUV (Autonomous Underwater Vehicles) [3], management and platooning of autonomous vehicles [4], [5], etc. However, the coordination of multi-robot is still among the most challenging tasks. In the literature, the problem has been tackled through different approaches. Among them, we can cite the leader follower approach [6]. In this approach, some mobile robots are considered as leaders which track predefined trajectories, while others act as followers and track leaders thanks to their states. In our work, the expected behavior of the flotilla is that the whole formation should not be affected if one robot, namely the leader, leaves the formation (because of breaking down, avoiding obstacles, etc.).

An other approach is the behavior based methods as in [7], [8]. In this case, each robot has a set of weighted behaviors (basic tasks) to achieve. The resulting behavior of the group emerges by accomplishing basic behaviors. It means that

there is not an explicit model of the overall cooperative behavior.

A moving virtual structure is an other strategy. Keeping a desired shape by the robots can then be achieved by considering the formation as a single virtual rigid body. The control law of each robot is derived by defining the dynamics of the virtual structure. The motion of the latter is then translated into the desired motion of each vehicle [9], [10]. In [11], virtual structures have been achieved by having all members of the formation tracking assigned nodes which moves into desired configuration. Many works use the potential fields with this approach: Ogren and al [12] consider the nodes of the desired virtual structure to reach as virtual leaders. Each robot is controlled using a potential field function which takes into account its neighbors and the corresponding virtual leader. Mastellone and al [13] design a controller based on potential fields that guarantees tracking and obstacle/vehicle collision avoidance for nonholonomic systems. They apply it to a formation of mobile robots. However, the weakness of virtual structure is that potential applications are limited especially when the formation shape needs to be frequently reconfigured. For example, changing the configuration by joining new robots to the formation leads to change the parameters of the embedded control into each robot, including the robots forming the old formation.

Combining different approaches to get their advantages has been little explored in the literature. In this paper, a group of mobile robots navigating in formation is considered. It is proposed to combine behavior based approach and virtual structure method to build a distributed control architecture. To overcome drawbacks of using potential fields in the virtual structure approach, the achieved task (reaching and maintaining a desired formation while avoiding obstacles) is divided into two basic tasks (behaviors): attraction to a dynamical target, and obstacle avoidance. A control law using geometric rules is thus designed. In fact, each node of the defined rigid body corresponds to a dynamic virtual target that one mobile robot of the group has to reach. A dynamic target assignment for each robot is also proposed giving a cooperative aspect to the robots.

It is noted that robots are evolving in unknown environment with a risk of collision between them and with outside obstacles. Each robot needs then to be able to avoid obstacles. Potential fields [14] are widely used in the literature. In fact, they offer a real time method adapted to this task. However, since potential applications have limitation when combined with the virtual structure approach, the used method is the limit-cycle navigation proposed in [15] and improved in [16].

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This method also allows to choose the direction of avoidance according to the target position.

The remainder of the paper is organized as follow: in next section (II), the proposed architecture and its controllers (attraction to a dynamical target and obstacle avoidance) are detailed. Section III gives the common control law of the controllers. Section IV discusses experimental results implemented on a set of Khepera III mobile robots. Finally, section V is devoted to conclusion and some prospects.

## II. NAVIGATION IN FORMATION

Consider  $N$  robots with the objective of reaching and maintaining them in a given formation even when obstacles disturb their navigation.

### A. The adopted cooperative control strategy

The adopted strategy consists to control each robot  $i$  to track a dynamical target (node) of a virtual geometrical structure.

Reaching or tracking a moving target has been widely explored in the literature [17], [18]. In [19], a specific set-point is designed for a mobile robot to reach a dynamical target. However, this work assumes that both the robot and the target are evolving with constant linear velocities (it is assumed that the robot goes faster than its target). Therefore, it is only proved that the robot meets the target but is not able to track it. The proposed virtual dynamical structure that must be followed by the group of robots is defined as follow:

- Define one point which gives the dynamics (velocities) of the applied structure. This point is called the main dynamical target (cf. Figure 1),
- Define the virtual structure to follow by defining as much nodes (virtual target) as necessary to obtain the desired geometry. Each node  $i$  is called a secondary target and is defined according to a specific distance  $D_i$  and angle  $\Phi_i$  with respect to the main target. Secondary targets defined by this way have then the same orientation  $\theta_T$  and velocity  $v_T$ .

An exemple to get a triangular formation is given in figure 1.

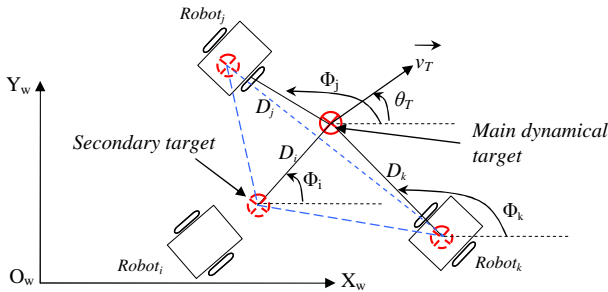


Fig. 1. Keeping a triangular formation by defining a virtual geometrical structure.

### B. Cooperative and Distributed virtual target assignment

As discussed above, each mobile robot should follow one of the secondary targets forming the wished geometric shape, but the asked question is what target $_j$  for what robot $_i$ ? The

only information available at the level of each robot $_i$  are its configuration  $(x_i, y_i, \theta_i)$ , the one of the main target  $(x_T, y_T, \theta_T)$  as well as the  $D_j$  and  $\Phi_j$  corresponding to the relative positions and orientations of the secondary targets $_j$  with regards to the main one (cf. Figure 1). It is also noted that to simplify the negotiation protocol between the robots [20], a specific priorities (like a hierarchy)  $p = 1..N$  is attributed for each robot. From these information, robots will cooperate to establish with a fully distributed manner the virtual target to follow. The proposed algorithm embedded in each robot is given below:

**Input:** Distances  $d_{sj}$  separating the robot with regards to the secondary targets $_j$  (cf. Figure 3)

**Output:** Choice of the virtual target to follow

**While (experimentation)**

- classify by growing order the distances  $d_{sj}$  separating the robot and the target $_j$ ,
- go toward the closest target but with the condition that it is not already chosen by one robot of superior hierarchy  $p$  (this, stipulates that each robot communicates with other robots its sorted list and its  $p$  rank in the hierarchy).

**EndWhile**

**Algorithm 1:** Distributed virtual target assignment

## III. THE PROPOSED CONTROL ARCHITECTURE:

As cited above, the proposed control architecture includes two controllers: Attraction to a Dynamical Target and Obstacle Avoidance controllers (cf. Figure 2). Before giving all details about this architecture, let's present the proposed *Attraction to a Dynamical Target* block and the *Obstacle Avoidance* block..

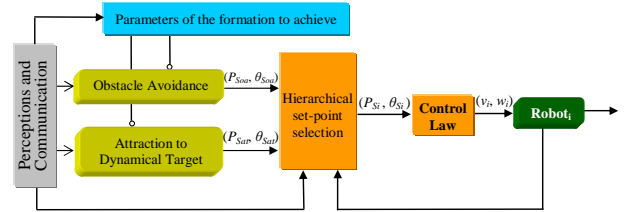


Fig. 2. The proposed architecture of control.

### A. Attraction to a Dynamical Target Controller

Consider a robot  $i$  with  $(x_i, y_i, \theta_i)$  pose. This robot has to track its secondary dynamical target  $T_i(x_{T_i}, y_{T_i}, \theta_{T_i})$  (cf. Section II-B) that the variation of its position can be described by

$$\begin{cases} \dot{x}_{T_i} = v_T \cdot \cos(\theta_T) \\ \dot{y}_{T_i} = v_T \cdot \sin(\theta_T) \end{cases} \quad (1)$$

Let's also introduce the used robot model. Experimental results are made on Khepera III, which are unicycle mobile robots. Their kinematic model can be described by the well-known equations (cf. Equation 2).

$$\begin{cases} \dot{x}_i = v_i \cdot \cos(\theta_i) \\ \dot{y}_i = v_i \cdot \sin(\theta_i) \\ \dot{\theta}_i = \omega_i \end{cases} \quad (2)$$

where  $\theta_i$ ,  $v_i$  and  $\omega_i$  are respectively the robot orientation, linear and angular velocities.

Figure (3) allows to define position errors as

$$\begin{cases} e_{x_i} = (x_{T_i} - x_i) = d_{S_i} \cos(\gamma_i) \\ e_{y_i} = (y_{T_i} - y_i) = d_{S_i} \sin(\gamma_i) \end{cases} \quad (3)$$

The current distance between the robot  $i$  and its target  $T_i$ , noted  $d_{S_i}$  can then be expressed as

$$d_{S_i} = \sqrt{e_{x_i}^2 + e_{y_i}^2} \quad (4)$$

Its derivative is

$$\dot{d}_{S_i} = \frac{e_{x_i} \dot{e}_{x_i} + e_{y_i} \dot{e}_{y_i}}{d_{S_i}} \quad (5)$$

Using equations (1 to 5) allows us to get

$$\dot{d}_{S_i} = v_T \cdot \cos(\gamma_i - \theta_T) - v_i \cdot \cos(\gamma_i - \theta_i) \quad (6)$$

Similarly, the current angle of the robot according to its dynamical target is noted  $\gamma_i$  and is calculated as

$$\gamma_i = \arctan\left(\frac{e_{y_i}}{e_{x_i}}\right) \quad (7)$$

Its derivative is

$$\dot{\gamma}_i = \frac{\dot{(e_{y_i}/e_{x_i})}}{1 + (e_{y_i}/e_{x_i})^2} \quad (8)$$

By using equations (1) and (2),  $\dot{e}_x$  and  $\dot{e}_y$  are given by

$$\begin{cases} \dot{e}_{x_i} = (\dot{x}_{T_i} - \dot{x}_i) = v_T \cdot \cos(\theta_T) - v_i \cdot \cos(\theta_i) \\ \dot{e}_{y_i} = (\dot{y}_{T_i} - \dot{y}_i) = v_T \cdot \sin(\theta_T) - v_i \cdot \sin(\theta_i) \end{cases} \quad (9)$$

and (8) becomes then

$$\dot{\gamma}_i = \frac{v_T \cdot \sin(\theta_T - \gamma_i)}{d_{S_i}} - \frac{v_i \cdot \sin(\theta_i - \gamma_i)}{d_{S_i}} \quad (10)$$

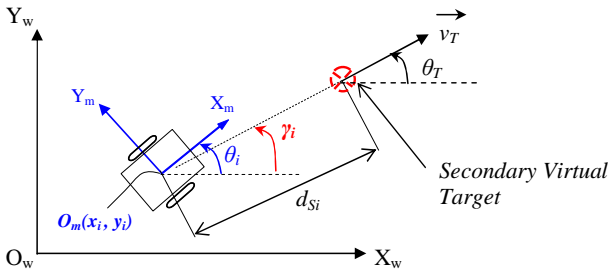


Fig. 3. Attraction to a dynamical target.

To obtain the set-point angle  $\theta_{S_{at}}$  applied to the robot in order to reach its dynamical target, our idea is to keep  $\gamma_i$  constant. In other words, we would like to have  $\dot{\gamma}_i = 0$ . Under this constraint, we show that the defined set-point angle leads the robot on its target. Equation (10) allows thus to write:

$$\frac{v_T \cdot \sin(\theta_T - \gamma_i)}{d_{S_i}} - \frac{v_i \cdot \sin(\theta_i - \gamma_i)}{d_{S_i}} = 0 \quad (11)$$

The set-point angle that the robot must follow to satisfy the constraint expressed by equation (11) and to reach its dynamical target is then given by

$$\theta_{S_{at}} = \arcsin\left(\frac{v_T}{v_i} \sin(\theta_T - \gamma_i)\right) + \gamma_i \quad (12)$$

In what follows, it is put  $b = \frac{v_T}{v_i}$ . As already cited, a close result was given in [19]. However, the two results are differently developed. In fact, in [19], the line of sight of an observer was used to build this set-point and the position of this observer affects the set-point. The proposed work is not based on any observer and our results depend only on the dynamics of the robot and its target. Also, and unlike [19], the robot velocity is not constant. The proposed control law (cf. Section IV) regulates it by accelerating or decelerating according to the robot distance  $d_{S_i}$  with respect to its target. The target is then tracked once reached whereas in [19], the goal was just to prove that the robot and its target meet each other.

To prove that the robot reaches its target, we have to prove that  $d_{S_i}$  is continually decreasing. For that, it is sufficient to prove that  $\dot{d}_{S_i} < 0$ . Before giving the proof, it is reported that the linear velocity of the robot will be elaborated satisfying the constraint  $v_i \geq v_T$ . It is natural that the robot goes faster than to the target to reach it, especially when the latter is escaping. Therefore, we have always  $b = \frac{v_T}{v_i} \leq 1$ . Moreover, the trajectory of the target is assumed smooth. For the proof, the following two properties are reminded

$$\begin{aligned} \cos(-x) &= \cos(x), \forall x \in R \\ \arcsin(x) &\in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right], \forall x \in [-1, 1] \end{aligned}$$

Consider the equation (6), two cases are then possible

1)  $(\theta_T - \gamma_i) \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$  (escaping target); we have:

$$\cos(\theta_T - \gamma_i) = \sqrt{1 - (\sin(\theta_T - \gamma_i))^2} \geq 0$$

which leads to

$$\dot{d}_{S_i} = v_T \sqrt{1 - (\sin(\theta_T - \gamma_i))^2} - v_i \sqrt{1 - (b \sin((\theta_T - \gamma_i))^2} \quad (13)$$

However, while the robot did not reach the target, we have  $b < 1$  since  $v_T < v_i$  (cf. Section IV). It means that

$$v_T \sqrt{1 - (\sin(\theta_T - \gamma_i))^2} < v_i \sqrt{1 - (b \sin((\theta_T - \gamma_i))^2}$$

thus

$$\dot{d}_{S_i} < 0$$

2)  $(\theta_T - \gamma_i) \in \left[\frac{\pi}{2}, \frac{3\pi}{2}\right]$  (approaching target):

$$\cos(\theta_T - \gamma_i) = -\sqrt{1 - (\sin(\theta_T - \gamma_i))^2} \leq 0$$

and

$$\dot{d}_{S_i} = -v_T \sqrt{1 - (\sin(\theta_T - \gamma_i))^2} - v_i \sqrt{1 - (b \sin((\theta_T - \gamma_i))^2} \quad (14)$$

It can then immediately be deduced that  $\dot{d}_{S_i} < 0$ .

Note that in the first case (escaping target), it can be observed that  $\dot{d}$  is as much more negative as the linear robot velocity is increasing. It will be seen later that the proposed control law increases the robot velocity as the distance robot-target increases. In addition, the control law is elaborated

such that the robot velocity  $v_i \rightarrow v_T$  when  $d_{S_i} \rightarrow 0$  (cf. Section IV). Hence, in equation (12) we have  $b = 1$ . It is interesting to note that the proposed set-point allows thereby to converge to  $\theta_T$  as  $d_{S_i} \rightarrow 0$ . In fact, Two cases are again possible

- 1)  $(\theta_T - \gamma_i) \in [-\frac{\pi}{2}, \frac{\pi}{2}]$  (escaping target):

$$\begin{aligned}\theta_{S_{at}} &= \arcsin(\sin(\theta_T - \gamma_i)) + \gamma_i \\ \theta_{S_{at}} &= \theta_T - \gamma_i + \gamma_i \\ \theta_{S_{at}} &= \theta_T\end{aligned}\quad (15)$$

The set-point angle tends directly to the target direction.

- 2)  $(\theta_T - \gamma_i) \in [\frac{\pi}{2}, \frac{3\pi}{2}]$  (approaching target):

$$\begin{aligned}\theta_{S_{at}} &= \pi - (\theta_T - \gamma_i) + \gamma_i \\ \theta_{S_{at}} &= \pi + 2\gamma_i - \theta_T\end{aligned}\quad (16)$$

However, the robot still reaches the target but with this set angle, it goes past it once reached. The robot is then behind the target and tries to join it again. Therefore,  $\gamma_i$  is recalculated. Since the target trajectory is assumed smooth, the new calculated  $\gamma_i$  verifies then the case 1 (the robot is now behind the target, and this one becomes then an escaping target).

### B. Obstacle Avoidance Controller

To perform the obstacle avoidance controller, the robot needs to follow accurately limit-cycle vector fields [15], [16]. Each obstacle is surrounded with an influence circle of radius  $R_I = R_O + R_r + \Delta$ , with  $R_O$  the real obstacle radius,  $R_r$  the robot radius and  $\Delta$  a safety margin. Vector fields are given by two differential equations:

- For the clockwise trajectory motion (cf. Figure 4(a)):

$$\begin{aligned}\dot{x}_s &= y_s + x_s(R_c^2 - x_s^2 - y_s^2) \\ \dot{y}_s &= -x_s + y_s(R_c^2 - x_s^2 - y_s^2)\end{aligned}\quad (17)$$

- For the counter-clockwise trajectory motion (cf. Figure 4(b)):

$$\begin{aligned}\dot{x}_s &= -y_s + x_s(R_c^2 - x_s^2 - y_s^2) \\ \dot{y}_s &= x_s + y_s(R_c^2 - x_s^2 - y_s^2)\end{aligned}\quad (18)$$

where  $(x_s, y_s)$  corresponds to the position of the robot according to the center of the convergence circle (characterized by an  $R_c$  radius). Figure 4 shows that the circle of “ $R_c = 1$ ” is a periodic orbit. This periodic orbit is called a limit-cycle. Figure 4(a) and 4(b) show the shape of equations (17) and (18) respectively. They show the direction of trajectories (clockwise or counter-clockwise) according to  $(x_s, y_s)$  axis. The trajectories from all points  $(x_s, y_s)$  including inside the circle, move towards the circle.

The set-point angle  $\theta_{S_{oa}}$  calculated thanks to the Obstacle Avoidance controller is given by the differential equation of the limit-cycle (17) or (18) as:

$$\theta_{S_{oa}} = \arctan\left(\frac{\dot{y}_s}{\dot{x}_s}\right)\quad (19)$$

However, note that obstacle avoidance controller itself is divided into two phases: attractive phase and repulsive phase. These two cases guarantee that the robot do not navigate very

closely to  $R_I$ . This causes oscillations of the robot due to useless switch between obstacle avoidance and attraction to target controllers (see [16] for more details).

Algorithm 2 and Figure 5 explain briefly the two phases principle.  $(x_O, y_O)$  (cf. Algorithm 2) are the relative position of the robot in the obstacle frame  $(O, X_O, Y_O)$  (cf. Figure 5). This frame is built such that direction of the X-axis goes through the virtual target to reach and the obstacle center. Y-axis can then be easily deduced.

**Input:** All the features of the closest obstacle  
**Output:** Radius of the limit-cycle trajectory to follow  
**if**  $y_O \geq 0$  **then**  
  | Avoid the obstacle in the clockwise direction  
**else**  
  | Avoid the obstacle in the counter-clockwise direction  
**end**  
**if**  $x_O \leq 0$  **then**  
  |  $R_c = R_I - \xi$  (**Attractive phase**)  
  | {with  $\xi$  a small constant value as  $\xi \ll \Delta$ }  
**else**  
  | {Escape criterion: go out of the obstacle circle of influence with a smooth way}  
  |  $R_c = R_c + \xi$  (**Repulsive phase**)  
**end**

**Algorithm 2:** Obtaining the radius  $R_c$  of the limit-cycle.

### C. The remaining control architecture blocks

The proposed control architecture is summarized in Figure 2. First, the parameters of the rigid virtual structure  $(D_i, \Phi_i)$  (cf. Section II) are given by the *Parameters of the formation to achieve* block. Besides, according to the task accomplished by the robot, the corresponding controller is chosen thanks to the *Hierarchical Set-Point Selection* block. The latter takes a decision thanks to environment information collected by the *Perceptions and Communication* block and the *robot* (block) which gives its current position. The corresponding set-points  $(P_{S_i}, \theta_{S_i})$  are then sent to the *Control Law* block according to the active controller such that

- $(P_{S_i} = (x_{S_i}, y_{S_i}))$  is the current position of the dynamical target  $(P_{S_{at}} = (x_{T_i}, y_{T_i}))$  and  $(\theta_{S_i} = \theta_{S_{at}})$  for *Attraction to Dynamical Target* controller,
- $P_{S_{oa}}$  is always set to  $(0,0)$  and  $(\theta_{S_i} = \theta_{S_{oa}})$  for *Obstacle Avoidance* controller.

It is important to emphasize that the control block uses the same control law for both controllers. Therefore, only the set-points change coming from a controller or an other. In next section, the proposed control law is given in details.

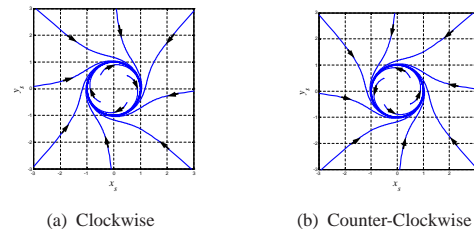


Fig. 4. Shape possibilities for the used limit-cycles



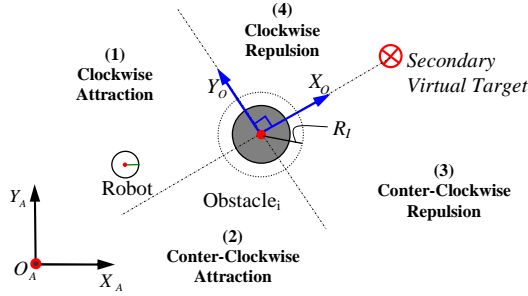


Fig. 5. The 4 specific areas surrounding the obstacle to avoid

#### IV. THE PROPOSED CONTROL LAW

The proposed control law allows to each robot  $i$  to converge to its set-point (cf. Figure 2). It is expressed as

$$v_i = v_{max} - (v_{max} - v_T)e^{-(d_{S_i}^2/\sigma^2)} \quad (20a)$$

$$\omega_i = \omega_{S_i} + k_1 \tilde{\theta}_i \quad (20b)$$

where

- $v_{max}$  is the maximum linear speed of the robot,
- $\sigma, k_1$  are positive constants,
- $v_i$  and  $\omega_i$  are as already defined (cf. Section III) linear and angular velocities of the robot.  $w_{S_i} = \dot{\theta}_{S_i}$ .

$$\tilde{\theta}_i = \theta_{S_i} - \theta_i \quad (21)$$

where  $\theta_{S_i}$  is the set-point angle according to the active controller (cf. Section III) and was already computed (cf. Equation (12), (19)).

By deriving

$$\dot{\tilde{\theta}}_i = w_{S_i} - \omega_i \quad (22)$$

Consider the Lyapunov function

$$V = \frac{1}{2} \tilde{\theta}_i^2 \quad (23)$$

The control law is asymptotically stable if  $\dot{V} < 0$ .

$$\dot{V} = k_1 \tilde{\theta}_i \dot{\tilde{\theta}}_i$$

By replacing equation (22) in the control law (20b), we get

$$\dot{\tilde{\theta}}_i = -k_1 \tilde{\theta}_i$$

and  $\dot{V}$  becomes  $\dot{V} = -k_1 \tilde{\theta}_i^2 < 0$

for every  $\tilde{\theta}_i \neq 0$  since  $k_1 > 0$ .

#### V. EXPERIMENTAL RESULTS

Experimentations are implemented on Khepera III robots. Navigation is achieved on a platform equipped with a camera giving positions and orientation of the robots and the obstacles to avoid. In fact, every element (robot, obstacle) has a different bar code to identify it at each moment: (position, orientation, radius, etc.) [21].

#### A. Extension of the navigating formation shape

To test the relevance of the proposed control architecture to reach and to maintain a formation shape, a triangular virtual structure is defined. It moves with a constant linear speed  $v_T = 4.2 \text{ cm/s}$ . Three Khepera III are randomly put on the platform. The proposed architecture of control is embedded on each robot. Results are given in figure (6). It can be seen that each one joins the closest virtual target of the virtual structure (cf. Figure 6(a)). The real trajectory of the three robots is given in figure 6(b). While navigation, it is proposed to extend the virtual structure to a diamond shape. Therefore, an other robot is added to the formation. It can be seen that the robot accelerates, and reaches the free virtual target without disturbing the other navigating robots. The distance errors between the robot and their targets are given in figure 6(c). It can be seen that the all the robots reaches their targets (the distance error tends to 0). The evolution of the Lyapunov function of each robot is given in figure 6(d). It can be seen that it is decreasing despite some variations (noise) due to the error localization given by the camera. The definition of the Lyapunov function (cf. Equation 23) allows to deduce that the angular error  $\tilde{\theta}$  tends also to 0.

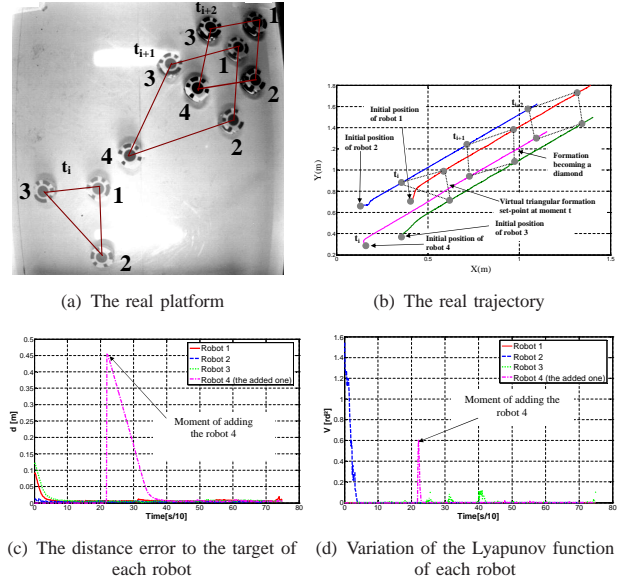


Fig. 6. Extension of the triangular formation to a diamond formation shape.

#### B. Joining the formation while avoiding obstacles

A triangular virtual shape is desired in this experimentation. Three Khepera III robots have then to reach the corresponding closest target. However, two hindering obstacles prevents two robots from directly catching their targets. It is observed (cf. Figure 7) that the two robots avoid the obstacles, and reach the closest target (cf. Figure 7(a)). The real trajectories of the robots and obstacle positions are given in figure 7(b). Distance errors of the robot to their chosen targets are given in figure 7(c). It can be seen that each robot converges to its virtual target. In the obstacle avoidance phase (cf. Figure 7(c)) for robot 2 and 3, it is noted that the distance of the robot to its target is not taken into

account ( $P_{S_i} = (0,0)$  (cf. Section III)). The last computed distance is kept in robot memory but is not used. When switching into Attraction to Dynamical Target controller again, the distance error decreases until the robot reaches the target. Switch moments can be easily detected thanks to the Lyapunov function variation (cf. Figure 7(d)). In fact, an abrupt change of the set-point angle leads to a jump in the Lyapunov function. Outside the switch moment, each Lyapunov function is decreasing. Note that in the obstacle avoidance phase, two jumps are observed for each robots. The second one corresponds to switching from attraction phase to repulsive phase (cf. Section III-B) [22].

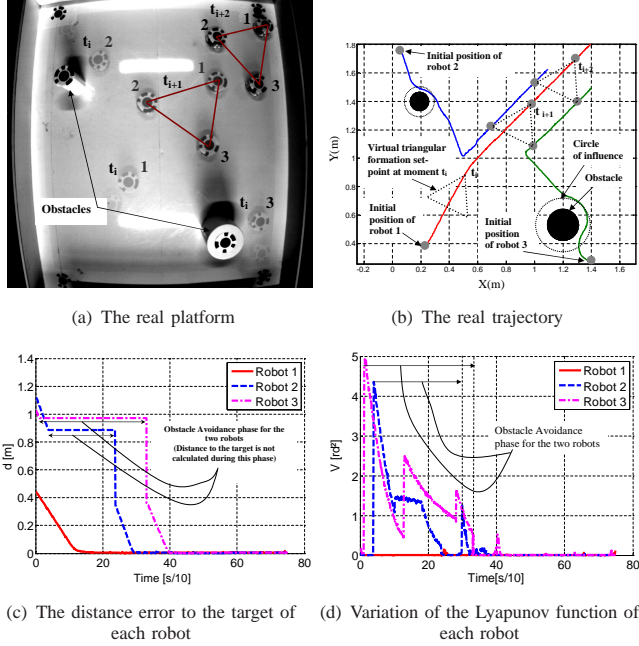


Fig. 7. Avoiding obstacles before joining the formation.

## VI. CONCLUSIONS AND FUTURE WORKS

The problem of multi-robot formation was studied while designing an appropriate control architecture. It allows to reach and to maintain a desired virtual shape for a group of robots during the navigation. This navigation is accomplished in unstructured environments. Consequently, each robot has to avoid disturbing obstacles using limit-cycle method before rejoining the formation. Limit-cycle method allows to the robot to choose the optimal avoidance side to rapidly reach its target. If two tasks have to be achieved (Attraction to a Dynamical Target and Obstacle Avoidance), only one sufficient control law is used. Switching between tasks occurs by choosing the appropriate set-points. The proposed architecture offers flexibility to add other robots to the formation even during the navigation. Unlike potential field methods, this is accomplished without affecting or modifying the control laws of the other existing robots.

Stability of the overall control especially in the switch moments will be deeply exposed in a future paper. Collision between robots was not treated in this paper (dynamical obstacle avoidance), it will be subject of future works.

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