Aharonov-Bohm oscillation in a ferromagnetic ring

Gen Tatara, Hiroshi Kohno, Edgar Bonet, Bernard Barbara

► To cite this version:

Gen Tatara, Hiroshi Kohno, Edgar Bonet, Bernard Barbara. Aharonov-Bohm oscillation in a ferromagnetic ring. *Physical Review B: Condensed Matter and Materials Physics* (1998-2015), 2004, 69 (5), pp.054420. 10.1103/PhysRevB.69.054420 . hal-01660458

HAL Id: hal-01660458

<https://hal.science/hal-01660458>

Submitted on 10 Dec 2017

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

Aharonov-Bohm oscillation in a ferromagnetic ring

Gen Tatara

Graduate School of Science, Osaka University, Toyonaka Osaka 560-0043, Japan

Hiroshi Kohno

Graduate School of Engineering Science, Osaka University, Toyonaka Osaka 560-8531, Japan

Edgar Bonet and Bernard Barbara

CNRS-Laboratoire de Magnétisme Louis Néel, 25 Avenue des Martyrs, BP 166, 38042, Grenoble Cedex 09, France

(Received 10 June 2003; published 24 February 2004)

Aharonov-Bohm effect in a ferromagnetic thin ring in diffusive regime is theoretically studied by calculating the cooperon and diffuson. In addition to the spin-orbit interaction, we include the spin-wave excitation and the spin splitting, which are expected to be dominant sources of dephasing in ferromagnets at low temperatures. The spin splitting turns out to kill the spin-flip channel of cooperon but leaves the spin-conserving channel untouched. For the experimental confirmation of interference effect (described by cooperons) such as weak localization and Aharonov-Bohm oscillation with period $h/2e$, we need to suppress the dominant dephasing by orbital motion. To do this we propose experiments on a thin film or thin ring with magnetization and external field perpendicular to the film, in which case the effective field inside the sample is equal to the external field (magnetization does not add up). The field is first applied strong enough to saturate the magnetization and then carrying out the measurement down to zero field keeping the magnetization nearly saturated, in order to avoid domain formations (negative fields may also be investigated if the coercive field is large enough).

DOI: 10.1103/PhysRevB.69.054420

PACS number(s): 75.47.-m, 73.23.-b, 72.25.-b, 72.15.Rn

Quantum electron transport in mesoscopic systems has been intensively studied for this couple of decades. Typical phenomena are weak localization^{1,2} and Aharonov-Bohm oscillation,³ both arising from the interference of electron wave function. Many experiments have been carried out on various nonmagnetic metals and semiconductors. Although the effect of magnetic impurities in nonmagnetic hosts has been studied in detail,¹ ferromagnetic metals themselves have not been explored in the context of quantum transport until very recently.⁴⁻⁷ One of the reasons may be that the dephasing mechanism in ferromagnetic metals was believed to be much more efficient and complex than nonmagnetic cases with, as a result, complete destruction of interferences. However, these apparent disadvantages are not always crucial, as discussed briefly in Ref. 6, where it was indicated that Aharonov-Bohm effect should be observed in ferromagnets. The first complexity is the existence of the internal field (related to the magnetization) M which generally can lead to dephasing even in the absence of the applied magnetic field. The field depends much on sample shape. Here, we consider an ultrathin ring with sufficiently high perpendicular anisotropy so that the magnetization is perpendicular to the ring. In this case, the total field in the sample is simply equal to the external field, $B_0 = \mu_0 H$. In fact, the effective field inside the sample is $B = B_0 + M + B'$, where $B' \equiv \mu_0 H_D$ denotes the field produced by the surface magnetic charge. The total field $\mathbf{B}$ satisfies the Maxwell equation, $\nabla \cdot \mathbf{B} = 0$, and thus its component perpendicular to the plane is continuous across the surface of the ring; i.e., $B = B_0$, or $B' = -M$. Hence the effect of M on the orbital motion can be neglected. This was pointed out in Ref. 8. Second, the spin splitting due to effective exchange interaction with the local spin, which arises from the s - d mixing, needs to be taken account of as a

source of dephasing. The splitting turns out to suppress spin-flip channel of cooperon and diffuson but spin-conserving channels survive. Here cooperon is a particle-particle propagator, which represents the interference effect, and Diffuson is the particle-hole propagator representing the diffusive motion. Third, ferromagnets generally contain domains and thus it is not always easy to identify magnetic structure. In addition, domain walls may also cause dephasing.^{4,5} Dephasing due to domain structures can be easily avoided by applying a magnetic field larger than the saturation field, H_s . In nanostructures with strong perpendicular anisotropies, $H_s \sim H_c$, the coercive field. Hysteretic behavior of ferromagnets with large perpendicular anisotropies should allow to reduce the external field without affecting the magnetic state, down to zero and even to negative values ($H > -H_c$). From this point of view, hard magnets with very sharp (squarelike) hysteresis loops would be suitable to study electronic coherence in ferromagnets.

The first experimental study of the Aharonov-Bohm effect in ferromagnetic metals was carried out quite recently,⁷ where the Aharonov-Bohm oscillation was observed on a permalloy ring in the presence of an applied field of ≥ 3 T. The Fourier transform of the conductance exhibits a peak corresponding to h/e oscillation. This oscillation period seems to be due to the interference of a single electron propagator.³ The oscillation period of $h/(2e)$ (called Altshuler-Aronov-Spivak oscillation¹⁰) was not seen. We believe this could be because of external field ~ 3 T, which kills the cooperon (see below) (In the nonmagnetic case, similar vanishing of $h/2e$ oscillation by applied field was observed¹⁰). The “dephasing length” was estimated there to be ~ 5000 Å (Ref. 7), which, being obtained from the correlation of conductance, would correspond to the length scale of diffusion (particle hole), which is not affected by the mag-

netic field B_0 [Eq. (17)]. Note that this length scale is not the dephasing length in a strict sense. The true dephasing length, where the interference is lost, is given by the Cooperon mass [Eq. (15)], and is estimated to be much shorter in the presence of external field of ~ 3 T (shorter than $L_B \equiv \sqrt{12}(\hbar/eaB_0) \sim 200$ Å [see Eq. (4)] for a ring of width $a = 400$ Å).

In the case of Ni wires, the resistivity measured down to 20 mK was shown to be explained by the enhanced electron-electron interaction due to the diffusive motion,¹² which indicates that diffuson channel exists, but no clear sign of cooperon channel was observed. Thus, at present, although experiments suggest the existence of diffuson in ferromagnets, there is no indication of the electron coherence represented by cooperons. We would like to stress nevertheless that the Aharonov-Bohm oscillation observed in Ref. 7 is an important first milestone in the study of electron interference effects in ferromagnetic systems.

The aim of this paper is to give a thorough description of Aharonov-Bohm effect in a ferromagnetic thin ring in diffusive regime, by calculating the cooperon and diffuson. Conductivity and conductance fluctuation in a ferromagnetic ring was briefly considered in Ref. 5 in the context of effect of domain walls, where the spin splitting and spin-wave excitation were neglected. We here include, as well as the spin-orbit interaction, the spin-wave excitation and the spin splitting, which are expected to be dominant sources of dephasing in ferromagnets at low temperatures. Spin-flip scattering by single localized spins (similar to those of magnetic impurities in nonmagnetic metals) must be suppressed by the strong exchange interaction in the ferromagnet. Instead of that, spin-wave excitation with long wavelength would be important. In fact, spin waves turn out to result in strong dephasing effect if gapless. In reality, this effect should be suppressed by perpendicular magnetic anisotropy and/or by the application of an external field B_0 (as well as finite system size). In zero field, the spin-wave gap depends on crystal-field symmetry and parameters. In a first approximation we will simply assume that it is given by $\Delta_g = \hbar \gamma (H_a + B_0/\mu_0)$, where H_a is the anisotropy field and γ is the gyromagnetic ratio. Dephasing due to spin wave can be neglected if $k_B T \ll \Delta_g$, and therefore the effect could be tuned from sample to sample by changing the anisotropy energy, or on a given sample by changing the applied field. This will allow to study dephasing effects by spin waves, if the $\hbar/(2e)$ oscillations (Altshuler-Aronov-Spivak oscillations) were to be observed in a ferromagnet. We believe that this will be the case because, contrary to previous experiments,^{7,12} we suggest low-field experiments in ultra-thin ferromagnets with perpendicular anisotropy. In this case, as we argued above, the field coherence length L_B should not be affected by the magnetization M_s of the ferromagnet, and therefore should be as large as in non-magnetic material. In low applied field B_0 , $L_B \propto 1/B_0$ should be long enough so that $\hbar/2e$ oscillation (cooperon) would be observed.

We consider a ring with mean radius R and width a (i.e., the outer and inner radii are $R + a/2$ and $R - a/2 \equiv R_0$, respectively), and thickness b . The width and thickness are assumed to be smaller than the coherence length of the elec-

tron ℓ_φ and R . We consider the equation of motion of the cooperon in this ring, but first without spin-orbit interaction, spin waves and spin splitting³

$$\left[D(-i\nabla - 2e\mathbf{A})^2 + \frac{1}{\tau_\varphi} \right] C_0(\mathbf{r} - \mathbf{r}') = \delta^3(\mathbf{r} - \mathbf{r}'). \quad (1)$$

Here $D = (k_F/m)^2(\tau/3)$ is the diffusion constant (τ is the elastic lifetime) and $\tau_\varphi (\sqrt{D}\tau_\varphi \equiv \ell_\varphi)$ is the dephasing time due to inelastic scattering from nonmagnetic sources, e.g., electron-electron interaction and phonons. The applied magnetic field $\mathbf{B}_0$ is in z direction, i.e., perpendicular to the ring. We consider the case where the magnetization $\mathbf{M}$ is also perpendicular to the ring and constant inside the ring. It is important to note here that in this configuration with a thin ring, the total field, $\mathbf{B} \equiv \mathbf{B}_0 + \mathbf{M} + \mathbf{B}'$ is identical outside and inside the ring, since $\nabla \cdot \mathbf{B} = 0$ requires the continuity of B (in other words, the field $\mathbf{B}'$ due to surface magnetic charges cancels the effect of $\mathbf{M}$). Thus $B = B_0$ and the vector potential is identical to that in the nonmagnetic case; $\mathbf{A} = (B_0/2)(-y, x, 0)$. The equation is thus rewritten as

$$\left[\partial_r^2 + \frac{1}{r} \partial_r + \frac{1}{r^2} \partial_\theta^2 - \frac{2ieB_0}{\hbar} \partial_\theta - \left(\frac{eB_0}{\hbar} \right)^2 r^2 - \ell \phi^{-2} \right] \times C_0(\mathbf{r} - \mathbf{r}') = -\frac{1}{D} \delta^3(\mathbf{r} - \mathbf{r}'), \quad (2)$$

where $\tan \theta \equiv y/x$. The boundary condition in r -direction is given by $(\partial C_0 / \partial r)|_{r=R \pm (a/2)} = 0$ (open boundary). Since we assume $a \ll \ell \phi$, only uniform mode contributes in r -direction. The equation for this uniform mode is obtained by integrating Eq. (2) over r from $R - a/2$ to $R + a/2$, for instance, $r^2 \rightarrow \langle r^2 \rangle \equiv 1/a \int_{R-a/2}^{R+a/2} dr r^2 = R^2 + a^2/12$. The equation thus reduces to

$$\left[\partial_u^2 - 4i \frac{\phi}{R\phi_0} \partial_u - 4 \left(\frac{\phi}{R\phi_0} \right)^2 - \ell \phi^{-2} \right] C_0(u - u') = -\frac{1}{Dab} \delta(u - u'), \quad (3)$$

where $u \equiv R\theta$, $\phi \equiv \pi R^2 B_0$ [$\phi/\phi_0 = eB_0 R^2/(2\hbar)$], and $\phi_0 \equiv h/e$ is the flux quantum]. The dephasing length with the effect of the orbital motion caused by B_0 is thus given by the same expression without M as in nonmagnetic case³

$$\ell \phi^{-2} \equiv \ell \phi^{-2} + \frac{1}{12} \left(\frac{eaB_0}{\hbar} \right)^2. \quad (4)$$

The on-site amplitude of the cooperon (without spin-flip scattering), $C_0(0)$, is thus obtained as

$$C_0(0) = \frac{1}{\pi abLD} \sum_{\ell=-\infty}^{\infty} \frac{1}{\frac{1}{R^2} \left(\ell - 2 \frac{\phi}{\phi_0} \right)^2 + \ell \phi^{-2}}, \quad (5)$$

where ℓ runs over integers.

We now include the spin-orbit coupling, scattering by spin waves, and spin splitting;

$$H' = \sum_{\mathbf{k}, \mathbf{k}'} i\lambda_{so}(\mathbf{k} \times \mathbf{k}') \cdot c_{\mathbf{k}}^\dagger \boldsymbol{\sigma} c_{\mathbf{k}} + \sqrt{2SJ} \sum_{\mathbf{q}, \mathbf{k}} \sum_{\pm} a_{\mathbf{q}}^{\pm} c_{\mathbf{k}+\mathbf{q}}^{\dagger} \sigma_{\pm} c_{\mathbf{k}} + gM \sum_{\mathbf{k}} c_{\mathbf{k}}^{\dagger} \sigma_z c_{\mathbf{k}}. \quad (6)$$

The scattering by spin waves is represented by the second term, where $a^+ \equiv a^\dagger$ and $a^- \equiv a$ are spin-wave operators. Assuming low temperature, the spin-wave interaction is included only at the linear order. The last term represents the spin splitting proportional to the magnetization. The spin-flip processes by spin waves result in new channels in cooperon¹³ The spin splitting results in a dephasing in the total $S^z=0$ channel.¹⁴ The full cooperon with H' included is obtained as¹³⁻¹⁵

$$C(0) = \frac{1}{abLD} \sum_{\ell=-\infty}^{\infty} \left[\frac{1}{\frac{1}{R^2} \left(\ell - 2 \frac{\phi}{\phi_0} \right)^2 + L_1^{-2}} + \frac{1/2(L_2^{-2} - L_3^{-2})}{\left[\frac{1}{R^2} \left(\ell - 2 \frac{\phi}{\phi_0} \right)^2 + L_2^{-2} \right] \left[\frac{1}{R^2} \left(\ell - 2 \frac{\phi}{\phi_0} \right)^2 + L_3^{-2} \right] + 4L_M^{-4}} \right], \quad (7)$$

where

$$L_1^{-2} \equiv \ell \phi^{-2} + \frac{1}{12} \left(\frac{eaB_0}{\hbar} \right)^2 + \frac{1}{D} \left(\frac{1}{\tau_{so}^x} + \frac{1}{\tau_{so}^y} + \frac{1}{\tau_{sw}^x} \right),$$

$$L_2^{-2} \equiv \ell \phi^{-2} + \frac{1}{12} \left(\frac{eaB_0}{\hbar} \right)^2 + \frac{1}{D} \frac{4}{\tau_{sw}^x},$$

$$L_3^{-2} \equiv \ell \phi^{-2} + \frac{1}{12} \left(\frac{eaB_0}{\hbar} \right)^2 + \frac{1}{D} \frac{4}{\tau_{so}^x}, \quad (8)$$

and $L_M^{-2} \equiv gM/D$. Here $1/\tau_{so}^\mu \equiv 2\pi\nu\lambda_{so}^2 \langle (\mathbf{k}' \times \mathbf{k})_\mu^2 \rangle$, where $\mu=x, y, z$, bracket denotes the average over configuration, ν is the density of states, and $1/\tau_{sw}^\mu$ is the spin-flip rate due to spin wave. We have assumed that $1/\tau_{so}^x = 1/\tau_{so}^y$. There is no z component in spin-wave scattering at the present lowest-order calculation [see Eq. (6)]. Spin-flip contribution, $1/\tau_{sw}^x (= 1/\tau_{sw}^y)$, is obtained as

$$\frac{1}{\tau_{sw}^x} = 2\pi SJ^2 \sum_{\pm} \sum_{\mathbf{q}} \frac{1}{\sinh \beta \omega_{\mathbf{q}}} \delta(\epsilon_{\mathbf{k}+\mathbf{q}} \pm \omega_{\mathbf{q}}), \quad (9)$$

where $\beta = 1/(k_B T)$ and $\omega_{\mathbf{q}} \equiv \Delta_g + Aq^2$ is the spin-wave energy, Δ_g and A being the spin-wave gap and stiffness, respectively. The gap is written in terms of the magnetic anisotropy energy H_a and the external field, B_0 , as $\Delta_g = \hbar \gamma (H_a + B_0/\mu_0)$. The spin-wave stiffness is roughly given as $A \approx J/k_F^2$, where J is the exchange coupling between the localized spins. The integration over $\mathbf{q}$ is treated as two-dimensional (this is allowed if $k_B T \ll J/(k_F b)^2$). The integration is carried out as

$$\frac{1}{\tau_{sw}^x} = \frac{SJ^2}{\pi} mA_r \sum_{\pm} \int_{q_{2\pm}}^{q_{1\pm}} \frac{q dq}{\sinh \beta \omega_{\mathbf{q}}} \frac{1}{\sqrt{(q_{1\pm}^2 - q^2)(q^2 - q_{2\pm}^2)}}, \quad (10)$$

where $q_{1\pm} \equiv k_F + \sqrt{k_F^2 \pm 2m\Delta_g}$, $q_{2\pm} \equiv k_F - \sqrt{k_F^2 \pm 2m\Delta_g}$ and A_r is the area of the ring. (We approximated the projection of three-dimensional Fermi wavelength onto the plane by k_F .) Since $J \approx Ak_F^2 \gg \Delta_g$, the integral is dominated by the contribution from the region close to the lower limit. We thus obtain

$$\frac{1}{\tau_{sw}^x} \approx 4\pi S \frac{\nu_{2D} J^2}{\sinh \beta \Delta_g}, \quad (11)$$

where $\nu_{2D} \equiv \nu/(k_F b)$ is the two-dimensional density of states. The effect of spin wave is thus different in two cases; $\hbar \gamma H_a \gg k_B T$ and $\hbar \gamma H_a \ll k_B T$. In the first case of strong anisotropy, the spin-wave excitation is negligible if $k_B T \ll \hbar \gamma H_a$, irrespective of the external field. In the second case with small anisotropy, the dephasing by spin wave is controlled by the external field, it is suppressed if $k_B T \lesssim \hbar \gamma B_0/\mu_0$. Hence in this case, the oscillation would be visible only at high-field region and would vanish at small field $\hbar \gamma B_0/\mu_0 \leq k_B T$. For the observation of Aharonov-Bohm oscillation, large anisotropy energy is of course favorable.

We note that spin waves can be extremely dangerous if gapless. In fact, in the gapless case, long-range ($q \sim 0$) contribution in Eq. (9) is given by $1/\tau_{sw}^x \propto \sum_{\mathbf{q}} 1/q^3$, which diverges ($\propto L$ in the two-dimensional case). This is compared to the phonon case, where the contribution is finite due to the linear energy dispersion and an extra factor proportional to q from coupling constants.¹⁶ Divergence of $1/\tau_{sw}^x$ indicates that the linear approximation breaks down, and more sophisticated calculation including higher-order contributions is needed to treat the gapless case correctly. Here we will not go further in this direction, since in reality there is generally a gap.

The Cooperon is directly related to the quantum correction to the conductivity as $\Delta\sigma = -2/\pi e^2 DC(0)^3$. Noting ℓ in Eq. (7) runs over all integers, it is seen that the conductance $G \equiv ab\sigma$ oscillates as a function of magnetic flux ϕ/ϕ_0

with the period of $\Delta\phi/\phi_0 = 1/2$, or $\Delta B_0 = \phi_0/(2\pi R^2)$. Note that the magnetization M does not affect this oscillation period. The oscillation appears also in the conductance fluctuation as a function of magnetic field (or correlation function between different magnetic fields). The fluctuation is given as³

$$\langle \Delta G(B_0) \Delta G(B_0 + b_0) \rangle = \frac{48e^4}{\pi^3} \frac{Dab}{R} [C'(0) + D'(0)], \quad (12)$$

where $C'(0)$ is the cooperon connecting electrons with different field (B_0 and $B_0 + b_0$), which is defined by Eq. (7), but with $\phi = \pi R^2(B_0 + b_0/2)$ and L_i 's defined by Eq. (8) with B_0 replaced by $B_0 + b_0/2$. Diffuson contribution $D'(0)$ is similarly given by the right-hand side of Eq. (7), but with $\phi = \pi R^2 b_0$ and L_i 's defined by Eq. (8) with B_0 replaced by $b_0/2$ (see Eqs. (15) and (17) below). (The diffuson is a particle-hole propagator which carries zero electric charge, and so $D'(0)$ is not affected by the field B_0 coupled to the center-of-mass motion.)

Let us look into each dephasing mechanism in Eq. (8). The nonmagnetic part $\ell\phi$ would be identical as in the nonmagnetic systems, i.e., the contribution is mainly from the electron-electron interaction at low temperatures^{1,9} (say, $T \lesssim 1$ K). Experimentally $\ell\phi$ is estimated to be $1 \sim 2 \mu\text{m}$ in Al and Ag,^{11,17} which is long enough for submicron rings. The spin-orbit interaction may be different in magnetic case, but is estimated in Ag as $\ell_{so} = 1/\sqrt{D\tau_{so}} \sim 0.47 \mu\text{m}$.¹⁰ Now turn to dephasing of magnetic origin. The dephasing length due to orbital effect, $L_B \equiv \sqrt{12}(\hbar/eaB_0)$ [the last term of Eq. (4)] can be short for a strong field; For $a = 400 \text{ \AA}$ and $B_0 = 1 \text{ T}$, $L_B = 570 \text{ \AA}$. But L_B can be easily controlled to be long enough by choosing B_0 to be small. In nonmagnetic case, clear oscillation pattern is observed for $B_0 \lesssim 0.02 \text{ T}$.¹¹ In ferromagnetic case, such small-field experiment must be done after saturating the magnetization by a strong field (in order to avoid domain formation). The dephasing length due to spin splitting is given by $L_M = k_F^{-1} \sqrt{\frac{2}{3}} k_F \ell (\epsilon_F/\Delta)$. This can be short; in dirty case of $k_F \ell \approx 10 \sim 100$, even if the splitting of s electron is $\frac{1}{100}$ times smaller than that of d electron ($\Delta_d/\epsilon_F \sim O(0.1)$ and so $\Delta/\epsilon_F \sim 0.001$), we have $L_M \approx k_F^{-1} \times (100 \sim 300)$. So the splitting is one of the dominant sources of dephasing in ferromagnetic systems,⁴ and the spin flip channel [the last term in Eq. (7)] can be neglected. Thus only the Cooperon in the vanishing total spin ($S^z = 0$) channel survives, which is calculated as (after the summation over ℓ)

$$C(0) \approx \frac{1}{2abD} L_1 \frac{\sinh \frac{L}{L_1}}{\cosh \frac{L}{L_1} - \cos \left(4\pi \frac{\phi}{\phi_0} \right)}. \quad (13)$$

It is important to note here that due to L_M , the antilocalization effect, which is expected when the spin-orbit interaction

is strong in nonmagnetic metals, does not appear in ferromagnets. [Anti-localization arises from spin-flip processes given by the last term in Eq. (7).] The cooperon which appears in the fluctuation, $C'(0)$, is given by³

$$C'(0) \approx \frac{1}{2abD} L_1' \frac{\sinh \frac{L}{L_1'}}{\cosh \frac{L}{L_1'} - \cos \left(4\pi \frac{\phi + \Delta\phi/2}{\phi_0} \right)}, \quad (14)$$

where $\Delta\phi \equiv b_0 \pi R^2$ is the flux due to the field difference, and

$$L_1'^{-2} \equiv \ell_\phi^{-2} + \frac{1}{12} \left(\frac{ea}{\hbar} \right)^2 (B_0 + b_0/2)^2 + \frac{1}{D} \left(\frac{1}{\tau_{so}^z} + \frac{1}{\tau_{so}^x} + \frac{1}{\tau_{sw}^x} \right). \quad (15)$$

Similarly, Diffuson is obtained as

$$D'(0) \approx \frac{1}{2abD} L_1'' \frac{\sinh \frac{L}{L_1''}}{\cosh \frac{L}{L_1''} - \cos \left(4\pi \frac{\Delta\phi/2}{\phi_0} \right)}, \quad (16)$$

where

$$L_1''^{-2} \equiv \ell_\phi^{-2} + \frac{1}{12} \left(\frac{eab_0/2}{\hbar} \right)^2 + \frac{1}{D} \left(\frac{1}{\tau_{so}^z} + \frac{1}{\tau_{so}^x} + \frac{1}{\tau_{sw}^x} \right). \quad (17)$$

Now we assume that $\ell\phi$ and ℓ_{so} are longer than the sample length, L . We neglect the spin-wave scattering, assuming low temperatures; $k_B T \lesssim \Delta_g$. For a ring of $L = 1.5 \mu\text{m}$ and $a = 400 \text{ \AA}$, magnetic field B_0 as large as 0.038 T (at which $L_B \sim L$) kills the cooperons $C(0)$ and $C'(0)$. Hence no Aharonov-Bohm oscillation appears in the conductance itself for $B_0 \gtrsim 0.038 \text{ T}$. Only the fluctuation of conductance shows oscillation due to $D'(0)$. In contrast, at very small field (after saturating the magnetization), all of $C(0)$, $C'(0)$, and $D'(0)$ survives, and oscillation will be seen in both G and $\langle \Delta G(B_0) \Delta G(B_0 + b_0) \rangle$.

In Ref. 7, the dephasing length was estimated to be $\sim 5000 \text{ \AA}$ under the field of $3 \sim 4 \text{ T}$. This is too long if we consider it as dephasing length of cooperon (L_1), since the orbital effect at $B_0 = 3 \text{ T}$ would be strong enough to kill the coherence at the length of $L_B \sim 200 \text{ \AA}$. In our opinion, the length above corresponds to the length scale of diffusion L_1'' which is not affected by B_0 , and further studies seem to be needed to confirm the coherence represented by cooperon.

In conclusion, we have shown that interference effects in conductance [$\hbar/2e$ oscillation or the Altshuler-Aronov-Spivak (AAS) effect] should be

observed in ferromagnetic films or rings, provided the magnetization is perpendicular to the surface and the sample is thin enough so that the perpendicular demagnetizing field cancels the magnetization contribution to B ($H_D = -M$). This requires materials with large perpendicular anisotropy. A new dephasing mechanism associated with spin waves, specific to ferromagnets, has been studied. We have shown

that it is easily tunable by a magnetic field. After the paper had been accepted, we found that dephasing by spin wave was calculated recently in Ref. 18.

G.T. is grateful to Ministry of Education, Culture, Sports, Science and Technology, Japan and The Mitsubishi Foundation for financial support. He thanks Laboratoire de Magnétisme Louis Néel for its hospitality during his stay.

-
- ¹G. Bergmann, Phys. Rep. **107**, 1 (1984).
²P.A. Lee and T.V. Ramakrishnan, Rev. Mod. Phys. **57**, 287 (1985).
³A.G. Aronov and Yu.V. Sharvin, Rev. Mod. Phys. **59**, 755 (1987).
⁴G. Tatara and H. Fukuyama, Phys. Rev. Lett. **78**, 3773 (1997).
⁵Y. Lyanda-Geller, I.L. Aleiner, and P.M. Goldbart, Phys. Rev. Lett. **81**, 3215 (1998).
⁶G. Tatara and B. Barbara, Phys. Rev. B **64**, 172408 (2001).
⁷S. Kasai, T. Niiyama, E. Saitoh, and H. Miyajima, Appl. Phys. Lett. **81**, 316 (2002); E. Saitoh, S. Kasai, and H. Miyajima, Physica E (Amsterdam) **18**, 237 (2003); S. Kasai, E. Saitoh, and H. Miyajima, J. Appl. Phys. **93**, 8427 (2003).
⁸V.K. Dugaev, P. Bruno, and J. Barna, Phys. Rev. B **64**, 144423 (2001).
⁹B.L. Altshuler and A.G. Aronov, in *Electron-Electron Interactions in Disordered Systems*, edited by A.L. Efros and M. Pollak (Elsevier, New York, 1985).
¹⁰B.L. Altshuler, A.G. Aronov, and B.Z. Spivak, Pis'ma Zh. Éksp. Teor. Fiz. **33**, 101 (1981) [JETP Lett. **33**, 94 (1981)].
¹¹C.P. Umbach, C. Van Haesendonck, R.B. Laibowitz, S. Washburn, and R.A. Webb, Phys. Rev. Lett. **56**, 386 (1986).
¹²T. Ono, Y. Ooka, S. Kasai, H. Miyajima, K. Mibu, and T. Shinjo, J. Magn. Magn. Mater. **226-230**, 1831 (2001).
¹³S. Hikami, A.I. Larkin, and Y. Nagaoka, Prog. Theor. Phys. **63**, 707 (1980).
¹⁴S. Maekawa and H. Fukuyama, J. Phys. Soc. Jpn. **50**, 2516 (1981).
¹⁵H. Fukuyama, in *Electron-Electron Interactions in Disordered Systems*, edited by A.L. Efros and M. Pollak (Elsevier, New York, 1985).
¹⁶A.A. Abrikosov, L.P. Gorkov, and I.E. Dzyaloshinski, *Methods of Quantum Field Theory in Statistical Physics*, (Dover, New York, 1975).
¹⁷V. Chandrasekhar, M.J. Rooks, S. Wind, and D.E. Prober, Phys. Rev. Lett. **55**, 1610 (1985).
¹⁸Y. Takane, J. Phys. Soc. Jpn. **72**, 1155 (2003).