Step-by-step evaluation of photovoltaic module performance related to outdoor parameters: evaluation of the uncertainty

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Abstract — Knowing the uncertainty in the PV production forecast is crucial in the optimization of smart-grid operations and in its stability. In this paper, we present uncertainty calculation in the PV energy production forecast process, calculated step by step. From horizontal irradiance and ambient temperature, all the steps needed to evaluate the PV production are studied with a special focus on the comparison between calculation and measurements. The uncertainty is evaluated by computing the relative mean bias error and the relative mean absolute error.

Index Terms — PV forecast, modelling, outdoor characterization, smart-grids.

I. INTRODUCTION

PV production mainly depends on the solar radiation incident on the PV modules. Solar resource variability and the uncertainty associated with the forecast of PV energy production are one of the most important factors that influence the grid stability, regardless of the size of the power grid.

The ability to precisely forecast the energy produced by PV systems is of great importance and has been identified as one of the key challenges for massive PV integration [1], [2].

Our approach is similar to indirect forecasts: firstly, we predict solar irradiance and ambient temperature, and then, using a PV performance model of the module, we calculate the PV power produced. The different stages of the PV forecast are summarized in Fig. 1, together with the methods used in this study.

Fig. 1. Schematic of the protocol of PV production forecast and studied models.

This study focuses on the evaluation of the uncertainty on PV production estimation, step by step, starting from horizontal irradiances and ambient temperature.

The meteorological forecast step is not considered here, even though we know that it may carry the largest part of uncertainty.

The estimation of the uncertainty is done by comparison of calculated and measured values, with different methods of calculations for each step shown in Fig 1.

For this purpose, we firstly present the experimental measurements: atmospheric-related and from a PV-module platform.

In section III we consider diverse models to estimate G_{POA} , T_{PV} and P_{MPP} . All models are evaluated against local measurements at 1-hour time step.

All the results are grouped in section IV.

II. EXPERIMENTAL PLATFORMS DESCRIPTION

The experimental platforms are installed at the SIRTa observatory [3] located in Palaiseau (France, 48.7N, 2.2E), on the campus of École Polytechnique (Université Paris-Saclay), 15 km South-East of Paris.

A. Instrumental atmospheric measurements

This study uses two types of atmospheric measurements as input: ground-based measurements and satellite images.

The ground-based measurements are realized at the SIRTa observatory. It is a reference meteorological and climate observatory with more than 150 remote sensing and in-situ instruments. In terms of radiometric measurements, the site is part of the Baseline Surface Radiation Network (BSRN, <http://bsrn.awi.de/>) since 2003. GHI, DHI and DNI, as well as ground albedo measurements are realized following BSRN standards (with Kipp & Zonen CMP22 and CHP1 radiometers).

This study considers also estimations of GHI, DHI and DNI from Meteosat geostationary satellite observations computed by CAMS [4], [5].

B. Outdoor photovoltaic characterization platform

A test bench PV platform was installed at SIRTa in 2014 and is composed of six commercial PV modules issued from different technologies (Fig. 2). In this paper, we only consider the c-Si PV module (see Table 1).

Fig. 2. Outdoor characterization PV platform located at SIRTa.

The current-voltage characteristics are measured with Agilent DC electronic loads (6060B), each minute from sunrise to sunset. The P_{MPP} is derived from these characteristics. T_{PV} is measured with 4-wired class A platinum sensors (Pt100) and G_{POA} is measured with a solar radiometer (Hukseflux NR01) and a reference PV cell (SOLEMS RG100) installed in the same plane as the PV module.

TABLE I

FRANCEWATTS FL60-250MBP TECHNICAL PARAMETERS

Maximum power	P_{MPP}	250 W
Open circuit voltage	V_{OC}	37.67 V
Short circuit current	I_{SC}	8.64 A
Power temperature coefficient	TC_P	-0.48%/°C
Current temperature coefficient	TC_I	0.02%/°C
Module area	A	1.6285 m ²

III. THEORETICAL MODELLING

A. POA irradiance calculation

In this part, the input data used are GHI, DHI and DNI solar irradiances given either by SIRTa ground measurements or by CAMS, as well as the tilt angle and the ground albedo.

The tilt irradiance is calculated using equation (1).

$$G_{POA} = B_{POA} + D_{POA} + A_{POA} \quad (1)$$

The beam irradiance is calculated using the DNI as follow:

$$B_{POA} = DNI \times \cos(AOI) \quad (2)$$

The angle of incidence between the sun's rays and the PV array can be determined as:

$$AOI = \cos^{-1} \left[\cos(\theta_z) \cos(\theta_{tilt}) + \sin(\theta_z) \sin(\theta_{tilt}) \cos(\theta_A - \theta_{A,array}) \right] \quad (3)$$

where θ_A and θ_z are the solar azimuth and zenith angles, respectively. θ_{tilt} and $\theta_{A,array}$ are the tilt and azimuth angles of the array, respectively.

The albedo arriving in the plane of array is calculated thanks to the fill factor in front of the array:

$$A_{POA} = GHI \times \text{Albedo} \times \frac{1 - \cos(\theta_{tilt})}{2} \quad (4)$$

Albedo corresponds to the coefficient of reflection of the ground and θ_{tilt} is the tilt angle of the PV module array.

Three models have been considered representing different ways to estimate the diffuse irradiance arriving on PV module:

1) Helbig Model [6]:

The fraction of diffuse irradiance is calculated only from GHI using an empirical relationship, giving an estimated value of DHI and DNI. The diffuse irradiance is then calculated in the same way as described in the isotropic hypothesis.

2) Isotropic hypothesis [7]:

The isotropic sky diffuse model assumes that the diffuse radiation from the sky vault is uniform across the sky. The diffuse irradiance in the plane of array is calculated by equation (5):

$$D_{POA} = DHI \times \frac{1 + \cos(\theta_{tilt})}{2} \quad (5)$$

3) Non isotropic irradiance [8]:

Klucher found that the isotropic model gave good results for overcast skies but underestimates irradiance under clear and partly overcast conditions, when there is increased intensity near the horizon and in the circumsolar region of the sky.

$$D_{POA} = DHI \times \frac{1 + \cos(\theta_{tilt})}{2} \times \left[1 + \left(1 - \frac{DHI}{GHI} \right) \sin^3 \left(\frac{\theta_{tilt}}{2} \right) \right] \times \left[1 + \left(1 - \frac{DHI}{GHI} \right) \cos^2(AOI) \sin^3(\theta_z) \right] \quad (6)$$

B. PV module temperature calculation

In this part, we evaluate two models to calculate T_{PV} from T_{amb} , G_{POA} and WS local measurements.

1) Sandia Model [9]:

$$T_{PV} = G_{POA} \times \exp(a + b \cdot WS) + T_{amb} \quad (7)$$

a and b are empirical coefficients establishing the upper limit for module temperature at low wind speeds and high solar irradiance and the rate at which T_{PV} drops as WS increases, respectively.

2) Faiman Model [10]:

$$T_{PV} = T_{amb} + \frac{G_{POA}}{U_0 + U_1 \cdot WS} \quad (8)$$

To evaluate the models, we first consider parameter values proposed by the authors ($a = -3.47$, $b = -0.0594 \text{ s.m}^{-1}$ and $U_0 = 25.0 \text{ W.m}^{-2}.\text{K}^{-1}$, $U_1 = 6.84 \text{ W.m}^{-3}.\text{s.K}^{-1}$). In a second step, we fit these coefficients to one year of measurements (2015) using the Levenberg-Marquardt method. The obtained coefficients were $a = -3.1398$, $b = -0.305 \text{ s.m}^{-1}$ for Sandia model and $U_0 = 21.777 \text{ W.m}^{-2}.\text{K}^{-1}$, $U_1 = 9.855 \text{ W.m}^{-3}.\text{s.K}^{-1}$ for Faiman model.

C. PV power modeling

In this study, we consider six different models to calculate P_{MPP} from the ground-based measurements of G_{POA} and T_{PV} :

1) Simple model:

It considers a constant CE measured by the manufacturer during a flash test and equal to 0.15086 for our studied PV module.

$$P_{MPP} = CE_{STC} \times G_{POA} \times A \quad (9)$$

2) Simple improved model:

For this case, the conversion efficiency is taken equal to the average of the measured one during 2015: $CE = 0.14339$.

3) Evans model [11]:

It takes into account the linear variation of the conversion efficiency with temperature and the low light effect.

$$P_{MPP} = CE_{STC} \times G_{POA} \times A \times \left[1 - TC_1 \times (T_{PV} - T_{STC}) + \gamma \times \log\left(\frac{G_{POA}}{G_{STC}}\right) \right] \quad (10)$$

With $TC_1 = 0.0048$ from manufacturer data and $\gamma = 0.1$ deduced from measurement during 2015.

4) Statistical model:

This model does not need internal information from the system to describe its performance. It is a data-driven approach which is able to extract relations on past data to predict the future behavior of the PV module. Here, the past is the year of 2015. Thus, quality of historical data is essential for accurate forecast.

5) One-diode electrical model [12]:

This model is based on the Shockley diode equation, with a current source to model the photo-current (I_{ph}), a single-diode junction (n is the ideality factor and I_0 the saturation current) and a series resistance (R_s), as shown in Fig. 3.

Fig. 3. One-diode electrical model.

The equation that drives this model is equation (11):

$$I = I_{ph} - I_0 \left[\exp\left(\frac{q(V + IR_s)}{nkT}\right) - 1 \right] \quad (11)$$

$$P_{MPP} = \max(I \times V) \quad (12)$$

I_{ph} depends on T_{PV} and G_{POA} , I_0 and R_s are temperature dependent and n is constant. All of the constants used in the above equation are determined by fitting the manufacturer flash test and ratings listed in Table 1, as shown in Fig 4.

Paramètres	STC	Modèle
P_{mpp}	245.682 W	246.467 W
V_{mpp}	30.780 V	30.700 V
I_{mpp}	7.982 A	8.028 A

Fig. 4. Determination of the 4 parameters of the one-diode electrical model by fitting manufacturer data of Table 1, $I(V)$ in (a) and $P(V)$ in (b).

6) Artificial neurons network [16]:

The ANN used was built using the feed forward neural network structure with a weighted linear combination and sigmoid function. The architecture chosen is one output (P_{MPP}), three inputs (G_{POA} , T_{amb} and WS) and one hidden layer of five neurons. The training period was the year 2015.

D. Evaluation indicators

In order to compare measurements and calculated values, we compute rMBE and rMAE, as defined in equations (13) and (14).

$$rMBE = \frac{\sum_{i=1}^N [P_{mpp,calc}(i) - P_{mpp,meas}(i)]}{\sum_{i=1}^N P_{mpp,meas}(i)} \quad (13)$$

$$rMAE = \frac{\sum_{i=1}^N |P_{mpp,calc}(i) - P_{mpp,meas}(i)|}{\sum_{i=1}^N P_{mpp,meas}(i)} \quad (14)$$

IV. RESULTS

All presented models in Section II are here evaluated for one independent year of data (2016). Fig. 4 to 6 compare the calculated values to the measured ones. Tables II to IV summarize the rMBE and rMAE obtained results.

A. POA irradiance calculation

In this part, we compare the G_{POA} calculation methods with in plane measurements.

Fig. 4. Comparison of the calculated and the measured global irradiance in the plane of array using ground measurements (a), (b) and (c) and satellite estimation (e), (f) and (g). The models are Helbig (a) and (d), isotropic (b) and (e) and Klucher (c) and (f).

The error estimations are summarized in Table II.

TABLE II

UNCERTAINTY ESTIMATION IN THE CALCULATION OF G_{POA}

Input data	Model	rMBE	rMAE
CAMS	Helbig	0.160	0.247
	Isotropic	0.045	0.189
	Klucher	0.078	0.199
SIRTA	Helbig	0.001	0.079
	Isotropic	-0.044	0.074
	Klucher	-0.018	0.070

Table II shows that all methods using satellite irradiances have a positive bias and absolute error more than double than the results with ground measurements. Isotropic model is the best if data comes from satellite.

B. PV module temperature calculation

The empirical coefficients of the PV module temperature models are first taken as literature values. Then, they were fitted using with the Levenberg-Marquardt method with data from 2015

Fig. 5. Comparison of the calculated and the measured PV module temperature using Sandia model (a) and (b) and Faiman model (c) and (d). The empirical coefficient are those found in the literature (a) and (c) and fitted with data of 2015 (b) and (d).

The error estimation is summarized in Table III.

TABLE III

UNCERTAINTY ESTIMATION IN THE CALCULATION OF T_{PV}

Model	Coef. from	MBE (°C)	MAE (°C)
Sandia	Literature	-0.193	1.883
	2015 meas.	0.597	1.364
Faiman	Literature	0.485	1.471
	2015 meas.	0.647	1.377

Table III shows slightly better results when the model parameters are fitted to the measurements from 2015.

C. PV power modeling

The next figure compare the uncertainty of the model used to simulate the photoelectric effect.

Fig. 6. Comparison of the calculated and the measured PV output maximum power using simple model (a), simple model with CE equal to the average CE of 2015 (d), Evans model (b), satstic model (e), one-diode electrical model (c) and ANN (f).

TABLE IV

UNCERTAINTY ESTIMATION IN THE CALCULATION OF P_{MPP}

Model	rMBE	rMAE
Simple	0.089	0.094
Improved simple	0.035	0.061
Evans	-0.025	0.041
Statistical	0.015	0.045
One-diode	0.034	0.043
ANN	0.0258	0.0425

Table IV shows the improvement of the accuracy of the models, from the simplest to the most complex. A good compromise seems to be the model of Evans.

Interestingly, the lowest rMAE value in the calculated G_{POA} (0.070) is 70% larger than for the best P_{MPP} calculation (4.1%).

V. CONCLUSION

In this paper, we have studied, step by step, the process of the estimation of the PV energy production from GHI, DHI, DNI and T_{amb} , with a special focus on the calculation of the uncertainty. Different models have been studied at each step of the calculation.

The next steps will be to show the link between all the models and the error propagation, to consider the step of meteorological and P_{MPP} forecast at different time horizons and to go through PV plants instead of a unique PV module.

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GLOSSARY

ANN:	Artificial neurons network
AOI:	Angle Of Incidence
A_{POA} :	Albedo in the plan of array ($W.m^{-2}$)
B_{POA} :	Beam irradiance in the plan of array ($W.m^{-2}$)
CAMS:	Copernicus Atmosphere Monitoring Service
CE:	Conversion efficiency
DHI:	Diffuse horizontal irradiance ($W.m^{-2}$)
DNI:	Direct normal irradiance ($W.m^{-2}$)
D_{POA} :	Diffuse irradiance in the plan of array ($W.m^{-2}$)
GHI:	Global horizontal irradiance ($W.m^{-2}$)
G_{POA} :	Plan of array irradiance ($W.m^{-2}$)
P_{MPP} :	Maximum power point (W)
rMAE:	Relative mean absolute error
rMBE:	Relative mean bias error
T_{amb} :	Ambient temperature ($^{\circ}C$)
T_{PV} :	PV module temperature ($^{\circ}C$)
WS:	Wind speed ($m.s^{-1}$)

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