On the assessment of train crankshafts fatigue life based on LCF tests and 2D-FE evaluation of J -integral

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A B S T R A C T

Low cycle fatigue (LCF) tests were carried out on forged carbon steel (AISI 4130) used in V12 Diesel engine crankshafts, at room temperature and 300 °C, under total strain control. These tests were performed in order to study the cyclic mechanical behavior, lifetime and damage mechanisms of the material. Then, a Chaboche nonlinear isotropic-kinematic hardening model available in the commercial FE code Abaqus was identified and a 2D-FE evaluation of J -integral, chosen as a crack driven force, has been carried out to estimate the crankshaft life under cyclic bending loads when a macroscopic crack propagates. It has been found that *i*) material lifetime was not affected by temperature at the studied domain, *ii*) the fractured surfaces examined with SEM exhibit typical features of ductile fracture behavior, and *iii*) the number of cycles spent until the total crankshaft fracture is relatively short compared to its total fatigue life.

Keywords:

Fatigue behavior
Lifetime prediction
Fracture mechanisms
Behavior law
 J -integral

1. Introduction

Over the last few decades, the improvement of the engine components and structures lifetime has become strongly required due to several economic and environmental reasons. Therefore, the forging process has grown to be one of the most interesting processes thanks to its aptitude to make up components with interesting mechanical properties [1,2].

The present paper is interested in the LCF behavior of AISI 4130 Forged steel used in crankshaft applications and FE simulation of crack growth on these structures under cyclic loads. The Crankshaft is a structural component commonly made up of a forging process. It converts the linear piston movement into rotary motion while the force connecting rod is transformed into torque. In general, after the forging process, crankshafts undergo a heat treatment to improve their mechanical properties (toughness, surface hardness and high fatigue resistance), thus allowing a higher resistance to the complex multi-axial thermo-mechanical loads. These severe loadings can occasionally cause fatigue failure [3–6] which is a damage process caused by the initiation and propagation of cracks under cyclic mechanical and/or thermal loadings.

The fatigue life of crankshaft structures has been widely studied in literature. Several authors have been interested in its manufacturing process [7–8] when they studied the influence of the residual stresses induced by the fillet rolling process on the fatigue process of a ductile cast iron crankshaft section under bending. Others are interested in crankshafts fatigue life under service conditions like Williams and Fatemi [9]. These authors have compared the fatigue behavior of forged steel and ductile iron crankshafts from a one-cylinder engine and found that, for a given bending moment amplitude, the forged steel

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crankshaft had a factor of six longer life than the ductile cast iron crankshaft. Henry et al. [10] has studied the durability of crankshafts based on a three-dimensional mechanical analysis. With consideration of rotating external bearing loads, torsional vibrations and internal centrifugal loads, a three-dimensional finite element analysis followed by a local boundary element analysis was used for stress calculations. Metkar et al. [11] has conducted a comparative study of two methods of fatigue life assessment of a single cylinder diesel engine crankshaft by using fracture mechanics approach based on linear elastic fracture mechanics (LEFM) and a developed critical distance approach (CDA).

As mentioned above, several efforts have been devoted to investigate the crankshaft fatigue life. However, the fatigue behavior of the AISI 4130 obtained from the forging process also the FE computation of crack growth on crankshaft have not been well investigated. Hence, this paper aims to study *i)* the LCF behavior of the forged steel and *ii)* investigates the train crankshafts fatigue life based on 2D-FE evaluation of J -integral calculated around crack tip.

2. Material and methods

2.1. Material and specimens manufacturing

The studied material was a high strength low alloy forged steel (AISI 4130) used in V12 train crankshafts (Fig. 1.a), whose chemical composition by weight % is presented in Table 1. In fact, Chrome (Cr) gives good hardness penetration, molybdenum (Mo) supplies uniformity of hardness and high strength [6], and Nickel (Ni), added in smaller amounts, increases the material toughness at low temperatures.

The LCF experiments were carried out on cylindrical specimens (see Fig. 1). The rough form of each one was obtained from the crankshaft counterwise using a wire EDM machine. Next, these samples were quenched and tempered at 600 °C for 1 h in order to obtain a similar hardness to the crankshaft journal and crankpin (235 HV₁).

The microstructure observed after the heat treatment (Fig. 2) presented a fine ferritic-perlitic grain with the presence of some bainitic lathes. The final dimensions of the specimens were obtained with CNC lathe machining. Then, specimens gauge length was mechanically polished using progressively finer grades of emery paper to obtain mirror bright surfaces i.e. to avoid micro-scratches which can lead to premature crack initiation on specimens surface. The monotonic mechanical properties of the forged AISI 4130 steel after the heat treatment at room temperature and 300 °C are summarized in Table 2.

2.2. Experimental procedure

This study is based on LCF total strain control tests conducted on a 250 kN servo-hydraulic machine “Schenck Hydropuls PSB®”. These tests were carried out under total strain ratio $R_\epsilon = -1$ and a permanent strain rate $\dot{\epsilon} = 10^{-2} \text{ s}^{-1}$, at room temperature and at 300 °C, for variable total strain range (the test conditions are summarized in Table 3).

The strain was measured by an extensometer with a gauge length of 10 mm. The specimens were tested at 300 °C by means of high frequency induction heater under temperature control. This temperature was measured by 0.2-mm-diameter Chromel-Alumel thermocouple, spot welded in the middle of the specimen gauge length surface.

The fatigue fracture surfaces were prepared and analyzed by means of a light microscope (LM) “Leica®” and a Scanning Electron Microscopy (SEM) “Nova nanoSEM 450®”. Based on the taken images, the mechanisms of the cracks initiation and propagation under different LCF test conditions were studied.

3. Experimental results and discussion

3.1. Cyclic behavior

Figs. 3 and 4 show the cyclic softening/hardening behavior of the forged steel under LCF conditions detailed in Section 2.2. These curves were obtained by plotting the peak tensile stress in successive cycles to illustrate the path by which the material

Fig. 1. (a) 3D view of one-half crankthrow, (b) geometry of the cylindrical specimen used for LCF tests (all dimension in mm).

Table 1

Chemical analysis of the forged steel (AISI 4130).

Elements	C	Si	Mn	P	S	Cr	Mo	Ni
Weight %	0.263	0.236	0.55	0.01	0.006	1.02	0.176	0.196

Fig. 2. Microstructure of AISI 4130 forged steel after heat treatment.

reaches its final cyclic flow stress level. The specimen fatigue lifetime, which corresponds to the macroscopic crack growth, is defined as a 10% stress drop compared to the stabilized stress.

During the first few cycles, the forged steel response (Fig. 3) of the tests conducted under a total strain range of $\pm 0.75\%$ and $\pm 1\%$, at room temperature, shows a cyclic hardening, named primary cyclic hardening, followed by a cyclic softening (i.e. the peak tensile stress ($\sigma_{\max}$) decreases gradually with a significant rate of change). It also presents a secondary cyclic hardening few cycles before the specimens failure. In contrast with the cyclic behavior observed under large total strain range, the one observed under small total strain range ($\pm 0.3\%$ and $\pm 0.4\%$) seems to be simpler i.e.: only a cyclic softening was observed during LCF tests). The forged steel behavior observed at 300 °C shows the presence of two phases (Fig. 4): a cyclic hardening followed by cyclic softening. This hardening/softening behavior appears to be depending on applied strain amplitude; it is more pronounced when total strain range is larger. In addition, the duration of the hardening phase is wider than that obtained at room temperature.

3.2. LCF lifetime and damage mechanisms

At present, several classical methods have been used to describe the failure in isothermal and uni-axial specimens such as Manson-Coffin (Eq. (1)) [12,13], Smith-Watson-Topper [14] or Ostergren [15].

$$\frac{\Delta \epsilon}{2} = \frac{\Delta \epsilon_{\text{plastic}}}{2} + \frac{\Delta \epsilon_{\text{elastic}}}{2} = \epsilon'_f (2 \cdot N_f)^c + \frac{\sigma'_f}{E} (2 \cdot N_f)^b \quad (1)$$

where σ'_f and ϵ'_f represent the fatigue strength and ductility coefficient, respectively, and c and b the fatigue strength and ductility exponents, respectively, and E the elastic modulus.

Nevertheless, these criteria are not adaptable to some structures which undergo a severe anisothermal multiaxial services loading. Hence, several energetic approaches have been proposed to predict the structures lifetime. These approaches can take into account the multi-axial loading character and the effect of temperature variation. These criteria are based on the dissipated

Table 2

Monotonic mechanical properties of the AISI 4130 forged steel at room temperature and 300 °C.

T (°C)	E (GPa)	Re (MPa)	R _{0.2} (MPa)	R _m (MPa)	Power law exponent (n)
25 °C	198	408	556	808	5.6
300 °C	176	288	459	799	5.4

Table 3

Summary of test conditions for low cycle fatigue.

Specimen	T (°C)	ε (%)	f (Hz)
1	25	± 1	0.25
2	25	± 0.75	0.333
3	25	± 0.4	0.625
4	25	± 0.3	0.833
5	300	± 0.75	0.333
6	300	± 0.5	0.5
7	300	± 0.4	0.625
8	300	± 0.3	0.833

Fig. 3. Cyclic behavior of the forged carbon steel (AISI 4130) at room temperature.

energy per cycle as a damage parameter [16–19] and defined as (Eq. (2)):

$$W_p N_f^\beta = c. \quad (2)$$

This damage induced in the material due to the cyclic loading can be estimated using the energy denoted as W [20–22]. The energy is presented by the area within the stabilized stress–strain hysteresis loops. The fatigue parameters are calculated from the stabilized cycle as (Eq. (3)):

$$W = \int_{\text{cycle}} \sigma : \varepsilon_{\text{plastic}} dt \approx \Delta\sigma \cdot \Delta\varepsilon_{\text{plastic}} \quad (3)$$

where σ is the axial stress and $\dot{\varepsilon}_p$ is the axial plastic strain rate.

Fig. 5 shows that the influence of temperature on the forged steel (AISI 4130) fatigue lifetime is negligible. This can be explained by the low variation of the mechanical behavior between room temperature and 300 °C (Figs. 3 and 4).

The fractographic analysis carried out by LM on the broken specimens obtained at room temperature reveals the presence of three characteristic zones of fatigue fracture (Fig. 6.a–b).

Fig. 4. Cyclic behavior of the forged carbon steel (AISI 4130) at 300 °C.

(a) Number of reversals to failure (Manson Coffin Basquin)

(b) Dissipated energy per cycle versus the number of cycle to failure

Fig. 5. LCF life of AISI 4130 forged steel at room temperature and 300 °C.

The first one corresponds to the crack initiation zone which probably initiates from small surface defects and then propagates. These features are approximated as semi-elliptical cracks. For the total strain range $\pm 0.3\%$ the fractured surfaces present only one crack initiation site, whereas the surface which corresponds to $\pm 1\%$ presents secondary sites (Fig. 6.b). This can be explained by the high plastic strain generated at this test. It can also be the consequence of some micro-defects in specimen gauge surface. The second and the final zones correspond to fatigue fractured surface and monotonic overload surfaces, respectively. The typical examples of SEM micrographs of fracture surfaces near the crack initiation site are revealed in Fig. 6 (details "A" and "B").

The SEM observation of the fatigue propagation surface carried out under a total strain range of $\pm 0.3\%$ shows a fatigue striations for short cracks length as well as the long one (near the final fatigue fractured zone (Fig. 7.b). These fatigue striations indicate that the local fatigue crack growth is about $0.93 \mu\text{m}/\text{cycle}$ in the end of the fatigue fractured surface. The presence of these fatigue striations can be explained by the ductile behavior of the forged steel at the room temperature [3]. The SEM micrographs of the final overload fracture (Fig. 7.c) shows spherical dimples which correspond to the micro-voids characteristic of monotonic ductile fracture (Fig. 7).

Fig. 6. LM images showing the typical fatigue features of the specimen fractured surfaces at room temperature and their corresponding crack initiation SEM image zones, (a) $\varepsilon \pm 0.3\%$, $N_f = 14,736$; (b); $\varepsilon \pm 1\%$, $N_f = 187$.

Fig. 7. SEM observation of the fatigue fractured surface obtained under LCF test (room temperature, $\varepsilon = \pm 0.4$); (a) mixed zone, (b) fatigue striations, (d) EDX analysis of particle "A".

Fig. 8. SEM observation of the void growth and coalescence in the AISI 4130 forged steel at room temperature ($\varepsilon = \pm 1$).

The fractured surface which corresponds to the total strain range $\pm 1\%$ reveals ductile micro-mechanisms which appear at the end of the fatigue fractured zone (Fig. 7). This phenomenon may be referred to as the small cavity or microvoid locking by the MnS inclusions (Fig. 7.d). When microvoid growth is important, it is usually terminated by void-linking or coalescence, leading to an elliptical form with long axis perpendicular to stress direction, which causes crack propagation (Fig. 8). The microvoid locking is generally prevalent at sufficiently low stress triaxiality defined as the ratio of the mean stress and von Mises equivalent stress. Many experiments suggested a decrease of material ductility with increasing stress triaxiality [23–26].

4. Crankshaft fatigue life assessment

The fatigue design of crankshafts depends on the precise evaluation of the local stress and strain in the structure using a FE Analysis. Indeed, the purpose of a robust cyclic plasticity model of the studied forged steel appears to be with a great interest to.

4.1. Mechanical cyclic behavior of AISI 4130

The adopted methodology follow up to model the mechanical behavior of the studied material is described in this section. All presented computations have been performed on a 2.5 GHz bi-processor with 6 GB of RAM. We assume that the forged steel obeys to an elastoplastic constitutive law. The viscous effects are neglected due to the relative low temperature range of the tested specimens varying from room temperature to 300 °C. A Chaboche nonlinear isotropic-kinematic hardening model available in the commercial FE code “Abaqus®”, is chosen to simulate the cyclic mechanical behavior of the studied material [27]. The evolution law of this model consists of two components: a nonlinear kinematic hardening component, which describes the translation of the yield surface in stress space through the backstress α ; and an isotropic hardening component, which describes the change of the equivalent stress defining the size of the yield surface σ^0 , as a function of plastic deformation. The kinematic hardening component is defined to be an additive combination of a purely kinematic term (linear Ziegler hardening law) and a relaxation term, which introduces the nonlinearity.

$$\dot{\alpha} = C \frac{1}{\sigma^0} (\sigma - \alpha) \dot{\varepsilon}^{pl} - \gamma \alpha \dot{\varepsilon}^{pl}$$

C is the initial kinematic hardening modulus, and γ determines the rate at which the kinematic hardening modulus decreases with increasing plastic deformation. When γ is zero, the linear Ziegler hardening law is recovered. The isotropic hardening

Table 4
Material parameters identified for Chaboche isotropic-kinematic non-linear hardening law.

E (GPa)	ν	σ_0 (MPa)	Q (MPa)	b	C (GPa)	γ (MPa)
198	0.3	330	−65	7	82	260

Fig. 9. Comparison of an isothermal uniaxial LCF tests with computed results using the identified constitutive law with Chaboche non-linear isotropic-kinematic hardening at room temperature.

behavior of the model defines the evolution of the yield surface size σ^0 as a function of the equivalent plastic strain,

$$\sigma^0 = \sigma_0 + Q \left(1 - e^{-b \cdot \epsilon^p} \right)$$

where σ_0 is the yield stress at zero plastic strain and Q and b are material parameters. Q is the maximum change in the size of the yield surface, and b defines the rate at which the size of the yield surface changes as plastic straining develops. These parameters have been obtained (Table 4) by minimization of the least squares distance between computed and measured stresses. Fig. 9 presents the computed and experimental material response at the quasi-stabilized hysteresis loop in terms of axial strain and stress.

4.2. Modeling and computation of crankshaft fatigue life

Figs. 10 and 11 shows the proposed 2D finite element model used to study the crack propagation on crankshaft under LCF conditions. The studied structure is symmetrical and all the crankthrows composed the crankshaft are the same, hence, one-half crankthrow model is used in this computation instead of whole crankshaft model. Fig. 11.a shows the boundary conditions applied on the crankshaft. A relatively fine mesh near the fillet is generated in order to accurately capture the characteristics of the stress field in this stress concentration area shows a schematically side view of a crankthrow section (Fig. 11.b). Two-dimensional plane strain 8-noded CPE8R elements are used in this model a sample of magnified finite element mesh near the crack tip. The method chosen to describe fatigue cracks growth was based on the calculation of the J -integral in the vicinity of the crack tip (Fig. 11.b). The J -integral is a useful parameter in the fatigue structures evaluation [28–30]. It is related to the energy release associated with crack growth and also involves the measurement of the intensity of deformation at crack tip.

In this analysis the J -integral was provided for fourteen contours surrounding the tips to study its dependence on contour number. Fig. 12 shows the evolution of ΔJ values obtained for contours surrounding one tip for the different crack length simulated. The calculated ΔJ values were quasi-identical at contours 9–14 which correspond to an integration radius up to 30 μm . Next the stabilized values of ΔJ were plotted against the crack length when it propagates along the crankweb section. Three major zones can be revealed (Fig. 13). In the first one, the crack driven force ΔJ decreases (from $28 \cdot 10^{-3} \text{ N/mm}$ to $17 \cdot 10^{-3} \text{ N/mm}$, approximately) when the crack growth. This can be explained by the fact that the crack tip moves away from the zone affected by

Fig. 10. Crack propagation modeling of one-half crankthrow section.

Fig. 11. A 2D finite element model of a one-half crankthrow section: (a) dimensions (in mm) and boundary conditions, (b) a magnified finite element mesh surrounding the crack tip.

the presence of the fillet radius in which a mechanical stress concentration occurs. After a small quasi-stabilization phase ($\Delta J \sim 17 \cdot 10^{-3}$ N/mm) the crack driven starts to rise (from $17 \cdot 10^{-3}$ N/mm to $24.6 \cdot 10^{-3}$ N/mm for a crack length of 20 mm and 60 mm, respectively). During the last phase ΔJ value increase quickly in concordance with crack propagation until the final fracture ($\Delta J \sim 17 \cdot 10^{-3}$ N/mm).

The determination of the number of cycles to failure were obtained using the fracture mechanics approaches based on the numerical computation performed on cracked crankweb section. The calculated ΔJ values are used with the modified equation of Paris law (Eq. (5.5)) obtained from previous work [31] (Fig. 14) to estimate the number of cycles to failure.

$$\frac{da}{dN} = C \cdot \Delta J^m \text{ where } C = 26.4 \text{ and } m = 5.22 \quad (5.5)$$

where C and m are constants dependent on the materials and the environmental factors, respectively.

It is now possible to estimate the life spent to grow the crack between an initial small crack (a_0) and final fracture (a_f), by integrating Eq. (5.5) with the crack driven force (ΔJ) calculated along the crankweb section, between $a_0 = 4$ mm, $a_f = 75$ mm.

$$\Rightarrow N(a) = \int_{a_0}^{a_f} \frac{\Delta J^{-n}}{C} \cdot da \quad (5.6)$$

Hence $2.07 \cdot 10^6$ cycles (about 64 h) were estimated to attain the crankshaft final failure. The calculated number of cycles appear to be relatively small compared to the crankshaft total life. This result can be explain by the fact that crankshafts are designed to resist on fatigue crack initiation and not in propagation. In fact, the major part of the crankshaft life was spent in initiation phase.

Fig. 12. Values of J -integral range (ΔJ) provided by FE code for different contours and different crack lengths.

Fig. 13. Evolution of crack driven force (ΔJ) along the crankweb section.

Fig. 14. Evolution of the crack growth rate (da/dN) of AISI 4130 forged steel with ΔJ at room temperature [24].

5. Conclusion

In the present paper, the LCF behavior, fatigue lifetime, and damage mechanisms of the AISI 4130 forged steel used in crankshafts are studied at room temperature and at 300 °C. The LCF behavior, observed until specimen fracture, exhibits a notable cyclic softening behavior at room temperature and a cyclic hardening followed by a cyclic softening behavior at 300 °C.

The fatigue lifetime is predicted for both studied temperature using Manson Coffin Basquin and Charkaluk energy criterion as initiation criteria. Results have shown that lifetime is not affected by temperature at the studied domain.

The SEM of the fractured surfaces at the room temperature has shown that crack initiation sites are located on the specimen surfaces. This indicates that surface micro-defects and/or the extrusion/intrusion mechanisms are probably the principal causes of crack initiation. The fatigue fractured surfaces reveal the presence of striations which cover the whole observed surfaces. These striations prove the ductile behavior of the material LCF fracture. This behavior is also highlighted with the presence of void locking by the MnS inclusions (observed easily for tests conducted under large total strain).

A 2D-FE model was carried out to study the crack propagation on crankshaft under LCF conditions. The FE evaluation of J -integral calculated around the crack tip was shown that the number of cycles spent until the total crankshaft fracture is relatively short compared to its total fatigue life.

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