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Pierre Gaillard

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Rational solutions of order 5 to the KPI equation depending on 8 parameters.

P. Gaillard,

Université de Bourgogne,
Institut de mathématiques de Bourgogne,
9 avenue Alain Savary BP 47870
21078 Dijon Cedex, France :
E-mail : Pierre.Gaillard@u-bourgogne.fr

Abstract

In this paper, we go on with the study of rational solutions to the Kadomtsev-Petviashvili equation (KPI). We construct here rational solutions of order 5 as a quotient of 2 polynomials of degree 60 in x , y and t depending on 8 parameters. The maximum modulus of these solutions at order 5 is checked as equal to $2(2N+1)^2 = 242$. We study their modulus patterns in the plane (x, y) and their evolution according to time and parameters $a_1, a_2, a_3, a_4, b_1, b_2, b_3, b_4$. We get triangle and ring structures as obtained in the case of the NLS equation.

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1 Introduction

We consider the Kadomtsev-Petviashvili equation (KPI) in the following form

$$(4u_t - 6uu_x + u_{xxx})_x - 3u_{yy} = 0, \quad (1)$$

where subscripts x , y and t denote partial derivatives.

Kadomtsev and Petviashvili [1] first proposed this equation in 1970. This equation is a model for example, for surface and internal water waves [2], and in nonlinear optics [3]. Zakharov extended the inverse scattering transform (IST) to this KPI equation, and obtained several exact solutions.

The first rational solutions were found in 1977 by Manakov, Zakharov, Bordag and Matveev [4]. Other researches were led and more general rational solutions to the KPI equation were obtained. We can mention the following works by Krichever in 1978 [5, 6], Satsuma and Ablowitz in 1979 [7], Matveev in 1979 [8], Freeman and Nimmo in 1983 [9, 10], Pelinovsky and Stepanyants in 1993 [11],

Pelinovsky in 1994 [12], Ablowitz and Villarroel [13, 14] in 1997-1999, Biondini and Kodama [15, 16, 17] in 2003-2007.

We recall the author's results about the representations of the solutions to the KPI equation, first in terms of Fredholm determinants of order $2N$ depending on $2N - 1$ parameters, then in terms of wronskians of order $2N$ with $2N - 1$ parameters. These representations allow to obtain an infinite hierarchy of solutions to the KPI equation, depending on $2N - 1$ real parameters .

Then we construct the rational solutions of order N depending on $2N - 2$ parameters without presence of a limit which can be written as a ratio of two polynomials of x, y and t of degree $2N(N + 1)$.

The maximum modulus of these solutions at order N is equal to $2(2N + 1)^2$. This method gives an infinite hierarchy of rational solutions of order N depending on $2N - 2$ real parameters. We construct here the explicit rational solutions of order 5, depending on 8 real parameters, and the representations of their modulus in the plane of the coordinates (x, y) according to the real parameters $a_1, b_1, a_2, b_2, a_3, b_3, a_4, b_4$ and time t .

2 Rational solutions to the KPI equation of order N depending on $2N - 2$ parameters

2.1 Fredholm representation

One defines real numbers λ_j such that $-1 < \lambda_\nu < 1$, $\nu = 1, \dots, 2N$ depending on a parameter ϵ that will be intended to tend towards 0; they can be written as

$$\lambda_j = 1 - 2\epsilon^2 j^2, \quad \lambda_{N+j} = -\lambda_j, \quad 1 \leq j \leq N, \quad (2)$$

The terms $\kappa_\nu, \delta_\nu, \gamma_\nu, \tau_\nu$ and $x_{r,\nu}$ are functions of λ_ν , $1 \leq \nu \leq 2N$; they are defined by the formulas :

$$\begin{aligned} \kappa_j &= 2\sqrt{1 - \lambda_j^2}, \quad \delta_j = \kappa_j \lambda_j, \quad \gamma_j = \sqrt{\frac{1 - \lambda_j}{1 + \lambda_j}},; \\ x_{r,j} &= (r - 1) \ln \frac{\gamma_j - i}{\gamma_j + i}, \quad r = 1, 3, \quad \tau_j = -12i\lambda_j^2 \sqrt{1 - \lambda_j^2} - 4i(1 - \lambda_j^2) \sqrt{1 - \lambda_j^2}, \quad (3) \\ \kappa_{N+j} &= \kappa_j, \quad \delta_{N+j} = -\delta_j, \quad \gamma_{N+j} = \gamma_j^{-1}, \\ x_{r,N+j} &= -x_{r,j}, \quad \tau_{N+j} = \tau_j \quad j = 1, \dots, N. \end{aligned}$$

e_ν $1 \leq \nu \leq 2N$ are defined in the following way :

$$\begin{aligned} e_j &= 2i \left(\sum_{k=1}^{1/2 M-1} a_k (je)^{2k-1} - i \sum_{k=1}^{1/2 M-1} b_k (je)^{2k-1} \right), \\ e_{N+j} &= 2i \left(\sum_{k=1}^{1/2 M-1} a_k (je)^{2k-1} + i \sum_{k=1}^{1/2 M-1} b_k (je)^{2k-1} \right), \quad 1 \leq j \leq N, \quad (4) \\ a_k, b_k &\in \mathbf{R}, \quad 1 \leq k \leq N - 1. \end{aligned}$$

ϵ_ν , $1 \leq \nu \leq 2N$ are real numbers defined by :

$$e_j = 1, \quad e_{N+j} = 0 \quad 1 \leq j \leq N. \quad (5)$$

Let I be the unit matrix and $D_r = (d_{jk})_{1 \leq j, k \leq 2N}$ the matrix defined by :

$$d_{\nu\mu} = (-1)^{\epsilon_\nu} \prod_{\eta \neq \mu} \left(\frac{\gamma_\eta + \gamma_\nu}{\gamma_\eta - \gamma_\mu} \right) \exp(i\kappa_\nu x - 2\delta_\nu y + \tau_\nu t + x_{r,\nu} + e_\nu). \quad (6)$$

Then we recall the following result :

Theorem 2.1 *The function v defined by*

$$v(x, y, t) = -2 \frac{|n(x, y, t)|^2}{d(x, y, t)^2} \quad (7)$$

where

$$n(x, y, t) = \det(I + D_3(x, y, t)), \quad (8)$$

$$d(x, y, t) = \det(I + D_1(x, y, t)), \quad (9)$$

and $D_r = (d_{jk})_{1 \leq j, k \leq 2N}$ the matrix

$$d_{\nu\mu} = (-1)^{\epsilon_\nu} \prod_{\eta \neq \mu} \left(\frac{\gamma_\eta + \gamma_\nu}{\gamma_\eta - \gamma_\mu} \right) \exp(i\kappa_\nu x - 2\delta_\nu y + \tau_\nu t + x_{r,\nu} + e_\nu). \quad (10)$$

is a solution to the KPI equation (1), depending on $2N - 1$ parameters a_k, b_k , $1 \leq k \leq N - 1$ and ϵ .

2.2 Wronskian representation

We use the following notations :

$$\phi_{r,\nu} = \sin \Theta_{r,\nu}, \quad 1 \leq \nu \leq N, \quad \phi_{r,\nu} = \cos \Theta_{r,\nu}, \quad N + 1 \leq \nu \leq 2N, \quad r = 1, 3, \quad (11)$$

with the arguments

$$\Theta_{r,\nu} = \frac{\kappa_\nu x}{2} + i\delta_\nu y - i\frac{x_{r,\nu}}{2} - i\frac{\tau_\nu}{2} t + \gamma_\nu w - i\frac{e_\nu}{2}, \quad 1 \leq \nu \leq 2N. \quad (12)$$

$W_r(w)$ denotes the wronskian of the functions $\phi_{r,1}, \dots, \phi_{r,2N}$ defined by

$$W_r(w) = \det[(\partial_w^{\mu-1} \phi_{r,\nu})_{\nu, \mu \in [1, \dots, 2N]}]. \quad (13)$$

We consider the matrix $D_r = (d_{\nu\mu})_{\nu, \mu \in [1, \dots, 2N]}$ defined in (10). Then we have the following statement :

Theorem 2.2 *The function v defined by :*

$$v(x, y, t) = -2 \frac{|W_3(\phi_{3,1}, \dots, \phi_{3,2N})(0)|^2}{(W_1(\phi_{1,1}, \dots, \phi_{1,2N})(0))^2}$$

is a solution to the KPI equation depending on $2N - 1$ real parameters a_k, b_k $1 \leq k \leq N - 1$ and ϵ , with ϕ_ν^r defined in (11)

$$\begin{aligned} \phi_{r,\nu}(w) &= \sin\left(\frac{\kappa_\nu x}{2} + i\delta_\nu y - i\frac{x_{r,\nu}}{2} - i\frac{\tau_\nu}{2}t + \gamma_\nu w - i\frac{e_\nu}{2}\right), \quad 1 \leq \nu \leq N, \\ \phi_{r,\nu}(w) &= \cos\left(\frac{\kappa_\nu x}{2} + i\delta_\nu y - i\frac{x_{r,\nu}}{2} - i\frac{\tau_\nu}{2}t + \gamma_\nu w - i\frac{e_\nu}{2}\right), \quad N+1 \leq \nu \leq 2N, \quad r = 1, 3, \end{aligned}$$

$\kappa_\nu, \delta_\nu, x_{r,\nu}, \gamma_\nu, e_\nu$ being defined in (3), (2) and (4).

2.3 Rational solutions

We recall the last result concerning the rational solutions to the KPI equation as a quotient of two determinants.

We use the following notations :

$$\begin{aligned} X_\nu &= \frac{\kappa_\nu x}{2} + i\delta_\nu y - i\frac{x_{3,\nu}}{2} - i\frac{\tau_\nu}{2}t - i\frac{e_\nu}{2}, \\ Y_\nu &= \frac{\kappa_\nu x}{2} + i\delta_\nu y - i\frac{x_{1,\nu}}{2} - i\frac{\tau_\nu}{2}t - i\frac{e_\nu}{2}, \end{aligned}$$

for $1 \leq \nu \leq 2N$, with $\kappa_\nu, \delta_\nu, x_{r,\nu}$ defined in (3) and parameters e_ν defined by (4).

We define the following functions :

$$\begin{aligned} \varphi_{4j+1,k} &= \gamma_k^{4j-1} \sin X_k, & \varphi_{4j+2,k} &= \gamma_k^{4j} \cos X_k, \\ \varphi_{4j+3,k} &= -\gamma_k^{4j+1} \sin X_k, & \varphi_{4j+4,k} &= -\gamma_k^{4j+2} \cos X_k, \end{aligned} \quad (14)$$

for $1 \leq k \leq N$, and

$$\begin{aligned} \varphi_{4j+1,N+k} &= \gamma_k^{2N-4j-2} \cos X_{N+k}, & \varphi_{4j+2,N+k} &= -\gamma_k^{2N-4j-3} \sin X_{N+k}, \\ \varphi_{4j+3,N+k} &= -\gamma_k^{2N-4j-4} \cos X_{N+k}, & \varphi_{4j+4,N+k} &= \gamma_k^{2N-4j-5} \sin X_{N+k}, \end{aligned} \quad (15)$$

for $1 \leq k \leq N$.

We define the functions $\psi_{j,k}$ for $1 \leq j \leq 2N, 1 \leq k \leq 2N$ in the same way, the term X_k is only replaced by Y_k .

$$\begin{aligned} \psi_{4j+1,k} &= \gamma_k^{4j-1} \sin Y_k, & \psi_{4j+2,k} &= \gamma_k^{4j} \cos Y_k, \\ \psi_{4j+3,k} &= -\gamma_k^{4j+1} \sin Y_k, & \psi_{4j+4,k} &= -\gamma_k^{4j+2} \cos Y_k, \end{aligned} \quad (16)$$

for $1 \leq k \leq N$, and

$$\begin{aligned} \psi_{4j+1,N+k} &= \gamma_k^{2N-4j-2} \cos Y_{N+k}, & \psi_{4j+2,N+k} &= -\gamma_k^{2N-4j-3} \sin Y_{N+k}, \\ \psi_{4j+3,N+k} &= -\gamma_k^{2N-4j-4} \cos Y_{N+k}, & \psi_{4j+4,N+k} &= \gamma_k^{2N-4j-5} \sin Y_{N+k}, \end{aligned} \quad (17)$$

for $1 \leq k \leq N$.

Then we get the following result :

Theorem 2.3 *The function v defined by :*

$$v(x, y, t) = -2 \frac{|\det((n_{jk})_{j,k \in [1, 2N]})|^2}{\det((d_{jk})_{j,k \in [1, 2N]})^2} \quad (18)$$

is a rational solution to the KPI equation (1).

$$(4u_t - 6uu_x + u_{xxx})_x - 3u_{yy} = 0,$$

where

$$\begin{aligned} n_{j1} &= \varphi_{j,1}(x, y, t, 0), \quad 1 \leq j \leq 2N & n_{jk} &= \frac{\partial^{2k-2} \varphi_{j,1}}{\partial \epsilon^{2k-2}}(x, y, t, 0), \\ n_{jN+1} &= \varphi_{j,N+1}(x, y, t, 0), \quad 1 \leq j \leq 2N & n_{jN+k} &= \frac{\partial^{2k-2} \varphi_{j,N+1}}{\partial \epsilon^{2k-2}}(x, y, t, 0), \\ d_{j1} &= \psi_{j,1}(x, y, t, 0), \quad 1 \leq j \leq 2N & d_{jk} &= \frac{\partial^{2k-2} \psi_{j,1}}{\partial \epsilon^{2k-2}}(x, y, t, 0), \\ d_{jN+1} &= \psi_{j,N+1}(x, y, t, 0), \quad 1 \leq j \leq 2N & d_{jN+k} &= \frac{\partial^{2k-2} \psi_{j,N+1}}{\partial \epsilon^{2k-2}}(x, y, t, 0), \\ & & & 2 \leq k \leq N, \quad 1 \leq j \leq 2N \end{aligned} \quad (19)$$

The functions φ and ψ are defined in (14), (15), (16), (17).

3 Explicit expression of rational solutions of order 5 depending on 8 parameters

In the following, we explicitly construct rational solutions to the KPI equation of order 5 depending on 8 parameters.

Because of the length of the expression, we cannot give it in this text. We only give the expression without parameters in the appendix.

We give patterns of the modulus of the solutions in the plane (x, y) of coordinates in function of parameters $a_1, a_2, a_3, a_4, b_1, b_2, b_3, b_4$ and time t .

When at least one parameter is not equal to 0, we observe the presence of 15 peaks. The maximum modulus of these solutions is checked in this case $N = 5$, equal to $2(2N + 1)^2 = 2 \times 11^2 = 242$.

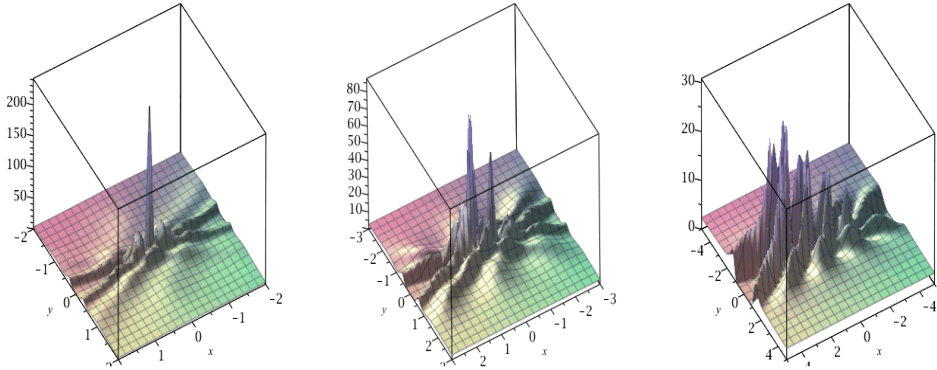


Figure 1. Solution of order 5 to KPI, on the left for $t = 0$; in the center for $t = 0,01$; on the right for $t = 0,1$; all parameters equal to 0.

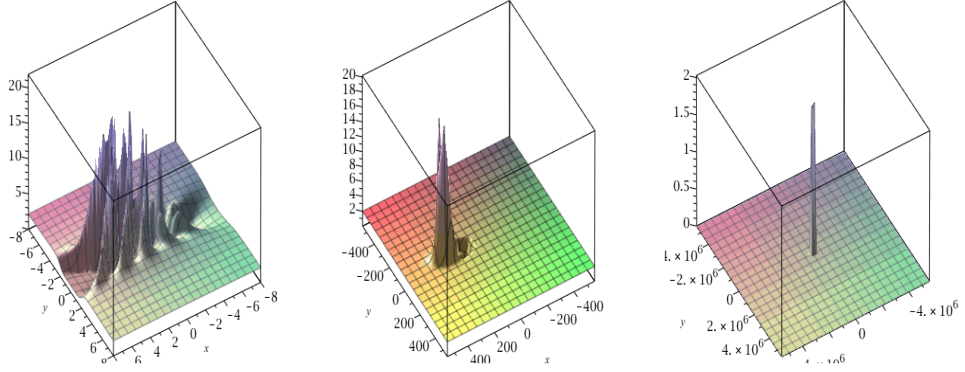


Figure 2. Solution of order 5 to KPI, on the left for $t = 0,2$; in the center for $t = 20$; on the right for $t = 50$; all parameters equal to 0.

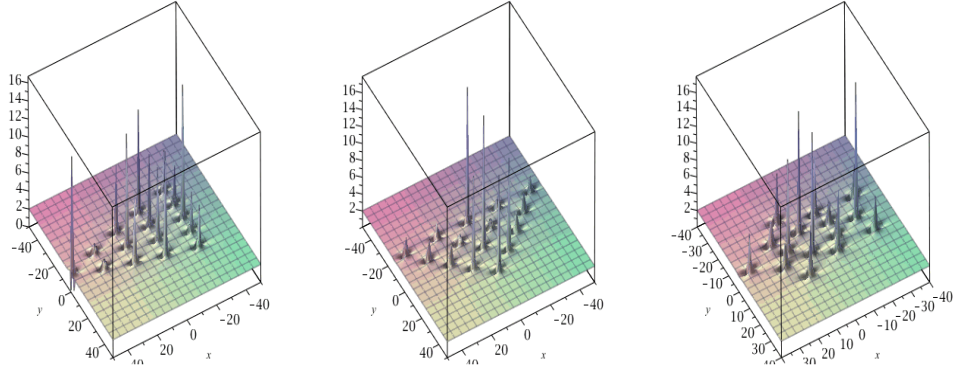


Figure 3. Solution of order 5 to KPI for $t = 0$, on the left for $a_1 = 10^4$; in the center for $b_1 = 10^4$; on the right for $a_2 = 10^6$; all other parameters equal to 0.

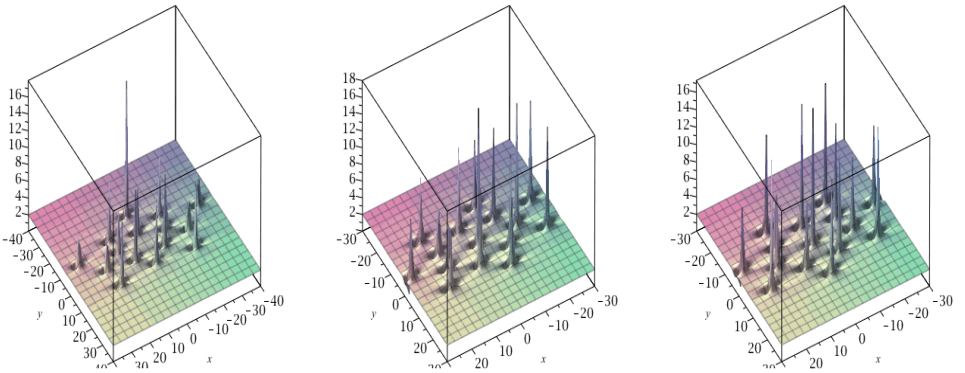


Figure 4. Solution of order 5 to KPI for $t = 0$, on the left for $b_2 = 10^6$; in the center for $a_3 = 10^8$; on the right for $b_3 = 10^8$; all other parameters equal to 0.

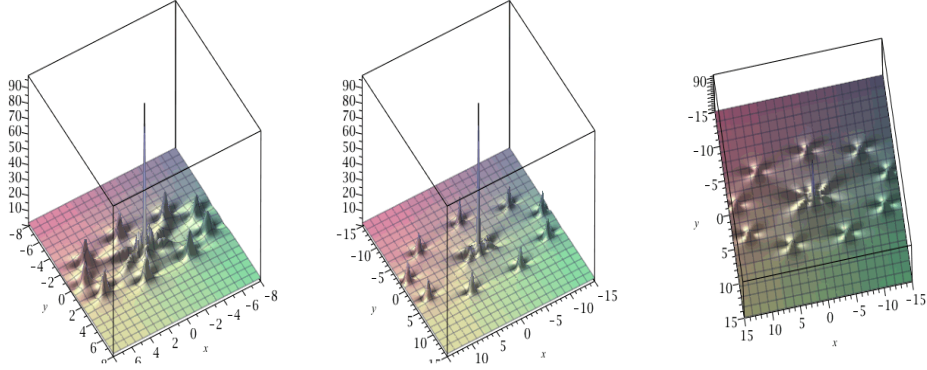


Figure 5. Solution of order 5 to KPI for $t = 0$, on the left for $a_4 = 10^8$; in the center for $b_4 = 10^8$; on the right for $b_4 = 10^8$, sight on top; all other parameters equal to 0.

4 Conclusion

We obtain N -th order rational solutions to the KPI equation depending on $2N - 2$ real parameters. These solutions can be expressed in terms of a ratio of two polynomials of degree $2N(N + 1)$ in x, y and t . The maximum modulus of these solutions is equal to $2(2N + 1)^2$. This gives a new approach to find explicit solutions for higher orders and try to describe the structure of these rational solutions. Here, we have given a complete description of rational solutions of order 5 with 8 parameters by giving explicit expressions of polynomials of those solutions.

We construct the modulus of solutions in the (x, y) plane of coordinates; different structures appear. For a given t , when one parameter grows and the other ones are equal to 0 we obtain triangular or rings or concentric rings. There are four types of patterns. For $a_1 \neq 0$ or $b_1 \neq 0$, and other parameters equal to zero, we obtain a triangle with 15 peaks. For $a_2 \neq 0$ or $b_2 \neq 0$, and other parameters equal to zero, we obtain three concentric rings of 5 peaks on each of them. For $a_3 \neq 0$ or $b_3 \neq 0$, and other parameters equal to zero, we obtain two concentric rings of 7 peaks on each of them with a central peak; in the last case, when $a_4 \neq 0$ or $b_4 \neq 0$, and other parameters equal to zero, we obtain one ring with 9 peaks with the lump L_3 in the center.

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Appendix : Because of the length of the complete expression, we only give in this appendix the explicit expression of the rational solution of order 5 to KPI equation without parameters. They can be written as

$$v(x, y, t) = -2 \frac{|n(x, y, t)|^2}{(d(x, y, t))^2}$$

with

$$\frac{n(x, y, t)}{d(x, y, t)} = \frac{F(2x, 4y, 4t) - iH(2x, 4y, 4t)}{Q(2x, 4y, 4t)}$$

with

$$\begin{aligned} F(X, Y, T) &= \sum_{k=0}^{30} f_k(Y, T) X^k, \\ H(X, Y, T) &= \sum_{k=0}^{30} h_k(Y, T) X^k, \\ Q(X, Y, T) &= \sum_{k=0}^{30} q_k(Y, T) X^k. \end{aligned}$$

$$\begin{aligned} f_{30} &= 1, \quad f_{29} = -90 T, \quad f_{28} = 3915 T^2 + 15 Y^2 - 45, \quad f_{27} = -109620 T^3 + (-1260 Y^2 + 5460) T, \quad f_{26} = \\ &2219805 T^4 + 105 Y^4 + (51030 Y^2 - 289170) T^2 - 3150 Y^2 - 1575, \quad f_{25} = -34628958 T^5 + (-1326780 Y^2 + 9287460) T^3 + \\ &(-8190 Y^4 + 260820 Y^2 + 77490) T, \quad f_{24} = 432861975 T^6 + 455 Y^6 + (24877125 Y^2 - 207309375) T^4 - 35175 Y^4 + \\ &(307125 Y^4 - 10347750 Y^2 - 297675) T^2 + 67725 Y^2 - 80325, \quad f_{23} = -4452294600 T^7 + (-358230600 Y^2 + 3462895800) T^5 + \\ &(-7371000 Y^4 + 261954000 Y^2 - 77225400) T^3 + (-32760 Y^6 + 2583000 Y^4 - 6388200 Y^2 + 5027400) T, \quad f_{22} = \\ &38401040925 T^8 + 1365 Y^8 + (4119651900 Y^2 - 45316170900) T^6 - 192780 Y^6 + (127149750 Y^4 - 4753444500 Y^2 + \\ &3163094550) T^4 + 1943550 Y^4 + (1130220 Y^6 - 90852300 Y^4 + 279814500 Y^2 - 169136100) T^2 + 1379700 Y^2 - 3472875, \quad f_{21} = \\ &-281607633450 T^9 + (-38842432200 Y^2 + 479056663800) T^7 + (-1678376700 Y^4 + 65844009000 Y^2 - 70879139100) T^5 + \\ &(-24864840 Y^6 + 2037004200 Y^4 - 7622861400 Y^2 + 4308406200) T^3 + (-90090 Y^8 + 12760440 Y^6 - 133364700 Y^4 - \\ &72160200 Y^2 + 211519350) T, \quad f_{20} = 1774128090735 T^{10} + 3003 Y^{10} + (305884153575 Y^2 - 4180416765525) T^8 - \\ &654885 Y^8 + (-17622955350 Y^4 - 723896781300 Y^2 + 1102112515350) T^6 + 14442750 Y^6 + (391621230 Y^6 - 32685310350 Y^4 + \\ &145679168250 Y^2 - 91054615050) T^4 - 6284250 Y^4 + (2837835 Y^8 - 403118100 Y^6 + 4390970850 Y^4 + 788640300 Y^2 - \\ &6550139925) T^2 + 55466775 Y^2 - 59634225, \quad f_{19} = -9677062313100 T^{11} + (-2039227690500 Y^2 + 30588415357500) T^9 + \\ &(-151053903000 Y^4 + 6483698298000 Y^2 - 12960424877400) T^7 + (-4699454760 Y^6 + 399453654600 Y^4 - 2085756334200 Y^2 + \\ &1576774949400) T^5 + (-56756700 Y^8 + 8085646800 Y^6 - 92211777000 Y^4 + 31696434000 Y^2 + 137638966500) T^3 + \\ &(-180180 Y^{10} + 39015900 Y^8 - 847513800 Y^6 + 752787000 Y^4 - 3105742500 Y^2 + 2173027500) T, \quad f_{18} = 45966045987225 T^{12} + \\ &5005 Y^{12} + (11623597835850 Y^2 - 189852097985550) T^{10} - 1522290 Y^{10} + (1076259058875 Y^4 - 48183290174250 Y^2 + \\ &120557572425675) T^8 + 53961075 Y^8 + (44644820220 Y^6 - 3863494057500 Y^4 + 23308627626900 Y^2 - 21898019625300) T^6 - \\ &248327100 Y^6 + (808782975 Y^8 - 115552275300 Y^6 + 1385054984250 Y^4 - 1381491814500 Y^2 - 21521292262625) T^4 + \\ &279979875 Y^4 + (5135130 Y^{10} - 1104052950 Y^8 + 23701500900 Y^6 - 36565735500 Y^4 + 80147009250 Y^2 - 24936234750) T^2 + \\ &3162300750 Y^2 + 3524968125, \quad f_{17} = -190935883331550 T^{13} + (-57061298466900 Y^2 + 1008082939581900) T^{11} + \\ &(-645755433250 Y^4 + 301021379851500 Y^2 - 911707327688850) T^9 + (-344402898840 Y^6 + 30333947628600 Y^4 - \\ &208974233853000 Y^2 + 243008235124200) T^7 + (-8734856130 Y^8 + 1251548103960 Y^6 - 15817012325100 Y^4 + 27698656368600 Y^2 + \\ &25683997326750) T^5 + (-92432340 Y^{10} + 19730749500 Y^8 - 420105155400 Y^6 + 1008423675000 Y^4 - 1224986206500 Y^2 - \\ &146950240500) T^3 + (-270270 Y^{12} + 81039420 Y^{10} - 2740396050 Y^8 + 13812913800 Y^6 - 18309989250 Y^4 - 192268282500 Y^2 - \\ &310728048750) T, \quad f_{16} = 695552146422075 T^{14} + 6435 Y^{14} + (242510518484325 Y^2 - 4607699851202175) T^{12} - \\ &2546775 Y^{12} + (32933527201575 Y^4 - 1596009395153250 Y^2 + 5707633598857575) T^{10} + 120860775 Y^{10} + (2195568480105 Y^6 - \\ &196756713794025 Y^4 + 1532235106692675 Y^2 - 2171399870551275) T^8 - 1303717275 Y^8 + (74246277105 Y^8 - 10668618894780 Y^6 + \\ &142516507710150 Y^4 - 367316581823100 Y^2 - 233903236078575) T^6 + 2575186425 Y^6 + (1178512335 Y^{10} - 249753960225 Y^8 + \\ &5293914711750 Y^6 - 18307533431250 Y^4 + 11947241194875 Y^2 + 7339410799875) T^4 + 23261812875 Y^4 + (6891885 Y^{12} - \\ &2036817090 Y^{10} + 65683505475 Y^8 - 379658267100 Y^6 + 296991835875 Y^4 + 5306024130750 Y^2 + 11990293930125) T^2 + \\ &134851240125 Y^2 + 46414974375, \quad f_{15} = -2225766868550640 T^{15} + (-895423452865200 Y^2 + 18206943541592400) T^{13} + \\ &(-143709936879600 Y^4 + 7229715286096800 Y^2 - 29946939923602800) T^{11} + (-11709698560560 Y^6 + 1067384061097200 Y^4 - \\ &9313909900218000 Y^2 + 15794795481771600) T^9 + (-509117328720 Y^8 + 73365112497600 Y^6 - 1037922900991200 Y^4 + \\ &3582548274110400 Y^2 + 1598676194631600) T^7 + (-11313718416 Y^{10} + 2380232297520 Y^8 - 50421277418400 Y^6 + \\ &237401051580000 Y^4 - 73786397806800 Y^2 - 84105766054800) T^5 + (-110270160 Y^{12} + 32114063520 Y^{10} - 987433902000 Y^8 + \\ &6788816798400 Y^6 + 215286498000 Y^4 - 78733894428000 Y^2 - 281497554450000) T^3 + (-308880 Y^{14} + 119805840 Y^{12} - \\ &5246957520 Y^{10} + 58975938000 Y^8 - 11206868400 Y^6 - 1359946098000 Y^4 - 9136788822000 Y^2 - 1877852970000) T, \quad f_{14} = \\ &6259969317798675 T^{16} + 6435 Y^{16} + (2878146812781000 Y^2 - 62359847610255000) T^{14} - 3148200 Y^{14} + (538912263298500 Y^4 - \\ &28106347270491000 Y^2 + 132796272634647300) T^{12} + 172386900 Y^{12} + (52693643522520 Y^6 - 4884295418818200 Y^4 + \\ &47389913750579400 Y^2 - 94499857473625800) T^{10} - 3227477400 Y^{10} + (2863784974050 Y^8 - 413853643942200 Y^6 + \\ &6209473531495500 Y^4 - 27032928566931000 Y^2 - 7792736255214750) T^8 + 514127250 Y^8 + (84852888120 Y^{10} - \\ &17721199326600 Y^8 + 376649696833200 Y^6 - 2311896626298000 Y^4 + 251203467375000 Y^2 + 281809220175000) T^6 + \\ &126059409000 Y^6 + (1240539300 Y^{12} - 355939353000 Y^{10} + 10435219105500 Y^8 - 87520569822000 Y^6 - 67443242422500 Y^4 + \\ &672149733255000 Y^2 + 4605837252502500) T^4 + 994204732500 Y^4 + (6949800 Y^{14} - 2640745800 Y^{12} + 106033422600 Y^{10} - \\ &1306648665000 Y^8 - 1706880357000 Y^6 + 26975963385000 Y^4 + 291783952215000 Y^2 + 16749041085000) T^2 - 1834094745000 Y^2 + \\ &637151011875, \quad f_{13} = -15465806549855550 T^{17} + (-8058811075786800 Y^2 + 185352654743096400) T^{15} + (-1741101158349000 Y^4 + \\ &94019462550846000 Y^2 - 500392472909502600) T^{13} + (-201193911631440 Y^6 + 18958657057578000 Y^4 - 20314865515416800 Y^2 + \end{aligned}$$

$$\begin{aligned}
& 468926485308615600)T^{11}+(-13364329878900Y^8+1936799807065200Y^6-30849172375707000Y^4+162452308078998000Y^2+ \\
& 22283040263431500)T^9+(-509117328720Y^{10}+105543938530800Y^8-2259793246989600Y^6+17468255271852000Y^4- \\
& 154281928122000Y^2+4048332872094000)T^7+(-10420530120Y^{12}+2945002127760Y^{10}-82343470519800Y^8+ \\
& 855034516274400Y^6+1085528791053000Y^4-3326543772678000Y^2-56897553479445000)T^5+(-97297200Y^{14}+ \\
& 36202042800Y^{12}-1322443810800Y^{10}+18861219846000Y^8+44878935654000Y^6-266559270390000Y^4-5703139488690000Y^2+ \\
& 555591931650000)T^3+(-270270Y^{16}+128898000Y^{14}-6205134600Y^{12}+124663114800Y^{10}+169775959500Y^8- \\
& 4380323346000Y^6-73132496325000Y^4+91524703410000Y^2-30811103898750)T, \quad f_{12}=33509247524687025T^{18}+ \\
& 5005Y^{18}+(19643351997230325Y^2-477988231932604575)T^{16}-2907135Y^{16}+(4850210369686500Y^4-270865594491723000Y^2+ \\
& 1607061242029817700)T^{14}+154998900Y^{14}+(653880212802180Y^6-62621604995285700Y^4+736599340057171500Y^2- \\
& 1941400968274485900)T^{12}-4780925100Y^{12}+(52120886527710Y^8-7574902175360520Y^6+128155418965091700Y^4- \\
& 791457484331896200Y^2+14857905645150750)T^{10}+4349031750Y^{10}+(2481946977510Y^{10}-510708320372250Y^8+ \\
& 11059633073771100Y^6-104656877241052500Y^4-759214678745250Y^2-69168108633419250)T^8+273006672750Y^8+ \\
& (67733445780Y^{12}-18850738987080Y^{10}+502940059958700Y^8-6508000174057200Y^6-9783511829500500Y^4+ \\
& 10591222025475000Y^2+556330537356772500)T^6+6770981038500Y^6+(948647700Y^{14}-345478032900Y^{12}+ \\
& 11375513194500Y^{10}-197767715008500Y^8-599706543082500Y^6+1461543260152500Y^4+78231597900907500Y^2- \\
& 20886946632877500)T^4-31511548057500Y^4+(5270265Y^{16}-2448646200Y^{14}+101467352700Y^{12}-2363397409800Y^{10}- \\
& 6042906686250Y^8+39456666459000Y^6+2170698639637500Y^4-1888506222435000Y^2+964379863085625)T^2- \\
& 14308470736875Y^2+3734295665625, \quad f_{11}=-63491205836249100Y^{19}+(-41597686582370100Y^2+1067673955614165900)T^{17}+ \\
& (-11640504887247600Y^4+671567589648900000Y^2-4402797117738188400)T^{15}+(-1810745204682960Y^6+176199437224918800Y^4- \\
& 2262916745511231600Y^2+6729704197250554800)T^{13}+(-170577446817960Y^8+24860569428545760Y^6-446869172856178800Y^4+ \\
& 3160406449274911200Y^2-586382417837634600)T^{11}+(-9927787910040Y^{10}+2027559761627400Y^8-44585706465846000Y^6+ \\
& 504372367396170000Y^4-25544526718347000Y^2+568325970663633000)T^9+(-348343435440Y^{12}+95446101310560Y^{10}- \\
& 2431982406344400Y^8+39240598074350400Y^6+59668270312014000Y^4-64094970017988000Y^2-4396907751782238000)T^7+ \\
& (-6830263440Y^{14}+2433500269200Y^{12}-71414066178000Y^{10}+1583926707963600Y^8+5365365599134800Y^6- \\
& 5225697746514000Y^4-804708355234518000Y^2+359955421399350000)T^5+(-63243180Y^{16}+28605376800Y^{14}- \\
& 991038661200Y^{12}+29272191026400Y^{10}+105160445019000Y^8+18931225068000Y^6-38676777367410000Y^4+ \\
& 25986159479700000Y^2-23206285086547500)T^3+(-180180Y^{18}+101496780Y^{16}-4315323600Y^{14}+162771865200Y^{12}+ \\
& 127031020200Y^{10}+2374196265000Y^8-396508029498000Y^6+1027745679870000Y^4+555612560527500Y^2- \\
& 1083072239232500)T, \quad f_{10}=104760489629811015T^{20}+3003Y^{20}+(76262425401011850Y^2-2059085485827319950)T^{18}- \\
& 2002770Y^{18}+(24008541329948175Y^4-1429431614567683650Y^2+10277502500089353375)T^{16}+76294575Y^{16}+ \\
& (4268185125324120Y^6-421893683541653400Y^4+5887311873952509000Y^2-19554121103579584200)T^{14}-4912147800Y^{14}+ \\
& (469087978749390Y^8-68559012278757000Y^6+1309280314393314900Y^4-10406077143129649800Y^2+3813470318931641550)T^{12}+ \\
& 10569248550Y^{12}+(32761700103132Y^{10}-6640544597827140Y^8+148854719734320600Y^6-1972596191699133000Y^4+ \\
& 349700116875209100Y^2-3142605331140174900)T^{10}-778433222700Y^{10}+(1436916671190Y^{12}-387525373014780Y^{10}+ \\
& 9441816308174250Y^8-189331951094886600Y^6-264230420830125750Y^4+761494344545434500Y^2+28178363040208053750)T^8+ \\
& 29737937895700Y^8+(37566448920Y^{14}-13087572858360Y^{12}+337516679780280Y^{10}-9923087725551000Y^8- \\
& 35846481921881400Y^6+32017478404527000Y^4+6364416585166353000Y^2-4071513439400085000)T^6-135471713895000Y^6+ \\
& (521756235Y^{16}-229572743400Y^{14}+6371415458100Y^{12}-263085719866200Y^{10}-1227127207146750Y^8-1167921778023000Y^6+ \\
& 472820855487592500Y^4-292139535659265000Y^2+383042109162076875)T^4-23856827990625Y^4+(2972970Y^{18}- \\
& 1622555550Y^{16}+51004031400Y^{14}-2744365843800Y^{12}-8143986734100Y^{10}-59552425894500Y^8+10890025690005000Y^6- \\
& 16281791651475000Y^4+5641166277416250Y^2+2522586344591250)T^2-204740671511250Y^2-63331122763125, \quad f_9= \\
& -149657423282301450T^{21}+(-120414355896334500Y^2+3411740083729477500)T^{19}+(-42368014111673250Y^4+ \\
& 260074425085019500Y^2-20373800262901088850)T^{17}+(-8536370250648240Y^6+856920244391996400Y^4-12936026897725654800Y^2+ \\
& 47562129682931883600)T^{15}+(-1082510720190900Y^8+158657212220799600Y^6-3218236241082219000Y^4+28310759035056918000Y^2- \\
& 15953699953418944500)T^{13}+(-8935009190360Y^{10}+17973114497137800Y^8-412234968449631600Y^6+6288034865280714000Y^4- \\
& 2325448127608515000Y^2+12728001398238945000)T^{11}+(-4789722237300Y^{12}+1271118593745000Y^{10}-29663935917115500Y^8+ \\
& 734900500396062000Y^6+883414271111872500Y^4-6205097669625855000Y^2-145655230334535652500)T^9+(-160999066800Y^{14}+ \\
& 54818118154800Y^{12}-1220092585311600Y^{10}+49143679775190000Y^8+189465765082902000Y^6-361052590485510000Y^4- \\
& 38986019618668290000Y^2+33253517753746290000)T^7+(-3130537410Y^{16}+1338906769200Y^{14}-27787844561400Y^{12}+ \\
& 1791675928904400Y^{10}+10571571242536500Y^8-17219590507854000Y^6-4161285095799195000Y^4+2862772152501870000Y^2- \\
& 433922455567221250)T^5+(-29729700Y^{18}+15704142300Y^{16}-314729226000Y^{14}+30112212942000Y^{12}+167721545565000Y^{10}- \\
& 1331258146155000Y^8-168618461812290000Y^6+158010162826950000Y^4-352799273171362500Y^2-91536114929962500)T^3+ \\
& (-90900Y^{20}+57957900Y^{18}-1242004050Y^{16}+152830314000Y^{14}+306119047500Y^{12}-5426555715000Y^{10}- \\
& 1791315007492500Y^8+4317208982730000Y^6-5739858578081250Y^4+8229374956687500Y^2+5060540265243750)T, \quad f_8= \\
& 183670988312006325T^{22}+1365Y^{22}+(162559380460051575Y^2-4822594953648196725)T^{20}-1015245Y^{20}+(63552021167509875Y^4- \\
& 4018443184591778250Y^2+34103970005290953075)T^{18}+2616075Y^{18}+(14405124797968905Y^6-1468214642869907625Y^4+ \\
& 23881914341060789475Y^2-96452734419336804075)T^{16}-4022822475Y^{16}+(2087699246082450Y^8-306838258424220600Y^6+ \\
& 6607981760554723500Y^4-63539929515767859000Y^2+49429683591988439250)T^{14}-5861220750Y^{14}+(201037705178310Y^{10}- \\
& 40130218841362650Y^8+945166525132038300Y^6-16341863250259228500Y^4+10243591309068594750Y^2-38957437995734963250)T^{12}+ \\
& 1761072090750Y^{12}+(12932250040710Y^{12}-3376312049089980Y^{10}+75636187443466650Y^8-2297665683104992200Y^6- \\
& 2304620451411027750Y^4+32742056045465266500Y^2+602488380962193783750)T^{10}+130537527513750Y^{10}+(543371850450Y^{14}- \\
& 180719904415050Y^{12}+3388868371939050Y^{10}-193007004877937250Y^8-813754102024190250Y^6+2944593571367621250Y^4+ \\
& 185347862407670208750Y^2-202936083764085393750)T^8-431140458813750Y^8+(14087418345Y^{16}-5851696851000Y^{14}+ \\
& 79805111255100Y^{12}-9394441030081800Y^{10}-68866767670538250Y^8+365522698600731000Y^6+2681402843043037500Y^4- \\
& 23211354865736835000Y^2+35197258821974195625)T^6+1390602477875625Y^6+(200675475Y^{18}-102483421425Y^{16}+ \\
& 851142127500Y^{14}-235019050276500Y^{12}-1960332535743750Y^{10}+36855573304331250Y^8+1660250864118577500Y^6- \\
& 1093880295215662500Y^4+5730126462068596875Y^2+1664565183339384375)T^4-1369009669190625Y^4+(1216215Y^{20}- \\
& 753741450Y^{18}+3105643275Y^{16}-2329361307000Y^{14}-14170065257250Y^{12}+940014064426500Y^{10}+35306326654278750Y^8- \\
& 50769104047515000Y^6+182477750149996875Y^4+7818096088293750Y^2-161040741062315625)T^2-2793189864740625Y^2- \\
& 238805043159375, \quad f_7=-191656683456006600T^{23}+(-185782149097201800Y^2+5759246622013255800)T^{21}+ \\
& (-80276237264223000Y^4+5224130517348666000Y^2-47791531590979037400)T^{19}+(-20336646773603160Y^6+ \\
& 2104060762345865400Y^4-36743695663109589000Y^2+161912201196809485800)T^{17}+(-3340318793731920Y^8+ \\
& 492311600676181440Y^6-11249866673071538400Y^4+117015338352785342400Y^2-118242767200367250000)T^{15}+
\end{aligned}$$

$$\begin{aligned}
& (-371146532636880 \text{ Y}^{10} + 73515563195382000 \text{ Y}^8 - 1784012727950560800 \text{ Y}^6 + 34493006842823340000 \text{ Y}^4 - 32688673408969578000 \text{ Y}^2 + \\
& 90915810640175934000) T^{13} + (-28215818270640 \text{ Y}^{12} + 7244953952876640 \text{ Y}^{10} - 156233516018907600 \text{ Y}^8 + 5769638535075105600 \text{ Y}^6 + \\
& 4895310703067694000 \text{ Y}^4 - 118967166461166660000 \text{ Y}^2 - 1976853696293476350000) T^{11} + (-1448991601200 \text{ Y}^{14} + \\
& 470476426820400 \text{ Y}^{12} - 7186947677910000 \text{ Y}^{10} + 599954617828566000 \text{ Y}^8 + 2849524975357830000 \text{ Y}^6 - 15866381004309990000 \text{ Y}^4 - \\
& 684128664698307570000 \text{ Y}^2 + 934330994134752690000) T^9 + (-48299720040 \text{ Y}^{16} + 19468502539200 \text{ Y}^{14} - 124483369903200 \text{ Y}^{12} + \\
& 38041341374836800 \text{ Y}^{10} + 339317905030650000 \text{ Y}^8 - 2975582608095384000 \text{ Y}^6 - 127129767271674300000 \text{ Y}^4 + 144536916402731160000 \text{ Y}^2 - \\
& 212479198864683345000) T^7 + (-963242280 \text{ Y}^{18} + 475026635160 \text{ Y}^{16} + 1809927957600 \text{ Y}^{14} + 1345071311589600 \text{ Y}^{12} + \\
& 14860180688850000 \text{ Y}^{10} - 377717578057134000 \text{ Y}^8 - 11029222691122356000 \text{ Y}^6 + 5603684559677820000 \text{ Y}^4 - 54232776209234385000 \text{ Y}^2 - \\
& 16072983246623625000) T^5 + (-9729720 \text{ Y}^{20} + 5800410000 \text{ Y}^{18} + 80679450600 \text{ Y}^{16} + 22254237432000 \text{ Y}^{14} + 214409229930000 \text{ Y}^{12} - \\
& 16734210725988000 \text{ Y}^{10} - 390822849099270000 \text{ Y}^8 + 179200373337720000 \text{ Y}^6 - 2869928051307975000 \text{ Y}^4 - 106026755533350000 \text{ Y}^2 + \\
& 2897203290589125000) T^3 + (-32760 \text{ Y}^{22} + 23367960 \text{ Y}^{20} + 522358200 \text{ Y}^{18} + 113507389800 \text{ Y}^{16} + 531763218000 \text{ Y}^{14} - \\
& 181511617770000 \text{ Y}^{12} - 3865904153370000 \text{ Y}^{10} + 9039489461730000 \text{ Y}^8 - 41811925414455000 \text{ Y}^6 - 17819468180325000 \text{ Y}^4 + \\
& 164388505479975000 \text{ Y}^2 + 9905630658525000) T, \quad f_6 = 167699598024005775 \text{ T}^{24} + 455 \text{ Y}^{24} + (177337505956419900 \text{ Y}^2 - \\
& 5733912692590910100) T^{22} - 367500 \text{ Y}^{22} + (84290049127434150 \text{ Y}^4 - 5640949441605208500 \text{ Y}^2 + 55378562276724236550) T^{20} - \\
& 22777650 \text{ Y}^{20} + (23726087902537020 \text{ Y}^6 - 2491239229766387100 \text{ Y}^4 + 46552726954320671700 \text{ Y}^2 - 222491371271617142100) T^{18} - \\
& 2774727900 \text{ Y}^{18} + (4384168416773145 \text{ Y}^8 - 647957609084113020 \text{ Y}^6 + 15699921710107411350 \text{ Y}^4 - 175104912906735291900 \text{ Y}^2 + \\
& 22093440678860676825) T^{16} + 2741884425 \text{ Y}^{16} + (556719798955320 \text{ Y}^{10} - 109416852794680200 \text{ Y}^8 + 2744445562712910000 \text{ Y}^6 - \\
& 58628533584322170000 \text{ Y}^4 + 78109850377068111000 \text{ Y}^2 - 160785221648838129000) T^{14} + 12029439681000 \text{ Y}^{14} + \\
& (49377681973620 \text{ Y}^{12} - 12465965556724680 \text{ Y}^{10} + 259656024110546700 \text{ Y}^8 - 11548527684010153200 \text{ Y}^6 - 8969736739415224500 \text{ Y}^4 + \\
& 307582771031041779000 \text{ Y}^2 + 5091163088122196536500) T^{12} + 180117230674500 \text{ Y}^{12} + (3042882362520 \text{ Y}^{14} - 963969527921400 \text{ Y}^{12} + \\
& 11404531584646200 \text{ Y}^{10} - 1466075511095995800 \text{ Y}^8 - 8031257324623625400 \text{ Y}^6 + 59427427516614927000 \text{ Y}^4 + 1956173568816684609000 \text{ Y}^2 - \\
& 3237015906581602005000) T^{10} - 691866296415000 \text{ Y}^{10} + (126786765105 \text{ Y}^{16} - 49544366671800 \text{ Y}^{14} - 49023761163300 \text{ Y}^{12} - \\
& 118455939366395400 \text{ Y}^{10} - 1256885611874660250 \text{ Y}^8 + 14547881692924587000 \text{ Y}^6 + 442484820445624897500 \text{ Y}^4 - \\
& 662105241219550275000 \text{ Y}^2 + 991786871544567800625) T^8 + 3819394004855625 \text{ Y}^8 + (3371347980 \text{ Y}^{18} - 1603464966180 \text{ Y}^{16} - \\
& 26211512552400 \text{ Y}^{14} - 5687867018005200 \text{ Y}^{12} - 77114001357250200 \text{ Y}^{10} + 2226307185829125000 \text{ Y}^8 + 50452701643543878000 \text{ Y}^6 - \\
& 21597257598738570000 \text{ Y}^4 + 344750475679982347500 \text{ Y}^2 + 89458449857973157500) T^6 + 1738851217582500 \text{ Y}^6 + (-51081030 \text{ Y}^{20} - \\
& 29247164100 \text{ Y}^{18} - 957796103250 \text{ Y}^{16} - 143403454782000 \text{ Y}^{14} - 1804603410004500 \text{ Y}^{12} + 141393400712865000 \text{ Y}^{10} + \\
& 2687606958260227500 \text{ Y}^8 + 1602267217116930000 \text{ Y}^6 + 30267088175830668750 \text{ Y}^4 + 2960382087845437500 \text{ Y}^2 - 38573736160241756250) T^4 - \\
& 28527529354931250 \text{ Y}^4 + (343980 \text{ Y}^{22} - 234885420 \text{ Y}^{20} - 11408625900 \text{ Y}^{18} - 1475828594100 \text{ Y}^{16} - 10174662477000 \text{ Y}^{14} + \\
& 312554024117000 \text{ Y}^{12} + 52333674631497000 \text{ Y}^{10} + 5584345909695000 \text{ Y}^8 + 619464673093297500 \text{ Y}^6 + 580375157372602500 \text{ Y}^4 - \\
& 3199464776942437500 \text{ Y}^2 - 182546296628062500) T^2 + 7090604658112500 \text{ Y}^{10} - 657932261765625, \quad f_5 = -120743710577284158 \text{ T}^{25} + \\
& (-138785874226763400 \text{ Y}^2 + 4672457765634367800) T^{23} + (-72248613537800700 \text{ Y}^4 + 4968481577137986600 \text{ Y}^2 - \\
& 52135711046008335900) T^{21} + (-22477346433982440 \text{ Y}^6 + 2394701908543513800 \text{ Y}^4 - 47738049897122739000 \text{ Y}^2 + \\
& 246162924975055397400) T^{19} + (-4642060676583330 \text{ Y}^8 + 687977197709016600 \text{ Y}^6 - 17661363672989616300 \text{ Y}^4 + \\
& 209647795700357040600 \text{ Y}^2 - 321181333519747046850) T^{17} + (-668063758746384 \text{ Y}^{10} + 13027243295544880 \text{ Y}^8 - \\
& 3387196362964528800 \text{ Y}^6 + 79098408897601212000 \text{ Y}^4 - 14086036377728645200 \text{ Y}^2 + 210856359003914962800) T^{15} + \\
& (-68369098117320 \text{ Y}^{12} + 16966054655882640 \text{ Y}^{10} - 342740532358539000 \text{ Y}^8 + 18177745004307352800 \text{ Y}^6 + 14842070845589421000 \text{ Y}^4 - \\
& 569489614737813126000 \text{ Y}^2 - 10142770076294410485000) T^{13} + (-4979262047760 \text{ Y}^{14} + 1538081279214480 \text{ Y}^{12} - \\
& 12949342798850640 \text{ Y}^{10} + 2780861271150690000 \text{ Y}^8 + 17812705237030645200 \text{ Y}^6 - 159450676712156466000 \text{ Y}^4 - \\
& 430264693644744774000 \text{ Y}^2 + 8346629184301336950000) T^{11} + (-253573530210 \text{ Y}^{16} + 95967828356400 \text{ Y}^{14} + 818263640363400 \text{ Y}^{12} + \\
& 280619265548437200 \text{ Y}^{10} + 3465581754780400500 \text{ Y}^8 - 47584063798999182000 \text{ Y}^6 - 1118854182590227755000 \text{ Y}^4 + \\
& 2186430295925466990000 \text{ Y}^2 - 3701205029344402361250) T^9 + (-8669180520 \text{ Y}^{18} + 3971151538200 \text{ Y}^{16} + 116565702069600 \text{ Y}^{14} + \\
& 17700494810392800 \text{ Y}^{12} + 280122977063739600 \text{ Y}^{10} - 8449461440097678000 \text{ Y}^8 - 158051371427710740000 \text{ Y}^6 + 76006967649032700000 \text{ Y}^4 - \\
& 1514194952657202585000 \text{ Y}^2 - 273332542172828985000) T^7 + (-183891708 \text{ Y}^{20} + 100951832520 \text{ Y}^{18} + 5300099802900 \text{ Y}^{16} + \\
& 638219705608800 \text{ Y}^{14} + 9613186089280200 \text{ Y}^{12} - 699729345490366800 \text{ Y}^{10} - 11625910325562267000 \text{ Y}^8 - 17944275064608900000 \text{ Y}^6 - \\
& 211596760291789687500 \text{ Y}^4 + 64063514905717005000 \text{ Y}^2 + 371515557850873222500) T^5 + (-2063880 \text{ Y}^{22} + 13464443560 \text{ Y}^{20} + \\
& 102674061000 \text{ Y}^{18} + 11169530429400 \text{ Y}^{16} + 99476912430000 \text{ Y}^{14} - 24489513663174000 \text{ Y}^{12} - 370612284513030000 \text{ Y}^{10} - \\
& 179798315980690000 \text{ Y}^8 - 810068081548665000 \text{ Y}^6 - 3386487671262675000 \text{ Y}^4 + 38736361360845225000 \text{ Y}^2 + 149641708603275000) T^3 + \\
& (-8190 \text{ Y}^{24} + 6302520 \text{ Y}^{22} + 622312740 \text{ Y}^{20} + 63669375000 \text{ Y}^{18} - 191237731650 \text{ Y}^{16} - 264197445498000 \text{ Y}^{14} - \\
& 3470195024037000 \text{ Y}^{12} - 4050198794250000 \text{ Y}^{10} - 46635445503281250 \text{ Y}^8 - 180897316052985000 \text{ Y}^6 + 1010351794809262500 \text{ Y}^4 + \\
& 199320246412875000 \text{ Y}^2 + 31960887204881250) T, \quad f_4 = 69659833025356245 \text{ T}^{26} + 105 \text{ Y}^{26} + (86741171391727125 \text{ Y}^2 - \\
& 3035940998710449375) T^{24} - 89775 \text{ Y}^{24} + (49260418321227750 \text{ Y}^4 - 3478543386068236500 \text{ Y}^2 + 38875564286523382950) T^{22} - \\
& 15066450 \text{ Y}^{22} + (16858009825486830 \text{ Y}^6 - 1821961831139153550 \text{ Y}^4 + 38638389376104521850 \text{ Y}^2 - 213963126721627005450) T^{20} - \\
& 1443591450 \text{ Y}^{20} + (3868383897152775 \text{ Y}^8 - 574901360715320100 \text{ Y}^6 + 15623131133724770250 \text{ Y}^4 - 196120571193091030500 \text{ Y}^2 + \\
& 357249431667880686375) T^{18} + 29933701875 \text{ Y}^{18} + (626309773824735 \text{ Y}^{10} - 121166852397631425 \text{ Y}^8 + 3274507475098237350 \text{ Y}^6 - \\
& 82793038504310615250 \text{ Y}^4 + 189905365358715076875 \text{ Y}^2 - 195946731212768668125) T^{16} + 8926947259875 \text{ Y}^{16} + \\
& (73252605125700 \text{ Y}^{12} - 17862366019113000 \text{ Y}^{10} + 351660264940309500 \text{ Y}^8 - 22010761791057438000 \text{ Y}^6 - 21773327176901002500 \text{ Y}^4 + \\
& 742227813403943895000 \text{ Y}^2 + 1529351660866935122500) T^{14} + 85757994472500 \text{ Y}^{14} + (6224077559700 \text{ Y}^{14} - 1873447345469700 \text{ Y}^{12} + \\
& 9448889660928900 \text{ Y}^{10} - 4009065097300672500 \text{ Y}^8 - 30172397289852730500 \text{ Y}^6 + 308113279210457752500 \text{ Y}^4 + 7168953774050770747500 \text{ Y}^2 - \\
& 15694552290887321197500) T^{12} + 319944513262500 \text{ Y}^{12} + (380360295315 \text{ Y}^{16} - 139270385053800 \text{ Y}^{14} - 2260665993177900 \text{ Y}^{12} - \\
& 496161030190656600 \text{ Y}^{10} - 6994012096222404750 \text{ Y}^8 + 107623962307517481000 \text{ Y}^6 + 2009636371279438492500 \text{ Y}^4 - \\
& 5120794944397939905000 \text{ Y}^2 + 11081845031052259681875) T^{10} + 365571370749375 \text{ Y}^{10} + (16254713475 \text{ Y}^{18} - 7160826467025 \text{ Y}^{16} - \\
& 307093801864500 \text{ Y}^{14} - 39967614231268500 \text{ Y}^{12} - 713578985267163750 \text{ Y}^{10} + 21439681349659571250 \text{ Y}^8 + 328428652686529657500 \text{ Y}^6 - \\
& 302425492990139662500 \text{ Y}^4 + 4589978754971499946875 \text{ Y}^2 + 33495176188398684375) T^8 + 19359580323234375 \text{ Y}^8 + \\
& (459729270 \text{ Y}^{20} - 241534685700 \text{ Y}^{18} - 17702357774850 \text{ Y}^{16} - 1963962798462000 \text{ Y}^{14} - 33839582520712500 \text{ Y}^{12} + \\
& 2177101101824145000 \text{ Y}^{10} + 30937958801113927500 \text{ Y}^8 + 65969037255332610000 \text{ Y}^6 + 946142428337667618750 \text{ Y}^4 - \\
& 627474771193059562500 \text{ Y}^2 - 2418325907236753106250) T^6 - 127220617667981250 \text{ Y}^6 + (7739550 \text{ Y}^{22} - 4813404750 \text{ Y}^{20} - \\
& 508408062750 \text{ Y}^{18} - 52761176165250 \text{ Y}^{16} - 588223154452500 \text{ Y}^{14} + 106976379654112500 \text{ Y}^{12} + 1431965678320642500 \text{ Y}^{10} + \\
& 6194409170655037500 \text{ Y}^8 + 64890913800283593750 \text{ Y}^6 + 7417055730315656250 \text{ Y}^4 - 310077666558050343750 \text{ Y}^2 + \\
& 19292129027586843750) T^4 + 10894649371593750 \text{ Y}^4 + (61425 \text{ Y}^{24} - 44925300 \text{ Y}^{22} - 6196204350 \text{ Y}^{20} - 614363494500 \text{ Y}^{18} + \\
& 1065570825375 \text{ Y}^{16} + 2121232109535000 \text{ Y}^{14} + 23860970644297500 \text{ Y}^{12} + 126079014649455000 \text{ Y}^{10} + 1407637708803309375 \text{ Y}^8 - \\
& 316440163943662500 \text{ Y}^6 - 16028909063797218750 \text{ Y}^4 - 4227753090058312500 \text{ Y}^2 - 1561951126772859375) T^2 + 10892434111453125 \text{ Y}^2 + \\
& 1535175277453125, \quad f_3 = -30959925789047220 \text{ T}^{27} + (-41635762268029020 \text{ Y}^2 + 1512766029071721060) T^{25} + \\
& (-25701087819771000 \text{ Y}^4 + 1862340363555714000 \text{ Y}^2 - 22095422899332665400) T^{23} + (-9633148471706760 \text{ Y}^6 +
\end{aligned}$$

$$\begin{aligned}
& 1055941274783241000 Y^4 - 23760853390053826200 Y^2 + 140712313542676457400) T^{21} + (-2443189829780700 Y^8 + \\
& 364097930530395600 Y^6 - 10464540831065601000 Y^4 + 138155721629108274000 Y^2 - 294359867429087785500) T^{19} + \\
& (-442101016817460 Y^{10} + 84849387458427900 Y^8 - 2389082761771057800 Y^6 + 64845921917944251000 Y^4 - 186210902122201498500 Y^2 + \\
& 117077571216873319500) T^{17} + (-58602084100560 Y^{12} + 14037453068395680 Y^{10} - 270815031813236400 Y^8 - 19789576350585451200 Y^6 + \\
& 25936973261357634000 Y^4 - 649563571356269724000 Y^2 - 16858754256969713970000) T^{15} + (-5745302362800 Y^{14} + \\
& 1683962854081200 Y^{12} - 2874539497561200 Y^{10} + 4244202773499654000 Y^8 + 37476966739910166000 Y^6 - 421123999512999510000 Y^4 - \\
& 8786607546930839010000 Y^2 + 20788580036720938050000) T^{13} + (-414938503980 Y^{16} + 146824393716000 Y^{14} + \\
& 3542054052423600 Y^{12} + 633781570796287200 Y^{10} + 10027268435092923000 Y^8 - 167571317769213204000 Y^6 - 2458232115957875250000 Y^4 + \\
& 8288597117115905940000 Y^2 - 25407633512804927107500) T^{11} + (-21672951300 Y^{18} + 9167658399900 Y^{16} + 522635022630000 Y^{14} + \\
& 63648520172622000 Y^{12} + 1251393053566005000 Y^{10} - 36334383832878075000 Y^8 - 418359328797601170000 Y^6 + \\
& 1071010025700668550000 Y^4 - 9609075229368178462500 Y^2 + 4246721613336016237500) T^9 + (-788107320 Y^{20} + \\
& 395468211600 Y^{18} + 37673982397800 Y^{16} + 4103258165496000 Y^{14} + 78830865202698000 Y^{12} - 4315639912514532000 Y^{10} - \\
& 46808508310830630000 Y^8 - 85923371067455880000 Y^6 - 2746631166706905975000 Y^4 + 2627031222775042650000 Y^2 + \\
& 9986434964897937525000) T^7 + (-18574920 Y^{22} + 10986350760 Y^{20} + 1504404203400 Y^{18} + 157772934307800 Y^{16} + \\
& 2172284241246000 Y^{14} - 276544515096486000 Y^{12} - 2944758032950230000 Y^{10} - 16825698104167890000 Y^8 - 295212321288129105000 Y^6 + \\
& 65408854321986525000 Y^4 + 1574988971214391425000 Y^2 - 175296125895916725000) T^5 + (-245700 Y^{24} + 170326800 Y^{22} + \\
& 30646236600 Y^{20} + 3135052242000 Y^{18} + 6699300898500 Y^{16} - 8509433044140000 Y^{14} - 73346269006710000 Y^{12} - \\
& 650106562060620000 Y^{10} - 13527750529689637500 Y^8 + 11273569520191650000 Y^6 + 150792066611179875000 Y^4 + \\
& 40071503964224250000 Y^2 + 18182137489964437500) T^3 + (-1260 Y^{26} + 1018500 Y^{24} + 226056600 Y^{22} + 22376957400 Y^{20} - \\
& 407753230500 Y^{18} - 88039851952500 Y^{16} - 182859728310000 Y^{14} - 5922475716150000 Y^{12} - 198206787746992500 Y^{10} + \\
& 773576520674737500 Y^8 + 4287672037077975000 Y^6 + 834834075555375000 Y^4 + 834364440405562500 Y^2 - 106146404898187500) T, \quad f_2 = \\
& 9951464717908035 T^{28} + 15 Y^{28} + (14412379246625430 Y^2 - 542866284956224530) T^{26} - 13230 Y^{26} + (963797932414125 Y^4 - \\
& 716170697131695750 Y^2 + 8993947407022208925) T^{24} - 4405275 Y^{24} + (3940833465698220 Y^6 - 438038796764148300 Y^4 + \\
& 10433653151449342500 Y^2 - 65830964042236976100) T^{22} - 460536300 Y^{22} + (1099435423401315 Y^8 - 16429511986791380 Y^6 + \\
& 4989309709418140050 Y^4 - 68945057216324169300 Y^2 + 169557352830226123875) T^{20} + 16520466375 Y^{20} + (221050508408730 Y^{10} - \\
& 42084616023969750 Y^8 + 1237262083239363300 Y^6 - 35775503385692647500 Y^4 + 125753073481149329250 Y^2 - 33677535139843722750) T^{18} + \\
& 1418063172750 Y^{18} + (32963672306565 Y^{12} - 7754069993344290 Y^{10} + 147508908045428475 Y^8 - 12444975573317387100 Y^6 - \\
& 22306597617171727125 Y^4 + 344149745922632238750 Y^2 + 12811748574445029523125) T^{16} - 39670880830875 Y^{16} + \\
& (3693408661800 Y^{14} - 1053379090902600 Y^{12} - 1672063783803000 Y^{10} - 3111035126418009000 Y^8 - 32066045650774485000 Y^6 + \\
& 387923615559565785000 Y^4 + 7499142630466614855000 Y^2 - 18261623152586447235000) T^{14} + 4392450625000 Y^{14} + \\
& (311203877985 Y^{16} - 106288093711800 Y^{14} - 3424946829689700 Y^{12} - 552475107518632200 Y^{10} - 9671533645353536250 Y^8 + \\
& 172535904226281771000 Y^6 + 1891686066598960537500 Y^4 - 8821204322605857315000 Y^2 + 40691659916841013670625) T^{12} + \\
& 14332963309363125 Y^{12} + (19505656170 Y^{18} - 7908793359390 Y^{16} - 5678497040454500 Y^{14} - 67763929988525400 Y^{12} - \\
& 14412086643182444500 Y^{10} + 39615837875226553500 Y^8 + 260307975087470709000 Y^6 - 2479776803701588755000 Y^4 + \\
& 13935492198905874896250 Y^2 - 20313398648831981568750) T^{10} - 101058662644931250 Y^{10} + (886620735 Y^{20} - 4239868582250 Y^{18} - \\
& 5028295894925 Y^{16} - 5558255148411000 Y^{14} - 117220242593711250 Y^{12} + 5275423483427506500 Y^{10} + 30130228135265028750 Y^8 - \\
& 688837783174033035000 Y^6 + 5388840945039804721875 Y^4 - 6733478711352833606250 Y^2 - 24979078901228656640625) T^8 - \\
& 488787845936315625 Y^8 + (27862380 Y^{22} - 15630795180 Y^{20} - 2665111661100 Y^{18} - 290608727742900 Y^{16} - 4877007740829000 Y^{14} + \\
& 417120212610045000 Y^{12} + 2717050823291385000 Y^{10} + 20775259590910335000 Y^8 + 795907087652851177500 Y^6 - \\
& 689772230620254337500 Y^4 - 4833976237453324237500 Y^2 - 149527346241567262500) T^6 - 18131461198987500 Y^6 + \\
& (552825 Y^{24} - 362142900 Y^{22} - 81570689550 Y^{20} - 8859278326500 Y^{18} - 68672144543625 Y^{16} + 18292823225775000 Y^{14} + \\
& 113892368365597500 Y^{12} + 1706493116652975000 Y^{10} + 57223959236099184375 Y^8 - 61149312544278262500 Y^6 - \\
& 547755603079956468750 Y^4 - 153618091694656312500 Y^2 - 79032956778642234375) T^4 - 168490471035796875 Y^4 + \\
& (5670 Y^{26} - 4318650 Y^{24} - 1211244300 Y^{22} - 129128636700 Y^{20} + 997668677250 Y^{18} + 361494850043250 Y^{16} + \\
& 648951801435000 Y^{14} + 35380036446615000 Y^{12} + 1686086368092866250 Y^{10} - 5320233692493693750 Y^8 - 34516558396379587500 Y^6 - \\
& 31566420262160437500 Y^4 - 4463452338500531250 Y^2 + 1770715027165218750) T^2 + 78513249904031250 Y^2 + 1096553769609375, \quad f_1 = \\
& -2058911320946490 Y^{29} + (-3202750943694540 Y^2 + 124907286804087060) T^{27} + (-2313097903779390 Y^4 + 176151301903199700 Y^2 - \\
& 233533929277268750) T^{25} + (-1028043512790840 Y^6 + 115852595864506200 Y^4 - 2914503358762031400 Y^2 + 19526104920057712200) T^{23} + \\
& (-314124406686090 Y^8 + 47070334171115640 Y^6 - 1508873522437820700 Y^4 + 21732708059947999800 Y^2 - 61018896649561108650) T^{21} + \\
& (-69805423708020 Y^{10} + 13182485784860700 Y^8 - 405432829795077000 Y^6 + 12403032565939155000 Y^4 - 52401552554380018500 Y^2 - \\
& 3313939268065828500) T^{19} + (-11634237284670 Y^{12} + 2686613871429180 Y^{10} - 50743580179266450 Y^8 + 4886535325113880200 Y^6 + \\
& 11938423096696650750 Y^4 - 84233411545016506500 Y^2 - 5998330265914954752750) T^{17} + (-1477363464720 Y^{14} + \\
& 409684253101200 Y^{12} + 1981165068615600 Y^{10} + 1410775990030990800 Y^8 + 16854596151636776400 Y^6 - 216669950191306962000 Y^4 - \\
& 3992081832562545414000 Y^2 + 9469197127526079510000) T^{15} + (-143632559070 Y^{16} + 47288257909200 Y^{14} + 1917625238638200 Y^{12} + \\
& 294132334756503600 Y^{10} + 5628878447506303500 Y^8 - 106272244110012498000 Y^6 - 775402029279596565000 Y^4 + \\
& 5562214627783561650000 Y^2 - 39495548583265682958750) T^{13} + (-10639448820 Y^{18} + 4127287723020 Y^{16} + 360516607239600 Y^{14} + \\
& 43293897822898800 Y^{12} + 982488954554893800 Y^{10} - 25199867496556935000 Y^8 + 5121959205834198000 Y^6 + 3146078548665549630000 Y^4 - \\
& 13395682909145770852500 Y^2 + 41738896972231619107500) T^{11} + (-591080490 Y^{20} + 268714284300 Y^{18} + 38559631776750 Y^{16} + \\
& 4406311608426000 Y^{14} + 100967205534583500 Y^{12} - 3596532612289155000 Y^{10} + 8283091141557067500 Y^8 + 285438227257592010000 Y^6 - \\
& 6993872293975995881250 Y^4 + 10615157859394072687500 Y^2 + 38511345961290620643750) T^9 + (-23882040 Y^{22} + \\
& 12670340760 Y^{20} + 2619244366200 Y^{18} + 301243524157800 Y^{16} + 6073941186306000 Y^{14} - 332810940481860000 Y^{12} - \\
& 206829380400426000 Y^{10} - 13973328095830110000 Y^8 - 1268595568954399455000 Y^6 + 1771986531631876875000 Y^4 + \\
& 789397030512158054390975000 Y^2 + 5350377830932756125000) T^7 + (-663390 Y^{24} + 409260600 Y^{22} + 112338972900 Y^{20} + \\
& 13119973234200 Y^{18} + 189523707688350 Y^{16} - 19704502964538000 Y^{14} - 116523993143061000 Y^{12} - 3469188882417930000 Y^{10} - \\
& 124676315436258101250 Y^8 + 111199783316007015000 Y^6 + 137325622498680262500 Y^4 + 142595022806606475000 Y^2 + \\
& 140023656053959781250) T^5 + (-11340 Y^{26} + 8108100 Y^{24} + 2791114200 Y^{22} + 326298634200 Y^{20} + 1723425133500 Y^{18} - \\
& 671297198008500 Y^{16} - 8083387605510000 Y^{14} - 209471375716470000 Y^{12} - 5861886454384852500 Y^{10} + 10596884905521337500 Y^8 + \\
& 46049392314741375000 Y^6 + 144099570783459375000 Y^4 + 5281401701264062500 Y^2 - 26910864994785187500) T^3 + \\
& (-90 Y^{28} + 74340 Y^{26} + 30740850 Y^{24} + 3486407400 Y^{22} - 29830408650 Y^{20} - 9945196726500 Y^{18} - 190468185216750 Y^{16} - \\
& 4379930772210000 Y^{14} - 101355116492778750 Y^{12} + 588804550073617500 Y^{10} + 2003467220102643750 Y^8 + 6215378415257025000 Y^6 + \\
& 487999665378281250 Y^4 - 993916336773937500 Y^2 - 80267735935406250) T, \quad f_0 = 205891132094649 T^{30} + Y^{30} + \\
& (343151886824415 Y^2 - 13840459435251405) T^{28} - 885 Y^{28} + (266895911974545 Y^4 - 20817881134014510 Y^2 + 290649648140279505) T^{26} - \\
& 518175 Y^{26} + (128505439098855 Y^6 - 14679275158599975 Y^4 + 389223204962878125 Y^2 - 2760445107350057925) T^{24} - \\
& 64415925 Y^{24} + (42835146366285 Y^8 - 6436255325805900 Y^6 + 217569593428138350 Y^4 - 3254350820009618700 Y^2 +
\end{aligned}$$

$$\begin{aligned}
& 10335412390763897325)T^{22} - 429932475 Y^{22} + (10470813556203 Y^{10} - 1961263923796485 Y^8 + 63206858568347550 Y^6 - \\
& 2033186697332012250 Y^4 + 10169816108260184775 Y^2 + 3786939964849193775)T^{20} + 253388798775 Y^{20} + (1939039547445 Y^{12} - \\
& 439416192828690 Y^{10} + 8301597810730875 Y^8 - 901916719268298300 Y^6 - 2948421838549249125 Y^4 + 552323211344304750 Y^2 + \\
& 1303979354257921543125)T^{18} + 18211006855125 Y^{18} + (277005649635 Y^{14} - 74628163095255 Y^{12} - 599597131108185 Y^{10} - \\
& 298215581578558875 Y^8 - 4097668234919365575 Y^6 + 55545795013687972875 Y^4 + 999721710985825792125 Y^2 - \\
& 216643502998858785625)T^{16} + 308449383834375 Y^{16} + (30778405515 Y^{16} - 9754386978600 Y^{14} - 479300845193100 Y^{12} - \\
& 72167245190875800 Y^{10} - 1494399523818930750 Y^8 + 29760739595699553000 Y^6 + 105539541330442432500 Y^4 - \\
& 1578199521254346585000 Y^2 + 17216540976307279516875)T^{14} + 3743615698711875 Y^{14} + (2659862205 Y^{18} - 985172039775 Y^{16} - \\
& 102226874733900 Y^{14} - 12556164497366700 Y^{12} - 300736687607530650 Y^{10} + 7125350615937240750 Y^8 - 68174890835981737500 Y^6 - \\
& 1658658093774662137500 Y^4 + 6582591430544280493125 Y^2 - 32665745021854435194375)T^{12} - 35436868535289375 Y^{12} + \\
& (177324147 Y^{20} - 76431254130 Y^{18} - 13010539271625 Y^{16} - 1553071592986200 Y^{14} - 38387575830955050 Y^{12} + \\
& 1029379891176119700 Y^{10} - 15748309000883198250 Y^8 - 203306916362197095000 Y^6 + 4550541140734269384375 Y^4 - \\
& 6956482828705269851250 Y^2 - 29626545040779349018125)T^{10} - 52818816039688125 Y^{10} + (8955765 Y^{22} - 4478571405 Y^{20} - \\
& 1102058551125 Y^{18} - 134629752192075 Y^{16} - 3214424357628750 Y^{14} + 103810562029770750 Y^{12} - 807910327029566250 Y^{10} + \\
& 9547733571385826250 Y^8 + 974556198963258935625 Y^6 - 1745591916197984990625 Y^4 - 6418557660215103440625 Y^2 - \\
& 11235442540726973559375)T^8 - 563834403599709375 Y^8 + (331695 Y^{24} - 191974860 Y^{22} - 63053637570 Y^{20} - \\
& 7958263729500 Y^{18} - 173242248242175 Y^{16} + 7843508909649000 Y^{14} + 85127427323158500 Y^{12} + 3648345623804385000 Y^{10} + \\
& 121688209685624990625 Y^8 - 59428033675926457500 Y^6 + 1884557279168523618750 Y^4 - 891729638488792687500 Y^2 + \\
& 1382422320605279559375)T^6 - 139776269093015625 Y^6 + (8505 Y^{26} - 5684175 Y^{24} - 2355289650 Y^{22} - 303985114650 Y^{20} - \\
& 5591003788125 Y^{18} + 432409451803875 Y^{16} + 15141752275072500 Y^{14} + 382740986155342500 Y^{12} + 8467495805148699375 Y^{10} - \\
& 5924076200578265625 Y^8 + 73786990917167718750 Y^6 - 306531770539276406250 Y^4 - 23337276008993296875 Y^2 - \\
& 173618454896021953125)T^4 + 269971538077828125 Y^4 + (135 Y^{28} - 103950 Y^{26} - 52071075 Y^{24} - 6714773100 Y^{22} - \\
& 90754459425 Y^{20} + 15220863960750 Y^{18} + 873166093120125 Y^{16} + 18866959714575000 Y^{14} + 311002510450708125 Y^{12} - \\
& 773569625941271250 Y^{10} - 1879021817045690625 Y^8 - 25514053093507387500 Y^6 - 23384115469046671875 Y^4 + \\
& 4485144165797531250 Y^2 + 20395900114734375)T^2 + 13377955989234375 Y^2 - 219310753921875. \\
& \mathbf{h}_{30} = 0, \quad \mathbf{h}_{29} = 0, \quad \mathbf{h}_{28} = 60 Y, \quad \mathbf{h}_{27} = -5040 T Y, \quad \mathbf{h}_{26} = 204120 T^2 Y + 840 Y^3 - 2520 Y, \quad \mathbf{h}_{25} = \\
& -5307120 T^3 Y + (-65520 Y^3 + 257040 Y) T, \quad \mathbf{h}_{24} = 99508500 T^4 Y + 5460 Y^5 - 96600 Y^3 + (2457000 Y^3 - 11907000 Y) T^2 - \\
& 81900 Y, \quad \mathbf{h}_{23} = -1432922400 T^5 Y + (-58968000 Y^3 + 340200000 Y) T^3 + (-393120 Y^5 + 7358400 Y^3 + 4687200 Y) T, \quad \mathbf{h}_{22} = \\
& 16478607600 T^6 Y + 21840 Y^7 - 882000 Y^3 - (1017198000 Y^3 - 6807402000 Y) T^4 + 831600 Y^3 + (13562640 Y^5 - \\
& 267775200 Y^3 - 90946800 Y) T^2 - 3855600 Y, \quad \mathbf{h}_{21} = -155369728800 T^7 Y + (-13427013600 Y^3 + 102251872800 Y) T^5 + \\
& (-298378080 Y^5 + 6197083200 Y^3 - 194594400 Y) T^3 + (-1441440 Y^7 + 58655520 Y^5 - 74642400 Y^3 + 247816800 Y) T, \quad \mathbf{h}_{20} = \\
& 1223536614300 T^8 Y + 60060 Y^9 - 4047120 Y^7 + (140983642800 Y^3 - 1203783411600 Y) T^6 + 24713640 Y^5 + (4699454760 Y^5 - \\
& 102424014000 Y^3 + 47701823400 Y) T^4 - 5821200 Y^3 + (45405360 Y^7 - 1861619760 Y^5 + 3210656400 Y^3 - 8307910800 Y) T^2 - \\
& 152806500 Y, \quad \mathbf{h}_{19} = -8156910762000 T^9 Y + (-1208431224000 Y^3 + 11433618504000 Y) T^7 + (-56393457120 Y^5 + \\
& 1286927611200 Y^3 - 1228773823200 Y) T^5 + (-908107200 Y^7 + 37511812800 Y^5 - 86143176000 Y^3 + 190416744000 Y) T^3 + \\
& (-3603600 Y^9 + 238392000 Y^7 - 1491285600 Y^5 + 984312000 Y^3 + 9549414000 Y) T, \quad \mathbf{h}_{18} = 46494391343400 T^{10} Y + \\
& 120120 Y^{11} - 11411400 Y^9 + (8610072471000 Y^3 - 89412291045000 Y) T^8 + 154350000 Y^7 + (535737842640 Y^5 - \\
& 12775287016800 Y^3 + 19055424603600 Y) T^6 - 200566800 Y^5 + (12940527600 Y^7 - 538525033200 Y^5 + 1607611698000 Y^3 - \\
& 3261827394000 Y) T^4 - 406161000 Y^3 + (102702600 Y^9 - 6667768800 Y^7 + 43826756400 Y^5 - 51570540000 Y^3 - \\
& 299274507000 Y) T^2 - 2385369000 Y, \quad \mathbf{h}_{17} = -228245193867600 T^{11} Y + (-51660434826000 Y^3 + 584160301494000 Y) T^9 + \\
& (-4132834786080 Y^5 + 102791019038400 Y^3 - 212792613818400 Y) T^7 + (-139757698080 Y^7 + 5859072727200 Y^5 - \\
& 22196715055200 Y^3 + 43339546303200 Y) T^5 + (-1848646800 Y^9 + 117744580800 Y^7 - 832242146400 Y^5 + 1441001016000 Y^3 + \\
& 6192044838000 Y) T^3 + (-6486480 Y^{11} + 592930800 Y^9 - 7837754400 Y^7 + 14755154400 Y^5 + 46699254000 Y^3 + \\
& 120522654000 Y) T, \quad \mathbf{h}_{16} = 970042073937300 T^{12} Y + 180180 Y^{13} - 21538440 Y^{11} + (263468217612600 Y^3 - 3222418969261800 Y) T^{10} + \\
& 469305900 Y^9 + (26346821761260 Y^5 - 682315127663400 Y^3 + 1832381801088300 Y) T^8 - 2353503600 Y^7 + (1187940433680 Y^7 - \\
& 50167638314640 Y^5 + 235968167962800 Y^3 - 455944830087600 Y) T^6 - 4399636500 Y^5 + (23570246700 Y^9 + 1472233870800 Y^7 + \\
& 11412666606600 Y^5 - 25946472258000 Y^3 - 92176486636500 Y) T^4 + 26397819000 Y^3 + (165405240 Y^{11} - 14525973000 Y^9 + \\
& 45820559584800 Y^7 - 483343232400 Y^5 - 2284179345000 Y^3 - 3204923841000 Y) T^2 + 126898852500 Y, \quad \mathbf{h}_{15} = -3581693811460800 T^{13} Y + \\
& (-1149679495036800 Y^3 + 15122707203945600 Y) T^{11} + (-140516382726720 Y^5 + 3783133381104000 Y^3 - 12611227861108800 Y) T^9 + \\
& (-8145877259520 Y^7 + 346513086501120 Y^5 - 1984916735020800 Y^3 + 3854481012345600 Y) T^7 + (-226274368320 Y^9 + \\
& 13854953629440 Y^7 - 119644591812480 Y^5 + 330748111814400 Y^3 + 1016622803448000 Y) T^5 + (-2646483840 Y^{11} + \\
& 222915369600 Y^9 - 2967012115200 Y^7 + 9572059526400 Y^5 + 52195271184000 Y^3 + 58675981392000 Y) T^3 + (-8648640 Y^{13} + \\
& 975300480 Y^{11} - 20216347200 Y^9 + 106770182400 Y^7 + 556542705600 Y^5 - 934080336000 Y^3 - 8946538776000 Y) T, \quad \mathbf{h}_{14} = \\
& 11512587251124000 T^{14} Y + 205920 Y^{15} - 28274400 Y^{13} + (4311298106388000 Y^3 - 60689811805308000 Y) T^{12} + \\
& 824191200 Y^{11} + (632323722270240 Y^5 - 17672637366014400 Y^3 + 70877356360826400 Y) T^{10} - 8130780000 Y^9 + \\
& (45820559584800 Y^7 - 1963234745287200 Y^5 + 13467933475164000 Y^3 - 26494216568316000 Y) T^8 - 47621196000 Y^7 + \\
& (1697057762400 Y^9 - 101823465744000 Y^7 + 990865619150400 Y^5 - 3152771466768000 Y^3 - 8370340328196000 Y) T^6 + \\
& 166745628000 Y^5 + (29772943200 Y^{11} - 2400920676000 Y^9 + 33064378200000 Y^7 - 129924135432000 Y^5 - 668838813300000 Y^3 - \\
& 709945587540000 Y) T^4 + 3067005060000 Y^3 + (194594400 Y^{13} - 20627006400 Y^{11} + 411884676000 Y^9 - 2370867408000 Y^7 - \\
& 15208430076000 Y^5 + 2184696360000 Y^3 + 274047939900000 Y) T^2 + 1485279180000 Y, \quad \mathbf{h}_{13} = -32235244303147200 T^{15} Y + \\
& (-13928809266792000 Y^3 + 208932139001880000 Y) T^{13} + (-2414326939577280 Y^5 + 6995357542877600 Y^3 - 329729232701131200 Y) T^{11} + \\
& (-213829278062400 Y^7 + 9227555768692800 Y^5 - 74713146002712000 Y^3 + 149448721649976000 Y) T^9 + (-10182346574400 Y^9 + \\
& 598408675603200 Y^7 - 6613833224073600 Y^5 + 23262995478240000 Y^3 + 50974727447448000 Y) T^7 + (-250092722880 Y^{11} + \\
& 19269964929600 Y^9 - 280607601456000 Y^7 + 1292453335555200 Y^5 + 5146445349864000 Y^3 + 5542623817416000 Y) T^5 + \\
& (-2724321600 Y^{13} + 270336528000 Y^{11} - 5290613496000 Y^9 + 34296097248000 Y^7 + 195047995464000 Y^5 + 320120171280000 Y^3 - \\
& 4943519206920000 Y) T^3 + (-8648640 Y^{15} + 1094385600 Y^{13} - 29484907200 Y^{11} + 301485240000 Y^9 + 1776048120000 Y^7 - \\
& 2000376000 Y^5 - 170822108520000 Y^3 - 78344726040000 Y) T, \quad \mathbf{h}_{12} = 78573407988921300 T^{16} Y + 180180 Y^{17} - \\
& 26056800 Y^{15} + (38801682957492000 Y^3 - 617842182476988000 Y) T^{14} + 864183600 Y^{13} + (7846562553626160 Y^5 - \\
& 235396876608784800 Y^3 + 1280511771920362800 Y) T^{12} - 14926615200 Y^{11} + (833934184443360 Y^7 - 36244062631576800 Y^5 + \\
& 342000491235530400 Y^3 - 696568312313546400 Y) T^{10} - 47584341000 Y^9 + (49638939550200 Y^9 - 2856148214119200 Y^7 + \\
& 36025885150491600 Y^5 - 135905216949684000 Y^3 - 220047998283477000 Y) T^8 - 162459108000 Y^7 + (1625602698720 Y^{11} - \\
& 119419275175200 Y^9 + 1878390270993600 Y^7 - 9808892925249600 Y^5 - 22141848885156000 Y^3 - 32027867107236000 Y) T^6 + \\
& 22556739870000 Y^5 + (26562135600 Y^{13} - 2455975922400 Y^{11} + 48173126274000 Y^9 - 360525575592000 Y^7 - 1404565842078000 Y^5 -
\end{aligned}$$

$$\begin{aligned}
& 8404158018060000 Y^3 + 60525769205790000 Y)T^4 - 4865914620000 Y^3 + (168648480 Y^{15} - 19524304800 Y^{13} + \\
& 490546173600 Y^{11} - 5658666804000 Y^9 - 26319756708000 Y^7 - 222646849740000 Y^5 + 4111457808780000 Y^3 + \\
& 1567269591300000 Y)T^2 + 17840228332500 Y, \quad h_{11} = -166390746329480400 T^{17} Y + (-93124039097980800 Y^3 + \\
& 1568781889419830400 Y)T^{15} + (-21728942456195520 Y^5 + 674154368512732800 Y^3 - 4171012214961009600 Y)T^{13} + \\
& (-2729239149087360 Y^7 + 119456698140823680 Y^5 - 1299187815456585600 Y^3 + 2694598806041251200 Y)T^{11} + \\
& (-19855578200800 Y^9 + 11180216538691200 Y^7 - 161332655638190400 Y^5 + 637978578571152000 Y^3 + 570248470704276000 Y)T^9 + \\
& (-8360242450560 Y^{11} + 584145145584000 Y^9 - 10124422119302400 Y^7 + 58246381175673600 Y^5 + 18105308872560000 Y^3 + \\
& 232351318980144000 Y)T^7 + (-191247376320 Y^{13} + 16388429016960 Y^{11} - 331136584833600 Y^9 + 2896965327110400 Y^7 + \\
& 6244863813720000 Y^5 + 129317255074224000 Y^3 - 540557215654680000 Y)T^5 + (-2023781760 Y^{15} + 212497084800 Y^{13} - \\
& 5061408508800 Y^{11} + 71653531824000 Y^9 + 301403891376000 Y^7 + 6779398287312000 Y^5 - 60532077891600000 Y^3 - \\
& 8216684446320000 Y)T^3 + (-6486480 Y^{17} + 836922240 Y^{15} - 24353784000 Y^{13} + 526537065600 Y^{11} + 1322105652000 Y^9 + \\
& 59419740240000 Y^7 - 1023330349944000 Y^5 - 107840270160000 Y^3 - 972790350210000 Y)T, \quad h_{10} = 305049701604047400 T^{18} Y + \\
& 120120 Y^{19} - 16548840 Y^{17} + (192068330639585400 Y^3 - 3412906490595709800 Y)T^{16} + 488890080 Y^{15} + (51218221503889440 Y^5 - \\
& 1641609663586200000 Y^3 + 11414468862580845600 Y)T^{14} - 21772346400 Y^{13} + (7505407659990240 Y^7 - 330815276090339040 Y^5 + \\
& 4106717638852701600 Y^3 - 8668745847288727200 Y)T^{12} - 6882246000 Y^{11} + (655234002062640 Y^9 - 36088272728988480 Y^7 + \\
& 596168406827753760 Y^5 - 2428234027504084800 Y^3 + 50055414863454000 Y)T^{10} - 5440951278000 Y^9 + (34486000108560 Y^{11} - \\
& 2285802827708400 Y^9 + 44437383951760800 Y^7 - 274922553639333600 Y^5 + 420662488039794000 Y^3 - 2429174247417918000 Y)T^8 + \\
& 92067448284000 Y^7 + (1051860569760 Y^{13} - 83016072659520 Y^{11} + 1783492119208800 Y^9 - 18223766338377600 Y^7 - \\
& 25255310905994400 Y^5 - 1396985405890536000 Y^3 + 3695432633748324000 Y)T^6 - 106330986468000 Y^5 + (16696199520 Y^{15} - \\
& 1573295724000 Y^{13} + 36498260383200 Y^{11} - 672135718716000 Y^9 - 4063833237996000 Y^7 - 107311625793540000 Y^5 + \\
& 622016572135140000 Y^3 - 189452805432660000 Y)T^4 + 67073857515000 Y^3 + (107026920 Y^{17} - 12140694720 Y^{15} + \\
& 309045391200 Y^{13} - 9645679713600 Y^{11} - 70780518522000 Y^9 - 2220330772296000 Y^7 + 21865238892252000 Y^5 - \\
& 2515162761720000 Y^3 + 29812467440385000 Y)T^2 + 89623095975000 Y, \quad h_9 = -481657423585338000 T^{19} Y + (-338944112893386000 Y^3 + \\
& 6335647648699446000 Y)T^{17} + (-102436443007778880 Y^5 + 3388282345641916800 Y^3 - 2621379410281036800 Y)T^{15} + \\
& (-17320171523054400 Y^7 + 768749151446337600 Y^5 - 10799671984987032000 Y^3 + 23180566621956408000 Y)T^{13} + \\
& (-1787001823807200 Y^9 + 96223175128080000 Y^7 - 1818691673595451200 Y^5 + 7526678046071184000 Y^3 - 8704011789925452000 Y)T^{11} + \\
& (-114953333695200 Y^{11} + 7206689766276000 Y^9 - 159570453402360000 Y^7 + 1040756085080712000 Y^5 - 3088318719786300000 Y^3 + \\
& 21641103489145140000 Y)T^9 + (-4507973870400 Y^{13} + 325267653110400 Y^{11} - 7690193607096000 Y^9 + 90688875365088000 Y^7 + \\
& 191505475404936000 Y^5 + 10963308751773840000 Y^3 - 20358971571213000000 Y)T^7 + (-100177197120 Y^{15} + 8360942990400 Y^{13} - \\
& 196733950459200 Y^{11} + 4803047088840000 Y^9 + 49366644041736000 Y^7 + 1094577615912312000 Y^5 - 4783618921316760000 Y^3 + \\
& 4413344842874520000 Y)T^5 + (-1070269200 Y^{17} + 104721724800 Y^{15} - 2349489240000 Y^{13} + 116309417616000 Y^{11} + \\
& 1825837558020000 Y^9 + 37096510928400000 Y^7 - 280210439660760000 Y^5 + 158328260118000000 Y^3 - 442844276575050000 Y)T^3 + \\
& (-3603600 Y^{19} + 419958000 Y^{17} - 9104961600 Y^{15} + 788941944000 Y^{13} + 12599654004000 Y^{11} + 357321211380000 Y^9 - \\
& 3933889432200000 Y^7 + 4226564444760000 Y^5 - 10971899829450000 Y^3 - 4839647182650000 Y)T, \quad h_8 = 650237521840206300 T^{20} Y + \\
& 60060 Y^{21} - 6791400 Y^{19} + (508416169340079000 Y^3 - 9972778706286165000 Y)T^{18} + 50179500 Y^{17} + (172861497575626860 Y^5 - \\
& 5895020301938044200 Y^3 + 50317727229079209900 Y)T^{16} - 30115864800 Y^{15} + (33403187937319200 Y^7 - 1492865553198650400 Y^5 + \\
& 23553140641257276000 Y^3 - 51353313650908668000 Y)T^{14} - 942355701000 Y^{13} + (4020754103566200 Y^9 - 21155323603021600 Y^7 + \\
& 4568236675022638800 Y^5 - 19004882784238260000 Y^3 + 48364028847330651000 Y)T^{12} - 24006440934000 Y^{11} + \\
& (310374000977040 Y^{11} - 18343899288514800 Y^9 + 468580477040676000 Y^7 - 3171137513421477600 Y^5 + 11861718275945538000 Y^3 - \\
& 137313278658313758000 Y)T^{10} + 298588802715000 Y^9 + (15214411812600 Y^{13} - 994788464670000 Y^{11} + 26815489481781000 Y^9 - \\
& 358089091748388000 Y^7 - 1613367396737019000 Y^5 - 63354712748280030000 Y^3 + 95735025380141595000 Y)T^8 - \\
& 687054141900000 Y^7 + (450797387040 Y^{15} - 32769502365600 Y^{13} + 826977985495200 Y^{11} - 26286541655220000 Y^9 + \\
& 425701980500580000 Y^7 - 7731992874432204000 Y^5 + 28658263905907020000 Y^3 - 4707700295797960000 Y)T^6 + \\
& 1830657223867500 Y^5 + (7224317100 Y^{17} - 594246391200 Y^{15} + 12119492322000 Y^{13} - 981093982428000 Y^{11} - \\
& 24410946788235000 Y^9 - 367218523391580000 Y^7 + 2446729986276450000 Y^5 - 2747535814642500000 Y^3 + 3427250905185187500 Y)T^4 - \\
& 349209389025000 Y^3 + (48648600 Y^{19} - 4636585800 Y^{17} + 62900258400 Y^{15} - 13590125892000 Y^{13} - 406892981502000 Y^{11} - \\
& 5953201491510000 Y^9 + 70677009780300000 Y^7 - 53450201749140000 Y^5 + 147359104554375000 Y^3 + 149204226372075000 Y)T^2 - \\
& 1266622455262500 Y, \quad h_7 = -743128596388807200 T^{21} Y + (-642209898113784000 Y^3 + 13190003292029256000 Y)T^{19} + \\
& (-244039761283237920 Y^5 + 8572678793795793600 Y^3 - 80145432639490125600 Y)T^{17} + (-53445100699710720 Y^7 + \\
& 2405029531486982400 Y^5 - 42324408592578604800 Y^3 + 93639180103559596800 Y)T^{15} + (-7422930652737600 Y^9 + \\
& 381424436617593600 Y^7 - 9391102820502076800 Y^5 + 38939850917083872000 Y^3 - 164243503452717864000 Y)T^{13} + \\
& (-677179638495360 Y^{11} + 37592151726729600 Y^9 - 1119615739917292800 Y^7 + 7765345102358188800 Y^5 - 28182319095529872000 Y^3 + \\
& 622008697713884208000 Y)T^{11} + (-40571764833600 Y^{13} + 23781296002246400 Y^{11} - 75680527346424000 Y^9 + 1119514013890272000 Y^7 + \\
& 9538764448070088000 Y^5 + 272050338584399760000 Y^3 - 397619797129599240000 Y)T^9 + (-1545591041280 Y^{15} + \\
& 95707752940800 Y^{13} - 2778783962169600 Y^{11} + 110035641016224000 Y^9 + 2533405784722848000 Y^7 + 39001700627215200000 Y^5 - \\
& 135819748301741280000 Y^3 + 320027061178591200000 Y)T^7 + (-34676722080 Y^{17} + 2311781472000 Y^{15} - 46281042057600 Y^{13} + \\
& 5912387434195200 Y^{11} + 197438241983976000 Y^9 + 2407506822207648000 Y^7 - 15133040576866800000 Y^5 + 27053126671828320000 Y^3 - \\
& 9344524455386820000 Y)T^5 + (-389188800 Y^{19} + 28829908800 Y^{17} - 143602502400 Y^{15} + 139722643872000 Y^{13} + \\
& 562236229104000 Y^{11} + 54662260287600000 Y^9 - 732292016450400000 Y^7 + 268049863902240000 Y^5 - 259879298124600000 Y^3 - \\
& 1553832915679800000 Y)T^3 + (-1441440 Y^{21} + 123076800 Y^{19} + 1615269600 Y^{17} + 956489990400 Y^{15} + 43717645944000 Y^{13} + \\
& 295089180624000 Y^{11} - 10492642245960000 Y^9 + 6234366126240000 Y^7 - 10047643601940000 Y^5 - 56026080923400000 Y^3 + \\
& 57571446397500000 Y)T, \quad h_6 = 709350023825679600 T^{22} Y + 21840 Y^{23} - 1459920 Y^{21} + (674320393019473200 Y^{13} - \\
& 14471953050187155600 Y)T^{20} - 125067600 Y^{19} + (284713054830444240 Y^5 - 10293471982331445600 Y^3 + 104739172127340181200 Y)T^{18} - \\
& 31705959600 Y^{17} + (70146694668370320 Y^7 - 3178184858436162960 Y^5 + 62006244332554897200 Y^3 - 139059690475964756400 Y)T^{16} - \\
& 1915582284000 Y^{15} + (11134395979106400 Y^9 - 558432782952105600 Y^7 + 15640306127550619200 Y^5 - 64190646579514896000 Y^3 + \\
& 398610856564180092000 Y)T^{14} + 9014694444000 Y^{13} + (1185064367366880 Y^{11} - 61532188305588000 Y^9 + 2155632571720555200 Y^7 - \\
& 15179195856028276800 Y^5 + 37227014548230780000 Y^3 - 2050925005465759332000 Y)T^{12} + 709438349340000 Y^{11} + \\
& (85200706150560 Y^{13} - 4417328918882880 Y^{11} + 171631758162664800 Y^9 - 2752078138124515200 Y^7 - 38556673251080292000 Y^5 - \\
& 871539680876096232000 Y^3 + 1430270119015409700000 Y)T^{10} - 237749688540000 Y^9 + (4057176483360 Y^{15} - 207540181648800 Y^{13} + \\
& 7522243087312800 Y^{11} - 350665630032564000 Y^9 - 10597945583409156000 Y^7 - 142104516736548492000 Y^5 + 505959450022334700000 Y^3 - \\
& 1512534343392592380000 Y)T^8 + 429538238010000 Y^7 + (121368527280 Y^{17} - 6199130931840 Y^{15} + 141560608392000 Y^{13} - \\
& 25698901685385600 Y^{11} - 1048042343925612000 Y^9 - 10947020473010160000 Y^7 + 65475859945926024000 Y^5 - 181750858318769040000 Y^3 - \\
& 87637173359225490000 Y)T^6 + 7941855288150000 Y^5 + (2043241200 Y^{19} - 107977438800 Y^{17} - 501179918400 Y^{15} -
\end{aligned}$$

$$\begin{aligned}
& 928436513256000 \, Y^{13} - 43962300358956000 \, Y^{11} - 339273836492220000 \, Y^9 + 4426622578619640000 \, Y^7 - 1947326218515720000 \, Y^5 - \\
& 8004663131305050000 \, Y^3 + 13909832269429950000 \, Y)T^4 - 27332174983050000 \, Y^3 + (15135120 \, Y^{21} - 873180000 \, Y^{19} - \\
& 38640596400 \, Y^{17} - 12999433910400 \, Y^{15} - 677780398764000 \, Y^{13} - 2106017856936000 \, Y^{11} + 128418933221460000 \, Y^9 + \\
& 144048856094640000 \, Y^7 - 92805576668910000 \, Y^5 + 1586362555102500000 \, Y^3 - 603989791237350000 \, Y)T^2 - 3820880690550000 \, Y, \quad \mathbf{h}_5 = \\
& -555143496907053600 \, T^{23} \, Y + (-577988908302405600 \, Y^3 + 12938059408923079200 \, Y)T^{21} + (-269728157207789280 \, Y^5 + \\
& 10028354562853704000 \, Y^3 - 110448718821858463200 \, Y)T^{19} + (-74272970825333280 \, Y^7 + 3387990130724818080 \, Y^5 - \\
& 72876673599910639200 \, Y^3 + 165511861874509298400 \, Y)T^{17} + (-13361275174927680 \, Y^9 + 653674693173384960 \, Y^7 - \\
& 20773748702392398720 \, Y^5 + 83907070526262009600 \, Y^3 - 718080536280324168000 \, Y)T^{15} + (-1640858354815680 \, Y^{11} + \\
& 79308153816091200 \, Y^9 - 3292671514690454400 \, Y^7 + 23376917271968668800 \, Y^5 - 1541298023563032000 \, Y^3 + 4963814601334964424000 \, Y)T^{13} + \\
& (-139419337337280 \, Y^{13} + 6284594744588160 \, Y^{11} - 308085861769358400 \, Y^9 + 5252092180763500800 \, Y^7 + 109253945161344715200 \, Y^5 + \\
& 2075901196344051888000 \, Y^3 - 4201868922308453592000 \, Y)T^{11} + (-8114352966720 \, Y^{15} + 327695023656000 \, Y^{13} - \\
& 16253214858619200 \, Y^{11} + 842786533229256000 \, Y^9 + 31583540743009416000 \, Y^7 + 373214611288504440000 \, Y^5 - 1449647920912406040000 \, Y^3 + \\
& 15135371023251934360000 \, Y)T^9 + (-312090498720 \, Y^{17} + 11075211544320 \, Y^{15} - 366012911779200 \, Y^{13} + 80679852732729600 \, Y^{11} + \\
& 379524220563112000 \, Y^9 + 34888117519525536000 \, Y^7 - 191403575032409712000 \, Y^5 + 892313966733729120000 \, Y^3 + \\
& 1162296924054221340000 \, Y)T^7 + (-7355668320 \, Y^{19} + 232552283040 \, Y^{17} + 4044485934720 \, Y^{15} + 4133857819190400 \, Y^{13} + \\
& 215751419642808000 \, Y^{11} + 1480079148577848000 \, Y^9 - 14890681469919024000 \, Y^7 + 30688187810869008000 \, Y^5 + \\
& 795048958569085000 \, Y^3 - 189497180398585500000 \, Y)T^5 + (-90810720 \, Y^{21} + 2724321600 \, Y^{19} + 31437376800 \, Y^{17} + \\
& 9794841198400 \, Y^{15} + 5364302299272000 \, Y^{13} + 14753257090992000 \, Y^{11} - 689103017016120000 \, Y^9 - 1309038653008800000 \, Y^7 - \\
& 2816316572994540000 \, Y^5 - 26061241842531000000 \, Y^3 + 2167268744938500000 \, Y)T^3 + (-393120 \, Y^{23} + 12529400 \, Y^{21} + \\
& 3055600800 \, Y^{19} + 732223346400 \, Y^{17} + 41934225009600 \, Y^{15} - 210441555576000 \, Y^{13} - 10817315273016000 \, Y^{11} - \\
& 37468552763880000 \, Y^9 - 51721876885140000 \, Y^7 - 634782261633660000 \, Y^5 + 493907312121300000 \, Y^3 + 223766085116700000 \, Y)T, \quad \mathbf{h}_4 = \\
& 346964685566908500 \, T^{24} \, Y + 5460 \, Y^{25} + 25200 \, Y^{23} + (394083346569822000 \, Y^3 - 9185173385435082000 \, Y)T^{22} - \\
& 87053400 \, Y^{21} + (202296117905841960 \, Y^5 - 7728749119992423600 \, Y^3 + 91686148555217970600 \, Y)T^{20} - 20265714000 \, Y^{19} + \\
& (6189412354444400 \, Y^7 - 2842369460431023600 \, Y^5 + 67072907482213122000 \, Y^3 - 154122906855121218000 \, Y)T^{18} - \\
& 11126074220500 \, Y^{17} + (12526195476494700 \, Y^9 - 597403168878978000 \, Y^7 + 21487621054592536200 \, Y^5 - 85001124308869314000 \, Y^3 + \\
& 960888516137184379500 \, Y)T^{16} + 16441233228000 \, Y^{15} + (1758062523016800 \, Y^{11} - 78662028273444000 \, Y^9 + 3896532363248280000 \, Y^7 - \\
& 27752999657789448000 \, Y^5 - 101067512224410900000 \, Y^3 - 8763298036639815060000 \, Y)T^{14} + 343497005310000 \, Y^{13} + \\
& (174274171671600 \, Y^{13} - 6676041345573600 \, Y^{11} + 427209367193154000 \, Y^9 - 7618494941831592000 \, Y^7 - 218912699412193374000 \, Y^5 - \\
& 3626476877147797260000 \, Y^3 + 9462196733729421150000 \, Y)T^{12} + 2910832133580000 \, Y^{11} + (12171529450080 \, Y^{15} - \\
& 360464526021600 \, Y^{13} + 27322202780056800 \, Y^{11} - 1501123926109500000 \, Y^9 - 66972173500712844000 \, Y^7 - 69525588989793988000 \, Y^5 + \\
& 3094424712352132740000 \, Y^3 - 12607027327873620180000 \, Y)T^{10} + 10266682898587500 \, Y^9 + (585169685100 \, Y^{17} - \\
& 11643376298400 \, Y^{15} + 792242127810000 \, Y^{13} - 181283921685468000 \, Y^{11} - 9479329208738235000 \, Y^9 - 76705655063291100000 \, Y^7 + \\
& 357001010822062530000 \, Y^5 - 3204036256969138500000 \, Y^3 - 6268896973351617412500 \, Y)T^8 + 80049458969550000 \, Y^7 + \\
& (18389170800 \, Y^{19} - 190964466000 \, Y^{17} - 10016568475200 \, Y^{15} - 12473518580712000 \, Y^{13} - 692107880824332000 \, Y^{11} - \\
& 440798436022140000 \, Y^9 + 22462641432819000000 \, Y^7 - 243671386119887880000 \, Y^5 - 323563119670132650000 \, Y^3 + \\
& 1842263577164281950000 \, Y)T^6 - 101650312916775000 \, Y^5 + (340540200 \, Y^{21} - 785862000 \, Y^{19} - 1310067675000 \, Y^{17} - \\
& 447430672584000 \, Y^{15} - 24944441173470000 \, Y^{13} - 80773877634660000 \, Y^{11} + 1453441883213250000 \, Y^9 - 1204055069805000000 \, Y^7 + \\
& 48323492127645525000 \, Y^5 + 265075582779992250000 \, Y^3 + 1951502407241625000 \, Y)T^4 - 30942753644250000 \, Y^3 + \\
& (2948400 \, Y^{23} + 9147600 \, Y^{21} - 26409726000 \, Y^{19} - 6771629970000 \, Y^{17} - 364319479188000 \, Y^{15} + 1196459892180000 \, Y^{13} + \\
& 45310691808900000 \, Y^{11} + 232342897254300000 \, Y^9 + 3296933269497550000 \, Y^7 + 9932226945187050000 \, Y^5 - 5004963818835750000 \, Y^3 + \\
& 201287397417750000 \, Y)T^2 - 7895187141187500 \, Y, \quad \mathbf{h}_3 = -166543049072116080 \, T^{25} \, Y + (-205608702558168000 \, Y^3 + \\
& 4982057023528480000 \, Y)T^{23} + (-115597781660481120 \, Y^5 + 4534989895911182400 \, Y^3 - 57696437946829096800 \, Y)T^{21} + \\
& (-39091037276491200 \, Y^7 + 1807208723320862400 \, Y^5 - 46571640318947016000 \, Y^3 + 108182395433461608000 \, Y)T^{19} + \\
& (-8842020336349200 \, Y^9 + 410813867934993600 \, Y^7 - 16681439528324776800 \, Y^5 + 64358214148582200000 \, Y^3 - 932948950892889546000 \, Y)T^{17} + \\
& (-1406450018413440 \, Y^{11} + 57880827680860800 \, Y^9 - 3443141224633824000 \, Y^7 + 24516907720060089600 \, Y^5 + 214577598455618832000 \, Y^3 + \\
& 11015297350886476368000 \, Y)T^{15} + (-160868466158400 \, Y^{13} + 5073543932688000 \, Y^{11} - 440650227528504000 \, Y^9 + \\
& 8115202892516832000 \, Y^7 + 3056688141030302856000 \, Y^5 + 4515024911274274320000 \, Y^3 - 1540025547433485588000 \, Y)T^{13} + \\
& (-13278032127360 \, Y^{15} + 250239836246400 \, Y^{13} - 34247858987260800 \, Y^{11} + 1920953228468400000 \, Y^9 + 99040608611728560000 \, Y^7 + \\
& 886901856300217296000 \, Y^5 - 4714587739153892880000 \, Y^3 + 22016752510238090640000 \, Y)T^{11} + (-780226246800 \, Y^{17} + \\
& 3360974601600 \, Y^{15} - 1333904155416000 \, Y^{13} + 284449974543504000 \, Y^{11} + 16113203705041380000 \, Y^9 + 111195588535572240000 \, Y^7 - \\
& 376788105499138200000 \, Y^5 + 8080999576859286000000 \, Y^3 + 18067694766213975750000 \, Y)T^9 + (-31524292800 \, Y^{19} - \\
& 341917329600 \, Y^{17} + 7245737452800 \, Y^{15} + 25213759867296000 \, Y^{13} + 1455239242696176000 \, Y^{11} + 8486309100512880000 \, Y^9 + \\
& 11242032333386400000 \, Y^7 + 973317921014668320000 \, Y^5 + 270420646275549000000 \, Y^3 - 10263022676045004600000 \, Y)T^7 + \\
& (-817296480 \, Y^{21} - 20746756800 \, Y^{19} + 3030998292000 \, Y^{17} + 1271660970182400 \, Y^{15} + 71431552607688000 \, Y^{13} + \\
& 275727431013552000 \, Y^{11} + 1087253675270280000 \, Y^9 + 40162923010274400000 \, Y^7 - 339004100996478540000 \, Y^5 - \\
& 1545479396363359800000 \, Y^3 - 5776420187871900000 \, Y)T^5 + (-11793600 \, Y^{23} - 449064000 \, Y^{21} + 109449144000 \, Y^{19} + \\
& 32285529360000 \, Y^{17} + 1678207824720000 \, Y^{15} - 1432809317520000 \, Y^{13} + 7650177963120000 \, Y^{11} + 545906111058000000 \, Y^9 - \\
& 33115966881543000000 \, Y^7 - 100723377185613000000 \, Y^5 + 26108689761063000000 \, Y^3 - 4923661999467000000 \, Y)T^3 + \\
& (-65520 \, Y^{25} - 3124800 \, Y^{23} + 1141005600 \, Y^{21} + 291239928000 \, Y^{19} + 12915784854000 \, Y^{17} - 150867024336000 \, Y^{15} + \\
& 679177661400000 \, Y^{13} + 6531807749040000 \, Y^{11} - 741058330279050000 \, Y^9 - 1565231758259400000 \, Y^7 + 2651747909901300000 \, Y^5 - \\
& 94607557877000000 \, Y^3 + 450318081386250000 \, Y)T, \quad \mathbf{h}_2 = 57649516986501720 \, T^{26} \, Y + 840 \, Y^{27} + 88200 \, Y^{25} + \\
& (77103263459313000 \, Y^3 - 1939443627015027000 \, Y)T^{24} - 24570000 \, Y^{23} + (47290001588378640 \, Y^5 - 1903725704968063200 \, Y^3 + \\
& 25874272611541149200 \, Y)T^{22} - 6698235600 \, Y^{21} + (17590966774421040 \, Y^7 - 818656530655748400 \, Y^5 + 22943500219407171600 \, Y^3 - \\
& 53836354223716755600 \, Y)T^{20} - 198707985000 \, Y^{19} + (4421010168174600 \, Y^9 - 199965690683589600 \, Y^7 + 9144227378857258800 \, Y^5 - \\
& 34280060491862892000 \, Y^3 + 623464627876627509000 \, Y)T^{18} + 5338396287000 \, Y^{17} + (791128135357560 \, Y^{11} - 29718018417918600 \, Y^9 + \\
& 2137520177910154800 \, Y^7 - 15180633766376038800 \, Y^5 - 232600397925076713000 \, Y^3 - 9362336705977386033000 \, Y)T^{16} - \\
& 182739348540000 \, Y^{15} + (103415442530400 \, Y^{13} - 2561520961137600 \, Y^{11} + 317824100169156000 \, Y^9 - 5985169941755088000 \, Y^7 - \\
& 284242826741751612000 \, Y^5 - 3793883573061633240000 \, Y^3 + 16908842306184772860000 \, Y)T^{14} - 2096839131660000 \, Y^{13} + \\
& (9958524095520 \, Y^{15} - 80434233079200 \, Y^{13} + 29941221405866400 \, Y^{11} - 1670296846640436000 \, Y^9 - 97321815609810372000 \, Y^7 - \\
& 724028313142624140000 \, Y^5 + 4807457447882363820000 \, Y^3 - 26093252921707698300000 \, Y)T^{12} + 60168130732395000 \, Y^{11} + \\
& (702203622120 \, Y^{17} + 7922297275200 \, Y^{15} + 1572998611010400 \, Y^{13} - 296207844207508800 \, Y^{11} - 17830173219253434000 \, Y^9 - \\
& 96493122705542472000 \, Y^7 + 145925978792374620000 \, Y^5 - 13365124470122213880000 \, Y^3 - 2665414250400064095000 \, Y)T^{10} + \\
& 119968081009875000 \, Y^9 + (35464829400 \, Y^{19} + 1137602604600 \, Y^{17} + 13998439375200 \, Y^{15} - 32734885716036000 \, Y^{13} -
\end{aligned}$$

$$\begin{aligned}
& 1937262236199822000 Y^{11} - 9704350494609750000 Y^9 - 95255799199161300000 Y^7 - 2099620909250886420000 Y^5 + \\
& 2658491017123424175000 Y^3 + 31792336082807701275000 Y)T^8 - 408044335415850000 Y^7 + (1225944720 Y^{21} + 65069373600 Y^{19} - \\
& 3734802010800 Y^{17} - 2201730533251200 Y^{15} - 124598369090412000 Y^{13} - 560145821620392000 Y^{11} - 10847252665187820000 Y^9 - \\
& 13870675930219920000 Y^7 + 1388723202715803570000 Y^5 + 5139836318374625700000 Y^3 - 446739603321327750000 Y)T^6 + \\
& 256154960580750000 Y^5 + (26535600 Y^{23} + 1938459600 Y^{21} - 231972174000 Y^{19} - 84079875474000 Y^{17} - 4397919939252000 Y^{15} - \\
& 10701856570860000 Y^{13} - 480334470906780000 Y^{11} - 5038378212060900000 Y^9 + 155113073038945350000 Y^7 + 504211787836101450000 Y^5 + \\
& 73644498000722250000 Y^3 + 635195079791385750000 Y)T^4 - 100005703788375000 Y^3 + (294840 Y^{25} + 26762400 Y^{23} - \\
& 5142387600 Y^{21} - 1518682284000 Y^{19} - 68780749779000 Y^{17} + 214513749576000 Y^{15} - 11549215844460000 Y^{13} - \\
& 120429406472760000 Y^{11} + 6236452501440525000 Y^9 + 19989184935402900000 Y^7 + 57525875331750000 Y^5 + 13561007365174500000 Y^3 - \\
& 2483235729316125000 Y)T^2 + 12281402219625000 Y, \quad \mathbf{h}_1 = -12811003774778160 T^{27} Y + (-18504783230235120 Y^3 + \\
& 482547808849977360 Y)T^{25} + (-12336522153490080 Y^5 + 509276940182539200 Y^3 - 7368699578603882400 Y)T^{23} + \\
& (-5025990506977440 Y^7 + 235448324519173920 Y^5 - 7149032161340882400 Y^3 + 16933194660168712800 Y)T^{21} + \\
& (-1396108474160400 Y^9 + 61428772863057600 Y^7 - 3156122873256847200 Y^5 + 11458047744364536000 Y^3 - 257122322800734762000 Y)T^{19} + \\
& (-279221694832080 Y^{11} + 9486378093654000 Y^9 - 831423275513863200 Y^7 + 5880831956337592800 Y^5 + 137530705452296310000 Y^3 + \\
& 4832262378372826782000 Y)T^{17} + (-41366177012160 Y^{13} + 744591186218880 Y^{11} - 142862286783988800 Y^9 + 2730744302239699200 Y^7 + \\
& 158687185378408344000 Y^5 + 1928619518343990192000 Y^3 - 11162813976218905560000 Y)T^{15} + (-4596241890240 Y^{15} - \\
& 12374497396800 Y^{13} - 16209466635499200 Y^{11} + 884002220321976000 Y^9 + 57214019317553784000 Y^7 + 329729434567932168000 Y^5 - \\
& 2920969221142442400000 Y^3 + 18877028349055340520000 Y)T^{13} + (-383020157520 Y^{17} - 10292439104640 Y^{15} - \\
& 1128079181880000 Y^{13} + 184055274401846400 Y^{11} + 11591551384474068000 Y^9 + 39570561550109520000 Y^7 + 17330064729553224000 Y^5 + \\
& 12890374408497040560000 Y^3 + 14780105310040936110000 Y)T^{11} + (-23643219600 Y^{19} - 1260365475600 Y^{17} - \\
& 31421342836800 Y^{15} + 24693233169528000 Y^{13} + 1483049451889908000 Y^{11} + 5566248052937460000 Y^9 + 133236721205353080000 Y^7 + \\
& 238379728822360000 Y^5 - 9453523853059331850000 Y^3 - 55321414856217905850000 Y)T^9 + (-1050809760 Y^{21} - \\
& 84873096000 Y^{19} + 1955277727200 Y^{17} + 2128002634195200 Y^{15} + 121995639154872000 Y^{13} + 6494945923217648000 Y^{11} + \\
& 18927701831570520000 Y^9 + 183415160328734880000 Y^7 - 3093092043717522420000 Y^5 - 99486579068727000000 Y^3 + \\
& 1910894939947734300000 Y)T^7 + (-31842720 Y^{23} - 3439830240 Y^{21} + 233786800800 Y^{19} + 113781129688800 Y^{17} + \\
& 6231969961560000 Y^{15} + 43798278528648000 Y^{13} + 1211139761476680000 Y^{11} + 8839351975812120000 Y^9 - 366985618162912980000 Y^7 - \\
& 1086455089789429500000 Y^5 - 1045191903468533100000 Y^3 - 2895193855711376100000 Y)T^5 + (-58960 Y^{25} - \\
& 78926400 Y^{23} + 9448941600 Y^{21} + 3429184248000 Y^{19} + 178486906374000 Y^{17} + 1527744876336000 Y^{15} + 36197453842200000 Y^{13} + \\
& 1276412292052400000 Y^{11} - 21659653787017050000 Y^9 - 74507130257603400000 Y^7 - 100365773943840300000 Y^5 - \\
& 77632497916281000000 Y^3 + 55531396877780250000 Y)T^3 + (-5040 Y^{27} - 791280 Y^{25} + 146210400 Y^{23} + 44367976800 Y^{21} + \\
& 2165002182000 Y^{19} + 21374803422000 Y^{17} + 307256896296000 Y^{15} - 39068243444920000 Y^{13} - 500728726806210000 Y^{11} - \\
& 1212609265191450000 Y^9 - 1394108018043300000 Y^7 + 3342285256520700000 Y^5 + 2085286397654250000 Y^3 + 305280569459250000 Y)T, \quad \mathbf{h}_0 = \\
& 1372607547297660 T^8 Y + 60 Y^{29} + 14280 Y^{27} + (2135167295796360 Y^3 - 57649516986501720 Y)T^{26} - 2622060 Y^{25} + \\
& (1542065269186260 Y^5 - 65241222927111000 Y^3 + 1001749322944458900 Y)T^{24} - 844225200 Y^{23} + (685362341860560 Y^7 - \\
& 32317740427732560 Y^5 + 1059412019975996400 Y^3 - 2531359449571906800 Y)T^{22} - 62099446500 Y^{21} + (209416271124060 Y^9 - \\
& 8956572826536720 Y^7 + 515899180588294440 Y^5 - 1808097155986237200 Y^3 + 49410780668344273500 Y)T^{20} - 1950322941000 Y^{19} + \\
& (46536949138680 Y^{11} - 1414007300752200 Y^9 + 152429661587876400 Y^7 - 1072930515550966800 Y^5 - 35364802605798393000 Y^3 - \\
& 1145511079099572969000 Y)T^{18} + 15589233796500 Y^{17} + (7756158189780 Y^{13} - 87107622746760 Y^{11} + 30095249748057900 Y^9 - \\
& 580741711672978800 Y^7 - 40336381312723559700 Y^5 - 447957615028165893000 Y^3 + 3342012307029573124500 Y)T^{16} + \\
& 831325259772000 Y^{15} + (984908976480 Y^{13} + 13258390068000 Y^{13} + 4077075476728800 Y^{11} - 215034614357724000 Y^9 - \\
& 15249510580479084000 Y^7 - 58976165558634660000 Y^5 + 794453293383133860000 Y^3 - 6299917076943049140000 Y)T^{14} + \\
& 24414465931852500 Y^{13} + (95755039380 Y^{17} + 4065906287520 Y^{15} + 366266373706800 Y^{13} - 5167783550346400 Y^{11} - \\
& 3359497847343813000 Y^9 - 2229735374457444000 Y^7 - 55441979884545282000 Y^5 - 5465746279540528380000 Y^3 + \\
& 2018444757614804452500 Y)T^{12} + 29863844597475000 Y^{11} + (7092965880 Y^{19} + 528698764440 Y^{17} + 18249854001120 Y^{15} - \\
& 8231186515053600 Y^{13} - 497604528853110000 Y^{11} - 9772373397242000 Y^9 - 64184028758026884000 Y^7 - 1147086793581178212000 Y^5 + \\
& 9670649590939153635000 Y^3 + 46128299717400945975000 Y)T^{10} + 119014886217937500 Y^9 + (394053660 Y^{21} + 42739666200 Y^{19} - \\
& 59645394900 Y^{17} - 880557158527200 Y^{15} - 51605024956821000 Y^{13} - 346736165789286000 Y^{11} - 11419482457917765000 Y^9 - \\
& 44797127731364300000 Y^7 + 2999698552619600107500 Y^5 + 8947293896735121375000 Y^3 - 5188671943455794062500 Y)T^8 - \\
& 634204420519950000 Y^7 + (15921360 Y^{23} + 2276754480 Y^{21} - 80886632400 Y^{19} - 62650104577200 Y^{17} - 3709921076920800 Y^{15} - \\
& 48739940386452000 Y^{13} - 1051122212832132000 Y^{11} - 6373029049255260000 Y^9 + 359700788114790570000 Y^7 + \\
& 677780785159128630000 Y^5 + 2139737253253453350000 Y^3 + 1113030888713008650000 Y)T^6 - 471845093328787500 Y^5 + \\
& (442260 Y^{25} + 78246000 Y^{23} - 5821162200 Y^{21} - 2841367410000 Y^{19} - 175989954892500 Y^{17} - 3557400808500000 Y^{15} - \\
& 49673624386050000 Y^{13} - 38056228226100000 Y^{11} + 28945718175276787500 Y^9 + 78126695870532750000 Y^7 + 189045582782942025000 Y^5 - \\
& 87871217621276250000 Y^3 - 252780206699400187500 Y)T^4 - 13451059573875000 Y^3 + (7560 Y^{27} + 1580040 Y^{25} - \\
& 193309200 Y^{23} - 74160046800 Y^{21} - 4940837433000 Y^{19} - 133691736465000 Y^{17} - 795619119708000 Y^{15} + 22679177884020000 Y^{13} + \\
& 1347083235295875000 Y^{11} + 4240509697224675000 Y^9 + 9977905356114150000 Y^7 - 10909947072020850000 Y^5 - \\
& 21082807979139375000 Y^3 - 4844135932626375000 Y)T^2 + 4386215078437500 Y.
\end{aligned}$$

$$\begin{aligned}
& \mathbf{q}_{30} = -90 T, \quad \mathbf{q}_{29} = -90 T, \quad \mathbf{q}_{28} = 3915 T^2 + 15 Y^2 + 15, \quad \mathbf{q}_{27} = -109620 T^3 + (-1260 Y^2 + 420)T, \quad \mathbf{q}_{26} = \\
& 2219805 T^4 + 105 Y^4 + (51030 Y^2 - 85050)T^2 - 630 Y^2 + 945, \quad \mathbf{q}_{25} = -34628958 T^5 + (-1326780 Y^2 + 3980340)T^3 + \\
& (-8190 Y^4 + 64260 Y^2 - 58590)T, \quad \mathbf{q}_{24} = 432861975 T^6 + 455 Y^6 + (24877125 Y^2 - 107800875)T^4 - 7875 Y^4 + \\
& (307125 Y^4 - 2976750 Y^2 + 2537325)T^2 + 4725 Y^2 + 64575, \quad \mathbf{q}_{23} = -4452294600 T^7 + (-358230600 Y^2 + 2029973400)T^5 + \\
& (-7371000 Y^4 + 85050000 Y^2 - 90833400)T^3 + (-32760 Y^6 + 617400 Y^4 - 642600 Y^2 - 4195800)T, \quad \mathbf{q}_{22} = 38401040925 T^8 + \\
& 1365 Y^8 + (4119651900 Y^2 - 28837563300)T^6 - 39900 Y^6 + (127149750 Y^4 - 1701850500 Y^2 + 2458880550)T^4 + \\
& 103950 Y^4 + (1130220 Y^6 - 23039100 Y^4 + 39860100 Y^2 + 136363500)T^2 + 548100 Y^2 + 3709125, \quad \mathbf{q}_{21} = -281607633450 T^9 + \\
& (-38842432200 Y^2 + 323686935000)T^7 + (-1678376700 Y^4 + 25562968200 Y^2 - 49189347900)T^5 + (-24864840 Y^6 + \\
& 545113800 Y^4 - 1425778200 Y^2 - 2771836200)T^3 + (-90090 Y^8 + 2670360 Y^6 - 9733500 Y^4 - 40257000 Y^2 - \\
& 232857450)T, \quad \mathbf{q}_{20} = 1774128090735 T^{10} + 3003 Y^{10} + (305884153575 Y^2 - 2956880151225)T^8 - 114345 Y^8 + \\
& (17622955350 Y^4 - 300945852900 Y^2 + 744230960550)T^6 + 859950 Y^6 + (391621230 Y^6 - 9188036550 Y^4 + 33615247050 Y^2 + \\
& 36176442750)T^4 + 4035150 Y^4 + (2837835 Y^8 - 85280580 Y^6 + 426733650 Y^4 + 1218879900 Y^2 + 7225465275)T^2 + \\
& 34827975 Y^2 + 133656075, \quad \mathbf{q}_{19} = -9677062313100 T^{11} + (-2039227690500 Y^2 + 22431504595500)T^9 + (-151053903000 Y^4 + \\
& 2858404626000 Y^2 - 8777393717400)T^7 + (-4699454760 Y^6 + 117486369000 Y^4 - 567470950200 Y^2 - 259313027400)T^5 + \\
& (-56756700 Y^8 + 1728896400 Y^6 - 11529945000 Y^4 - 19837062000 Y^2 - 147652753500)T^3 + (-180180 Y^{10} + 6583500 Y^8 - \\
& 63592200 Y^6 - 162729000 Y^4 - 2502454500 Y^2 - 7265254500)T, \quad \mathbf{q}_{18} = 45966045987225 T^{12} + 5005 Y^{12} + (11623597835850 Y^2 -
\end{aligned}$$

$$\begin{aligned}
& 143357706642150)T^{10} - 200970Y^{10} + (1076259058875Y^4 - 22353072761250Y^2 + 82805716206675)T^8 + 3649275Y^8 + \\
& (44644820220Y^6 - 1184804844300Y^4 + 7236492347700Y^2 - 369958824900)T^6 + 220500Y^6 + (808782975Y^8 - \\
& 24968582100Y^6 + 215430374250Y^4 + 167299303500Y^2 + 2255342079375)T^4 + 277333875Y^4 + (5135130Y^{10} - \\
& 179729550Y^8 + 2244557700Y^6 + 3391510500Y^4 + 89180453250Y^2 + 190647938250)T^2 + 959505750Y^2 + 1115785125, \quad \mathbf{q}_{17} = \\
& -190935883331550T^{13} + (-57061298466900Y^2 + 779837745714300)T^{11} + (-6457554353250Y^4 + 146040075373500Y^2 - \\
& 637509635150850)T^9 + (-344402898840Y^6 + 96697773698200Y^4 - 72272775544200Y^2 + 36573828669000)T^7 + (-8734856130Y^8 + \\
& 273244217400Y^6 - 2970054693900Y^4 - 13438240200Y^2 - 27800198669250)T^5 + (-92432340Y^{10} + 3092928300Y^8 - \\
& 49806981000Y^6 - 57919617000Y^4 - 2030375686500Y^2 - 3236840554500)T^3 + (-270270Y^{12} + 9688140Y^{10} - \\
& 233122050Y^8 - 345303000Y^6 - 22167857250Y^4 - 65315848500Y^2 + 14547377250)T, \quad \mathbf{q}_{16} = 695552146422075T^{14} + \\
& 6435Y^{14} + (242510518484325Y^2 - 3637657777264875)T^{12} - 204435Y^{12} + (32933527201575Y^4 - 805604742315450Y^2 + \\
& 4066023935271375)T^{10} + 10174815Y^{10} + (2195568480105Y^6 - 65022604987725Y^4 + 579696166093275Y^2 - 541685929164975)T^8 + \\
& 42170625Y^8 + (74246277105Y^8 - 2353035859020Y^6 + 31489767177750Y^4 - 19781700403500Y^2 + 289330527665025)T^6 + \\
& 2030639625Y^6 + (1178512335Y^{10} - 37621739925Y^8 + 775679728950Y^6 + 957694893750Y^4 + 32898822208875Y^2 + \\
& 40532346327375)T^4 + 7693410375Y^4 + (6891885Y^{12} - 217359450Y^{10} + 7091880075Y^8 + 25663950900Y^6 + 690946837875Y^4 + \\
& 2326499799750Y^2 - 2785590556875)T^2 - 27357820875Y^2 + 24214372875, \quad \mathbf{q}_{15} = -2225766868550640T^{15} + \\
& (-895423452865200Y^2 + 14625249730131600)T^{13} + (-143709936879600Y^4 + 3780676800986400Y^2 - 21722309689878000)T^{11} + \\
& (-11709698560560Y^6 + 364802147463600Y^4 - 3801344116323600Y^2 + 5129179073802000)T^9 + (-509117328720Y^8 + \\
& 16343971680960Y^6 - 264064561336800Y^4 + 303975087595200Y^2 - 2587336325758800)T^7 + (-11313718416Y^{10} + \\
& 343762982640Y^8 - 8995662295200Y^6 - 13910071744800Y^4 - 404340187381200Y^2 - 410101956104400)T^5 + (-110270160Y^{12} + \\
& 300274120Y^{10} - 135469681200Y^8 - 812993025600Y^6 - 13849198398000Y^4 - 56230426476000Y^2 + 96537883806000)T^3 + \\
& (-308880Y^{14} + 7373520Y^{12} - 578022480Y^{10} - 5866182000Y^8 - 88199118000Y^6 - 723921786000Y^4 + 2153904858000Y^2 - \\
& 1157431842000)T, \quad \mathbf{q}_{14} = 6259969317798675T^{16} + 6435Y^{16} + (2878146812781000Y^2 - 50847260359131000)T^{14} + \\
& 59400Y^{14} + (538912263298500Y^4 - 15172452951327000Y^2 + 97974249467667300)T^{12} + 21035700Y^{12} + 256263435225250Y^6 - \\
& 1722676807467000Y^4 + 20637756269915400Y^2 - 36268975558204200)T^{10} + 451672200Y^{10} + (2863784974050Y^8 - \\
& 93109726848600Y^6 + 1786027202347500Y^4 - 2836148447727000Y^2 + 19835779480445250)T^8 + 2902331250Y^8 + \\
& (84852888120Y^{10} - 2447679465000Y^8 + 80578388746800Y^6 + 160217472366000Y^4 + 3924855698463000Y^2 + 3606189371883000)T^6 + \\
& 79622109000Y^6 + (1240539300Y^{12} - 28436977800Y^{10} + 1812516709500Y^8 + 15152729130000Y^6 + 211473469777500Y^4 + \\
& 1001803839435000Y^2 - 1913433139957500)T^4 - 319613647500Y^4 + (6949800Y^{14} - 111018600Y^{12} + 15472182600Y^{10} + \\
& 238682619000Y^8 + 3101833035000Y^6 + 31080306285000Y^4 - 72934601985000Y^2 + 40952876265000)T^2 + 191285955000Y^2 + \\
& 463546951875, \quad \mathbf{q}_{13} = -1546580654985550T^{17} + (-8058811075786800Y^2 + 153117410439949200)T^{15} + (-1741101158349000Y^4 + \\
& 52233034750470000Y^2 - 375033189508374600)T^{13} + (-201193911631440Y^6 + 6887022359691600Y^4 - 93575355588716400Y^2 + \\
& 202341187950274800)T^{11} + (-13364329878900Y^8 + 439994860628400Y^6 - 9877454719587000Y^4 + 19328746192686000Y^2 - \\
& 129049771528912500)T^9 + (-509117328720Y^{10} + 13902819361200Y^8 - 571090230496800Y^6 - 1425375491652000Y^4 - \\
& 30840659025498000Y^2 - 28656565635978000)T^7 + (-10420530120Y^{12} + 193982176080Y^{10} - 17992689132600Y^8 - \\
& 190066725828000Y^6 - 2545405696323000Y^4 - 13275003731598000Y^2 + 26372292309027000)T^5 + (-97297200Y^{14} + \\
& 785862000Y^{12} - 257443628400Y^{10} - 5116715730000Y^8 - 75868204986000Y^6 - 746552825550000Y^4 + 1469628738270000Y^2 - \\
& 1123593695910000)T^3 + (-270270Y^{16} - 831600Y^{14} - 1059193800Y^{12} - 30420003600Y^{10} - 502445632500Y^8 - \\
& 7348214538000Y^6 + 16094275155000Y^4 - 12504850470000Y^2 - 22679575458750)T, \quad \mathbf{q}_{12} = 33509247524687025T^{18} + \\
& 5005Y^{18} + (19643351997230325Y^2 - 399414823943683275)T^{16} + 155925Y^{16} + (4850210369686500Y^4 - 154460545619247000Y^2 + \\
& 1222029157297781700)T^{14} + 33585300Y^{14} + (653880212802180Y^6 - 23388792227154900Y^4 + 356342847073749900Y^2 - \\
& 914393525009737500)T^{12} + 1481098500Y^{12} + (52120886527710Y^8 - 1737362884257000Y^6 + 45082744437849300Y^4 - \\
& 102412074801090600Y^2 + 705477876223506750)T^{10} + 42118035750Y^{10} + (2481946977510Y^{10} - 63957864420450Y^8 + \\
& 3254864424493500Y^6 + 9865838196805500Y^4 + 198836092900194750Y^2 + 204233318709351750)T^8 + 639849435750Y^8 + \\
& (67733445780Y^{12} - 969109301160Y^{10} + 137179452746700Y^8 + 1722999362994000Y^6 + 2393231955371500Y^4 + \\
& 130295245151799000Y^2 - 274323069168151500)T^6 - 1190848837500Y^6 + (948647700Y^{14} - 170270100Y^{12} + 2969618897700Y^{10} + \\
& 69920100841500Y^8 + 1197222549421500Y^6 + 10977042671122500Y^4 - 21138885238432500Y^2 + 21771514150312500)T^4 + \\
& 1787210932500Y^4 + (5270265Y^{16} + 81081000Y^{14} + 24732294300Y^{12} + 843741927000Y^{10} + 187209748005750Y^8 + \\
& 227504346111000Y^6 - 306742031662500Y^4 + 478173629745000Y^2 + 592594980665625)T^2 + 4850130403125Y^2 + \\
& 5581517878125, \quad \mathbf{q}_{11} = -63491205836249100T^{19} + (-41597686582370100Y^2 + 901283209284685500)T^{17} + (-11640504887247600Y^4 + \\
& 392195472354957600Y^2 - 3392759462906242800)T^{15} + (-1810745204682960Y^6 + 67554724943941200Y^4 - 1143040480461154800Y^2 + \\
& 3394420538297065200)T^{13} + (-170577446817960Y^8 + 5755895384934240Y^6 - 170796135852342000Y^4 + 434316422282652000Y^2 - \\
& 3217998781976869800)T^{11} + (-9927787910040Y^{10} + 240557937820200Y^8 - 15077266093234800Y^6 - 53860167736830000Y^4 - \\
& 1057971621386043000Y^2 - 1261081149657147000)T^9 + (-348343435440Y^{12} + 3483434354400Y^{10} - 821027995678800Y^8 - \\
& 11773903992177600Y^6 - 174502372922514000Y^4 - 947084307096564000Y^2 + 2241578159268210000)T^7 + (-6830263440Y^{14} - \\
& 52715622960Y^{12} - 25132201108560Y^{10} - 667128468006000Y^8 - 12728981098638000Y^6 - 104963034841434000Y^4 + \\
& 238734163086426000Y^2 - 297807832848834000)T^5 + (-63243180Y^{16} - 1751349600Y^{14} - 353547406800Y^{12} - \\
& 13475158250400Y^{10} - 340829099541000Y^8 - 3517220113092000Y^6 + 4350290200830000Y^4 - 13219389778140000Y^2 - \\
& 10198540090147500)T^3 + (-180180Y^{18} - 8773380Y^{16} - 1461272400Y^{14} - 71246725200Y^{12} - 2361855850200Y^{10} - \\
& 30220930467000Y^8 + 5099458518000Y^6 - 105477326010000Y^4 - 352298094592500Y^2 - 233138196742500)T, \quad \mathbf{q}_{10} = \\
& 104760489629811015T^{20} + 3003Y^{20} + (76262425401011850Y^2 - 1754035784223272550)T^{18} + 279510Y^{18} + (24008541329948175Y^4 - \\
& 853226622648927450Y^2 + 8017005993331155975)T^{16} + 40951575Y^{16} + (4268185125324120Y^6 - 165802576022206200Y^4 + \\
& 3090009007201624200Y^2 - 10424772892710729000)T^{14} + 2550025800Y^{14} + (469087978749390Y^8 - 16021158658825320Y^6 + \\
& 538532681617394100Y^4 - 1496423455565711400Y^2 + 12189347811375994350)T^{12} + 112585249350Y^{12} + (32761700103132Y^{10} - \\
& 743438579263380Y^8 + 57121959445551000Y^6 + 234611514409872600Y^4 + 4650065744678253900Y^2 + 652515519315090300)T^{10} + \\
& 1486454400900Y^{10} + (1436916671190Y^{12} - 8179371820620Y^{10} + 3910792444609050Y^8 + 62240180575973400Y^6 + \\
& 987692006489438250Y^4 + 5094579984955456500Y^2 - 14651706729192860250)T^8 + 2935114197750Y^8 + (37566448920Y^{14} + \\
& 586614548520Y^{12} + 161289578169720Y^{10} + 4675891080861000Y^8 + 95767657685469000Y^6 + 671629291823259000Y^4 - \\
& 2151688051568727000Y^2 + 2971482205900383000)T^6 + 10430710605000Y^6 + (521756235Y^{16} + 20870249400Y^{14} + \\
& 3449580542100Y^{12} + 141778751776200Y^{10} + 3778174041185250Y^8 + 31222192752261000Y^6 - 60188776488067500Y^4 + \\
& 238680624773115000Y^2 + 125112202454176875)T^4 + 58973741229375Y^4 + (2972970Y^{18} + 196902090Y^{16} + 28940020200Y^{14} + \\
& 1501648129800Y^{12} + 50642472566700Y^{10} + 486132643615500Y^8 - 117361309779000Y^6 + 6224343706665000Y^4 + \\
& 931232635776250Y^2 + 5187571071536250)T^2 + 49590883833750Y^2 + 14657286301875, \quad \mathbf{q}_9 = -149657842328301450T^{21} + \\
& (-120414355896334500Y^2 + 2930082660144139500)T^{19} + (-42368014111673250Y^4 + 1583911912174861500Y^2 -
\end{aligned}$$

$$\begin{aligned}
& 16071817291561958850)T^{17}+(-8536370250648240Y^6+344738029353102000Y^4-7026232108815334800Y^2+26548954994362928400)T^{15}+ \\
& (-1082510720190900Y^8+37416011559418800Y^6-1412941440025395000Y^4+4218158206327086000Y^2-38182262742010264500)T^{13}+ \\
& (-89350091190360Y^{10}+1890098082873000Y^8-177450421137116400Y^6-821476582783038000Y^4-16843729702364019000Y^2- \\
& 27689879799593739000)T^{11}+(-4789722237300Y^{12}+6631923097800Y^{10}-14941066639999500Y^8-25852185904545000Y^6- \\
& 4357637325669127500Y^4-20069104533713235000Y^2+77029103753340007500)T^9+(-160999066800Y^{14}-3785542160400Y^{12}- \\
& 800504248143600Y^{10}-24806163896514000Y^8-527775154864650000Y^6-2830486949738910000Y^4+15135962329981710000Y^2- \\
& 22432707027279990000)T^7+(-3130537410Y^{16}-163751187600Y^{14}-24281642662200Y^{12}-1052943959113200Y^{10}- \\
& 28148864831167500Y^8-161054816447574000Y^6+665750126247885000Y^4-2929250293043130000Y^2-1119917969690861250)T^5+ \\
& (-29729700Y^{18}-2490434100Y^{16}-344367450000Y^{14}-18625424202000Y^{12}-600202543059000Y^{10}-3512898931815000Y^8+ \\
& 7434396570510000Y^6-146392904192850000Y^4-163039104965362500Y^2-86638031763412500)T^3+(-90090Y^{20}- \\
& 10510500Y^{18}-1482336450Y^{16}-94513230000Y^{14}-3627540976500Y^{12}-19765393767000Y^{10}+27283253287500Y^8- \\
& 1902530108430000Y^6-2155834908281250Y^4-3919421087662500Y^2+447510678693750)T, \quad q_8 = 183670988312006325T^{22}+ \\
& 1365Y^{22}+(162559380460051575Y^2-4172357431807990425)T^{20}+246015Y^{20}+(63552021167509875Y^4-2493194676571541250Y^2+ \\
& 27181688315045262075)T^{18}+36850275Y^{18}+(14405124797968905Y^6-603907154991773325Y^4+1337725410372695675Y^2- \\
& 55974815513793276975)T^{16}+2719544625Y^{16}+(2087699246082450Y^8-73015942862986200Y^6+3074952267184423500Y^4- \\
& 9740941894903023000Y^2+98414407552796291250)T^{14}+98273999250Y^{14}+(201037705178310Y^{10}-3943431909266850Y^8+ \\
& 451541636724987900Y^6+2318860543607653500Y^4+50035856666945262750Y^2+95114506609638447750)T^{12}- \\
& 830307854250Y^{12}+(-12932250040710Y^{12}+37801961657460Y^{10}+45911908119127050Y^8+850521262477887000Y^6+ \\
& 15031950718054520250Y^4+55810035521516776500Y^2-325165281879377882250)T^{10}-8598553724250Y^{10}+(543371850450Y^{14}+ \\
& 17067449148750Y^{12}+3105646244350650Y^{10}+101323239250983750Y^8+2175395497471869750Y^6+6874522451445206250Y^4- \\
& 81182643512887901250Y^2+132022417838203541250)T^8+211739487041250Y^8+(14087418345Y^{16}+910263954600Y^{14}+ \\
& 127138836894300Y^{12}+5735877306528600Y^{10}+148425714637593750Y^8+374701102816383000Y^6-508296537001142500Y^4+ \\
& 25720936510904145000Y^2+7192580977150655625)T^6+162726680615625Y^6+(200675475Y^{18}+20329969275Y^{16}+ \\
& 2740578907500Y^{14}+152738477293500Y^{12}+4538744632532250Y^{10}+7083944611616250Y^8-111691683464602500Y^6+ \\
& 1921132808205187500Y^4+2000919227888896875Y^2+1286942656773571875)T^4+731900852746875Y^4+(1216215Y^{20}+ \\
& 170581950Y^{18}+23908533075Y^{16}+1552735737000Y^{14}+50841154554750Y^{12}-50207848015500Y^{10}-1312353863651250Y^8+ \\
& 48265125888105000Y^6+88587177040096875Y^4+158556548340618750Y^2-34242288683990625)T^2-370328202365625Y^2+ \\
& 93610564228125, \quad q_7 = -191656683456006600T^{23}+(-185782149097201800Y^2+5016118025624448600)T^{21}+ \\
& (-80276237264223000Y^4+3297500823007314000Y^2-38454787687632485400)T^{19}+(-20336646773603160Y^6+ \\
& 883861955929675800Y^4-21162695519641321800Y^2+97160045807492829000)T^{17}+(-3340318793731920Y^8+ \\
& 118195895778206400Y^6-5514796251833349600Y^4+18364278526266859200Y^2-207240072124273650000)T^{15}+ \\
& (-371146532636880Y^{10}+6709187320743600Y^8-936656644207284000Y^6-5267974473187524000Y^4-120971825196098058000Y^2- \\
& 261969795915526314000)T^{13}+(-28215818270640Y^{12}-204022070572320Y^{10}-113258654345163600Y^8-2220155451056088000Y^6- \\
& 40523317071694002000Y^4-97016859245933172000Y^2+1095243066022060242000)T^{11}+(-1448991601200Y^{14}- \\
& 5695651601600Y^{12}-9452724698617200Y^{10}-321145024314114000Y^8-6771322874919834000Y^6-1465181549141310000Y^4+ \\
& 326943096644221470000Y^2-615992255567580150000)T^9+(-48299720040Y^{16}-3715363080000Y^{14}-503153175016800Y^{12}- \\
& 23398409216952000Y^{10}-569070160152102000Y^8+854472231441864000Y^6+25004463359091300000Y^4-165662373262102920000Y^2- \\
& 31327530140955825000)T^7+(-963242280Y^{18}-114477640200Y^{16}-15368386672800Y^{14}-87704728246800Y^{12}- \\
& 23519320158222000Y^{10}+76300146659898000Y^8+754324671382380000Y^6-16312004195365620000Y^4-17969842739178225000Y^2- \\
& 159316636558534925000)T^5+(-9729720Y^{20}-1594177200Y^{18}-226210887000Y^{16}-14954225832000Y^{14}-419638710582000Y^{12}+ \\
& 2806470803052000Y^{10}+13618808783370000Y^8-603776038559400000Y^6-1729980781503975000Y^4-3252659797601550000Y^2+ \\
& 827743555288125000)T^3+(-32760Y^{22}-6902280Y^{20}-1057681800Y^{18}-78475635000Y^{16}-2164090446000Y^{14}+ \\
& 32486034798000Y^{12}+100613411766000Y^{10}-6381501996870000Y^8-27686110260375000Y^6-75133016102025000Y^4+ \\
& 18532739750175000Y^2-3727206833175000)T, \quad q_6 = 167699598024005775T^{24}+455Y^{24}+(177337505956419900Y^{20}- \\
& 5024562668765230500)T^{22}+134820Y^{22}+(84290049127434150Y^4-3617988262546788900Y^2+44952531584653920150)T^{20}+ \\
& 23403870Y^{20}+(23726087902537020Y^6-1067673955614165900Y^4+27498853284898634100Y^2-137463102940230792900)T^{18}+ \\
& 1942384500Y^{18}+(4384168416773145Y^8-156930746405520780Y^6+8064723790434795750Y^4-28024953494911411500Y^2+ \\
& 35278313267247505225)T^{16}+36981653625Y^{16}+(556719798955320Y^{10}-9207288982722600Y^8+1569338540917988400Y^6+ \\
& 9566055995845230000Y^4+235409072754050559000Y^2+572575656191875371000)T^{14}-1371507795000Y^{14}+(49377681973620Y^{12}+ \\
& 569742484311000Y^{10}+222736711127193900Y^8+4578121690199038800Y^6+84896875144621039500Y^4+44654097342592647000Y^2- \\
& 2913590206983461827500)T^{12}+3080287318500Y^{12}+(3042882362520Y^{14}+143639652035880Y^{12}+22506838986111480Y^{10}+ \\
& 789756178432221000Y^8+15911106314480685000Y^6-59747890906907973000Y^4-976191259483014183000Y^2+ \\
& 2279561306532207327000)T^{10}+299367020421000Y^{10}+(126786765105Y^{16}+11313280578600Y^{14}+1512989184930300Y^{12}+ \\
& 72070606920173400Y^{10}+1603817468500479750Y^8-10559267708942673000Y^6-79944749707283842500Y^4+785968750274743665000Y^2+ \\
& 93790049199800900625)T^8+3135310421315625Y^8+(3371347980Y^{18}+459799997580Y^{16}+62294151956400Y^{14}+ \\
& 3628246882201200Y^{12}+86758553692276200Y^{10}-727535653243623000Y^8-2248310416408938000Y^6+96084828184814910000Y^4+ \\
& 126209167576731067500Y^2+145621021569318067500)T^6+10570433743012500Y^6+(51081030Y^{20}+9574418700Y^{18}+ \\
& 1390831069950Y^{16}+93729403530000Y^{14}+2313824708947500Y^{12}-25114791943395000Y^{10}-37551370205632500Y^8+ \\
& 4775517426021930000Y^6+18992860969517268750Y^4+34183747164628687500Y^2-12338281534363706250)T^4- \\
& 3151872128081250Y^4+(343980Y^{22}+82952100Y^{20}+13145195700Y^{18}+991468503900Y^{16}+23634549603000Y^{14}- \\
& 405308433663000Y^{12}-846215308575000Y^{10}+85260617233155000Y^8+649830080716897500Y^6+1563032616773512500Y^4- \\
& 173596645659937500Y^2+117063206871187500)T^2+1114718902762500Y^2+412481438184375, \quad q_5 = -120743710577284158T^{25}+ \\
& (-138785874226763400Y^2+4117314268727314200)T^{23}+(-2248613537800700Y^4+3234514852230769800Y^2- \\
& 4266585088699690300)T^{21}+(-22477346433982440Y^6+1046061122504567400Y^4-28857078892577489400Y^2+ \\
& 156047559542707203000)T^{19}+(-4642060676583330Y^8+168066401931683640Y^6-9462770354962442700Y^4+ \\
& 34116873635493343800Y^2-477873929348003484450)T^{17}+(-668063758746384Y^{10}+10020956381195760Y^8- \\
& 2092180461394615200Y^6-13703835091854247200Y^4-362817552253053214800Y^2-978823391779323291600)T^{15}+ \\
& (-68369098117320Y^{12}-1083387247089840Y^{10}-344633830460249400Y^8-7373780943647479200Y^6-136520070172183971000Y^4+ \\
& 282687916302321138000Y^2+602907703528623878000)T^{13}+(-4979262047760Y^{14}-274370106170160Y^{12}-41498133259761360Y^{10}- \\
& 1494656949189222000Y^8-27920171774168478000Y^6+257704848203354118000Y^4+2123740273153485546000Y^2- \\
& 6590009666559291714000)T^{11}+(-253573530210Y^{16}-25747466144400Y^{14}-3441771667164600Y^{12}-167209670409289200Y^{10}- \\
& 3314522239179511500Y^8+43269109229019114000Y^6+149859329987155005000Y^4-2725152277145925690000Y^2- \\
& 292336131702061361250)T^9+(-8669180520Y^{18}-1334386940040Y^{16}-184001455159200Y^{14}-10920592714096800Y^{12}- \\
& 232044128139121200Y^{10}+3117880892930202000Y^8-1563477625544436000Y^6-406362888618269940000Y^4-
\end{aligned}$$

$$\begin{aligned}
& 694397030937410745000 Y^2 - 924253481322563805000) T^7 + (-183891708 Y^{20} - 38805865560 Y^{18} - 5809788463500 Y^{16} - \\
& 400068370144800 Y^{14} - 9080541270876600 Y^{12} + 109094367585999600 Y^{10} - 413971551272979000 Y^8 - 26818314970526100000 Y^6 - \\
& 133090390808534407500 Y^4 - 184512148249949415000 Y^2 + 119620495025367682500) T^5 + (-2063880 Y^{22} - 560581560 Y^{20} - \\
& 92429278200 Y^{18} - 7151484702600 Y^{16} - 169022698866000 Y^{14} + 1872647491554000 Y^{12} - 10295449680726000 Y^{10} - \\
& 778793783210730000 Y^8 - 7379585875119465000 Y^6 - 12518591008985775000 Y^4 + 2163685340135025000 Y^2 - 2385367308511425000) T^3 + \\
& (-8190 Y^{24} - 2739240 Y^{22} - 497686140 Y^{20} - 42313509000 Y^{18} - 949485017250 Y^{16} + 16281846126000 Y^{14} + \\
& 69360287283000 Y^{12} - 5893919348562000 Y^{10} - 98035556907881250 Y^8 - 234459588867525000 Y^6 - 138903899649637500 Y^4 - \\
& 18746417414025000 Y^2 - 16739391726618750) T, \quad q_4 = 69659833025356245 Y^{26} + 105 Y^{26} + (86741171391727125 Y^{22} - \\
& 268897631343540875) T^{24} + 46725 Y^{24} + (49260418321227750 Y^4 - 2296293346358770500 Y^2 + 32054890980507232950) T^{22} + \\
& 9856350 Y^{22} + (16858009825486830 Y^6 - 810481241609943750 Y^4 + 23855211529139147850 Y^2 - 138771892395654610050) T^{20} + \\
& 950244750 Y^{20} + (3868383897152775 Y^8 - 141642364234209300 Y^6 + 8695748277900416250 Y^4 - 32375938571960728500 Y^2 + \\
& 503036106482815896375) T^{18} + 28094731875 Y^{18} + (626309773824735 Y^{10} - 8431093109179125 Y^8 + 2168348059173936150 Y^6 + \\
& 15153188853736221750 Y^4 + 432418134354311770875 Y^2 + 1280197269469600563375) T^{16} + 11015463375 Y^{16} + (73252605125700 Y^{12} + \\
& 1476321734071800 Y^{10} + 410487741672025500 Y^8 + 9089426917135530000 Y^6 + 164860389373811197500 Y^4 - 933574336195334085000 Y^2 - \\
& 9485774174739720217500) T^{14} - 7594552507500 Y^{14} + (6224077559700 Y^{14} + 392116886261100 Y^{12} + 58111600673844900 Y^{10} + \\
& 2138066324254633500 Y^8 + 35718197119496797500 Y^6 - 609640417916112397500 Y^4 - 3267008928683007952500 Y^2 + \\
& 1446753722309529527500) T^{12} + 191792925292500 Y^{12} + (380360295315 Y^{16} + 43302556697400 Y^{14} + 5833401091125300 Y^{12} + \\
& 288168300950329800 Y^{10} + 4941283451721671250 Y^8 - 105940276577597259000 Y^6 - 94797737732917327500 Y^4 + \\
& 6785186437400928795000 Y^2 + 1409787245268487141875) T^{10} + 6041183185209375 Y^{10} + (16254713475 Y^{18} + 2877058119675 Y^{16} + \\
& 393309298147500 Y^{14} + 23773321169293500 Y^{12} + 451266446368568250 Y^{10} - 7951899750216423750 Y^8 + 37956773712790957500 Y^6 + \\
& 1245705353889721987500 Y^4 + 2893151595551915446875 Y^2 + 4046402506864153471875) T^8 + 13451797993921875 Y^8 + \\
& (459729270 Y^{10} + 107859559500 Y^{18} + 16709438998350 Y^{16} + 1178710484490000 Y^{14} + 25963392325279500 Y^{12} - \\
& 235739489343699000 Y^{10} + 4507206098598787500 Y^8 + 110640807479552490000 Y^6 + 628422700206154218750 Y^4 + \\
& 38351406627010487500 Y^2 - 725874033603785456250) T^6 + 29454394197768750 Y^6 + (7739550 Y^{22} + 2337939450 Y^{20} + \\
& 402405995250 Y^{18} + 32163679563750 Y^{16} + 832162399267500 Y^{14} + 540731013322500 Y^{12} + 231493536979582500 Y^{10} + \\
& 5406684043667287500 Y^8 + 50776308003166593750 Y^6 + 34292514960693281250 Y^4 - 29913929238180093750 Y^2 + \\
& 25109809764733968750) T^4 + 1342447645218750 Y^4 + (61425 Y^{24} + 22887900 Y^{22} + 4369273650 Y^{20} + 386332631500 Y^{18} + \\
& 11470169379375 Y^{16} + 100933078995000 Y^{14} + 4275194210437500 Y^{12} + 105536658412395000 Y^{10} + 1341367927426209375 Y^8 + \\
& 1434310052730187500 Y^6 + 1803864179909531250 Y^4 + 1762274886029437500 Y^2 + 446350550474390625) T^2 + 5894807234203125 Y^2 + \\
& 232602314765625, \quad q_3 = -30959925789047220 T^{27} + (-41635762268029020 Y^2 + 1346222979999604980) T^{25} + \\
& (-257010878197771000 Y^4 + 1245514255881210000 Y^2 - 18347018091156833400) T^{23} + (-9633148471706760 Y^6 + \\
& 477952366480835400 Y^4 - 14957637709755648600 Y^2 + 93152911833766474200) T^{21} + (-2443188929780700 Y^8 + \\
& 90460669594957200 Y^6 - 6029211601617561000 Y^4 + 23092756907190138000 Y^2 - 396654004520342257500) T^{19} + \\
& (-442101016817460 Y^{10} + 5271204431285100 Y^8 - 1684441756505075400 Y^6 - 12484396292516001000 Y^4 - 384147777083271106500 Y^2 - \\
& 1236801664400695186500) T^{17} + (-58602084100560 Y^{12} - 1433497134152160 Y^{10} - 3633161767639658800 Y^8 - 8286272819332200000 Y^6 - \\
& 144134586603731934000 Y^4 + 1537261039716868116000 Y^2 + 10950663625584318846000) T^{15} + (-5745302362800 Y^{14} - \\
& 407327205978000 Y^{12} - 59772478528047600 Y^{10} - 2238014569439250000 Y^8 - 31875603932639754000 Y^6 + 924433558629484050000 Y^4 + \\
& 3362761237454048430000 Y^2 - 23129405197587607590000) T^{13} + (-414938503980 Y^{16} - 52346088194400 Y^{14} - 7146761810101200 Y^{12} - \\
& 358222887901418400 Y^{10} - 5131052143806645000 Y^8 + 167536160238839868000 Y^6 - 246478092418990530000 Y^4 - \\
& 11764025280828239580000 Y^2 - 574450272380644947500) T^{11} + (-21672951300 Y^{18} - 4096187795700 Y^{16} - 59368864330000 Y^{14} - \\
& 36546368640138000 Y^{12} - 628936269329403000 Y^{10} + 12454170506279145000 Y^8 - 144106904653217730000 Y^6 - \\
& 2722408758831431250000 Y^4 - 8758722569417322862500 Y^2 - 11787223164622516012500) T^9 + (-788107320 Y^{20} - \\
& 203493351600 Y^{18} - 32695513968600 Y^{16} - 2368264701096000 Y^{14} - 53358796639638000 Y^{12} + 11950067490440000 Y^{10} - \\
& 19743113850234390000 Y^8 - 322214497569334440000 Y^6 - 1991154672422522775000 Y^4 + 946846826531824050000 Y^2 + \\
& 2831656501427762925000) T^7 + (-18574920 Y^{22} - 6176875320 Y^{20} - 1111573222200 Y^{18} - 92252661669000 Y^{16} - \\
& 2738678846274000 Y^{14} - 36672797690046000 Y^{12} - 1526472097312806000 Y^{10} - 24548193590426730000 Y^8 - 215397832224618225000 Y^6 + \\
& 115398710023349025000 Y^4 + 237189756986404425000 Y^2 - 139975295152881825000) T^5 + (-245700 Y^{24} - 100926000 Y^{22} - \\
& 202776212000 Y^{20} - 1888082406000 Y^{18} - 7171953409500 Y^{16} - 1897907453820000 Y^{14} - 5922859538295000 Y^{12} - \\
& 946960220058300000 Y^{10} - 9608297711062837500 Y^8 + 1259409061899450000 Y^6 - 2506912429699125000 Y^4 - 32184539868678750000 Y^2 - \\
& 8790728205636562500) T^3 + (-1260 Y^{26} - 619500 Y^{24} - 137932200 Y^{22} - 14130433800 Y^{20} - 662012662500 Y^{18} - \\
& 25307274730500 Y^{16} - 787970610630000 Y^{14} - 12761831273310000 Y^{12} - 135219968450752500 Y^{10} + 74641608109687500 Y^8 - \\
& 76090346046225000 Y^6 - 1169816852980125000 Y^4 - 519460780895437500 Y^2 + 9862338146062500) T, \quad q_2 = 9951404717908035 T^{28} + \\
& 15 Y^{28} + (14412379246625430 Y^2 - 485216767969722810) T^{26} + 9450 Y^{26} + (9637907932414125 Y^4 - 484860906753756750 Y^2 + \\
& 7517123360763059925) T^{24} + 2461725 Y^{24} + (3940833465698220 Y^6 - 201588788822255100 Y^4 + 6686829948677804100 Y^2 - \\
& 44394675195143668500) T^{22} + 296748900 Y^{22} + (1099435423401315 Y^8 - 41158351747844100 Y^6 + 2966348530359720450 Y^4 - \\
& 11650786377020172900 Y^2 + 220463519441588269875) T^{20} + 21862740375 Y^{20} + (221050508408730 Y^{10} - 2295524510398350 Y^8 + \\
& 923030283593722500 Y^6 + 7218828635635606500 Y^4 + 239380194333873269250 Y^2 + 831778382131571810250) T^{18} + \\
& 1401063945750 Y^{18} + (32963672306565 Y^{12} + 948339495588870 Y^{10} + 225100321320881475 Y^8 + 5267250869764936500 Y^6 + \\
& 85692378234818698875 Y^4 - 1521908965972300484250 Y^2 - 8739820021991600563875) T^{16} + 53045439418125 Y^{16} + \\
& (3693408661800 Y^{14} + 291021661992600 Y^{12} + 42605655687289800 Y^{10} + 1618539964425531000 Y^8 + 18299699941604571000 Y^6 - \\
& 898798518182933235000 Y^4 - 2070094820535474705000 Y^2 + 25248974601629694825000) T^{14} + 801963419355000 Y^{14} + \\
& (311203877985 Y^{16} + 43089767721000 Y^{14} + 5985858440576700 Y^{12} + 303971169516903000 Y^{10} + 3474398356320291750 Y^8 - \\
& 1683341225423050401000 Y^6 + 681750810951812437500 Y^4 + 13441879568562148305000 Y^2 + 13853497622284347890625) T^{12} + \\
& 7240875247423125 Y^{12} + (19505656170 Y^{18} + 4028668216650 Y^{16} + 601049248468200 Y^{14} + 37692349294005000 Y^{12} + \\
& 602473954367155500 Y^{10} - 11242291312225984500 Y^8 + 280110271421420685000 Y^6 + 4029818587144996905000 Y^4 + \\
& 18048181450423593656250 Y^2 + 20748593883185515856250) T^{10} - 18225599206106250 Y^{10} + (886620735 Y^{20} + 249845176350 Y^{18} + \\
& 41682799816875 Y^{16} + 3106556611641000 Y^{14} + 74665123502964750 Y^{12} + 534142184016136500 Y^{10} + 45972471925488858750 Y^8 + \\
& 606610004138534025000 Y^6 + 4040594908303349221875 Y^4 - 7439208303408771881250 Y^2 - 6935819570856885515625) T^8 - \\
& 19943100941990625 Y^8 + (27862380 Y^{22} + 10114043940 Y^{20} + 1903890006900 Y^{18} + 164651716561500 Y^{16} + 5668875655443000 Y^{14} + \\
& 138862637018721000 Y^{12} + 4704900462778257000 Y^{10} + 63511108995426435000 Y^8 + 536790850176688537500 Y^6 - \\
& 1078925221493400487500 Y^4 - 1011002909386419337500 Y^2 + 1074339110791649587500) T^6 + 193179545303062500 Y^6 + \\
& (552825 Y^{24} + 248175900 Y^{22} + 52497367650 Y^{20} + 5168429815500 Y^{18} + 238374497946375 Y^{16} + 8850586276035000 Y^{14} + \\
& 27113150876757500 Y^{12} + 3767521822218315000 Y^{10} + 35267364047091684375 Y^8 - 38892611633500012500 Y^6 + \\
& 22127086039950281250 Y^4 + 330826444321625437500 Y^2 + 90635811325793015625) T^4 + 118075580755453125 Y^4 +
\end{aligned}$$

$$\begin{aligned}
& (5670 Y^{26} + 3052350 Y^{24} + 718823700 Y^{22} + 79112092500 Y^{20} + 4620841769250 Y^{18} + 221043771632250 Y^{16} + \\
& 7141636482435000 Y^{14} + 103508757238635000 Y^{12} + 1015327719169706250 Y^{10} - 412507894719768750 Y^8 + 768374499128512500 Y^6 + \\
& 17751118754923312500 Y^4 + 7990846504579968750 Y^2 - 346311617783906250) T^2 - 5861578332093750 Y^2 + 299060118984375, \quad \mathbf{q}_1 = \\
& -2058911320946490 T^{29} + (-3202750943694540 Y^2 + 112096283029308900) T^{27} + (-2313097903779390 Y^4 + 120636952212494340 Y^2 - \\
& 1963820120308702110) T^{25} + (-1028043512790840 Y^6 + 54169985097055800 Y^4 - 1899112689205540200 Y^2 + 13391057556802837800) T^{23} + \\
& (-314124406686090 Y^8 + 11888400622273560 Y^6 - 923152321047757500 Y^4 + 3708205670816703000 Y^2 - 77034760175239533450) T^{21} + \\
& (-69805423708020 Y^{10} + 617509517417100 Y^8 - 318229746639827400 Y^6 - 2614896527607945000 Y^4 - 93336429316395226500 Y^2 - \\
& 347767826255658238500) T^{19} + (-11634237284670 Y^{12} - 384824771723700 Y^{10} - 87149793466987650 Y^8 - 2085383065602979800 Y^6 - \\
& 30755778146008193250 Y^4 + 865772990916574135500 Y^2 + 4306816518950882081250) T^{17} + (-1477363464720 Y^{14} - \\
& 128076048056880 Y^{12} - 18810111900419280 Y^{10} - 723245780863494000 Y^8 - 5720253447152286000 Y^6 + 514177793785476198000 Y^4 + \\
& 564801286096701738000 Y^2 - 16761364588803306402000) T^{15} + (-143632559070 Y^{16} - 21655370444400 Y^{14} - 3069297212272200 Y^{12} - \\
& 157738187047971600 Y^{10} - 1345528904618776500 Y^8 + 97961457598829622000 Y^6 - 696273502542763005000 Y^4 - \\
& 9074968983265939110000 Y^2 - 17589445369515278358750) T^{13} + (-10639448820 Y^{18} - 2384054954820 Y^{16} - 366632430267600 Y^{14} - \\
& 23432517013726800 Y^{12} - 3592387997640091800 Y^{10} + 4718379529937997000 Y^8 - 289697132657308698000 Y^6 - 3612815584880104890000 Y^4 - \\
& 22341223720366514932500 Y^2 - 18223480285848493582500) T^{11} + (-591080490 Y^{20} - 180506888100 Y^{18} - 31284257630850 Y^{16} - \\
& 2402965397070000 Y^{14} - 63344801316352500 Y^{12} - 1105794713723175000 Y^{10} - 55865245593916552500 Y^8 - 643450736493112590000 Y^6 - \\
& 4748165160242207681250 Y^4 + 15394968789630573937500 Y^2 + 8254010444065136493750) T^9 + (-23882040 Y^{22} - \\
& 9396664200 Y^{20} - 1849930374600 Y^{18} - 167095588678200 Y^{16} - 6623492829534000 Y^{14} - 220140941074866000 Y^{12} - \\
& 697550904674730000 Y^{10} - 81901126660142790000 Y^8 - 695089268636136255000 Y^6 + 2723006045118896775000 Y^4 + \\
& 2664473085690924375000 Y^2 - 5448473494388544375000) T^7 + (-663390 Y^{24} - 323121960 Y^{22} - 71929948860 Y^{20} - \\
& 7505303589000 Y^{18} - 401975673293250 Y^{16} - 17425508594130000 Y^{14} - 526836051310653000 Y^{12} - 6559820577961938000 Y^{10} - \\
& 6279966622838381250 Y^8 + 87598972192506075000 Y^6 - 296602185070281037500 Y^4 - 1474549884565353225000 Y^2 - \\
& 376367433547989318750) T^5 + (-11340 Y^{26} - 6633900 Y^{24} - 1653258600 Y^{22} - 195980488200 Y^{20} - 13106441722500 Y^{18} - \\
& 662673648514500 Y^{16} - 20887179980310000 Y^{14} - 282058529536350000 Y^{12} - 3018223686271972500 Y^{10} - 4384821363343312500 Y^8 - \\
& 21525129857522025000 Y^6 - 103471877025208125000 Y^4 - 11989971456564937500 Y^2 + 5774359109837062500) T^3 + \\
& (-90 Y^{28} - 61740 Y^{26} - 17013150 Y^{24} - 2253598200 Y^{22} - 176788190250 Y^{20} - 9754930804500 Y^{18} - 318801378750750 Y^{16} - \\
& 4447241995770000 Y^{14} - 52651311898578750 Y^{12} - 180623197653412500 Y^{10} - 526027698056306250 Y^8 - 2572888193311275000 Y^6 - \\
& 772890971503218750 Y^4 - 247781277249187500 Y^2 - 12959271822656250) T, \quad \mathbf{q}_0 = 90 T X^{30} + 205891312094649 T^{30} + \\
& X^{30} + Y^{30} + (343151886824415 Y^2 - 12467851887953745) T^{28} + 855 Y^{28} + (266895911974545 Y^4 - 14412379246625430 Y^2 + \\
& 245811134928555945) T^{26} + 275625 Y^{26} + (1285054390988855 Y^6 - 6968948812668675 Y^4 + 257554555055435925 Y^2 - \\
& 1922391943749986625) T^{24} + 44441775 Y^{24} + (42835146366285 Y^8 - 1638718932781980 Y^6 + 136644116908449150 Y^4 - \\
& 560086013795471100 Y^2 + 12730753775566554525) T^{22} + 4060783125 Y^{22} + (10470813556203 Y^{10} - 76517483679945 Y^8 + \\
& 51930597815513550 Y^6 + 446668065138963150 Y^4 + 17134239772133241975 Y^2 + 68083614964471020075) T^{20} + 207533751075 Y^{20} + \\
& (1939039547445 Y^{12} + 72490247696790 Y^{10} + 15872801459062275 Y^8 + 387335760139055700 Y^6 + 4966260292078792875 Y^4 - \\
& 219391313625118514250 Y^2 - 987121566914058583875) T^{18} + 5923312282125 Y^{18} + (277005649635 Y^{14} + 26201893371885 Y^{12} + \\
& 3876302771947935 Y^{10} + 150552748144346625 Y^8 + 611528589858839625 Y^6 - 132315060718915853625 Y^4 + 11896115762319067125 Y^2 + \\
& 5091352640433096100875) T^{16} + 77461769896875 Y^{16} + (30778405515 Y^{16} + 5019247668600 Y^{14} + 727212650994900 Y^{12} + \\
& 37793261862001800 Y^{10} + 214511736599417250 Y^8 - 25126138303645491000 Y^6 + 274776697273223092500 Y^4 + 2735159588700616035000 Y^2 + \\
& 9163014664668879616875) T^{14} + 1691986493491875 Y^{14} + (2659862205 Y^{18} + 642663629685 Y^{16} + 101952332313300 Y^{14} + \\
& 6644086914269700 Y^{12} + 101346793849844550 Y^{10} - 298739643719564250 Y^8 + 126859497950110306500 Y^6 + 1474770785254926772500 Y^4 + \\
& 12353324750841035233125 Y^2 + 4701616168042373698125) T^{12} + 21127132873153125 Y^{12} + (177324147 Y^{20} + 58335097590 Y^{18} + \\
& 1050264260575 Y^{16} + 832483300912200 Y^{14} + 24428227005948150 Y^{12} + 670167595543868100 Y^{10} + 27909592318881519750 Y^8 + \\
& 284868817499929005000 Y^6 + 2474446523044839564375 Y^4 - 9797539843874926946250 Y^2 + 711575050142526766875) T^{10} + \\
& 60580010182426875 Y^{10} + (8955765 Y^{22} + 3796555455 Y^{20} + 781214825475 Y^{18} + 73798662229425 Y^{16} + 3320791358519250 Y^{14} + \\
& 131842615029441750 Y^{12} + 4001251919029611750 Y^{10} + 38622239875976321250 Y^8 + 354175782842632235625 Y^6 - \\
& 1918410303332196253125 Y^4 - 1751845493630807465625 Y^2 + 9443971835072962228125) T^8 + 225021251512378125 Y^8 + \\
& (331695 Y^{24} + 174216420 Y^{22} + 40774449870 Y^{20} + 4511008624500 Y^{18} + 271665478688625 Y^{16} + 12732511726557000 Y^{14} + \\
& 375130032565018500 Y^{12} + 4045763811379941000 Y^{10} + 46685866420475690625 Y^8 + 17034748127560012500 Y^6 + \\
& 644222760196600068750 Y^4 + 3366662881162066762500 Y^2 + 898711974965844309375) T^6 + 50098108080234375 Y^6 + \\
& (8505 Y^{26} + 5372325 Y^{24} + 1416167550 Y^{22} + 180484519950 Y^{20} + 13304000185875 Y^{18} + 682841792091375 Y^{16} + \\
& 20712824439772500 Y^{14} + 255790716490732500 Y^{12} + 3468407818261719375 Y^{10} + 16693527887869021875 Y^8 + 48029919060345468750 Y^6 + \\
& 240167299660771218750 Y^4 - 115468740156070546875 Y^2 + 17221204161424265625) T^4 + 67806897644390625 Y^4 + \\
& (135 Y^{28} + 100170 Y^{26} + 29387925 Y^{24} + 4246092900 Y^{22} + 358633184175 Y^{20} + 19028361381750 Y^{18} + 581147239609125 Y^{16} + \\
& 7773885322875000 Y^{14} + 126384813847648125 Y^{12} + 1109621551203033750 Y^{10} + 3306804953883834375 Y^8 + 12758673814194262500 Y^6 + \\
& 2447767199204578125 Y^4 + 2944864928980406250 Y^2 + 295212212120109375) T^2 + 5881515673359375 Y^2 + 19937341265625.
\end{aligned}$$