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Microslip Induced Damping in the Contact of Nominally Flat Surfaces with Geometric Defects

Noussa Bouchaala, Jean-Luc Dion, and Nicolas Peyret

In this chapter, a rheological contact model (the EGM) is developed in order to quantify the energy dissipated by microslip in a jointed interface. The proposed rheological contact model is based upon a statistical description of contact between asperities. The key assumption for this model is that the coefficient of friction between the nominally flat surfaces is constant and that friction is the only source of energy dissipation. Measurements of static normal load and dynamic tangential load without any coupling between these two directions are used to inform and guide the model development.

19.1 Historical Perspectives on Dissipation Due to Microsliding

For many industrial applications in which the products are designed for dynamic solicitation (shock and vibration excitation), the vibration amplitudes of mechanical systems are not well predicted during the design phase. The source of inaccuracy in prediction of the vibration amplitudes is due to the lack of understanding of how to predict the amount of energy dissipated by an interface. Current approaches require that models be calibrated from measurements of existing systems, which precludes the prediction of the response of a system before it is fabricated for the first time.

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Thus, the ultimate goal of joints modeling is to predict the dynamic properties (mode shapes, natural frequencies, and damping in particular) of a jointed system accurately.

19.1.1 Sources of Energy Dissipation

The sources of damping in assembled structures are classified into two categories: material damping (which is often low) and damping in joints (which is more difficult to quantify due to its dependence on vibration level). Material damping, while difficult to model in inelastic solids, is typically low and easily modeled in engineering metals, which are the primary material of concern in this work. Damping due to joints, however, is significantly more difficult to model due to the complex interactions that occur at the interface surfaces (including wear, plasticity, etc.). Consequently, the measurement and prediction of damping in joints is an active research area (Le Loch 2003; Caignot et al. 2005).

In assembled structures, the damping is due to both macroslip (Berthillier et al. 1998; Poudou and Pierre 2003) (i.e., the bulk movement of the entire interface) and microslip (Goodman and Klumpp 1956; Beards and Williams 1977) (i.e., the relative motion of sub-elements of the interface). In order to study the damping due to both microslip and macroslip, a number of different experimental setups have been developed (see, for instance, Chap. 5). One experimental setup, in particular, is a clamped beam with a longitudinal interface (see Goodman and Klumpp 1956 and Fig. 19.1).

19.1.2 Perspectives on Dissipation Due to Microslip

Contact between two bodies, either in motion or stationary, is a phenomenon that all interacting parts of a mechanism are subjected to. Regardless of the condition of the surface finish (whether cut, or polished to a mirror-like smoothness), contact at the nano- and microscale is rough. Often, a relative movement between the elements in contact occurs producing microslip at the interface of contact. Such slip should be well studied to evaluate frictional forces induced on the surface. Thus, the relative motion at the interface of a contact is a source of friction that is dependent upon the area of contact engaged in microslip, which plays an important role in energy dissipation.

As the adhesion area and microslip zone are not well known a priori, it should be obtained from experiments. This kind of problem is referred to in the literature as incipient sliding or quasi-static contact. The problem with partial slip was addressed for the first time by Cattaneo (1938). Cattaneo considers the case of quasi-static contact of two spheres with the same elastic properties, loaded normally and tangentially. In the absence of microslip, Cattaneo shows that the tangential force

Fig. 19.1 A press-fit joint subjected to a clamping pressure p and a vertical shear load F . (a) A bolted structure—A free-free beam with a lap joint subjected to an axial load F . (b) A press-fit joint subjected to a clamping pressure p and a vertical shear load F . (c) A lap-shear joint subjected to a clamping pressure p and an axial load F

is expected to generate an infinite tangential traction along the contact, which is physically inadmissible. So under the action of a tangential force, even very small, microslip is inevitable at the contact edges. Cattaneo assumes that the tangential force is equal to the normal force multiplied by the coefficient of friction, and the elliptical contact area is divided into two parts:

- Elliptical central area in which there is no relative movement between surfaces and where the tangential traction (tension) $q(x)$ satisfies the equation $q(x) < \mu p(x)$
- An annular-elliptical zone of microslip where $q(x) = \mu p(x)$

This decomposition leads to a tangential traction q , shown in Fig. 19.2.

Building on the results of Cattaneo (1938), Mindlin investigated the compliance of two perfectly smooth elastic spheres, loaded normally and tangentially (Mindlin 1949). Mindlin determined the distribution of tangential tractions (Fig. 19.3) assuming that both bodies have the same geometry and elastic properties. The results from both (Cattaneo 1938; Mindlin 1949) serve as a basis for modeling the contact of asperities.

Fig. 19.2 Partial slip distribution of tangential traction by Cattaneo (1938)

Fig. 19.3 Distribution of normal traction p and tangential traction q on the surface (Mindlin 1949)

19.1.3 Contact of Asperities

For contact between rough surfaces, Greenwood and Williamson (1966) proposed a rough model, using several assumptions including:

- The asperities are spherical, with the same mean curvature ρ at the top.
- Asperities are sufficiently far apart to behave independently.
- The heights of asperities follow a probability distribution $\varphi(y_i)$.

- Individual behavior of each asperity can be described by the Hertz theory (Hertz 1882; Johnson 1985).

This statistical representation for contact along an interface has been extensively developed over the last 50 years (for instance, see the review presented in Chap. 18). In what follows, this branch of contact modeling is further extended to study the energy dissipation within a jointed interface.

Therefore, the aim of this chapter is to quantify the dissipated energy by microsliding using both experimental and model based approaches. In Sect. 19.2, the experimental procedure is presented and experimental results are discussed. In Sect. 19.3, a mathematical model is developed considering the hypotheses of Greenwood and Williamson (1966) for the contact between two nominally flat surfaces. The energy dissipated and the damping ratio are determined in Sect. 19.4. Numerical results are presented, discussed, and compared with those obtained experimentally.

19.2 Tribometer and Measurements

19.2.1 Tribometer Set

In order to perform accurate measurements, a tribometer with a hydraulic actuator is used. This kind of tribometer is described in Dion et al. (2009). The test fixture allows uncoupling normal and tangential loads over a wide frequency bandwidth to ensure good quality of measurements and test conditions (Fig. 19.4). This tribometer allows obtaining at 200 Hz and 1–100 μm displacement range, inducing a 1.2–120 mm/s velocity range.

Fig. 19.4 Global description of the tribometer

Fig. 19.5 The sample in allied aluminum Al 2017 machined by milling

The studied surface (approximately 2 cm^2) is a small planar contact (Fig. 19.4). The normal static load F_n varies between 100 and 5000 N while the tangential load F_t is dynamic and varies between -5000 N and $+5000 \text{ N}$. The studied samples shown in Fig. 19.5 are in allied aluminum Al 2017 machined by milling. For this sample, the roughness R_a is lower than $0.4 \mu\text{m}$ and the flatness error is lower than 0.02 mm (see Fig. 19.6). The effective contact area (measured after the test) is estimated to 10% of the apparent contact area with 2000 N normal load. For all the tests, the hydraulic jack movements are displacement controlled with the feedback signal of the internal displacement transducer (LVDT) (Fig. 19.4). Here, it is assumed that there is no coupling between normal and tangential loads. When the dynamic tangential load is applied, the static normal load keeps its nominal value with a 2% maximum deviation that stems from the dynamic tangential load. The displacement excitation is controlled and assumed to be sinusoidal. The harmonic ratio (between the fundamental and the 3rd harmonic) is around 5% in the worst case.

19.2.2 Experimental Result

The evolution of the normalized load T/N versus the tangential displacement is depicted in Fig. 19.7. This type of representation is often used to show a contact's dissipative behavior. The area inside the curve is the dissipated energy during microslip per cycle. The nature of the behavior (linear or not, dissipative or not) is clearly shown through the shape of the curve. The quasi-horizontal parts of the curve are indicative of macroslip and the oblique parts represent the tangential stiffness.

Fig. 19.6 Roughness of the surface. (a) Position along surface, mm. (b) Probability of asperity heights, %

19.3 Microcontact Model

Consider a contact between a plane and a nominally flat surface covered with a large number of asperities. It is assumed that all asperity summits are spherical with the same radius ρ and that their heights vary randomly $\varphi(y_i)$. Figure 19.8 shows schematically the considered type of contact.

19.3.1 Normal Distribution of the Load on the Asperities

The contact model between an individual spherical asperity and a rigid plane is shown in Fig. 19.9. It is assumed that the elastic proprieties of the contacting bodies

Fig. 19.7 Slipping behavior under normalized load T/N versus tangential displacement

Fig. 19.8 Contact between a rough surface and a rigid plane

Fig. 19.9 The contact model for a single asperity

are identical to an equivalent elastic material on a rigid plane (Greenwood and Williamson 1966). The frictional load is parallel to the x -axis.

The behavior of an individual asperity can be derived from the Hertzian equations. For the contact between a sphere of radius ρ and a rigid plane, the contact radius a_i , area A_i , and load N_i can be expressed in terms of the compliance δ_{ni} by Greenwood and Williamson (1966), Johnson (1985)

$$a_i = \sqrt{\rho\delta_{ni}} \quad (19.1)$$

$$A_i = \pi\rho\delta_{ni} \quad (19.2)$$

$$N_i = \frac{4}{3}\sqrt{\rho}E^*\delta_{ni}^{3/2}. \quad (19.3)$$

Here, E^* is a composite modulus of elasticity given by

$$\frac{1}{E^*} = \frac{1 - \nu_1^2}{E_1} + \frac{1 - \nu_2^2}{E_2}, \quad (19.4)$$

where ν and E are Poisson's ratio and Young's modulus, with the subscripts referring to the two bodies in contact. For a distance δ_n between the rigid plane and the mean plane of the rough surface (Fig. 19.8), there will be contact at any asperity whose height is greater than δ_n . Thus, the probability of contact at any given asperity of height y_i is

$$\text{Prob}(y_i > \delta_n) = \int_{\delta_n}^{\infty} \varphi(y_i)dy_i. \quad (19.5)$$

The total number of asperities is $N_a = \rho_a S_a$, where ρ_a is the density of asperities distributed over the apparent area of contact S_a . The number of asperities in contact is given by Greenwood and Williamson (1966)

$$n_a = N_a \int_{\delta_n}^{\infty} \varphi(y_i)dy_i. \quad (19.6)$$

The total contact area is expressed by

$$S = \pi N_a \rho \int_{\delta_n}^{\infty} (y_i - \delta_n) \varphi(y_i) dy_i. \quad (19.7)$$

For the compliance $\delta_{ni} = y_i - \delta_n$ (the distance over which points outside the deforming zone move together during the deformation), the total load supported by asperities is expressed as (Greenwood and Williamson 1966)

$$N = \frac{4}{3} N_a E^* \sqrt{\rho} \int_{\delta_n}^{\infty} (y_i - \delta_n)^{3/2} \varphi(y_i) dy_i. \quad (19.8)$$

Fig. 19.10 Contact area

19.3.2 Distribution of Tangential Load on the Asperities

Consider an asperity in contact with the plane submitted first to a constant normal force N_i then to a tangential displacement δ_{ti} . Two slip conditions can be distinguished as partial slip and total slip in what follows.

19.3.2.1 The Partial Slip Condition

The contact area is split into a stick zone and slip zone (Fig. 19.10). The maximum tangential force $T_{i\max}$ does not exceed in absolute value the product of the normal force by the coefficient of friction $T_{i\max} < \mu N_i$.

The stick region is the circle of radius c whose value can be found from the magnitude of the tangential force

$$\frac{c}{a_i} = \left(1 - \frac{T_i}{\mu N_i}\right)^{1/3}. \quad (19.9)$$

The force displacement relationship for an individual asperity is given by Gallégo (2007)

$$T_i = \mu N_i \left(1 - \left(1 - \frac{16a_i\delta_{ti}}{3\mu N_i G^*}\right)^{3/2}\right), \quad (19.10)$$

where G^* is a composite shear modulus

$$\frac{1}{G^*} = \frac{2 - \nu_1}{G_1} + \frac{2 - \nu_2}{G_2}. \quad (19.11)$$

The tangential force has maximum $T_i = \mu N_i$ for total slip. Correspondingly, from Eq. (19.10), the maximum tangential deflection before the inception of sliding is

$$\delta_{Li} = \frac{3}{16} \frac{G^* \mu N_i}{a_i}. \quad (19.12)$$

19.3.2.2 The Total Slip Condition

In this state, there is no area that is permanently adhered. During the cycle, the maximum tangential force reaches the absolute product of the normal force by the coefficient of friction $T_{i\max} = \mu N_i$. From Johnson (1985), the solutions of a circular contact initially charged by constant normal force P and subjected to a tangential load Q_x ($Q_x < \mu P_0$) oscillating between the values $\pm Q^*$ are given (see Fig. 19.11).

During unloading (between A and C), the distribution of tangential load on the asperities is (Gallégo 2007)

$$T_{id} = 2\mu N_i \left(\left(\frac{1}{2} \frac{16a_i\delta_{ti}}{3\mu N_i G^*} + \left(1 - \frac{T_{i\max}}{\mu N_i} \right)^{2/3} + 1 \right)^{3/2} - 1 \right) - T_{i\max}. \quad (19.13)$$

The situation at $Q_x = -Q^*$ is identical with that at $Q_x = Q^*$, except for the reversal of sign. Hence, between (C and A) the distribution of tangential load on the asperities then becomes (Gallégo 2007)

Fig. 19.11 Load-displacement cycle (Johnson 1985)

$$\begin{aligned}
T_{ic} &= -T_{id}(-\delta) \\
&= -2\mu N_i \left(\left(-\frac{1}{2} \frac{16a_1\delta_{ti}}{3\mu N_i G^*} - \left(1 - \frac{T_{i\max}}{\mu N_i} \right)^{2/3} - 1 \right)^{3/2} - 1 \right) - T_{i\max}.
\end{aligned} \tag{19.14}$$

In Greenwood and Williamson (1966), a model based on a statistical distribution of asperities in contact in the state of partial sliding is proposed. In order to generalize the Greenwood model for damping in an assembly, stick, partial slip, and total sliding have to be modeled with independent initial conditions and a standalone set of equations for each asperity Eqs. (19.15)–(19.17).

If $\delta_{ti\max} > \delta_{Li}$ (total slip), the maximum tangential force reaches the absolute product of the normal force by the coefficient of friction $T_{i\max} = \mu N_i$ and the asperity moves by an amount $\delta_0 = \delta_{ti\max} - \delta_{Li}$. Thus, Eqs. (19.10), (19.13), and (19.14) are recast as

$$T_i = \begin{cases} \mu N_i \left(1 - \left(1 - \frac{16a_i\delta_{ti}}{3\mu N_i G_{eq}} \right)^{3/2} \right), & \delta_{ti} < \delta_{Li} \\ \mu N_i, & \delta_{ti} \geq \delta_{Li} \end{cases} \tag{19.15}$$

$$T_{id} = \begin{cases} 2\mu N_i \frac{1}{2} \left(\frac{16a_i(\delta_{ti} - \delta_0)}{3\mu N_i G_{eq}} + \left(1 - \frac{T_{i\max}}{\mu N_i} \right)^{2/3} + 1 \right)^{3/2} - 1) + T_{i\max}, & \delta_{ti} > \delta_0 - \delta_{Li} \\ -\mu N_i, & \delta_{ti} \leq \delta_0 - \delta_{Li} \end{cases} \tag{19.16}$$

$$T_{ic} = \begin{cases} -2\mu N_i \frac{1}{2} \left(\frac{16a_i(\delta_{ti} + \delta_0)}{3\mu N_i G_{eq}} - \left(1 - \frac{T_{i\max}}{\mu N_i} \right)^{2/3} - 1 \right)^{3/2} - 1) - T_{i\max}, & \delta_{ti} < \delta_{Li} - \delta_0 \\ -\mu N_i, & \delta_{ti} \geq \delta_{Li} - \delta_0 \end{cases} \tag{19.17}$$

Notice that this EGM allows partial slip and total sliding for two asperities in the same interface.

19.4 Model Properties

It is assumed that the coefficient of sliding friction μ between the surfaces is constant and that dry friction is modeled by Coulomb's law. In accordance with experimental results, numerical simulations will be performed with the following material data: $\mu = 0.55$ and $E_1 = E_2 = 69$ GPa.

19.4.1 Changing Phases for a Single Asperity

In this section, an asperity in contact with the rigid plane is compressed by a constant normal force N_i parallel to the y-axis (Fig. 19.9), to which a tangential displacement δ_{ti} oscillating is subsequently applied.

19.4.1.1 Oscillating Tangential Displacement with a Constant Amplitude

First, an oscillating tangential displacement with a constant amplitude $\pm\delta_{ti\max}$ is considered. The contact radius and the contact area due to N_i are held constant and as given by Hertz. Figure 19.12 shows the evolution of the tangential displacement versus time.

The first application of δ_{ti} in a positive direction $\dot{\delta}_{ti} > 0$ causes microslip in the annulus $c \leq r \leq a_i$. The tangential force is given by Eq. (19.10), and shown by the curve OA in Fig. 19.13. Keeping the normal force constant, the tangential force is increased from zero and the stick region decreases in size according to Eq. (19.9).

At point A in Fig. 19.12, the tangential displacement begins to decrease $\dot{\delta}_{ti} < 0$, which is equivalent to the application of a negative increment in δ_{ti} . During unloading, the tangential force is given by Eq. (19.13), and shown by the curve ABC in Fig. 19.13. The slip region is then defined by Gallégo (2007)

$$\left(\frac{c}{a_i}\right)^3 = \frac{1}{2} \left[1 + \left(\frac{c_*}{a_i}\right)^3 \right], \quad (19.18)$$

where c_* is the value of c in A.

Fig. 19.12 The loading path for the constant amplitude case

Fig. 19.13 Tangential force evolution according to the tangential displacement (partial slip)

At point C, when the tangential displacement is completely reversed, substituting $\delta_{ti} = -\delta_{ti\max}$ in Eq. (19.14) gives $T_{ic} = T_{i\max}$. Thus, original slip is covered by the reversed slip and the state achieved is a complete reversal of that at $\delta_{ti} = \delta_{ti\max}$. Further loading leads to a series of states similar to unloading from $\delta_{ti} = \delta_{ti\max}$, but of opposite sign, as depicted by the curve CDA in Fig. 19.13.

In fact, it is shown in what follows that the effect of a tangential displacement with a magnitude lower than the limit deflection δ_{Li} does not give rise to a total slip motion but, nevertheless, induces a partial slip referred to as slip or microslip. Conversely, when $\delta_{ti\max} > \delta_{Li}$, the tangential force increases from zero to a limiting value $T_{i\max} = \mu N_i$, the asperity moves by an amount $\delta_0 = \delta_{ti\max} - \delta_{Li}$, and the stick region dwindles to a single point at the origin resulting in the bodies being on the verge of sliding. Taking into account Eqs. (19.15)–(19.17), the hysteretic force–deflection relation for a contact is shown in Fig. 19.14.

Keeping N_i constant and increasing the amplitude of the tangential displacement per iteration (Fig. 19.15a), the hysteretic force–deflection relations for a contact are shown in Fig. 19.15b.

19.4.1.2 Oscillating Tangential Displacement with Variable Amplitude

The second case considered is the case where the tangential displacement oscillates with variable amplitude acting along the x -direction, as shown in Fig. 19.16.

In this case, the force–deflection relationship between the relative tangential displacement δ_{ti} of the contact surface and the corresponding tangential load in the case of constant normal load are given by

Fig. 19.14 Tangential force evolution according to the tangential displacement (total slip)

Fig. 19.15 The (a) loading path, and (b) hysteretic force-deflection from partial slip to total slip

Fig. 19.16 The loading path for the variable amplitude case

- During the loading between O and A ($\dot{\delta}_{ti} > 0$)

$$T_i = \mu N_i \left(1 - \left(1 - \frac{16a_i \delta_{ti}}{3\mu N_i G^*} \right)^{3/2} \right). \quad (19.19)$$

- During the unloading between A and B ($\dot{\delta}_{ti} < 0$)

$$T_{id} = 2\mu N_i \left(\left(\frac{1}{2} \frac{16a_i \delta_{ti}}{3\mu N_i G^*} + \left(1 - \frac{T_{i\max}}{\mu N_i} \right)^{2/3} + 1 \right)^{3/2} - 1 \right) + T_{i\max}. \quad (19.20)$$

- During the reloading between B and C ($\dot{\delta}_{ti} > 0$)

$$T_{ic} = -2\mu N_i \left(\left(-\frac{1}{2} \left(\frac{16a_i (\delta_{ti} - \delta_0)}{3\mu N_i G^*} - \left(1 - \frac{\max |T_{id}|}{\mu N_i} \right)^{2/3} - 1 \right)^{3/2} \right) - 1 \right) - \max |T_{id}|, \quad (19.21)$$

where

$$\delta_0 = \delta_{ti}(B) - -\delta_{Li} + \delta_{Li} \left(1 - \frac{\max |T_{id}|}{\mu N_i} \right)^{2/3}, \quad (19.22)$$

and $\delta_{ti}(B)$ is the value of δ_{ti} in B.

- During the unloading between C and D ($\dot{\delta}_{ti} < 0$)

$$T_{id} = 2\mu N_i \left(\left(\frac{1}{2} \left(\frac{16a_i (\delta_{ti} + \delta_0)}{3\mu N_i G^*} + \left(1 - \frac{T_{ic \max}}{\mu N_i} \right)^{2/3} + 1 \right)^{3/2} \right) - 1 \right) + T_{ic \max}, \quad (19.23)$$

with

$$\delta_0 = \delta_{Li} - \delta_{Li} \left(1 - \frac{\max(T_{ic})}{\mu N_i} \right)^{2/3} - \delta_{ti}(C), \quad (19.24)$$

and $\delta_{ti}(C)$ is the value of δ_{ti} in C.

If the limit tangential deflection δ_{Lt} (total slip) is reached, the force–deflection relationships during unloading T_{id} and reloading T_{ic} for an individual asperity are given by Eqs.(19.16) and (19.17). According to Eqs.(19.19)–(19.21), (19.23), (19.16), and (19.17), the corresponding hysteretic force–deflection relations for a contact are shown in Fig. 19.17.

19.4.2 Case of N Asperities

In this section, a Gaussian (or normal) distribution of asperity heights $\varphi(y_i)$ is used. Several experimental results (Greenwood and Williamson 1966) show that for many

Fig. 19.17 Hysteretic force–deflection from partial slip to total slip

Fig. 19.18 (a) Normal distribution of asperity heights, and (b) cumulative distribution function

surfaces the height distribution is Gaussian to a very good approximation. The probability density function of a Gaussian distribution (see Fig. 19.18) is given by

$$\varphi(y_i) = \frac{1}{\sigma \sqrt{2\pi}} e^{-(y_i - m)^2 / 2\sigma^2}, \quad (19.25)$$

where parameter m (location of the peak) is the mean and σ^2 is the variance (the measure of the width of the distribution). The cumulative distribution function (Fig. 19.18b) is

$$\varphi(y_i) = \frac{1}{2} \operatorname{erf} \left(\frac{1}{\sqrt{2}} \frac{y_i - m}{\sigma} \right). \quad (19.26)$$

The total normal load N applied to the contact between a plane and a nominally flat surface (Fig. 19.8) can be expressed as the sum of each elementary normal load on each asperity N_i

$$N = \sum N_i. \quad (19.27)$$

Fig. 19.19 Slipping behavior under tangential force T versus tangential displacement δ_t

Keeping N constant, the loading cycle for the tangential displacement δ_t oscillates between $\delta_{t\max}$ and $-\delta_{t\max}$. The total tangential force T that can be supported by N_a asperities is

$$T = \sum T_i. \quad (19.28)$$

The evolution of total tangential force T versus tangential displacement δ_t is shown in Fig. 19.19. The shape of this curve is very similar to that obtained experimentally (see Fig. 19.7).

19.4.3 Relations Between the Iwan, Coulomb, and Extended Greenwood Models

In this section, N is kept constant and the total number of asperities N_a in contact with the flat surface is varied. The hysteretic force–deflection relations for a contact are depicted in Fig. 19.20. It is interesting to mention that the variation of the total number of asperities influences significantly the load–deflection curve, although with an increase of the parameter N_a the stiffness characteristics of the model increase. When the number of asperities in contact increases, the EGM tends to the Coulomb friction model. Notice that this result is different from that obtained by the Iwan model (Segalman 2005; Argatov and Butcher 2011). The Iwan model is based on several cells composed of a stiffness and Coulomb friction model. When the number of cells increases, the Iwan model is close to the EGM composed with a single asperity (Fig. 19.21).

Fig. 19.20 Evolution of Extended Greenwood Model (EGM) against the number of asperities

Fig. 19.21 Likeness between the Coulomb model, Iwan model, and EGM

19.4.4 *Extended Greenwood Model Identification*

In Fig. 19.22, the theoretical model is compared with experimental results. It is observed that the shape of the curve obtained by the theoretical model is very similar to that obtained experimentally.

19.4.5 *Damping Ratio*

This section aims to define the dissipated energy in order to compute the damping ratio. The area enclosed by the curves T_{id} [Eq.(19.16)] and T_{ic} [Eq.(19.17)]

Fig. 19.22 The theoretical model and measured result for the material aluminum allied Al 2017

gives the energy dissipation E_d during microslip per cycle by integration over displacement limits:

$$E_d = \int_{-\delta_{t\max}}^{\delta_{t\max}} T_{ic} - T_{id} d\delta_t. \quad (19.29)$$

The curve in Fig. 19.23 shows the evolution of dissipated energy E_d as a function of the tangential displacement δ_t . The energy dissipated by the friction increases as the magnitude of the tangential displacement increases. It can thus be concluded that the dissipated energy depends strongly on the amplitude of the displacement. This dependence induces nonlinear effects, which are shown clearly in Fig. 19.23 by the fact that the curve is parabolic.

The damping ratio ξ can be defined by the ratio between the dissipated energy E_d and the supplied energy E_s

$$\xi = \frac{4}{\pi} \frac{E_d}{E_s}, \quad (19.30)$$

where $E_s = 4\delta_{t\max}T_{\max}$. Figure 19.24 shows the evolution of ξ as a function of the tangential displacement δ_t .

It is noticed that the damping ratio increases as the tangential displacement increases. Figure 19.24 also shows the nonlinear character of this evolution.

Fig. 19.23 Dissipated energy as a function of tangential displacement

Fig. 19.24 Damping ratio as a function of tangential displacement

19.5 Summary of the Extended Greenwood Model

In this chapter, an extension of the Greenwood model is proposed (the Extended Greenwood Model, EGM) that is based on a statistical distribution of asperities in contact between two assembled parts. These micro-contacts produce a damping effect in both total sliding and partial sliding. This new model is studied and identified with experimental results. The numerical results show that for a cyclic

tangential displacement, the dissipated energy increases with the tangential displacement. The shape of the hysteretic force–deflection for a contact is very similar to that obtained experimentally.

References

- I.I. Argatov, E.A. Butcher, On the Iwan models for lap-type bolted joints. *Int. J. Non Linear Mech.* **46**, 347–356 (2011)
- C.F. Beards, J.L. Williams, The damping of structural vibration by rotational slip in joints. *J. Sound Vib.* **53**, 333–340 (1977)
- M. Berthillier et al., Blades forced response analysis with friction dampers. *ASME J. Vib. Acoust.* **120**, 468–474 (1998)
- A. Caignot et al., Prediction of damping in space launch vehicles using a virtual testing strategy, in *6th International Symposium on Launcher Technologies*, Munich, 2005
- C. Cattaneo, Sul Contatto di due Corpi Elastici: Distribuzione Locale Degli Sforzi. *Rendiconti dell'Accademia Nazionale dei Lincei* **27**, 342–348/434–436/474–478 (1938)
- J.-L. Dion et al., A new test bench for friction measurements and the evolution of the Lugre model to the frozen model, in *ASME International Design Engineering Technical Conferences IDETC/CIE*, San Diego, CA, 2009
- L. Gallégo, Fretting et Usure Des Contacts Mécaniques: Modélisation Numérique. Doctoral Dissertation. INSA, Villeurbanne, 2007
- L.E. Goodman, J.H. Klumpp, Analysis of slip damping with reference to a turbine blade vibration. *ASME J. Appl. Mech.* **23**, 421–429 (1956)
- J.A. Greenwood, J.B.P. Williamson, Contact of nominally flat surfaces. *Proc. R. Soc. Lond. Ser. A* **295**, 300–319 (1966)
- H. Hertz, Über die Berührung Fester Elastischer Körper (On the contact of elastic solids). *J. für die Reine und Angewandte Math.* **92**, 156–171 (1882)
- K.L. Johnson, *Contact Mechanics* (Cambridge University Press, Cambridge, 1985)
- S. Le Loch, Modélisation et Identification de l'Amortissement Dans les Structures Spatiales. Doctoral Dissertation. ENS de Cachan; LMT-Cachan, Cachan, 2003
- R.D. Mindlin, Compliance of elastic bodies in contact. *ASME J. Appl. Mech.* **16**, 259–268 (1949)
- O. Poudou, C. Pierre, Hybrid frequency-time domain methods for the analysis of complex structural systems with dry friction damping, in *44th AIAA/ASME/ASCE/AHS/ASC Structures, Structural Dynamics, and Materials Conference*, Norfolk, VA, 2003
- D.J. Segalman, A Four-parameter Iwan model for lap-type joints. *ASME J. Appl. Mech.* **72**, 752–760 (2005)