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Epidemiological Feedbacks Affect Evolutionary Emergence of Pathogens

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abstract: The evolutionary emergence of new pathogens via mutation poses a considerable risk to human and animal populations. Most previous studies have investigated cases where a potentially pandemic strain emerges through mutation from an initial maladapted strain (i.e., its basic reproductive ratio \( R_0 \leq 1 \)). However, an alternative (and arguably more likely) cause of novel pathogen emergence is where a “weakly adapted” strain (with \( R_0 \approx 1 \)) mutates into a strongly adapted strain (with \( R_0 \gg 1 \)). In this case, a proportion of the host susceptible population is removed as the first strain spreads, but the impact this feedback has on emergence of mutated strains has yet to be quantified. We produce a model of pathogen emergence that takes into account changes in the susceptible population over time and find that the ongoing depletion of susceptible individuals by the first strain has a drastic effect on the emergence probability of the mutated strain, above that assumed by just scaling the reproductive ratio. Finally, we apply our model to the documented emergence of Chikungunya virus on La Réunion Island and demonstrate that the emergence probability of the mutated strain was reduced approximately 10-fold, compared to models assuming that susceptible depletion would not affect outbreak probability. These results highlight the importance of taking population feedbacks into account when predicting disease emergence.

Keywords: epidemiology, evolution, outbreaks, pathogen emergence, changing population sizes, Chikungunya virus.

Introduction

The emergence of new pathogens arising from preexisting zoonotic or human strains poses a major worldwide health risk. For humans, the most well-documented examples include pathogens spilling over from zoonotic reservoirs (Wolfe et al. 2007), but this is not the only mechanism that can lead to emergence. An existing pathogen could be contained with a low rate of spread but then create a stronger outbreak, either due to the pathogen mutating or to environmental change. For example, there exists evidence that following a vaccination program, new pathogenic strains can arise that are evolved so are resistant to existing treatment (Gandon and Day 2008). Pathogen emergence also poses a severe risk to livestock populations (e.g., through foot and mouth disease; Woolhouse et al. 2012), and plant crop populations (Fargette et al. 2006). It is therefore important to ascertain when spillovers and emergence of new outbreaks are likely to occur, especially from preexisting strains, in order to monitor and control their spread (Arinaminpathy and McLean 2009; Pérez-Reche et al. 2012).

Stochasticity has long been known to be at the heart of emergence processes because in the initial stages of an outbreak the number of infected hosts is very low. In a deterministic model, the spread of a pathogen strain in a host population is governed solely by the number of secondary infections it generates, which is the basic reproductive ratio \( R_0 \) (Anderson and May 1991). In stochastic models, this is not the case as the number of secondary infections caused by each infected host is drawn from a distribution. For instance, if the duration of infection is exponentially distributed and contacts follow a Poisson process, then the probability of emergence equals \( 1 - 1/R_0 \) (Diekmann and Heesterbeek 2000). Additionally, the role of pathogen evolution and migration in causing new outbreaks in novel populations has been recognized and widely studied (recently reviewed in Gandon et al. 2013). Previous models highlighted the important fact that even benign strains can be dangerous, as even though they are due to become extinct, they may persist in large populations long enough to give rise to well-adapted mutants that can subsequently cause an outbreak (Antia et al. 2003; Iwasa et al. 2003, 2004). The effect of pathogen life history (André and Day 2005) and population structure (Alexander and Day 2010; Kubiak et al. 2010) have also been
modeled, as well as the effect of host heterogeneity and assortative mating (Yates et al. 2006).

Importantly, previous models have focused on the case where the pandemic (well-adapted) strain, with an $R_0 > 1$, emerges through mutation from a maladapted strain, with an $R_0 < 1$, which is bound to become extinct rapidly (see table 1 for the nomenclature we use to denote general $R_0$ values for different strains). However, this is not the only scenario that can lead to a pandemic, nor arguably the likeliest. An alternate scenario, which has received less attention, is where an intermediately adapted strain would first create an initial outbreak, which would be limited in spread as it would have a low $R_0$ close to 1. A mutation could then arise in one individual that would subsequently increase the $R_0$ of the pathogen to a much higher level, creating a more potent outbreak. This type of emergence, from a limited to a large outbreak, plays an important role in the transferring of zoonotic pathogens into complete human agents (Wolfe et al. 2007). This scenario is also an example of “evolutionary rescue” (Gonzalez et al. 2013), where evolution is needed to prevent quick extinction of the weaker strain, which can also be important regarding the emergence of novel drug-resistant strains at the intra-host, cellular level (Alexander and Bonhoeffer 2012).

Although this scenario is more likely to occur for many microparasitic infections (because the initial and the mutant strain are likely to be antigenically close), it is also more difficult to capture mathematically because it leads to the violation of one of the important simplifying assumptions made by earlier models. When a pathogen mutates from $R_0 < 1$ to $R_0 > 1$, it is safe to assume that the number of hosts infected by the initial (maladapted) strain is negligible. However, if $R_0 > 1$ initially, then the susceptible population would, in general, reduce over time as individuals become immune or die out. This reduces the emergence probability of the second strain, as there are fewer susceptible individuals available to transmit the pathogen to. Furthermore, the initial strain might continue to spread for awhile, hence further depleting the pool of susceptible hosts available to the mutant strain. This process is likely to arise due to infection by the first strain rendering the host immune to the mutant strain (cross-immunity), which is the basis for vaccination (Keeling and Rohani 2007).

A model incorporating such population dynamics feedbacks is needed to allow the analysis of several outbreaks. For instance, mutations arising in the vector-borne Chikungunya virus around the Indian Ocean caused a new infection wave to arise, with a higher reproductive rate, from an initially smaller one where viruses had a lower reproductive rate (Schuffenecker et al. 2006). The first strain, which created a minor outbreak in May–June 2005 at La Réunion (Renault et al. 2007), seemed to have an $R_0$ of around 1, because while it did not greatly increase in frequency over time, it was maintained in the population at a low frequency. The second strain, which appears to consistently differ from the first by two point mutations (Schuffenecker et al. 2006), created a major outbreak in La Réunion over January and February 2006 (Renault et al. 2007). Further analyses revealed that this mutated strain was particularly well adapted to exploit the mosquito vector Aedes albopictus (Vazeille et al. 2007), the dominant vector on the island, infecting it in around 90% of cases, while experimental infections of vectors using the previous strain only had a success rate of around 20%. This effect most likely explains the increase in its $R_0$. Additionally, these virus mutations seem to have occurred independently in several distant populations (de Lamballerie et al. 2008), which underlines the importance of virus evolution in triggering further outbreaks. Finally, it is known that recovering from a Chikungunya infection generates a strong immunity, which seems to target both the initial and the mutated strain (Renault et al. 2007).

Another example is the so-called Spanish flu of 1918, which started with a mild first wave in summer 1918, before a second wave was triggered in August that caused millions of deaths (Frost 1919). However, it is unknown whether the more virulent second wave was caused due to the strain evolving or due to demographic or environmental changes (Méthot and Alizon 2014). Again, cross-immunity is thought to be strong for antigenically close influenza viruses (Ferguson et al. 2003). Modeling this evolutionary process can therefore provide insight into the possible causes of the onset of the second strain.

Finally, in a modeling study of dengue fever, Lourenço and Recker (2010) found that novel strains of the disease had their highest emergence probability when existing strains are at a low frequency. This is because invasion of new genotypes can be hampered by competition from existing strains, exemplifying how population feedbacks can prevent the spread of new strains, in a manner similar to the above examples.

<table>
<thead>
<tr>
<th>Reproductive ratio</th>
<th>Name</th>
<th>Properties</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_0 &lt; 1$</td>
<td>Maladapted</td>
<td>Guaranteed to become extinct unless mutation occurs</td>
</tr>
<tr>
<td>$R_0 = 1 + \xi$, $\xi \ll 1$</td>
<td>Weakly adapted</td>
<td>Can cause a large outbreak, but likely to become extinct by drift</td>
</tr>
<tr>
<td>$R_0 &gt; 1$</td>
<td>Strongly adapted</td>
<td>Almost certain to cause a major epidemic in the population</td>
</tr>
</tbody>
</table>
Here, we outline an analytical model to investigate the effect of epidemiological feedbacks on pathogen emergence. We derive the probability that, given an initial weakly spreading pathogen ($R_0$ close to but exceeding 1), it can mutate into a second pathogen with a much greater rate of spread ($R_0$). We form this probability via a two-step model. In the first stage, the initial pathogen spreads deterministically but can mutate into a new strain at any time before it goes extinct. The second stage calculates the probability that this second strain emerges, instead of becoming extinct by drift. We find that the ongoing depletion of the susceptible population by the initial strain drastically reduces the emergence probability, compared to classical branching process results that assume that the susceptible population remains fixed as the new strain emerges (Allen 2008). We produce analytical solutions for the probability of emergence in this scenario, which we show to be accurate when compared to stochastic simulations. Specifically, we derive an equation for the emergence probability for the second strain, while accounting for the feedback that causes continual depletion of the susceptible population (an effect often overlooked in emergence modeling), and show how this mechanism drastically decreases the emergence probability. Our model therefore highlights how epidemiological feedbacks can strongly affect emergence probabilities of emerging strains. Finally, we apply our model to the Chikungunya virus outbreak in La Réunion and show the severe reduction in emergence probability due to susceptible depletion, which could counteract the adaptive ability of the initial strain and limit the possibility for future outbreaks to arise.

Model Formulation and Analysis

Model Outline

In order to produce the probability of emergence of a mutated strain, we proceed as follows. A schematic of the process is outlined in figure 1, and table 2 outlines the notation used in this model. We first assume that an initial

Table 2: Glossary of notation

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Usage</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_0$</td>
<td>Basic reproductive ratio of first outbreak</td>
</tr>
<tr>
<td>$\Phi_e$</td>
<td>Basic reproductive ratio of second (mutated) outbreak</td>
</tr>
<tr>
<td>$b_1$, $b_2$</td>
<td>Transmission rate of first, second pathogen</td>
</tr>
<tr>
<td>$d_1$, $d_2$</td>
<td>Total removal rate of first, second pathogen</td>
</tr>
<tr>
<td>$\mu$</td>
<td>Mutation rate from first to second strain</td>
</tr>
<tr>
<td>$S$</td>
<td>Size of susceptible class (number of individuals)</td>
</tr>
<tr>
<td>$I_1$, $I_2$</td>
<td>Size of those infected with first, second pathogen</td>
</tr>
<tr>
<td>$R$</td>
<td>Size of removed class</td>
</tr>
<tr>
<td>$N$</td>
<td>Total host population size ($S + I_1 + I_2 + R$)</td>
</tr>
<tr>
<td>$Q$</td>
<td>Extinction probability in an nonequilibrium population for a single strain</td>
</tr>
<tr>
<td>$\Pi$</td>
<td>Extinction probability in an nonequilibrium population if a strain is already present</td>
</tr>
<tr>
<td>$P_{\text{em}}$</td>
<td>Overall probability of mutated strain emerging</td>
</tr>
</tbody>
</table>

act the adaptive ability of the initial strain and limit the possibility for future outbreaks to arise.

Figure 1: A schematic of the model and second-strain emergence possibilities. A, An adaptive mutation arises early on as the first strain is emerging (denoted by X). As there are enough susceptible individuals present (denoted by gray shading; the plus sign (+) indicates susceptible frequency when the second strain arises) then this strain can emerge into a stronger outbreak. B, The second strain appears later on and has less chance of emerging due to fewer susceptible individuals present. Therefore it is more likely to become extinct.
strain is spreading throughout the population with reproductive ratio $R_e$. Generally, this $R_e$ will be close to but exceeding 1; additionally, we assume that the epidemic is not lost in its early stages and generates a small outbreak. Therefore, the first strain will spread in a fairly deterministic manner and exists for long enough to potentially mutate into a new strain. Second, at any point in time during the emergence of this first strain, one of the hosts infected by this initial strain can transmit a pathogen that mutated into a new strain. This results in a larger reproductive ratio, $R > R_e$. The emergence of mutated strains therefore depends on a balance between the size of the initial outbreak at a certain time, which determines the overall probability of mutation, and there being enough susceptible hosts to enable the second strain to spread, while the first strain is still transmitting infection.

The second (mutated) strain can emerge in the host population with probability $P$. In traditional epidemic models, $P$ is equal to $1 - 1/\Phi_0$ (Allen 2008). However, this result assumes that the underlying host population is fully susceptible. This assumption is violated in this model in two ways. First, the initial strain is still spreading as the second strain emerges, using up the underlying susceptible population. Additionally, the second strain can appear at any time during the spread of the first strain (fig. 1); unless the second strain appears as the first strain is emerging, then the assumption of a fully susceptible population is also violated. Normally, the effects of a partially susceptible population are accounted for by using an “effective” reproductive ratio, $P = 1 - 1/\Phi_{0,eff}$ where $\Phi_{0,eff} = \Phi_0(S/N)$ (McCallum et al. 2001; Lloyd-Smith et al. 2005a). However, this term does not take epidemiological feedbacks into account due to ongoing susceptible depletion and will therefore overestimate the actual emergence probability. We will subsequently discuss an approximation for $P$ that can be used to provide an accurate emergence probability in this case, which accounts for both the susceptible population present when a new strain emerges and how it is affected by subsequent population feedbacks. Finally, by integrating these probabilities over the entire course of the initial epidemic, we obtain the overall probability of the second strain emerging and causing a major outbreak.

\begin{align}
\frac{dS}{dt} &= -b_s \frac{S}{N} I_s, \\
\frac{dI_s}{dt} &= \left(b_s \frac{S}{N} - d_s\right)I_s, \\
\frac{dR}{dt} &= d_s I_s,
\end{align}

where $S$, $I_s$, and $R$ are the absolute number of susceptible, infected, and either recovered and/or immunized individuals present at time $t$; $N$ is the total population size; $b_s$ is the transmission rate of new infection on contact; and $d_s$ is the recovery rate. Note that these equations sum to 0, indicating that the population size $N$ is constant over time (as $dN/dt = 0$). Also note that in the long-term, the initial and mutated pathogens will both become extinct, as $I_s$ goes to 0 if the susceptible population becomes too low to carry an epidemic. However, it still makes sense to discuss pathogens emerging as there is a certain time frame at the start of an epidemic when the pathogen reaches a high-enough frequency and spreads in a fairly deterministic manner (Allen 2008; Hartfield and Alizon 2013b). In order to track the deterministic spread of the first pathogen strain, an analytical form for $I_s$ as it changes over time is needed. However, it is not possible to solve equation (1) analytically to find $I_s$ as a function of $t$. To make progress, we follow the approach used in Hansen and Day (2011) and note that since the current number of susceptible hosts $S$ is a strictly decreasing function of time, then we can rewrite equations (1) as functions of $S$ instead. Specifically, by dividing equation 1b by equation 1a, we obtain:

$$\frac{dI_s}{dS} = \frac{N}{SR_o} - 1.$$  

(2)

Here, $R_o = b_s/d_s$ and is the basic reproductive ratio of the epidemic (Anderson and May 1991). Equation (2) makes explicit that if the population is fully susceptible ($N = S$), the epidemic can spread deterministically if $R_o > 1$. We can solve this differential equation with the condition $I_s(S = N) = I_0$ to obtain:

$$I_s(S) = (N - S) - \frac{N}{R_o} \log \left(\frac{N}{S}\right) + I_0.$$  

(3)

Normally, $I_0 = 0$; that is, if the population is fully susceptible, then no infected individuals exist. However, this formalization does not take into account the fact that if the epidemic escapes stochastic loss, then it will increase in frequency faster than predicted by the deterministic rate of change (eq. [2]). This is because there is a large stochastic effect on trait frequency when it is rare, and cases
where the trait increases in frequency faster than expected are more likely to lead to the new trait emerging. This is a well-known issue in population-genetic studies of emergence of new adaptive traits (Maynard Smith and Haigh 1974; Otto and Barton 1997; Barton 2000). To correct for this effect, it is sufficient to simply increase the initial frequency of the pathogen $I_0$ in order to account for this oversampling (Barton 1994), and to minimize the effects of drift while the trait is emerging. We set it to $5/\log(R_0)$, which is the number of infected individuals needed to make it unlikely ($P < .005$) that the strain is lost by drift in a large population (Hartfield and Alizon 2013b). Note that when we compared our model to simulations, this frequency was reduced to $1/\log(R_0)$ for $N = 100$, as otherwise the previous threshold would exceed $N$ if $R_0$ was small enough, due to this result primarily holding for large populations.

For a specific number of susceptible hosts $S$, a current infection can mutate with probability $\mu$ into a new strain; assuming that $\mu \ll 1$, so that it is rare for more than one new mutant to appear per generation, then the probability that a new strain appears by mutation is $\mu I(S)$. The new strain can then fully emerge and overcome stochastic loss with probability $\Pi(S)$. In order for this strain to never emerge at all, then at each step a mutant strain never emerges; the probability of this at a single time point is $1 - \mu I(S)\Pi(S)$. One minus this probability, multiplied for all time points, is the probability $P_{\text{mut}}$ that a mutant strain ultimately emerges. That is,

$$P_{\text{em}} = 1 - \prod_{S=S_{\text{min}}}^{S_{\text{mut}}} (1 - \mu I(S)\Pi(S)), \quad (4)$$

where $S_{\text{min}}$ is the minimum susceptible population needed to give a nonzero emergence probability of the mutant strain. If each probability $\Pi(S)$ is small, then we can approximate this product function by an exponential integral (see Hartfield and Otto 2011 for a similar derivation):

$$P_{\text{em}} \approx 1 - \sum_{S=S_{\text{min}}}^{S_{\text{mut}}} \exp(-\mu I(S)\Pi(S)) = 1 - \exp\left(-\sum_{S=S_{\text{min}}}^{S_{\text{mut}}} \mu I(S)\Pi(S)\right) \approx 1 - \exp\left(-\int_{S=S_{\text{min}}}^{S_{\text{mut}}} \mu I(S)\Pi(S)\right). \quad (5a)$$

To complete this derivation, we need to find an analytical form for $\Pi(S)$ and $S_{\text{min}}$, which we will analyze in turn.

**Probability of a Mutant Strain Emerging ($\Pi(S)$).**

In the appendix (and supplementary material S1, available online), we derive the form for the emergence probability of a mutant strain, given that the susceptible population is being depleted by a preexisting strain (strain 1):

$$\Pi(S) = \frac{\Phi_0 - I(S)R_0 + \Phi_1}{\Phi_0} \left[1 - \frac{N}{S} \left(1 - \frac{\Phi_0 - 1}{\Phi_0} e^{-(\Phi_0 - 1)/\Phi_0}\right)^{1/S} \right] \quad (6)$$

where $\Phi_0$ is the reproductive ratio of the mutant strain. This equation assumes that the rate at which an infection ends are approximately equal for both strains; we will show that for $R_c$ close to 1, this solution remains accurate, even if the recovery rates differ. The important thing to note is that not only is part of this solution proportional to $N/S$ (reflecting the growth rate $R_c$ decreasing by a fraction $S/N$ as susceptible individuals are removed), but it is also proportional to $1/(I_iR_c + \Phi_0)$. This highlights the fact that even as the second strain appears by mutation and spreads, the emergence probability is decreasing during this initial phase, as the susceptible population is reduced due to the continuing spread of the first strain. This formulation assumes complete cross-immunity is present between the original and mutated strains. It also assumes that the death rates for both strains are approximately equal, so that the final equation is only given as a function of reproductive ratios, which are easier to measure from empirical data. We will show that this equation to remain accurate if $R_c$ is close to 1, even if the death rates differ.

**Minimum Susceptible Level ($S_{\text{min}}$)**

The lowest limit of $S$ for the emergence of the mutant strain to be possible depends on which limit is attained first. Either the first strain $I_1$ exhausts itself (by running out of hosts to infect), therefore there are no infected individuals that can mutate into the second strain. This arises when equation (3) equals 0, which holds for

$$S_{\text{min,1}} = \frac{N}{R_c} W_\nu(-e^{-\nu(N+\lambda)/N}), \quad (7)$$

where $W_\nu$ is the Lambert W function (Abramowitz and Stegun 1970) and $I_i$, the initial frequency of the first strain. Note that this limit is determined solely by the reproductive ratio of the first strain ($R_c$). Alternatively, $S$ can drop low enough so that $\Pi$ falls below zero; that is, there are no longer enough susceptible individuals in the population that can carry a new epidemic if it appears. In this case, the lower limit for $S$ is

$$S_{\text{min,2}} = N\left[1 - \frac{\Phi_0 - 1}{\Phi_0} e^{-(\Phi_0 - 1)/\Phi_0}\right]. \quad (8)$$
In contrast, \( S_{\text{min},2} \) is determined solely by the reproductive ratio of the second, mutated strain (\( R_0 \)). Overall, the lower limit of integration \( S_{\text{min}} \) is the maximum out of \( S_{\text{min},1} \) or \( S_{\text{min},2} \); that is, either when the first epidemic exhausts itself or when there are no longer susceptible individuals present to carry a new infection, whichever limit is reached first.

Figure 2 displays \( S_{\text{min}} \), as a function of the reproductive ratios of both strains (\( R_0 \) and \( \Phi_0 \)). In general, we see that as \( R_0 \) increases, the limitation on emergence is caused by the burnout of the susceptible population by the first strain. What is unexpected is that the increase in the boundary between \( S_{\text{min},1} \) and \( S_{\text{min},2} \) is nonlinear as a function of \( R_0 \). This is due to the fact that not only are susceptible individuals being removed after the first strain clears (reducing emergence probability by a factor of \( S/N \) at a set timepoint) but also that the susceptible population continues to decrease as the second strain emerges because the first strain is still spreading. This nonlinearity with increased \( R_0 \) clearly illustrates how ongoing feedbacks, which are usually neglected in epidemiological models, lead to a larger, negative effect on pathogen emergence.

Note also that if \( R_0 \) is very close to 1 (less than 1.04 with the default parameter used in fig. 2), \( S_{\text{min},2} \) becomes more likely to determine the minimum susceptible population size \( S_{\text{min}} \) (i.e., \( S_{\text{min}} = S_{\text{min},2} \) in this parameter space), even though the first infection should not spread for a long time. This is due to the fact that our assumption of an increased \( I_0 \) value has important consequences for these small \( R_0 \) values, as the maintenance of weakly spreading strains by drift can create more opportunities for emerging strains to arise, compared to deterministic models where these pathogens quickly become extinct. However, this does not appear to make the analytical results inaccurate compared to simulations, as the high \( I_0 \) compensates for the fact that the infected population size drifts at low frequency (if it does not become extinct), which can create more frequent opportunities for adaptation. Furthermore, the maintenance of this weak strain at a low frequency, rather than having it rapidly spread, will not create large feedbacks that can deplete existing susceptible populations, which can be the case if initial \( R_0 \) is higher. This effect dissipates with increased population size, as drift effects are reduced in larger populations (see fig. S1 and supplementary material S2 for a similar plot but with \( N = 100,000 \)).

**Simulation Methods**

In order to test the accuracy of these solutions, we compare the analytical solution, as derived above in equation (5c), with simulation data produced using the Gillespie algorithm with tau-leaping approximations (Gillespie 1977, 2001) and a step size of \( \Delta t = 0.05 \). We chose this step size since it was accurate for larger population sizes; that is, the results did not significantly change with a smaller step size (see also Keeling and Rohani 2007), and it was not too expensive in terms of computational time. The step size was reduced to \( \Delta t = 0.01 \) if \( N = 100 \), as larger step sizes in small populations can overestimate the rate of change of each compartment (Keeling and Rohani 2007); simulations results were not strongly affected for \( N = 1,000 \) if \( \Delta t = 0.01 \) (see Mathematica, supplementary material S2). Simulation data was obtained based on 1,000,000 reintroductions of the first strain into a fully susceptible population (increased to 10,000,000 reintroductions for \( N = 50,000 \) and \( N_P = 0.001 \)). We looked at the case where the initial \( R_0 \) is low, ranging between 1 and 1.2, and can mutate into a more adapted strain with \( \Phi_0 \) equal to 1.2, 1.5, 1.8, or 2.5. For simplicity (unless stated otherwise), the removal rates for both strains (by this we mean the recovery rate) was set to 1, therefore the transmission rate was equal to the reproductive ratio. Since the long-term probability of extinction for both strains is 1 with SIR dynamics, we say that the second strain has “emerged” if it reaches its outbreak threshold, here set to \( 5/\log(\Phi_0) \) infected hosts. This threshold means that it subsequently has less than a 0.5% probability of becoming extinct by stochastic drift (Hartfield and Alizon 2013b). Note that the analytical solution (eq. [5c]) gives the emergence probability of a second strain given that the first strain has emerged. Therefore, we scale down our analytical simulation by \( 1 - 1/R_0 \) the emergence probability of the first strain in a fully susceptible population (Allen 2008), in order to account for the first strain emerging in the simulations. Simulations were written in C, and source code was deposited in the Dryad Digital Repository: http://dx.doi.org/10.5061/dryad.kj238 (Hartfield and Alizon 2013a).

**Comparison of Analytical Solutions with Simulation Data**

Plots of the main comparisons are provided in figure 3 (and fig. S2, supplementary material S2). For \( N = 10,000 \) and \( N = 50,000 \), it is seen that the analytical solution generally provides an accurate solution of emergence probability, although it slightly underestimates simulation results when \( R_0 > 1.1 \). This is because integration over all extinction probabilities as the first strain spreads as well as the second strain emergence probability both assume that these values change by a small amount per time step. This assumption is valid for \( R_0 \) close to 1 but is slightly

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1 Code that appears in the American Naturalist is provided as a convenience to the readers. It has not necessarily been tested as part of the peer review.
violated if larger due to the increased rate at which the first pathogen spreads and therefore by the increased propensity to mutate into a fitter strain. For smaller host population sizes ($N = 1,000$), results are generally accurate but tend to consistently slightly underestimate simulation results. This is probably due to increased stochastic effects affecting the spread of both the original and second pathogen due to the small population size. To account for these factors a fully stochastic analytical treatment should be implemented (Karlin and Taylor 1981), but this is complex for an SIR-type infection and appears to be intractable if considering more than one strain spreading (see Allen and Burgin 2000 for an example of how to formulate a fully stochastic model for a one-strain SIR epidemic). We also investigated the case where the transmission rates $b_i$ were fixed at 1 and the recovery rates varied to define the reproductive rates. We observed that simulation results were generally the same for $R_0 < 1.1$, where the original model is most accurate (figs. S3, S4; supplementary material S2).

It was also of interest to determine whether the solutions were accurate if the mutation rate $\mu$ was large, as this might have violated the assumption that only a single new strain can appear at a given time. Figure 4 shows results for $N\mu = 10$ with $N = 10,000$ and 50,000. As with smaller $\mu$ results, the analytical solution is accurate yet slightly underestimates simulation values for large $R_0$ values. Similar results were obtained for $N\mu = 0.1$ or 1 (fig. S5).

However, the analytical solution consistently underestimates simulations for $N = 1,000$ (for $N\mu = 0.1$ and 1), creating a large discrepancy in very small populations ($N = 100$; fig. S6). We interpret this result as arising due to stochastic forces (population drift) dominating over deterministic ones in driving the size of the infected population, so both strains can reach high frequencies by chance. Additionally, the mutation rate is high enough so as to consistently introduce the second strain purely through mutation, which is not accounted for in the model formulation.

In general, the analytical solution appears to be accurate as long as the population size is not too small ($N \leq 1,000$) and the mutation rate is not extremely high. Considering that most outbreaks arise over large areas, where $N$ is large, and point mutation estimates (for beneficial, neutral, and deleterious mutations) for viruses and bacteriophages seldom exceed $1 \times 10^{-4}$ (Sniegowski et al. 2000), then these assumptions should not be greatly violated when considering real-world cases.

**Figure 2**: Contour plot of the minimum susceptible population needed for the original strain to mutate into a faster-spreading strain. Below this proportion, emergence of a new strain is impossible. The overall population size is $N = 10,000$. Contour labels indicate the minimum susceptible proportion. The red contour shows where the transition from where emergence is prevented due to the first strain becoming extinct ($S_{\min,1}$, above the red line), to where emergence is limited due to the first strain burning out the existing susceptible population ($S_{\min,2}$, below the red line).
Application to a Two-Wave Outbreak of Chikungunya Virus, La Réunion Island

We will now apply our model to the two-wave outbreak of Chikungunya virus on La Réunion. Over 2005, the virus was present at a low frequency in the population of La Réunion Island, peaking at 500 reported cases and stabilizing at 100 until the end of September. Afterward, a secondary wave emerged in December 2005, causing nearly a 100-fold increase in the number of cases, peaking at more than 45,000 (Renault et al. 2007). More than 90% of viruses in the secondary outbreak harbored two novel substitutions in the structural region (Schuffenecker et al. 2006). Viruses harboring these substitutions also replicated faster, compared to ancestral variants (Vazeille et al. 2007). Therefore, it is clear that the secondary outbreak was almost surely caused by adaptive mutation increasing the replication rate of the pathogen. Here, we use our analytical results to provide estimates of the emergence probability of this pathogen and how it compares to models where emergence probabilities are not affected by depletion of susceptible individuals by the first strain. Specifically, given that a first strain already appeared in the population, was there a high probability that a second strain would appear over time, due to the large susceptible pop-

Figure 3: Plots of the analytical solution for emergence probability of second strain (eq. [5c]; solid lines) in comparison with simulation data (points; error bars are 95% confidence intervals). The first strain mutates into a new strain with \( N_0 \) equal to 1.2 (red lines/points), 1.5 (green), 1.8 (blue), or 2.5 (purple). Population sizes are 1,000 (A, B), 10,000 (C, D) or 50,000 (E, F), with compound mutation rate \( N_m \) equal to 0.001 (A, C, E) or 0.01 (B, D, F). Plots covering \( R_0 \) between 1 and 1.1 only are shown in figure S2, available online.
Mutation Creating a New Outbreak

Figure 4: Plots of the analytical solution for emergence probability of second strain (eq. [5c]; solid lines) in comparison with simulation data (points; error bars are 95% confidence intervals). Color scheme is the same as in figure 3. Term $N_u = 10$, and $N = 10,000$ (A) or 50,000 (B). In this plot, error bars lie within individual points.

Figure 5: Three-dimensional plots of emergence probability of a mutated strain of the Chikungunya virus in La Réunion. A, Results predicted by our model ($P_S$), as scaled to the emergence probability for a de novo strain. B, Results scaling our model to one that assumes that emergence of new pathogens are not affected by limitation of the susceptible population. Values are given as a function of the reproductive ratio of the mutated strain $F_0$ and the advantageous mutation rate $m$. See “Application to a Two-Wave Outbreak of Chikungunya Virus, La Réunion Island” for the other parameters used.

The population size of La Réunion is around 776,000 individuals (Renault et al. 2007). We assume that the susceptible population size before infection would cover the whole island. This seems a reasonable assumption since infection did not seem to be located at any one location on La Réunion (Renault et al. 2007). It is also generally assumed that cross-immunity between Chikungunya strains is extremely strong, due to the onset of strong innate immunity (both with Chikungunya virus, and alphaviruses in general; Wauquier et al. 2011; Volk et al. 2010), combined with the fact that Chikungunya virus strains are antigenically similar, which forms the basis of vaccine creation against it (Akahata et al. 2010; Wang et al. 2011). The estimated substitution rate for the virus was $8.8 \times 10^{-4}$ substitutions per site per year (Cherian et al. 2009). However, what is of interest for our model is the advantageous mutation rate. While the substitution rate is equal to the neutral mutation rate (Kimura 1983), the advantageous mutation rate is generally greatly lower than this, as advantageous mutations only make up a tiny proportion of all mutations (Eyre-Walker and Keightley 2007).

However, if we consider the per-genome mutation rate (as opposed to the per-site rate), then this would increase the adaptive mutation rate. Again, to be conservative, we investigate $\mu$, varying between $10^{-5}$ and $10^{-7}$. Finally, we estimated the reproductive ratios by comparing epidemic data from (Renault et al. 2007) with those produced from analytical results. It appears that a good fit for $R_0$ is 1.04, while that for $F_0$ is higher at approximately 1.4 (supplementary material S3). We therefore fix $R_0$ at 1.04 and vary $F_0$ between 1.05 and 1.5 to determine to what extent $F_0$ affects emergence probability.

Figure 5A shows the probability of emergence according to our model, $P_S$, scaled to that expected for a single infected individual in a fully susceptible homogeneous population (that is, $1 - \frac{1}{F_0}$). We see that, unless the mutation rate is very low, the scaled probability of emergence gen-
erally lies between 0.2 and 0.4. Therefore, the need to mutate from a preexisting strain reduces the probability of emergence only by two- to fivefold, compared to the emergence of a single strain in a fully susceptible population. This is due to the fact that, even though the mutation rate is low, the susceptible population in La Réunion is assumed to be very large, creating multiple opportunities for the first strain to mutate into a faster-spreading strain.

We can also determine how saturation of the susceptible population affected the emergence probability. Figure 5B compares $P_s$ to a model that assumes that susceptible depletion does not affect the emergence probability of new strains (that is, the emergence probability of a single strain is $1 - 1/(\Phi_0)$). The overall probability of emergence is denoted as $P_{NS}$. We clearly see that the ongoing depletion of the susceptible population greatly reduced the emergence probability of mutated strains in this epidemic, with a 10–20-fold reduction in probability observed. Similar values are obtained if the pathogen emergence probability is set to the naive expectation using an “effective” reproductive rate that does not account for feedbacks, $1 - N/(5\Phi_0)$ in $P_{NS}$; that is, susceptible dilution affects pathogen emergence when it first appears but not in subsequent generations (result not shown). This result gives a clear indication as to how susceptible depletion strongly affects the emergence of new mutated strains from preexisting ones. It could also explain why observing mutated strains arising in the field is uncommon, as the change in the underlying population size would impact their appearance.

However, we wish to stress that this is a basic analysis, based on broad-scale parameters used. These results are likely to be qualitatively robust because we used conservative estimates for the parameters. Nevertheless, in order to make it more accurate, we need a detailed knowledge of population structure, so as to determine the initial susceptible population size, as well as improved knowledge of the beneficial mutation rate.

Discussion

The evolution of infectious diseases, especially causing spillovers from zoonotic reservoirs into human populations, is a major health threat. Due to this hazard, there has been a substantial research focus on determining the likelihood of pathogens mutating into more virulent strains. However, most previous research has focused on cases where the initial pathogen is maladapted and is bound to become extinct rapidly unless it mutates. Here, we investigate a related but overlooked scenario, where a weakly emerging strain (with $R_0 \approx 1$) can mutate into a faster-spreading strain before dying out, causing a second outbreak that has the potential to be maintained for a longer period of time. Studying emergence of pandemic strains originating from intermediated adapted strains offers more applications for monitoring outbreaks than searching for strains originating from maladapted ones, because the initial strain is present in the population for a longer time. It also opens a new perspective for predicting the pandemic risk for pathogens that are known to be emerging (or re-emerging) but generate only localized outbreaks (e.g., with avian influenza or ebola).

We have derived an analytical formulation for the emergence probability of the second strain from the first, by tracking the population trajectory over time and calculating the emergence probability at each time point (eq. [5c]). One of the most important insights from our derivation is that even though the first strain’s $R_0$ is low enough to ensure that, in general, a large susceptible population remains for the second strain to spread through, the decreasing susceptible population would still act to reduce the emergence probability of the second strain. This finding reflects similar results on how a reduced population size reduces emergence probabilities in evolutionary genetics (Otto and Whitlock 1997) and evolutionary rescue models (Martin et al. 2013).

By applying our model to a well-documented case of pathogen reemergence, that of the Chikungunya virus in La Réunion Island, we provide a stark example of how the ongoing depletion of the susceptible population has a strong negative effect on the emergence probability of the mutated virus strain. However, the overall emergence probability is only slightly lower than that for a single strain in a fully susceptible population. Overall, this example highlights that while susceptible depletion can strongly limit the emergence of mutated strains, the risk remains on the order of that expected for completely new strains emerging, meaning that there is still a nonnegligible risk of emergence. This model was based on broad-scale estimates of mutation rates, population sizes, and population structure, for which most of the finer details are unknown. Therefore, we hope that this model, as well as others, would encourage further investigations into adaptive mechanisms and rates of pathogens, in order to aid the application of emergence models to understanding the risk of secondary outbreaks emerging through evolution of the pathogen.

Our model assumes that both pathogens are apparent in a large homogeneous population. However, most real populations of interest are heterogeneous, due to either the presence of subpopulations (Alexander and Day 2010; Kubiak et al. 2010) or differences in immune history or contact structure. Specifically, most outbreaks show the presence of "super-spreaders" that cause a greater amount of secondary infections than average (Galvani and May 2005). Super-spreaders have also been detected in vector-borne disease outbreaks (Woolhouse et al. 1997), which
could also affect the dynamics of the Chikungunya example, although the degree of heterogeneity with this outbreak is unknown. The presence of host heterogeneity is known to decrease the emergence probability of new outbreaks, as an increased proportion of the population are unlikely to spread the initial pathogen and trigger a full outbreak (Lloyd-Smith et al. 2005b). However, Yates et al. (2006) concluded that the presence of super-spreaders only has a minute impact on emergence probabilities, if the initial strains have $R_0 < 1$. Therefore, implementing host heterogeneity and spatial structure in addition to epidemiological feedbacks would be an important next step in increasing the realism of the model.

The application of our model to the Chikungunya outbreak also poses the question as to how population feedbacks in pathogen vectors would affect the emergence probability. The likelihood of emergence could be further decreased if the preexisting pathogen confers immunity to a large fraction of the vector population, as with the host population studied here. Furthermore, immunity can be conferred on vectors by having their immune system “primed” by a weaker version of a pathogen (reviewed in Little and Kraaijeveld 2004). Alternatively, priming can arise due to the presence of a competing pathogen (e.g., with Wolbachia preventing infection in Aedes aegypti mosquitoes from a variety of infections; Moreira et al. 2009). Immunity can also be transgenerational in invertebrates due to this “immune priming,” of which there are several cataloged examples (Little et al. 2003; Sadd et al. 2005; Sadd and Schmid-Hempel 2007) that could maintain immunity in a vector population, even if it has a high turnover. However, this reduction may be offset by different replication rates in the vector; for example, the mutated strain of the Chikungunya virus had a greatly higher replication rate in Aedes albopictus, compared to the ancestral strain (Vazeille et al. 2007). It is clear that this intriguing question requires further study using an extended model in order to quantify the effect of differences between the host and vector populations.

Since it can be tricky to infer the effect of mutation and population feedbacks from real-world epidemic data, experimental bacterial systems might be useful in testing the predictions of the model (as discussed in Denneyh 2009-Martin et al. 2013). For example, Benmayor et al. (2009) found that phages could evolve to infect novel host bacteria only if seeded at initial frequencies between 0.1% and 1%. It was argued that lack of adaptation occurred at higher initial frequencies due to increase costs of host switching and lack of mutation supply. However, our results also suggest that a decrease of susceptible individuals, caused by seeding the initial strain at too high a frequency, could also prevent new types from appearing. We therefore hope that our model would motivate further experimental work on the relative impact of demographic effects and evolutionary effects on pathogen emergence.

In summary, we have produced a model for the probability that a second, stronger outbreak can be caused from an initial weaker one, which is accurate if the population size $N$ is large and $R_0$ is close to 1. This study highlights how to implement information about changing population sizes (specifically the susceptible population size) into analytical models to determine the probability of a new strain emerging, without relying solely on numerical simulations. By applying the model to a well-known example of disease reemergence, we have shown that these population feedbacks can drastically reduce the emergence of new, mutated strains arising from preexisting outbreaks. These findings therefore have implications in public health management and also highlight how competition between new strains can prevent the subsequent emergence of new outbreaks once a preexisting epidemic has established itself.

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Literature Cited


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